

**Esercizio 1.** The language  $L$  contains only the binary relations  $<$  and  $e$ . The theory  $T_0$  says that  $<$  is a strict linear order and that  $e$  is an equivalence relation. Let  $\mathcal{M}$  consist of models of  $T_0$  and partial isomorphisms.

1. Do rich models exist?
2. Can we axiomatize their theory  $T_1$ ?
3. If so, does  $T_1$  have elimination of quantifiers?
4. Is  $T_1$   $\lambda$ -categorical for some  $\lambda$ ?

**Esercizio 2.** Let  $T_0$  and  $\mathcal{M}$  be as in Example 7.15 except that we restrict the language to the relations  $r_0, \dots, r_n$  for a fixed  $n$ .

1. Do  $\omega$ -rich models of  $T_0$  exist? If so, let  $T_1$  be the set of sentences that hold in all rich model.
2. Does  $T_1$  has elimination of quantifiers?
3. Is  $T_1$   $\omega$ -categorical?

Answer the questions above if we add to the language a constant 0 to the language. Answer the questions above when we drop the axioms  $\neg\exists x [r_n(x) \wedge r_m(x)]$ . (Rispondere sinteticamente.)