**Esercizio 1.** Let M be a group. Given a 2-coloring of  $M^{(2)}$  prove that there is a sequence  $\langle a_i : i < \omega \rangle$  such that the set of pairs  $\{ \prod a \upharpoonright I, \prod a \upharpoonright J \}$  for any I < J subsets of  $\omega$  is monocromatic. By  $\prod \langle a_1, \ldots, a_n \rangle$  we denote the product  $a_1 \cdots a_n$ .

**Esercizio 2.** Let A be a coheir extension base. Prove that for every  $b \in \mathcal{U}^z$  there is a structure  $\mathcal{V} \leq \mathcal{U}$  isomorphic to  $\mathcal{U}$  over A such that  $\mathcal{V} \downarrow_M b$  for every  $A \subseteq M \leq \mathcal{V}$ .

**Esercizio 3.** Let  $\varphi(x;z) \in L$ . Let  $p(x) \in S(\mathcal{U})$  be finitely satisfied in every  $M \supseteq A$ . Prove that if  $\mathcal{D}_{p,\varphi}$  is saturated. We say that  $\mathcal{D} \subseteq \mathcal{U}^x$  is saturated when the model  $\mathcal{U}$  expanded with a predicate for  $\mathcal{D}$  is saturated (in the expanded language).

**Esercizio 4.** Prove that the equivalence relation  $a \stackrel{\mathbb{L}}{=}_A b$  is the transitive closure of the relation: there is a sequence  $\langle c_i : i < \omega \rangle$  indiscernible over A such that  $c_0 = a$  and  $c_1 = b$ .

**Esercizio 5.** Let  $G = \{ f \in \text{Aut}(\mathcal{U}/A) : f\mathcal{D} = \mathcal{D} \text{ for every } \mathcal{D} \text{ with } o(\mathcal{D}/A) \text{ bounded} \}.$  Prove that  $G = \text{Aut}^{f}(\mathcal{U}/A)$ .