

Dominic Farolino

Math Logic Assignment 3 2/8/2019

5.3) #5:

$(A \vee B) \wedge (C \vee D) \wedge (E \vee F)$ in DNF.

✓ $(A \wedge C \wedge E) \vee (A \wedge C \wedge F) \vee (A \wedge D \wedge E) \vee (A \wedge D \wedge F) \vee (B \wedge C \wedge E) \vee (B \wedge C \wedge F) \vee (B \wedge D \wedge E) \vee (B \wedge D \wedge F)$

Trivial going from CNF \Rightarrow DNF.

6.4 Section Exercises

1.)

A	B	$A \rightarrow B$	$\neg A \vee B$	$\neg(A \wedge \neg B)$
T	T	T	T	T
T	F	F	F	F
F	T	T	T	T
F	F	T	T	T

Equal Values ✓

2.)

A	B	C	$A \rightarrow B$	$B \wedge C$	$B \wedge C \rightarrow A$	$(A \rightarrow B) \wedge (B \wedge C \rightarrow A)$
T	T	T	T	T	T	T
T	T	F	T	F	T	T
T	F	T	F	F	T	F
T	F	F	F	F	T	F
F	T	T	T	T	F	F
F	T	F	T	F	T	T
F	F	T	T	F	T	F
F	F	F	T	F	T	T

✓

3.) $A \rightarrow B$ and $\neg B \rightarrow \neg A$

A	B	$A \rightarrow B$	$\neg B \rightarrow \neg A$
T	T	T	T
T	F	F	F
F	T	T	T
F	F	T	F

Equal Values ✓

4.) $A \rightarrow B \vee C, \neg B \rightarrow \neg C \models A \rightarrow B$

$$\{A \wedge B \vee C, \neg B \rightarrow \neg C\} \models A \rightarrow B$$

A	B	C	$B \vee C$	$A \rightarrow B \vee C$	$\neg B \rightarrow \neg C$	$A \rightarrow B$	
T	T	T	T	T	T	T	✓
T	T	F	T	T	T	T	✓
T	F	T	T	T	F	F	
T	F	F	F	F	T	F	
F	T	T	T	T	T	T	✓
F	T	F	T	T	T	T	✓
F	F	T	T	T	F	T	
F	F	F	F	F	F	T	✓

$C \rightarrow B$