

Exercise 1. The language contains only a symbol for a binary relation e . The theory T says that e is an equivalence relation and that for each $n \in \omega \setminus \{0\}$ there are 2 classes containing n elements.

Most of the following questions have a short answer.

1. Show that every saturated model of T contains a class with infinitely many elements.
2. Show that every model countable model of T that has infinitely many infinite classes is saturated.
3. Is the previous claim true for uncountable models?
4. Prove that the theory T has quantifier elimination.
5. Is T countably categorical?
6. Is T categorical in some uncountable cardinal?
7. Is T complete?
8. What is $\text{acl}(\emptyset)$?
9. Let $\mathcal{U} \models T$ be saturated. If $e(a, \mathcal{U})$ contains 2 elements, what is $\text{dcl}\{a\}$?
10. Let $e(b, \mathcal{U})$ be infinite, what is $\text{acl}\{b\}$?
11. If b is like above, what is the orbit of b under $\text{Aut}(\mathcal{U})$?
12. Is T strongly minimal?