

**Quesito 1.** La v.a. discreta  $X$  ha distribuzione di probabilità

$$\Pr(X = -2) = \frac{1}{2}, \quad \Pr(X = 1) = \frac{1}{3}, \quad \Pr(X = 2) = \frac{1}{6}.$$

1. Calcolare la distribuzione di probabilità di  $X^2$
2. Calcolare  $\text{Var}(X)$ .

Esprimere i numeri razionali come frazioni.

**Quesito 2.** Si consideri la funzione  $f(x) = \cos\left(\left|\frac{4x-2}{3x+1}\right|\right)$ .

1. Determinare dominio e immagine della funzione.
2. Determinare il punto di massimo assoluto per  $x \geq 0$ .

**Quesito 3.** Marie is getting married tomorrow at an outdoor ceremony in the desert. In recent years it has rained only 7 days each year. But the weatherman has predicted rain for tomorrow. When it actually rains, the weatherman correctly forecasts rain 95% of the time. When it doesn't rain, he incorrectly forecasts rain 10% of the times. What is the probability that it will rain on the day of Marie's wedding?

**Quesito 4.** Si considerino le funzioni  $f(x) = \frac{1}{5x}$  e  $g(x) = \log(x)$ .

1. Scrivere esplicitamente le funzioni  $f \circ g$  e  $g \circ f$ .
2. Determinare dominio di  $f \circ g$  e  $g \circ f$ .

**Quesito 5.** If 20% of the bolts produced by a machine are defective.

1. Determine the probability that out of 4 bolts chosen at random less than 2, bolts will be defective.
2. Out of 2000 bolts how many would you expect to be defective.

**Quesito 6.** La v.a. discreta  $X$  ha valore atteso  $E(X) = 6$  e varianza  $\text{Var}(X) = 2$ . Qual è il valore atteso di  $X(X-3)$ ?