

**Exercise 1.** The language contains only a symbol for a binary relation  $e$ . The theory  $T$  says that  $e$  is an equivalence relation and that for each  $n \in \omega \setminus \{0\}$  there are 2 classes containing  $n$  elements.

Most of the following questions have a short answer.

1. Is every countable model of  $T$  with infinitely many infinite classes saturated?
2. Is every uncountable model of  $T$  with infinitely many infinite classes saturated?
3. Describe a non homogeneous model of  $T$ .
4. Sketch a proof that the theory  $T$  has quantifier elimination.
5. Is  $T$  countably categorical?
6. Is  $T$  categorical in some uncountable cardinal?
7. Is  $T$  complete?
8. What is  $\text{acl}(\emptyset)$ ?
9. Let  $\mathcal{U} \models T$  be saturated. If  $e(a, \mathcal{U})$  contains 2 elements, what is  $\text{dcl}\{a\}$ ?
10. Let  $e(b, \mathcal{U})$  be infinite, what is  $\text{acl}\{b\}$ ?
11. If  $b$  is like above, what is the orbit of  $b$  under  $\text{Aut}(\mathcal{U})$ ?
12. Is  $T$  strongly minimal?