

***Mathematicians in Torino University  
from 16<sup>th</sup> to 20<sup>th</sup> century***

**Browsing through Mathematics**

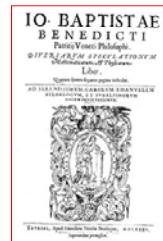
Clara Silvia Roero – Dept. Math. Univ. Torino      Torino 28 April 2014

## **The Duchy of Savoy in the Late Renaissance Giovanni Battista Benedetti 1530-1590**

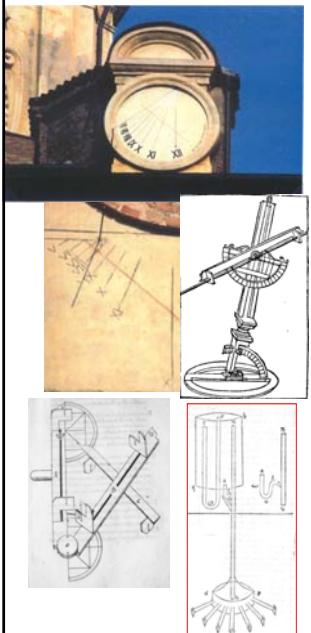
- ❖ Venetian mathematician, from 1558 to 1566 was at the court of Ottavio Farnese in Parma.
- ❖ Benedetti was invited by **Duke Emanuele Filiberto** who had great plans to raise the cultural level of the Duchy and the **scientific culture** at the University, transferred by him in Torino in 1567. His aim was also to establish a museum-library called **Theater of all sciences** [*Teatro di tutte le scienze*]
- ❖ He reached Savoy at the end of **1566** or beginning of 1567 and remained until his death (Jan. 20, **1590**).
- ❖ His activity covered a range of interests: classical geometry, mechanics, physics, metereology, music, acoustics, optics, hydrostatics, astronomy, astrology, etc.

*Diversarum speculationum mathematicarum  
et physicarum Liber* 1585

Collection of letters to mathematicians, scientists,  
philosophers, musicians and scholars of all Europe



## Giambattista Benedetti 1530-1590



- ❖ *Resolutio omnium Euclidis problematum una tantummodo circini data apertura* 1553
- ❖ *Demonstratio proportionum motuum localium contra Aristotilem et omnes philosophos* 1554
- ❖ *De gnomonum* 1574
- ❖ *Diversarum speculationum mathematicarum et physicarum Liber* 1585

He performed the duties of a ‘**court mathematician**’, employed to **plan and construct sundials** and other scientific **instruments** (oil lamp, mechanical clocks, tools for surveying and mensuration), to **advise** on engineering and the architecture of public works (fortifications, fountains) and on university affairs, to **interpret astronomical events** and to **provide astrological forecasts**, to give lectures on mathematics and science to the Duke and the princes of the house of Savoy, like Carlo Emanuele I, etc.

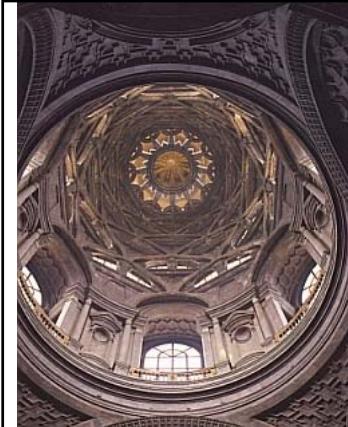
## Guarino Guarini 1624-1683



A cosmopolitan artist, born in Modena, studied theology, philosophy, mathematics and architecture. During his travels to Rome, Vicenza, Prague, Parma, Messina, Lisbon, Paris, Nice, Torino and Milan he came into contact with scholars and artists. The fruit of these exchanges ripened during Guarini’s **period in Torino**, from **1666** until his death (March 6, 1683). In 1668 became **Royal Engineer and Mathematician of Savoy**

- ❖ *Placita philosophica*, 1665
- ❖ *Euclides adauctus et methodicus*, 1671, 1676
- ❖ *Modo di misurare le fabbriche*, 1674
- ❖ *Compendio della sfera celeste*, 1675
- ❖ *Trattato di fortificazioni*, 1676
- ❖ *Leges temporum et planetarum*, 1678
- ❖ *Caelestis matematicae*, 1683
- ❖ Plates in *Novum Theatrum Sabaudiae*, 1675
- ❖ *Disegni di architettura civile ed ecclesiastica*, 1686
- ❖ *L’architettura civile*, 1737

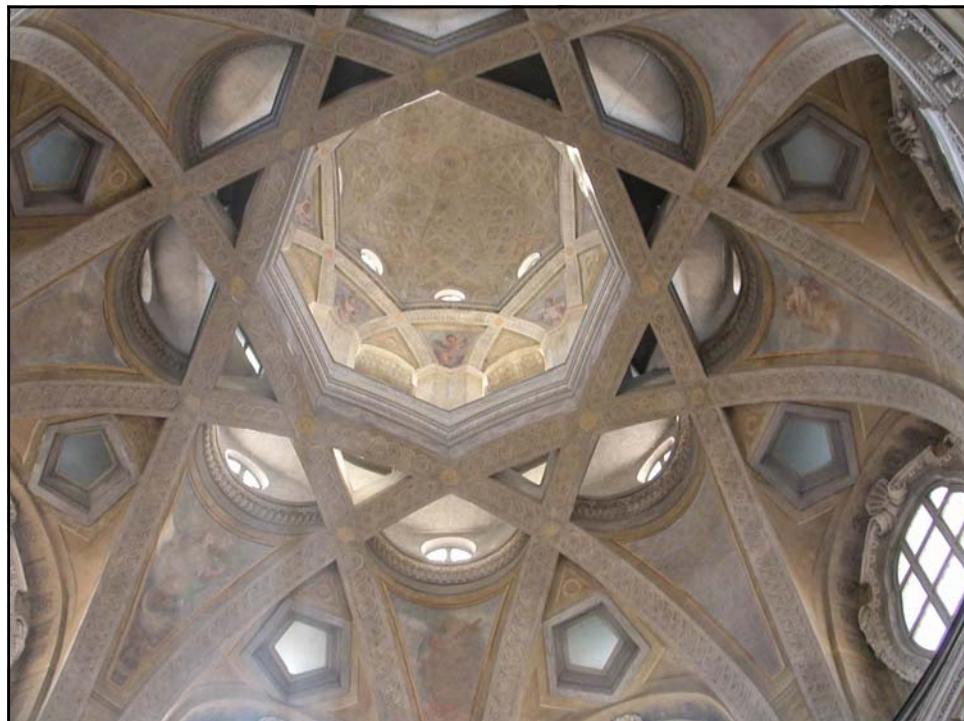
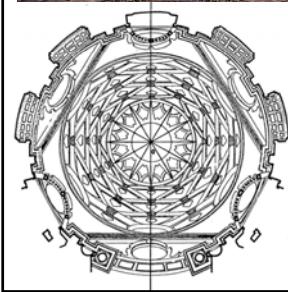




**Guarini, Euclides adiunctus ... 1671**

*Thaumaturga Mathematicorum miraculorum insigni  
vereque regali architectura coruscat*

underlines the **miraculous power** that **mathematics** exerts on **architecture**, declaring that it is possible to draw on mathematics' most sublime ideas, a science that he sought to enrich with the fruits of his labour



## Carignano Palace

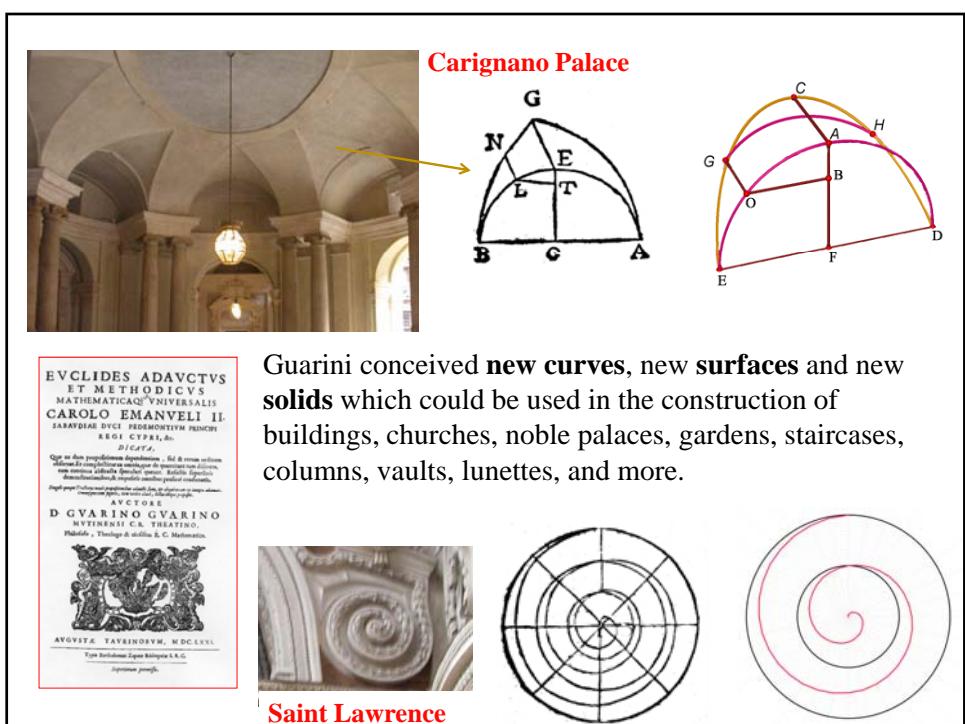


## Carignano Palace

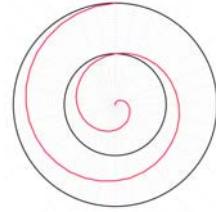


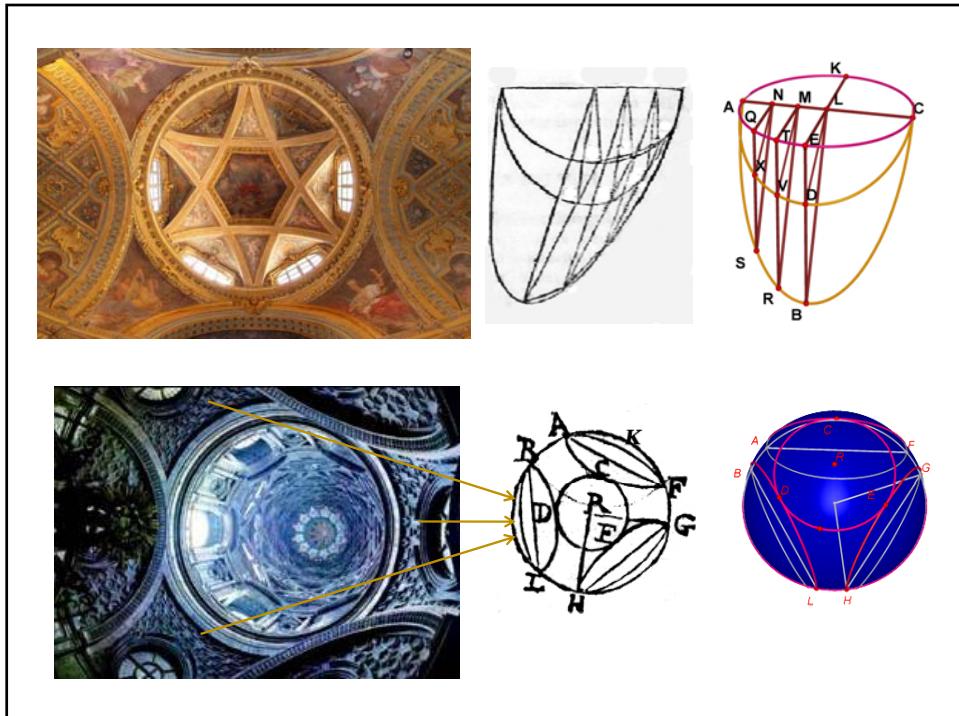


San Lawrence



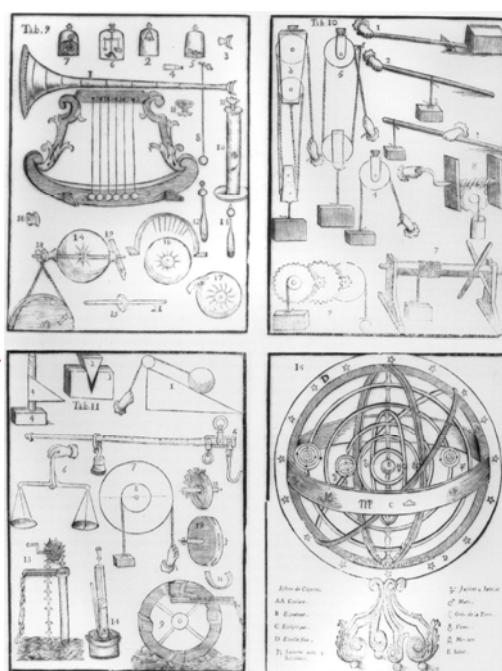
Guarini conceived **new curves**, new **surfaces** and new **solids** which could be used in the construction of buildings, churches, noble palaces, gardens, staircases, columns, vaults, lunettes, and more.





## 1739 Scientific Museum

- Chamber of **Experimental Physics**
- Chamber of **Mathematics**
- Chamber of **Botany and Zoology**
- Chamber of **Anatomy**
- Chamber of **Marvels Wunderkammer**



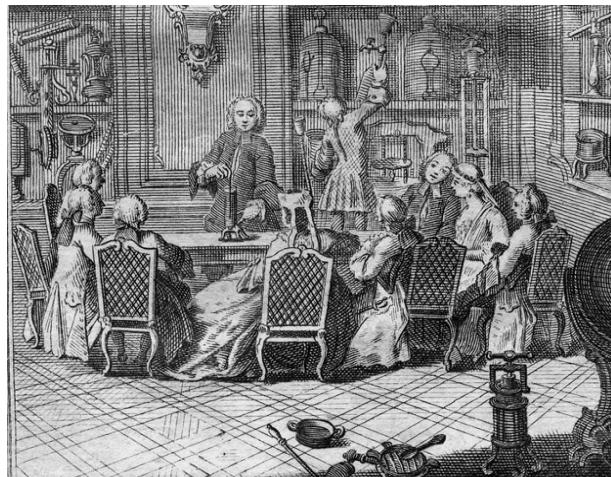


1700-1770

French clergyman and physicist Nollet spent 6 months in Torino, invited by the Duke to teach **Physics** to prince Vittorio Amedeo III.

He conducted physical **experiments** in the face of court and **sold instruments** to the Duke for his Museum.

### The soujourn of Jean Antoine Nollet in Torino 1739-1740



### Giambattista Beccaria 1716-1781

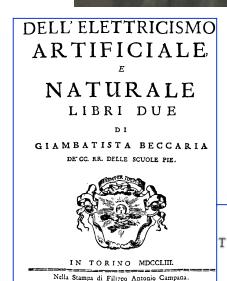


#### ❖ 1748-1781 Torino University Professor of Experimental Physics – lectures on

- Galileo's and Newton's theories
- results of scientists

Kepler, Descartes, Huygens, Newton, Leibniz, Boyle, Musschenbroek, Johann Bernoulli, Daniel Bernoulli, ... B. Franklin

- Among his students at the university:  
mathematician Joseph Louis **Lagrange** and his friend the physician Gian Francesco **Cigna**, two of the founders of the Turin Academy of Sciences.



Torino 1748-1781

**Institutio I De Physica et de optima Physicae excolenda via**

**Institutio II De corpore, et corporum affectionibus**

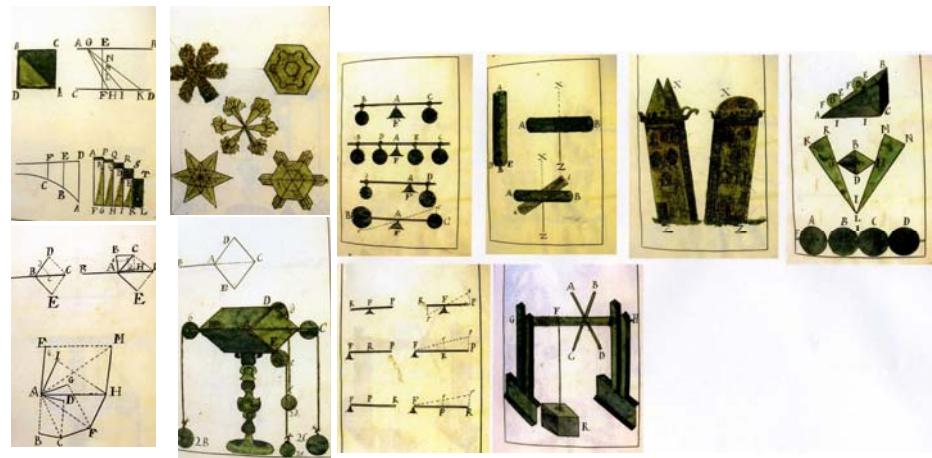
**Institutio III De affectionibus actuosis praesertim de motu universe**

**Institutio IV De vi inertiae, deque tribus legibus Newtonianis**

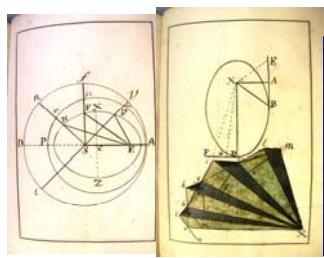
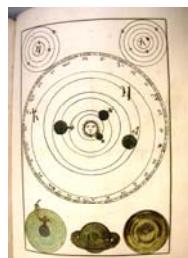
**Institutio V De motuum differentiis, de aestimatione motus uniformis**

**Institutio VI De pressione et compositione motuum, resolutione, aequilibrio**

**Institutio VII De pressionibus diffusis, earum aequilibrio, et centro communi**

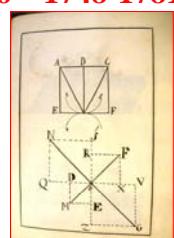


Torino 1748-1781



responsum per partem solidi ad immobile centrum  
la deficiuntur, & in planis immobiliis conficiuntur  
per partes proportionales.

quatenus ipsi A B : addit. ut radii A S, B S,  
in aere concentrici ferent aequalis area A S B,  
in ubi corpus venit ad E, agit in complicita



Kepler's Laws in Newton's Principia

Leibniz  $mv^2$

**Institutio X De gravitate coelesti**

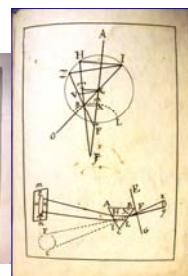
**Institutio XI De motu qui fit ex percussione**

**Institutio XII De Liquidis**

**Institutio XIII De Aere**

**Institutio XIV De Lumine**

**Institutio XV De re electrica ...**



Newton's Optiks



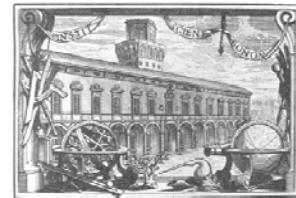
➤ Follower of B. Franklin, Beccaria published works on **electrical phenomena** and erected the first iron rod on his house in Turin and hailed its usefulness in providing protection against lightning.



### *Dell'Elettricismo artificiale e naturale* 1753

(*Lettere a G. B. Beccari*) *Dell'elettricismo* 1758

*De electricitate vindice* (to B. Franklin) 1767



*Elettricismo artificiale* 1772 (English transl. 1774)

➤ member of Royal Society and Bologna's Institute of Sciences



25 January 1736 in Torino

### Torino 1736-1766

Kingdom of Carlo Emanuele III  
1730-1773

Reform of University by Vittorio Amedeo II 1680-1730

#### Faculties

- Theology
- Jurisprudence
- Medicine, Arts and Philosophy



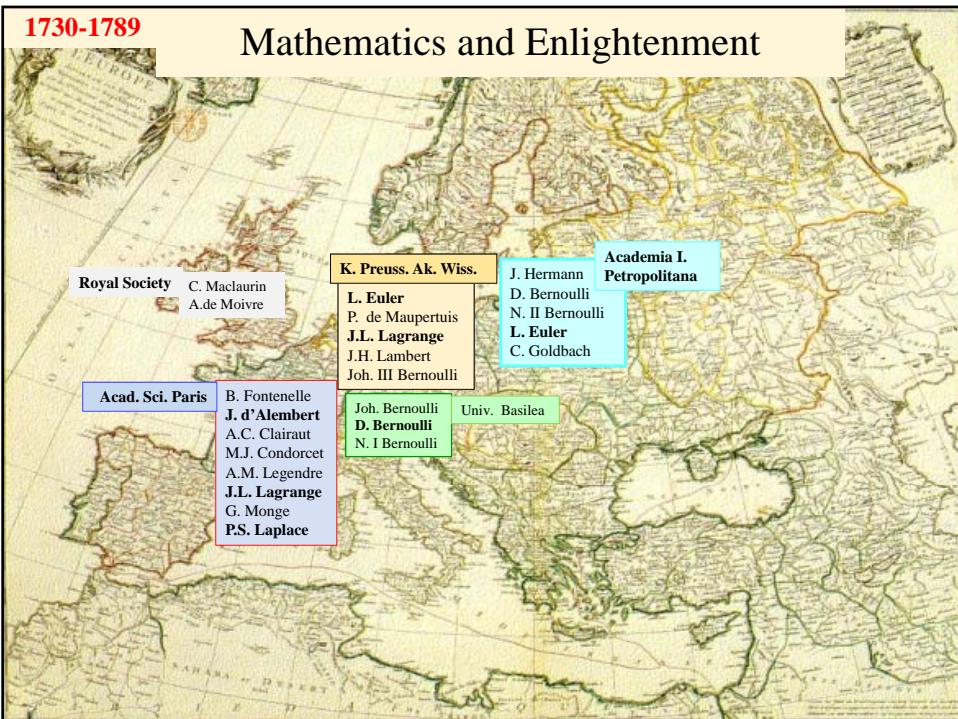
**June 1752** Lagrange obtained the title of *maître-es-art pour le Droit* and follow the lectures of Physics, Mathematics and Logic  
Studied at the Public Library and wrote letters to the Italian mathematician Giulio Carlo Fagnani and then to Leonhard Euler in Berlin



**J. L. Lagrange** Turin 1755-1766  
“substitute of the teacher of Mathematics”  
Military Schools courses of **Analysis and Mechanics**

**1754-1759** from Lagrange's correspondence to G.C. Fagnani and the quotation in his lessons *Principi d'Analisi sublime* of treatises on Calculus we know that he studied

M.G. Agnesi *Instituzioni Analitiche ad uso della gioventù italiana*, 1748,  
**L. Euler** *l'Introductio in analysin infinitorum*, 1748; *Institutiones calculi differentialis*, 1755; il *Commercium Epistolicum* fra **Leibniz** e **Johann Bernoulli** (1742); **Jac. Bernoulli** *Opera omnia* 1744; **Joh. Bernoulli** *Opera* 1742; **L. Euler** *Mechanica, sive motus scientia analytice exposita* 1734, 1736; *Methodus inveniendi lineas curvas maximi minimive proprietate gaudentes* 1744.



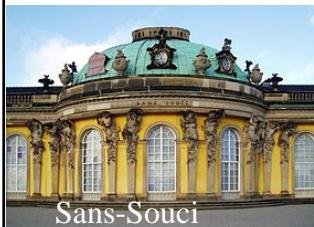
## Berlino 1740-1766

*Académie Royale des Sciences et de Belles Lettres*



Federico II *il Grande*  
1712-1786

Voltaire



Pierre L. M. de Maupertuis  
1740-1759      Leonhard Euler  
1744-1766

Sans-Souci

**1756** Discussions with G. Beccaria who threw Lagrange, Saluzzo and Cigna out of his Laboratory of Physics. **1757** The three young men met weekly in Saluzzo's home and founded a *Private Scientific Society*



Giuseppe Angelo SALUZZO  
1734 – 1810 chemist

**1747** Military career - R. Scuola di Artiglieria Lagrange

**1757-1788** President of the *Private Scientific Society*

**1759** *Sur la nature du Fluide Elastique qui se développe de la Poudre à Canon*

**1794** General of Artillery



Gianfrancesco CIGNA  
1734-1790 physician



**1750** Studied Physics under Beccaria's guide

**1755** degree in Medicine

**1757** Secretary of the *Private Scientific Society*

**1757-1765** research on breathing and electricity

**1770** Lecturer at hospital (San Giovanni)

**1775** Professor of Anatomy at Torino University

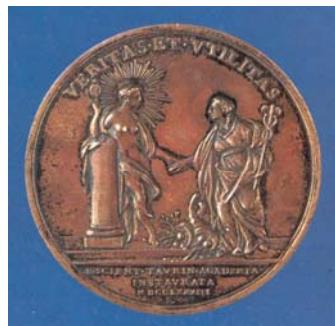
## SOCIETAS PRIVATA TAURINENSIS

1757

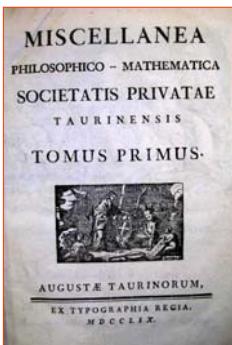


J.L. Lagrange, G. Cigna and A. Saluzzo founded the *Private Scientific Society* the nucleus of the **Torino Academy of Sciences**

"Esclusivamente si adoprava nel promuovere i progressi delle scienze positive e sperimental: **matematica, fisica, chimica, anatomia, fisiologia.**"



*Veritas et Utilitas*



1759

*Miscellanea Philosophico-Mathematica Societatis  
Privatae Taurinensis*

Lagrange J.L. *Recherches sur la méthode de maximis et minimis*, I<sup>2</sup>, p. 18-32

Lagrange J.L. *Sur l'intégration d'une équation différentielle à différences finies, qui contient la théorie des suites récurrentes*, I<sup>2</sup>, p. 33-42

Lagrange J.L. *Recherches sur la nature et la propagation du son*, I<sup>3</sup>, p. 1-112 *vibrating strings*

J.L. Lagrange to L. Euler, September 1759

Il y a quelques jours, je vous ai envoyé un exemplaire de l'ouvrage qu'une Société privée de Turin a fait paraître sous le titre *Miscellanea Philosophico-Mathematica*.

L. Euler to J.L. Lagrange, 23 October 1759

... tout le monde doit convenir que ce premier Volume de vos travaux est un vray **chef d'œuvre**, et renferme bien plus de profondeur que tant d'autres volumes des Académies établies et **jamais société particulière n'a plus mérité d'être soutenue par son souverain.**"



Vittorio Amedeo III

1760

**Società Reale  
di Torino**

*MISCELLANEA* 1759

Lagrange J.L. *Recherches sur la nature et la propagation du son*, Misc. Taur. 1759, p. 1-112

“Je tire de mes formules la même construction du problème *de chordis vibrantibus* que M. Euler a donné, et qui a été si fort contestée par M. D’Alembert. Je donne de plus à cette construction toute la généralité dont elle est capable...”

- established the conditions for the initial configuration of the string
  - substitute to the elastic string an oscillatory system formed by  $n$  points and found  $n \rightarrow \infty$  for the elongation of the string at point  $x$  and time  $t$ , the expression

$$y(x,t) = \frac{2}{l} \sum_{\xi=0}^l Y(\xi) \sum_{r=1}^{+\infty} \sin \frac{r\pi\xi}{l} d\xi \sin \frac{r\pi x}{l} \cos \frac{rc\pi t}{l} + \frac{2}{c\pi} \int_0^l V(\xi) \sum_{r=1}^{+\infty} \frac{1}{r} \sin \frac{r\pi\xi}{l} d\xi \sin \frac{r\pi x}{l} \sin \frac{rc\pi t}{l}$$

where  $\mathbf{Y}$  and  $\mathbf{V}$  represent the initial position and velocity.

MÉLANGES II. 1760-1761

Euler member of Turin Society    Lagrange foreign member of Berlin Academy

Euler member of  
1 January 1760

Member of Berlin Academy  
**September 1756**

**Euler L.**, *Lettre à M.r De La Grange. Recherches sur la propagation des ébranlements dans un milieu élastique*, II<sup>2</sup>, p. 1-10.

**Lagrange J.L.**, *Nouvelles recherches sur la nature et la propagation du son*, II<sup>1</sup>, p. 11-172.

**de Foncenex D.**, *Sur les principes fondamentaux de la méchanique*

## **Lagrange II** Addition à la première partie des recherches sur la nature

- et la propagation du son*, II<sup>2</sup>, p. 323-336

  - Convergence of research and results
  - General Formulation of the theory of **acoustic waves**
  - First foundations of the theory of **finite deformations of continuous media**
  - Studies of **differential equations**
  - Calculus of variations

**Euler L.**, *Methodus inveniendi lineas curvas maximi minimive proprietate gaudentes*, 1744

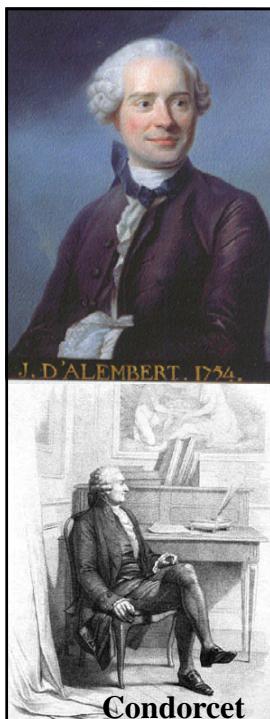
## MÉLANGES II, 1760-1761

**Lagrange J. L.**, *Essai d'une nouvelle méthode pour déterminer les maxima et les minima des formules intégrales indéfinies*, II<sup>2</sup>, p. 173-195.

**Lagrange J.L.**, *Application de la méthode précédent à la solution de différens problèmes de Dynamique*, II<sup>2</sup>, p. 196-298.

**Lagrange a Euler, 28.10.1762** “Ayant appris, par une de vos lettres de 1759, que vous aviez fait assez de cas de ma méthode *de maximis et minimis* pour l’**étendre** et la **perfectionner** dans un **Traité** particulier, j’ai cru devoir supprimer entièrement celui que j’avais presque déjà achevé sur ce sujet, et je me suis borné à en exposer simplement les principes dans un **Mémoire** que j’ai tâché de rendre **le plus court** qu’il m’a été **possible**; je ne me suis même déterminé à composer ce Mémoire que parce que vous m’avez fait l’honneur de me mander dans la même lettre que vous ne vouliez point publier votre travail avant le mien.”

**Euler a Lagrange, 2.10.1759** “Analytica tua solutio problematis isoperimetrii continet, ut video, **quicquid in hac quaestione desiderari potest** et ego maxime gaudeo hoc argumentum a te potissimum **ad summum perfectionis fastigium** esse evectum. Rei dignitas me excitavit, ut tuis luminibus adiutus, ipse solutionem analyticam conscripserim, quam autem celare statui donec ipse tuas meditationes publici iuris feceris, ne ullam partem gloriae tibi debitae praeripiam.”



A. Clairaut



LUIGI LAGRANGE

### Lagrange's travel to Paris 1763-1764

### Lagrange to Condorcet 19.10.1773

Il y a bientôt dix ans que j'ai eu le bonheur de faire votre connaissance à **Paris**, et que j'ai conçu pour vous le plus tendre attachement. Je regarde toujours **cette époque** comme **la plus heureuse** de ma vie. »

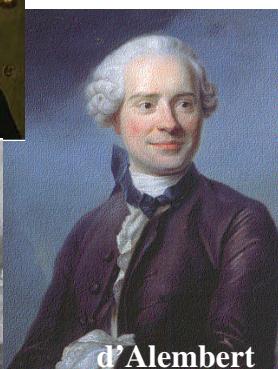
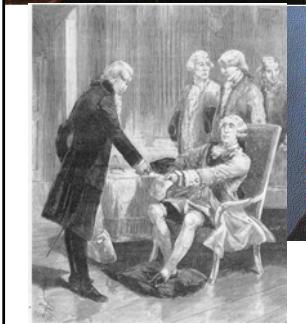


The strategies by D'Alembert with Frederick the Great in 1765-66

“un homme du plus **rare talent dans la Géométrie**, fort au dessus de **tout ce que l'Italie renferme** en ce genre, et à côté pour le moins de **tout ce qu'il y a de meilleur** dans le reste de l'**Europe**”.



**Berlin 1766-1787**  
*“Philosophe sans crier”*  
*Philosopher without clamour*



Sans-Souci

## Paris 1787 - 10 aprile 1813



**1788** *Méchanique analytique* M. Marie, A.M. Legendre

❖ Bailly, Lavoisier, Lemonnier, Guyton-Morveau, ...

**1794** professor at École Normale

**1795-1799** taught mechanic and analysis at the Ecole Centrale des Travaux Publics - Ecole Polytechnique

**1797** *Théorie des fonctions analytiques* 2 ed. 1813

**1798** *Traité de la résolution des équations numériques*

**1806** *Leçons sur le calcul des fonctions*

**1811** *Mécanique analytique* 2 ed. 2 vol. 1811, 1815; 3 ed. 1853-55

## University of Turin

*Risorgimento 1848-1860 and the Unification of Italy 1861*



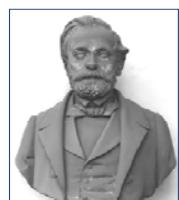
Carlo Ignazio Giulio  
1803-1859



Giovanni Plana  
1781-1864



Luigi F. Menabrea  
1809-1896



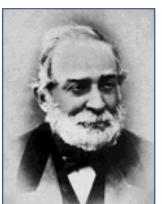
Felice Chiò  
1813-1871



Quintino Sella  
1827-1884



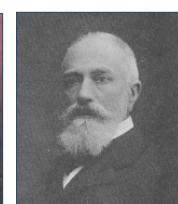
F. Faà di Bruno  
1825-1888



Angelo Genocchi  
1817-1889



Francesco Siacci  
1839-1907



Enrico D'Ovidio  
1843-1933

## ➤ Context – Risorgimento and Unification of Italy 1840-1880

- political and social background (Math. research, teaching and education)
  - Scientific journals in Piedmont before Unification (Kingdom of Savoy)

➤ **strategies** to overcome the cultural backwardness

- (International)** travels, visits and stays for making reports on scientific institutions, factories, manufacturing, technical instruction, sojourns of study, legislations & decrees, congresses, Universal Exhibitions, international relationships with foreign Institutions, Scientific National Societies, ...
  - (National)** congresses, legislations & decrees on public instruction, technical courses (then Polytechnic), Italian translations of papers by foreign mathematicians, periodicals (Math. research, teaching and education)

19<sup>th</sup> century



## **Carlo Ignazio Giulio**

**1840** member of the Statistic Commission

TURIN

**1841** dean of Faculty (Mathematical, Physical and Natural Sciences)

**1844** rector of University; Commissioner of the Universal Exhibition in Turin

1845 member of Public Education Ministry

1848 senator

Commissioner of Universal Exhibitions 1851 London 1855 Paris





Carlo Ignazio Giulio  
1803-1859

**1847** He travelled for 3 months in Switzerland, France, Germany, Belgium, Great Britain and returned with as many new ideas on **scientific and technical instructions**. From these visits and stays he brought back **scientific journals**, books, **treatises**, catalogues, diaries, now in his Archives with his own Library (BSCP Turin). Geneva, Lausanne, Neuchâtel, Basel, Colmar, Strasbourg, Heidelberg, Frankfurt, Cologne, Aacken, Bruxelles, Antwerp, Gand, Bruges, London, Oxford, Gloucester, Leicester, Birmingham, Manchester, Liverpool, Sheffield, Dover, Folkestone, Boulogne-sur-Mer, Abbeville, Amiens, Paris, Orleans, Lyon, Chambéry.

[Detailed reports in Letters to his wife](#)

*École Polytechnique:* D. Poisson's *Traité des mécanique* 1811, 1833; J. N. Hachette *Traité élémentaire des machines* 1811; L. B. Francoeur *Traité de mécanique élémentaire, à l'usage des élèves de l'École polytechnique* 1801; C. Navier *Résumé des leçons données à l'École des ponts et chaussées sur l'application de la mécanique à l'Établissement des constructions et des machines* 1826

**1845-1859** *Regio Istituto tecnico* (1852) *Scuola di applicazione per gli ingegneri* (1859)  
Technical Institut - Polytechnic School



### Translations

- C.I. GIULIO (ed.) *Elementi di geometria di Clairaut, nuova traduzione italiana con note. Approvata dal Consiglio superiore di Pubblica Istruzione per uso delle scuole secondarie e speciali*, Torino, Stamperia Reale, 1850.
- C.I. GIULIO (ed.), *Teoria matematica dei ponti pensili con tavole per agevolarne la costruzione del Signor Davies Gilbert, vice-presidente della Società R. di Londra tradotta dall'inglese con note ed aggiunte*, Torino, Stamperia Reale, 1851.
- C.I. GIULIO (ed.) *Elementi di meccanica del capitano Enrico Kater e del dottore Lardner, prima versione italiana con note ed aggiunte*, Torino, Cugini Pomba e compagni, 1851.

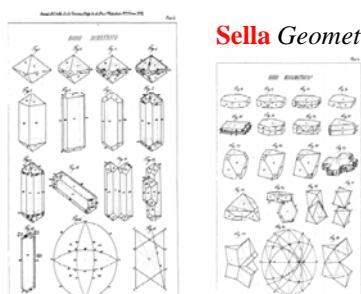
## Travels, visits and stays for study of young graduated



from **Turin** to France, Switzerland, Germany, Great-Britain, Russia, ...

**1847-1851** **Quintino Sella** was invited to continue his studies at the École des Mines in **Paris**, on behalf of Savoy Kingdom and he spent 2 months, travelling in Germany (in **Berlin** met Jacobi), and **Great-Britain** (11-25 June 1851 and April-September 1852). Then he became prof. Mathematics in Turin Technical Institute and University.

**1857-1859** **Berlin – St. Petersbourg** **Giovanni Virginio Schiaparelli** sojourns for study at the **Berlin University** and **Pulcovo Observatory** (from 1860 he became the astronomer in Brera, Milan)



**Sella Geometria applicata alle arti 1852** Techn. Institute Torino  
**Mathematical Cristallography**

**1860** Professor of Mineralogy

**1861** Politician, Ministry, President of the Accademia Nazionale dei Lincei, devoted to the development of Research and Italian Scientific Culture

## Memberships in Turin Academy of Sciences

Among the consequences of the relationships of European mathematicians and scientists with Italians colleagues became corresponding members of the Turin Academy

**1841 Poncelet, Babbage, Coriolis, Hamilton, the 2 Jacobi** (phys. and mathem);

**1845 Bélanger, Liebig, 1853 Faraday**

**1870 H. von Helmholtz, 1878 Hermite, 1880 F. Klein, 1881 K. Weierstrass**

and also became members the Italian mathematicians, engineers, chemists, physicists, astronomers, ... **who took active part to the Unification of Italy**:

**1856 Sella, 1857 Piria, 22.1.1861 Matteucci, Carlini, Amici;**

**25.1.1862 Genocchi, Brioschi, 1863 Govi; 1865 B. S. Robert; 1868 M. Lessona, G. Codazza, 1870 Lombroso, G.V. Schiaparelli, A. Dorna, A. Secchi**

**1878 L. Bellardi, G. Basso, 1879 G. Bizzozero, E. D'Ovidio**



**Giovanni Plana**  
1781-1864

Ecole centrale – Grenoble      Ecole polytechnique - Paris  
 Mathematician and astronomer, Prof. Infinitesimal Calculus – Turin University, Director of Observatory, President of Academy of Sciences  
 Prize Lalande      Académie Sciences Parigi  
 Iron Crown      Austria Emperor  
 Gold Medal Copley      Royal Astronomical Society



**F. Faà di Bruno**  
1825-1888

**1849-51** Paris  
**1854-56** PhD thesis A.L. Cauchy  
**1860-1888** Prof. Higher Analysis - Turin University  
*Théorie générale de l'élimination* (1859), *Traité élémentaire du calcul des erreurs* (1869), *Théorie des formes binaires* (1876)



**Angelo Genocchi**  
1817-1889

*Note sur la théorie des résidus quadratiques*, Mém. couronnés et mém. des savants étrangers, Académie royale des sciences, des lettres et des beaux-arts de Belgique, 25, **1852**, pp. 1-54

**1884** *Calcolo differenziale e principii di calcolo integrale* con aggiunte dal Dr. G. Peano      **1899, 1903, 1922** German and Russian translations



1858-1932

### **1880-1900 Mathematical Schools in Turin** **Relationships with the international scientific community**

#### **Giuseppe Peano**

Analysis, Logic

From the manuscripts of courses and the hundreds of letters and postcards (1879-1923) can emerge the mechanisms by which the most recent styles of scientific research circulated between Italy and Germany, as well as some of their relapses on the cultural and academic life, and the publishing policies of the two countries.



1863-1924

#### **Corrado Segre**

Algebraic Geometry



1860-1940

#### **Vito Volterra**

Analysis, Physical Mathematics



Göttingen

## Giuseppe Peano

**27 August 1858** Spinetta (CN)

**16 July 1880** degree in Mathematics Univ. Torino

**1880** Assistent of E. D'Ovidio

**1881-1890** Assistent of A. Genocchi

**1884** Supplied him course of Infin. Calculus

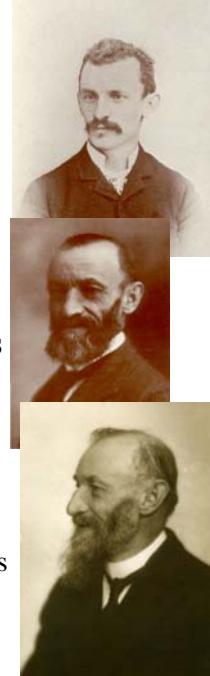
**1890** winner of a competition for the **chair of Analysis**  
and obtained the full professorship in 1895

**1908/09-1909/10** Course of Higher Analysis

**1925/26-** Course of Mathematics for teachers

**20 April 1932** death

Main contributions: Analysis, Vector Calculus, Foundations  
of Maths (Arithmetic, Geometry, Analysis), Mathematical  
Logic, Education, Linguistic



Drafting the **lectures of Genocchi**, the young assistant soon earned international renown with the publication of Genocchi's treatise *Calcolo differenziale e principii di calcolo integrale*, in 1884.

Peano with his refined critical sense discovered the **defects, errors** and **imprecisions** of the principal treatises of **infinitesimal calculus** then in use in **France, Germany and Italy**, and **retouched** definitions, statements, theorems and proofs. A feature that distinguishes this book from the mathematical literature of the times are the **examples** (now called '**counterexamples**'), **so simple and well chosen** that Peano contrived to show the **fallaciousness of the results** presented up to that time in even the best books of analysis.

The *Enzyklopädie der Mathematischen Wissenschaften* reported among the **most authoritative books of analysis** not only this 1884 treatise, but also his 1887 *Applicazioni geometriche del calcolo infinitesimale*, and his 1893 two-volume *Lezioni di analisi infinitesimale* for the Military Academy.



Among the noteworthy ‘**Peano’s additions**’ are

- the theorems and observations on the limits of indeterminate expressions;
- the generalisation to the functions with several variables of Weierstrass’ theorem on maxima and minima;
- the example of functions with two variables continuous along every straight line in the plane but not continuous in the whole plane;
- the theorem of uniform continuity of the functions with several variables;
- the generalisation of the theorem of mean value;
- the properties of existence and derivability of implicit functions;
- the integration of peculiar rational functions;
- the analytic expression of the function of Dirichlet;
- the definition of the definite integral as the upper and lower extreme of finite sums.



Moreover there are sections on **avant-garde results** derived from the **study of**

**G. Cantor, Dini, Dedekind, Harnack, Lipschitz, Du-Bois-Reymond, Darboux, Heine and Schwarz.**

### January 1890 Peano’s famous curve that fills an area

Taking as a point of departure a famous work by **Georg Cantor**, in which the correspondence between a segment and a square is established, in just a few pages Peano defines the parametric equations of a continuous curve that passes through all points in a square.



0 —————— 1

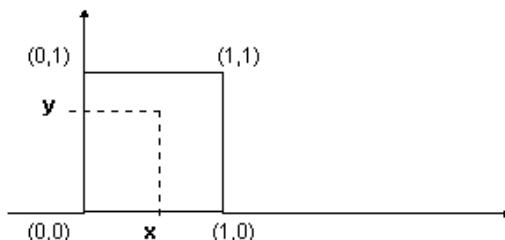
**P segment (0,1)**

$t = 0, a_1 b_1 a_2 b_2 a_3 b_3 \dots$

**Q square**

$x = 0, a_1 a_2 a_3 \dots$

$y = 0, b_1 b_2 b_3 \dots$



The astonishment of contemporaries about this event, which marks a significant fundamental step in studies of analysis, topology, set theory and measure theory, is evident from both the comments made by many as well as by the multitude of papers that follow the path opened by Peano:

**D. Hilbert** in 1891, E. H. Moore in 1900, H. von Koch in 1904, E. Cesàro in 1897 and 1905, H. Lebesgue and È. Picard in 1904, W. Sierpinski in 1912, followed by A. Schönlies, E. Jürgens, W. Killing, G. Polya, ....



David Hilbert  
1891

1 2 3 4

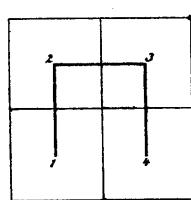


Fig. 1.

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

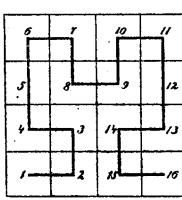


Fig. 2.

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

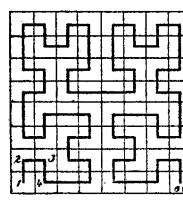
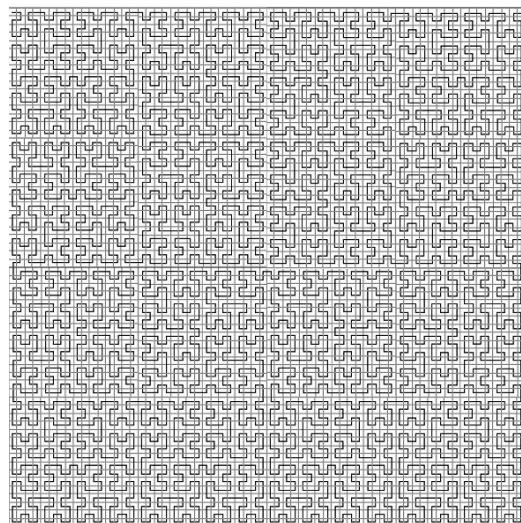


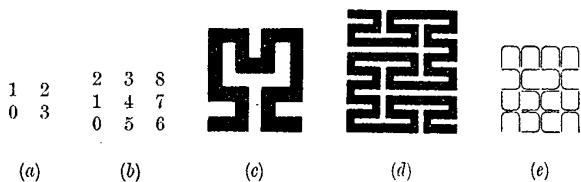
Fig. 3.



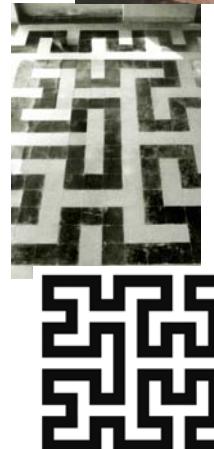
Peano – Hilbert

### Cavoretto (hill of Torino) 1891

In the last edition of 1908 of the *Formulario Mathematico*, Peano, with the use of symbols, illustrates and comments on the principle on which the construction of his curve is based and offers the visualisation of some steps.



In the meantime he had in fact ordered the construction of a reproduction, in black tiles on a white background, on the **balcony of his house** in **Cavoretto**, which he bought in 1891.



### *Formulaire de Mathématiques* 1895

- |  |        |
|--|--------|
| I. Logique mathématique Peano, G. Vailati<br>II. Opérations algébriques Peano, F. Castellano<br>III. Arithmétique Peano, C. Burali-Forti<br>IV. Théorie des grandeurs C. Burali-Forti<br>V. Classes de nombres Peano<br>VI. Théorie des ensembles G. Vivanti<br>VII. Limites R. Bettazzi<br>VIII. Séries F. Giudice<br>IX. Théorie des nombres algébriques G. Fano | 144 p. |
|--|--------|

Chaque partie du **Formulaire**, bien que commencée par **un Auteur**, sera en définitive le **résultat du travail de tous les collaborateurs**.

#### Addictions et Corrections

Otto Stolz, C. Ciamberlini, A. Ramorino, G. Morera, A. Arbicone, E. Cantoni, Buhl, Louis Couturat, Gustav Eneström, A. Borio, W. Beman, F. D'Arcais, J. Rius y Casas, F. Severi, F. Invrea, A. Korselet, I. Zignago

<b>I. Logica-Mathematica.</b>	Cfr	cifra	54	$\exists^*$	limite superio	108	vet	vectorre	165	
Symbolo	Nomen	pag.		$\exists_*$	limite infero	109	dist	distancia	176	
$\equiv$	aequalitate	3	!	$\otimes$	infinito	109	$\vec{U}$	vectorre unitarie	179	
$\supset$	deductione	3	C	$\theta$	107	recta $p_1$	180			
$\wedge$	conjunctione	3	mult	$\downarrow$	indice	108	plan $p_1$	180		
$\varepsilon$	individuo	4	minimo multiplo comun	$\eta$	quantitatem	112	empl	componente	180	
Clis	Classe	4	maximo divisor commun	$\equiv \theta$	intervallo	118	empl.	comp. normale	180	
;	sistema	6	numero primo	Log	logarithmo	119	proj	projectione	180	
$\exists$	« que »	9	mp	$\Sigma$	summa	120	Transl	translatio	181	
-	negatione	10	max. potestate	$\prod$	producto	128	Sym	symmetria	181	
$\vee$	disjunctio	10	indicatore	$\Delta$	differencia	140	Motor		181	
$\exists$	existe	12	f	R	número de Bernoulli	194	Hemat	hemisferia	182	
$\wedge$	nullo	12	functio		Med	medio	193	cos	coordin	183
$\wedge$	aequo	13	J		Sum	numero cardinalis	193	sin	sinu	183
$\wedge$	« to, illo »	13	simile		inf	infinito	193	coord	coordinata	184
			reciproco		A	Unicas de classe	199	A	absoluto	184
			idem		$\dot{r}$	classe derivata	141	quadrat		185
			variable		Intv	intervallo	142	$x^*$	trivectorre	188
					In	inferior	142	$y^*$	bivectorre	189
					es	extremo	142	$p^*$	trivectorre	189
					am	confine	142	$p^1 p^2 p^3$		189
					prob	probabilido	142	$\#$	forma	191
					Ex	numero complexe	144	$\#$	predicatio regressiva	192
					unit	unidade	145	I	indice	193
					Distr	determinante	146	penit	positio	193
					fun	funcio lineare	148			
					Subst	substitutione	148			
					ab	substitutiones	149	V.	Limits,	
						ivariable	151	Lm	limites de functio	194
						constante	151			194
					I	unitalte imaginaria	152	const	constante	195
					q	quantitatem imaginaria	152	ores	crecentes	195
					real	parte reala	152	decr	decrecentes	196
					imag	coefficiente de i	152	cont	continuo	197
					K	conjugato	152	e		197
					$\sqrt[n]{}$	radicus	152	ing	tgente	198
								#		198
								log <sup>n</sup>	logarithmos	199
					pat	puncto	155	sin <sup>-1</sup>	anti-sinu	201

### Strategies to promote the *Formulario* asking for collaboration

- ❖ Journals
- ❖ International Conferences (Math., Phil.)
- ❖ Societies of teachers (Ass. Franç. Avan. Sciences, Mathesis)
- ❖ Contacts with colleagues, teachers, editors of journals, historians of mathematics, philosophers, assistants, students (Klein, Mittag-Leffler, Jordan, Frege, Cantor, ..., Cesàro, Vitali, Levi-Civita, Marcolongo, Pincherle, ..., R. de Montessus, ...)
- ❖ Editorial Announces in RdM, other periodicals (for mathematicians, teachers, ...), meetings
- ❖ ‘Payment’ consisted in the annual subscription to his *Rivista di Matematica*

27. Et pour les en récompenser en quelque façon, nous offrons l'abonnement annuel à la *Rivista di Matematica* à tous ceux qui contribueront au développement du Formulaire, en ajoutant de nouvelles parties, ou en corrigeant les parties publiées, et les notes historiques.



### **International congresses: Logic and *Formulaire***

**1897** in Zurich ICM plenary lecture by G. PEANO *Logica matematica*

**1900** At the second ICM held in Paris there were Peano, Padoa, Vacca and Vailati. Among those in the *Comité de patronage* of the **congress of philosophy** that had taken place the week before that of the mathematicians, also in Paris, were the Germans G. Cantor, R. Dedekind, G. Frege and F. Klein, while among the Italians was Peano. Through him were presented at the congress, in addition to his own, communications by Burali-Forti, Padoa, Pieri and Vailati.

On that occasion Peano, Vailati, M. Calderoni and C. Cantoni were elected as referees for Italy.

**1903** At the second international congress of historical sciences, which took place in Rome in April 1903, during which E. Lampe, F. Müller, S. Günther and G. Itelson were present, Vacca illustrated the fourth edition of Peano's *Formulaire* (1902-03).

**1904** In August 1904 Peano, Vacca and Vailati were in Heidelberg for the third ICM, where Vailati made a communication, as he also did in September 1904 in Geneva at the second IC Phil.

**1908** Rome **1911** Bologna **1912** Cambridge .... **1924** Toronto

### **Corrado Segre (1863-1924)**

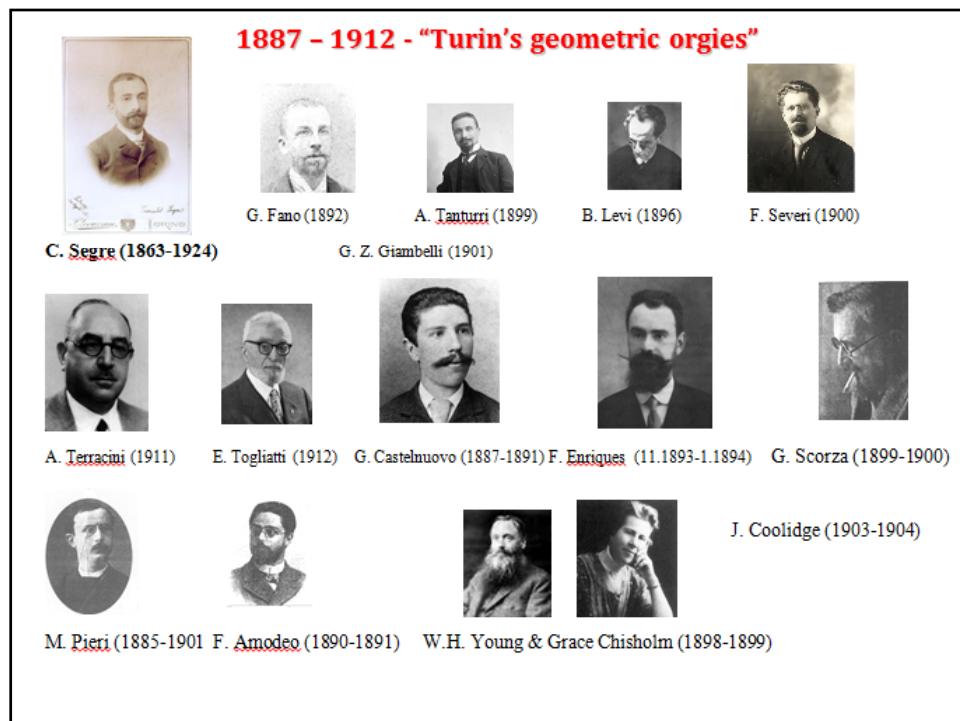


**1883** He took his degree in mathematics at the University of Turin with Enrico D'Ovidio

**1888** he obtained the chair of higher geometry at the University of Turin

**1904-1924** Co-director of *Annali di matematica pura ed applicata*

**From 1887-88 to 1890-91 and from 1907-08 to 1920-21** he taught a course for future teachers in the Scuola di Magistero (Teacher Training School)



**The model of Göttingen**

**F. Klein 1872-1875** Erlangen; **1875-1880** Munich;  
**1880-1886** Leipzig; **1886-1925** Göttingen

**1895 -1920 D. Hilbert**

Klein adopted an **innovative style of teaching**, initiating a tradition of teaching that was essentially **oral**, based on a system of **seminars** and **colloquia** on topics of **advanced research**.  
F. Klein, *The Evanston colloquium ... 1893 ... in Chicago... 1894*  
He was joined by **David Hilbert** in **1895**, that he would carry out his plan to create a School of mathematics, exerting from 1895 to 1920

*a profound impact on mathematics and physics throughout the world. Many factors contributed to the creation of a special atmosphere that served as a model for several other important centres for mathematical research. Göttingen exemplified a dynamic new way of doing mathematics within a highly competitive community in which the spoken word often carried more weight than did information conveyed in written texts.*

[Rowe 2004, p. 85]

## Felix Klein as Segre's 'Maestro a distanza'

**1878-1879** through Luigi Cremona, **Enrico D'Ovidio** (rector of Torino University) came into contact with **Klein** (Munich) with the aim to promote the **internationalisation of mathematical knowledge**. He asked Klein for news about recent publications printed abroad and, for example, begged to be kept informed about the publication of the *Vorlesungen über Geometrie* by Clebsch and Lindemann.



**1880** **F. Klein** corresponding member of the Torino Academy of Sciences  
**16 August 1883** **C. Segre** and G. Loria sent Klein the paper which arose out of research carried out in their **degree dissertations**, written under D'Ovidio's advisement, *Sur les espèces diverses de complexes du 2<sup>e</sup> degré des droites qui coupent harmoniquement deux surfaces du second ordre*. This memoir was influenced, in both its contents and the method used, by the works of the **German School** (articles by **A. Weiler, T. Hirst** and **F. Schur**, as well as those of **Klein** himself).

**1883-1923** onset of an intense, on-going **dialogue** between Klein and Segre. For Segre Klein became -and remain ever after- a **Maestro**, first **indirectly** through the **reading** of his **works** and exchanges of **letters**, and later **directly** through **personal meetings** in Göttingen in **1891** and in Italy in **1899**.

## Felix Klein as Segre's 'Maestro'



*C'est que, sans le savoir ... vous êtes, Monsieur, pour nous non seulement un maître mais aussi un ami, dont nous étudions les travaux avec passion, car c'est par eux que nous avons commencé à vous connaître et à vous aimer.*

[**C. Segre to F. Klein**, 7 Sept. 1883, Luciano-Roero 2012, p.83]

Segre to Klein: 22 September 1883, 3 January 1884, 8 February 1884, 27 March 1884

➤ **1883-1888** the dialogue was essentially '**asymmetrical**'.

Segre discussed the **topics** he intended to tackle, in order to sound out Klein's opinions on **originality**, usefulness and **importance**, presented his **difficulties**, ... Klein suggested **strategies** to him for addressing them, he was able above all to open Segre's eyes to **new horizons in cutting-edge mathematical knowledge**, he recommended him with indications of **new papers**.

It was by following the advice of Klein that Segre studied in depth the **memoirs** of A. Weiler, A. Cayley, L. Schläfli, G. Darboux, T. Hirst, F. Schur, J. Sylvester, R. Ball, K. Weierstrass, A. Ameseder, M. Nöther and B. Riemann.

These would have an **impact on Segre's courses in Higher Geometry** in Turin, the topics of which, changed each year, would **become the legacy inherited** by his first disciples, **G. Castelnuovo** and **G. Fano**.

➤ **1883-1886** Klein invited Segre to contribute to the *Math. Annalen* not only as an author but also as a **reviewer** and **reviser** of the works in geometry and analysis



### (after 1888) Dialogues between equals

**1888** after winning the chair in **Higher Geometry**, the relationship between *Maestro* and disciple was transformed into a dialogue between equals, between two ‘leaders’ of mathematical **Schools** engaged in promoting and advancing their respective traditions. The new dynamics between Segre and Klein are evident in both the changes in the stylistic forms of the letters and in the subjects discussed.

- (new responsibilities) specific topics are alternated with **comments on lectures** and **students**, on their training, on **publishing policies**, and on the **most suitable means** for favouring the **internationalisation** of mathematical knowledge with **sojourns for study** and **translations**.
- 1890 Segre assumed the role of **promoter** and spokesman with **Klein** and **Hurwitz** for the results of his friend **Castelnuovo** and of **his student Fano**.

*Siccome nel prossimo anno scolastico io farò un corso di geometria sulle curve algebriche di genere p nel quale svilupperò alcuni dei risultati da Lei ottenuti sulle corrispondenze in generale, e particolarmente su quelle univoche, avrei piacere che Ella mi suggerisse, se ne conosce, quei miglioramenti, quelle generalizzazioni che Ella credesse opportuno di introdurre nei Suoi due importanti lavori.*

[C. Segre to F. Klein, 29 July 1890, Luciano-Roero 2012, p. 156]



Mario Pieri

### 1886-1890 Publishing Initiatives promoted by Segre

Up to the 1880s, the desire to give an **European dimension** to his **teaching** led Segre to overcome the ‘problem of language’, by becoming the promoter of the **Italian translations** of several **memoirs** and **treatises written in German**.

**1886** Segre expressed for the first time to Klein his interest in *Beiträge zur Geometrie der Lage* and in **1887** he proposed that **Mario Pieri** carry out the Italian translation of **von Staudt's book**, asking Klein for his help in finding information regarding his life and to ask authorisation.

- **1889** Italian version of the *Geometrie der Lage*, Mario Pieri ed., (Torino, Bocca) accompanied by a valuable Segre’s essay on von Staudt’s biography and his contributions.
- **1889** November Segre urged Klein to reprint his famous *Erlangen Program*, of which he appreciated the ‘substantial identity between various mathematical disciplines (in particular between analytical and geometrical disciplines). The text, although held to be of capital importance, was **not yet well-known in Italy** at the time.
- **1890** Segre entrusted the work to **Gino Fano**, at that time still a student. Carried out under Segre’s meticulous supervision, the Italian version of the *Program* was compiled from a print copy in parallel with a manuscript draft by F. Gerbaldi made available by E. D’Ovidio.



Gino Fano

*Annali di Matematica* (2) 17, 1890, p. 307-343

### Segre's reasons to suggest Italian version of the *Erlangen Program*

*The reasons for my proposing this work ... do not consist for me only in the historic interest, which this essay assumes from the multitude of research, especially those of Mr Klein and his School, which were inspired to a greater or lesser extent by almost twenty years of panoramic insights and to the profound concepts that it contained. ... Many general and ingenious ideas are to be found in these pages, such as the substantial identity between different mathematical disciplines (and in particular between analytical and geometrical disciplines!) each of which represents the other when account is taken of the transformations groups that underlie them; the various considerations about these groups; many correct observations that shed the truest light on and specify in the best possible way the character of many topics and doctrines, and especially of some of those most discussed, such as that of generalised varieties, and non-Euclidean geometry. All of these are things that are not sufficiently known and studied by young people, or are known only by indirect ways. Let me draw the full attention to these matters.*

- **1896** Francesco Giudice translated Klein's *Vorträge über ausgewählte Fragen der Elementargeometrie*, Leipzig, Teubner, 1895.

F. Klein, *Conferenze sopra alcune questioni di Geometria elementare* (Torino Rosenberg-Sellier)  
[G. Loria to F. Klein, 22 July 1895, Luciano-Roero 2012, p.183]

### Italian versions of Klein's writings in university teaching

- C. Segre's forty handwritten *Quaderni* (1888-1924) regarding his courses in Higher Geometry  
[Terracini 1953; Giacardi 2001, 2002, Conte-Giacardi 2013]
- G. Castelnuovo's forty-nine notebooks (1903-1923) in Rome univ.
- the thirty-five *Taccuini* by A. Terracini related to courses in Higher Geometry, Complementary Mathematics, Higher Mathematics and Probability Theory. Through the considerable number of quotations from works by Klein they show the breadth of dissemination of his results and 'views'.
- G. Fano's and other assistents' handwritten *Quaderni* regarding courses in Higher Geometry (Torino univ.)
- ❖ In Italian Universities began to be requests the **lithographs** of the **lectures of Klein and Hilbert**. A large collection of Klein's lithograph courses were either brought back to Italy by Fano or sent by Klein to the professors. *Nicht-Euklidische Geometrie I, Vorlesung ... 1889-90 von F. Klein Ausgearbeitet von Fr. Schilling*, Göttingen, 1893; *N.-E. Geometrie II, Vorlesung ...*, Göttingen, 1893 (Fano G 95); *F. KLEIN, Einleitung in die höhere Geometrie I, Vorlesung gehalten im Wintersemester 1892-93 von F. Klein Ausgearbeitet von Fr. Schilling*, Göttingen, 1893 (Fano G 36)

## 1891 Segre's Travels to Germany and stay in Göttingen

1891 June-August Segre visited Frankfurt am Main, Berlin, Nuremberg, Dresden, Munich, Leipzig and Göttingen, where he met **T. Reye**, **M. Cantor**, K. Rohn, **M. Nöther**, **F. Klein** and **W. Von Dyck**.

The trip offered him both the opportunity to visit scientific institutions (observatories) and to keep him up to date with the most recent publications (new ed. of T. Reye's *Geometrie der Lage*, the 2nd vol. of M. Cantor's *Vorlesungen über Geschichte der Mathematik* and Hurwitz's writings on Riemann surfaces and on the theory of ideals. He also seized the opportunity to **promote Italian studies in algebraic geometry outside** of Italy. In particular, with Klein, Nöther and Rohn.

*Chi non è stato qui, non può immaginare che razza d'uomo è Klein e che specie di organizzazione egli ha saputo, con un'abilità che nessun altro può avere, imporre agli studi matematici in quest'Università. È una cosa che m'ha fatto un'impressione straordinaria. E si che di impressioni vivissime da parte degli scienziati ne ho già avute parecchie in questo viaggio!*

[C. Segre to G. Castelnuovo, 30 June 1891]

## 1893-94 Gino Fano in Göttingen and Erlangen

Fano arrived in **Göttingen** in **October 1893** to spend the winter semester. He attended **Klein's lectures on functions and hypergeometric series**, as well as a course by **Weber** on the **theory of algebraic numbers**.

He also **gave** some **talks** himself at the **Mathematische Gesellschaft**, in which he illustrated the **results** of the **Italian School** of geometry, contributing to their diffusion.



*Il soggiorno a Göttingen favorì in lui il pieno maturarsi di certi modi di pensare già appresi alla scuola dei Maestri italiani; anzitutto la tendenza alla valorizzazione di quei procedimenti di scoperta che si sogliono sintetizzare col termine alquanto vago di intuizione.'*

[A. Terracini, *Commemorazione*, 1953, p. 704]

Erlangen summer of 1894 Fano met **Max Nöther**, with whom he discussed **Enriques's discovery** of the existence of non-rational surfaces of genre 0.

[F. Enriques to G. Castelnuovo, 29.8.1894, Conte 1994, p. 106]

### 1899 Klein's proposal to Gino Fano - chair in Göttingen

Klein so highly esteemed his capacities that he offered Fano a teaching position in Göttingen.

*Prof. Schönflies has been called to Königsberg as full professor and will move there by 1 April. His teaching here by us regarded the initial required courses and in particular he had to teach the classes in **Descriptive Geometry**. Further, he had time to occupy himself with more advanced classes. I conceive the chair essentially as a geometric chair, that is, I wish the new occupant to emphasise geometric representation and cultivate geometric studies in all directions. Now however you know the decline of the geometry in the new generation of Germans. I have therefore come to think that you might be the right man for us!*

[**F. Klein to G. Fano**, 5 Febr. 1899, Luciano-Roero 2012, 195-196]  
**G. Fano to F. Klein**, 10 Feb. 1899, Luciano-Roero 2012, 197-198]



### Circulation of texts

➤ Circulation of texts, papers, litographies from his disciplines to foreign scholars (correspondences with Nöther, Zeuthen, Schur, Hurwitz, ...)

*Je me suis mis en correspondance, par l'intermédiaire de Segre, de Turin, avec M. Beppo Levi dont je t'ai emprunté deux notes. Il m'écrivit: Je dois avouer que j'ai trouvé dans mes démonstrations quelques lacunes, etc; d'autres occupations m'ont détourné provisoirement de ces recherches, etc.*

[**R. Baire to E. Borel**, 16.12.1903, Dugac 1990, p. 65]

*Mes théorèmes invoqués par Fatou sont mis en doute actuellement par Beppo Levi dans les Rendiconti dei Lincei. Beppo Levi n'a pas su rétablir quelques raisonnements intermédiaires simples et il s'est cassé le nez sur une faute de rédaction grave que Montel m'a jadis signalée et qu'il est facile de réparer. Naturellement j'ai commencé par rédiger une note ou je l'attrapais comme du poisson pourri puis, sur une lettre de Segre, et parce que ce n'est pas le moyen d'acquérir une réputation mondiale que d'attraper ceux qui s'occupent de mes histoires, j'ai été moins dur.*

[**H. Lebesgue to E. Borel**, 1.6.1906, Bru-Dugac 1991, p. 148-149]

## Scientific and human relationships: 1904 in Heidelberg

*Tutta una scuola di geometri italiani riconosce nella Memoria di Brill e Noether il suo punto di partenza! Più fecondi ancora divennero quei concetti, quando, per opera appunto di questa scuola, essi acquistarono un carattere più astratto e più generale, venendo riferiti a curve iperspaziali ...*

[C. Segre, *La Geometria d'oggi e i suoi legami coll'Analisi*, ICM Heidelberg, 1904, p. 115]



C. Segre, *On Some Tendencies in Geometric Investigations*, Bulletin of the American Mathematical Society, 11, 1904, p. 442-468; J. Coolidge, *The opportunities for mathematical study in Italy*, Bull. AMS, 11, 1904, p. 9-17; E.B. Stouffer, *Mathematics in Italian Universities, the 12<sup>th</sup> annual meeting of the Rocky Mountain Section*, Colorado, 1928.

La Geometria d'oggi e i suoi legami coll'Analisi.  
Vortrag, gehalten in der 3. allgemeinen Sitzung am 13. August  
von  
C. Segre aus Turin.

Voi conoscete il volumetto che l'Università di Kolozsvár ha pubblicato due anni sono, per centenario dalla nascita di Giovanni Bolyai.\* Ne sono parte prese una parte di L. Schlesinger delle applicazioni della geometria analitica alla teoria delle funzioni di variabile complessa, ed un'altra di P. Stäckel sulla meccanica analitica in relazione alle varietà di più dimensioni.\*\* Così alla glorificazione del grande geometra ungherese prendevano parte l'Analisi e la Meccanica!

A me parve di vedere in ciò un nuovo indicio dei sentimenti fraterni che vanno sempre più legando fra loro i vari rami della Matematica!

Per quel che riguarda la Meccanica, non oserei che io dica quanta pace abbiano le cose nella finzione! Solo io permetto a me stesso di ricordarvi, a proposito della Geometria moderna, una rappresentazione, di grande importanza suggeriva, a cui ormai, dopo l'esempio dato da Hertz, tutti i cultori della Meccanica ricorrono liberamente. Voglio dire la rappresentazione di un sistema mobile con  $n$  gradi di libertà per mezzo di un punto dello spazio ad  $n+1$  dimensioni. Indicando la forza viva con  $\frac{dx}{dt}$ , il problema del moto equivale a quello geometrico delle geodetiche di uno spazio ad  $n$  dimensioni, in cui *ds* sia l'elemento lineare!

Quanto ai legami che stringono la Geometria e l'Analisi, si può dire che essi derivano principalmente da ciò che in molta parte gli oggetti di cui esse si occupano sono gli stessi, almeno in un

\* Joannis Bolyai in memoriam.

\*\* V. nach Stäckel, Bericht über die Mechanik mehrfacher

Mannigfaltigkeiten, Jahrest. d. Deutschen Math.-Verein. 12, 1903, p. 488.

## A first student (not Italian): J. Coolidge



In the academic year 1903-04 Coolidge attended to the lessons of Higher Geometry held in Turin University by C. Segre on *Applications of Abelian Integrals to Geometry*.

Then he went to Germany to work with E. Study. To both (Segre and Study) Coolidge owed his deep interests in the geometrical interpretation of complex numbers and their functions, a subject which always fascinated him.

*Every student in complex domain will find that he is forced to refer continually to the work of two admirable contemporary geometers, Professor Corrado Segre of Turin, and Professor Eduard Study of Bonn. The names of both appear throughout this book; the author had the rare privilege to be the pupil of each of these masters. Geographical separation has cut him off from the one, the inexorable logic of history has impeded his communion with the other. But his sense of obligation has never wavered, and he begs to offer the present work as a small token of admiration and esteem.*

## Papers of Coolidge influenced by Segre

Some of the principal papers written by Coolidge under the influence of Segre and Study:

- *Die dual-projektive Geometrie im elliptischen und sphärischen Raume. Dissertation, 1904.*
- Les congruences isotropes qui servent à representer les fonctions d'une variable complexe, *Atti Acc. Sci. Torino*, 1904.
- *The elements of non euclidean geometry*, Clarendon, 1908.
- A study of the circle cross, *Trans. of the AMS*, 1913.
- *A treatise on the circle and sphere*, Clarendon, 1916.
- The characteristic numbers of a real algebraic plane curve, *Rend. Circ. Palermo*, 1917
- *The geometry of the complex domain*, Oxford, OUP, 1924
- Questioni di geometria nel campo complesso, *Rend Roma*, 1928.
- *A Treatise on algebraic plane curves*, Clarendon, 1931.

## The interruption of international exchanges

*La formation des professeurs des écoles moyennes supérieures a certainement une grande importance .... J'espère que mon ami Loria voudra accepter la tâche que vous désirez lui confier. A Stockholm il faudra présenter une vue d'ensemble de notre enquête. ... J'ai préparé, en suivant vos instructions, le discours (assez courte) que je dois prononcer à Paris en votre lieu.*

*Je comprends et j'apprécie les motifs qui vous ont inspiré. Mais, d'accord avec M. Smith, et dans l'intérêt de notre Commission, je vous prie de vouloir bien renoncer pour le moment à mettre à effet votre propos. ... D'ailleurs le moment grave que traversent toutes les institutions internationales conseille de n'introduire aucun changement dans leur organisation de crainte que ces faibles organismes ne doivent succomber. Il faut au contraire s'effacer de les faire survivre jusqu'à la conclusion de la paix, à fin qu'elles puissent faciliter la reprise des relations normales entre les peuples, dès que la guerre sera terminée.*

[**G. Castelnuovo to F. Klein**, 3.3.1914 and 10.3.1915, Luciano-Roero 2012, p. 208-209, 212-213 ]



### The *Encyklopädie der Mathematischen Wissenschaften* (1912-1920)

*Above all we will try, even though we are not directly involved in the actual circumstances, to assure the survival of our scientific undertakings. This refers especially to the work on the mathematical encyclopaedia. I am happy to hear from Mohrmann that the completion of the essays written by you and Enriques on algebraic curves are coming to a good end. Having already taken charge of the chapter on correspondences, Mohrmann first of all approached Berzolari, whose previous careful work had earned him the special sympathy of the editorial team of the third volume. The article by Loria is a good as finished, the very detailed and extremely carefully crafted article by Segre is in the phase of being translated by Mohrmann. I hope that you are well in this critical period. We are all involved in these immense events, when not personally, then through the involvement of members of our family, but this is not the place to comment on that.*

[F. Klein to G. Castelnuovo, 4.3.1915, Luciano-Roero 2012, p. 209-211]

### Bibliography

- L. Giacardi – C.S. Roero, *Bibliotheca Mathematica*, Torino 1987
- C.S. Roero (ed.) *La Facoltà di Scienze Matematiche Fisiche Naturali di Torino 1848-1998*, vol. 1, *Ricerca, Insegnamento, Collezioni scientifiche*, vol. 2, *I docenti*, Torino 1999
- E. Luciano - C. S. Roero *Giuseppe Peano Matematico e Maestro*, Torino 2008
- E. Luciano - C. S. Roero *From Turin to Göttingen: dialogues and correspondence (1879-1923)*, Boll. Storia delle Scienze Matematiche, 31, 2012, pp. 1-232
- C. S. Roero *Guarino Guarini and Universal Mathematics*, Nexus Network Journal, 11, 3, 2009, pp. 415-439
- C. S. Roero (ed.) *Giuseppe Peano e la sua Scuola fra matematica, logica e interlingua. Atti del Congresso internazionale di studi Torino, 6-7 ottobre 2008*, Torino 2010
- F. Skof (ed.) *Giuseppe Peano between Mathematics and logic*, Milan 2011
- C. S. Roero (ed.) *Dall'Università di Torino all'Italia unita*, Torino 2013