



FRIEDRICH-ALEXANDER-  
UNIVERSITÄT  
ERLANGEN-NÜRNBERG  
SCHOOL OF ENGINEERING

# Recurrent Neural Networks

**Leonid Mill**, Tobias Würfl, Katharina Breininger, Nishant Ravikumar, Sebastian Gündel, Mathis Hoffmann, Florian Thamm, Felix Denzinger  
Pattern Recognition Lab, Friedrich-Alexander University of Erlangen-Nürnberg  
October 30, 2018



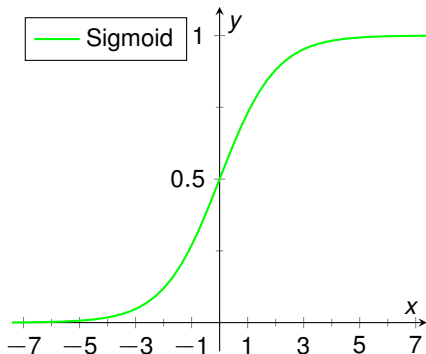


FRIEDRICH-ALEXANDER-  
UNIVERSITÄT  
ERLANGEN-NÜRNBERG  
SCHOOL OF ENGINEERING

# Activation Functions



## Sigmoid Activation Function



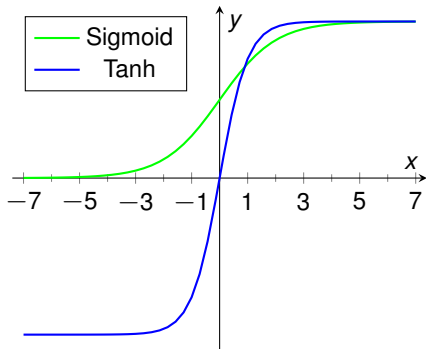
Sigmoid (logistic function)

$$f(x) = \frac{1}{1 + \exp(-x)}$$

$$f'(x) = f(x)(1 - f(x))$$

→ Observe that the derivative can be solely expressed in terms of the activation!

## Tanh Activation Function



Tanh

$$f(x) = \tanh(x)$$

$$f'(x) = 1 - f(x)^2$$

→ The derivative is still a function of the activation!



FRIEDRICH-ALEXANDER-  
UNIVERSITÄT  
ERLANGEN-NÜRNBERG  
SCHOOL OF ENGINEERING

# Elman Recurrent Neural Network



## General strategy

- We interpret the **batch** dimension as **time** dimension now

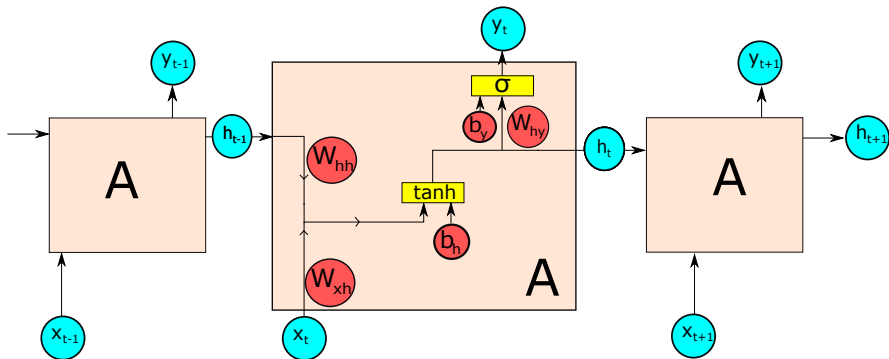
## General strategy

- We interpret the **batch** dimension as **time** dimension now
- Samples are correlated in this dimension

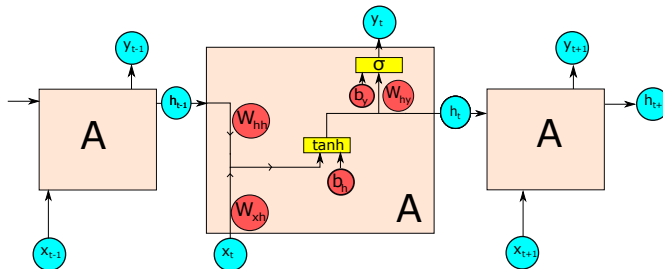
## General strategy

- We interpret the **batch** dimension as **time** dimension now
- Samples are correlated in this dimension
- This allows to **reuse** loss functions, optimizers, initializers, activation functions and the Neural Network class





## Elman RNN Cell



Output formula:

$$\mathbf{y}_t = \sigma(\mathbf{h}_t \cdot \mathbf{W}_{hy} + \mathbf{b}_y)$$

$\mathbf{W}_{hy}$ : Weight matrix for current hidden state  $\mathbf{h}_t$

$\mathbf{b}_h$ : Output bias

## A word on software engineering

- In terms of **encapsulation** - how good was the idea to demand exposition of the weights as member?

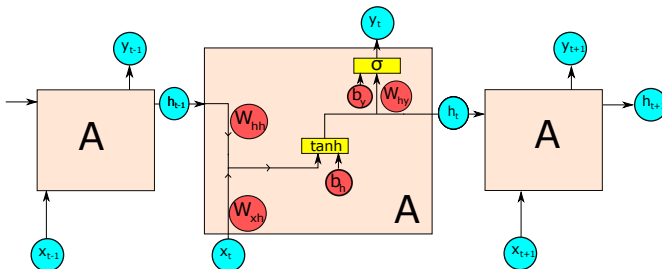
## A word on software engineering

- In terms of **encapsulation** - how good was the idea to demand exposition of the weights as member?
- Suppose we implement the RNN cell as **composite** structure
- **Getters** and **Setters** provide us the flexibility to do so

## A word on software engineering

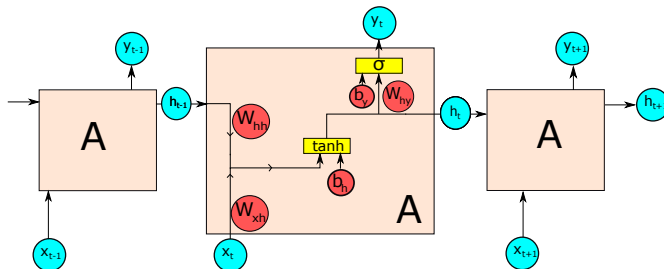
- In terms of **encapsulation** - how good was the idea to demand exposition of the weights as member?
- Suppose we implement the RNN cell as **composite** structure
- **Getters** and **Setters** provide us the flexibility to do so
- Takeaway? Not doing **proper software engineering** most of the time will demand a price at some point.

# Elman RNN Cell



$$\mathbf{h}_t = \tanh(\mathbf{h}_{t-1} \cdot \mathbf{W}_{hh} + \mathbf{x}_t \cdot \mathbf{W}_{xh} + \mathbf{b}_h)$$

# Elman RNN Cell



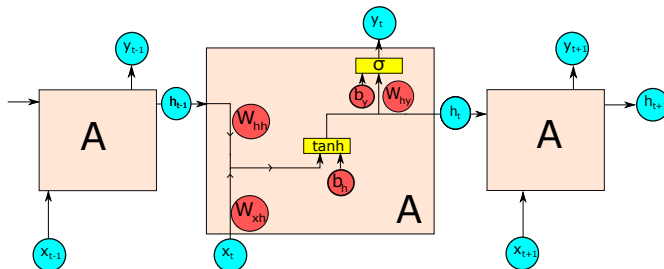
$$\mathbf{h}_t = \tanh(\mathbf{h}_{t-1} \cdot \mathbf{W}_{hh} + \mathbf{x}_t \cdot \mathbf{W}_{xh} + \mathbf{b}_h)$$

$\mathbf{W}_{hh}$ : Weight matrix for previous hidden state  $\mathbf{h}_{t-1}$

$\mathbf{W}_{xh}$ : Weight matrix for current input  $\mathbf{x}_t$

$\mathbf{b}_h$ : Update bias

# Elman RNN Cell



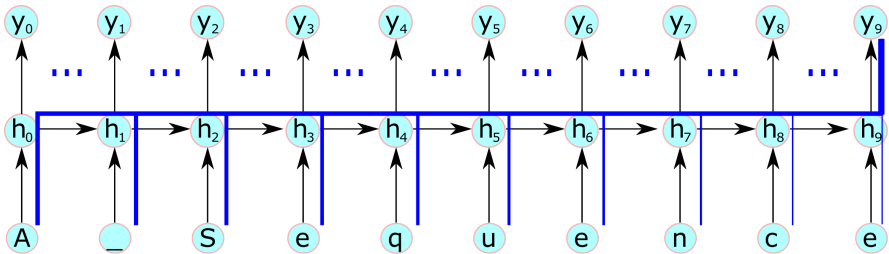
$$h_t = \tanh(\tilde{x}_t \cdot W_h)$$

$W_h$ : Weight matrix of a fully connected layer

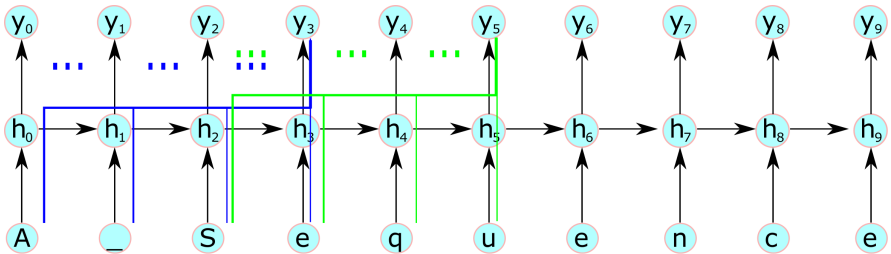
$\tilde{x}_t$ : Concatenation of  $x_t$ ,  $h_{t-1}$  and a 1

Different from output: Not processed independently!





- Implemented by passing the whole sequence as a **batch**



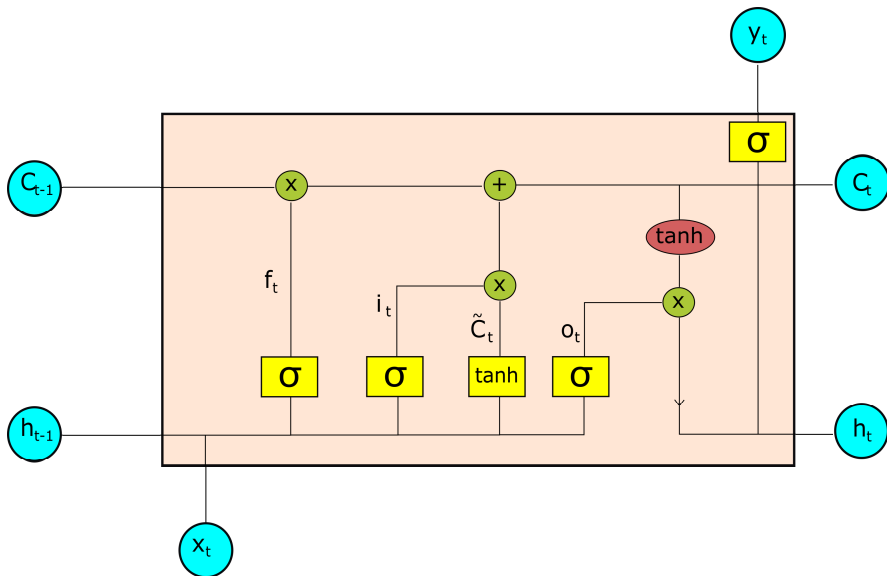
- Implemented by passing **overlapping** parts as a **batch**
- We need to implement memory **Between states**
- Simply store the **last hidden state** and implement a **method** switching whether this state is reused in subsequent forward passes.
- Data has to be fed in **accordingly!**



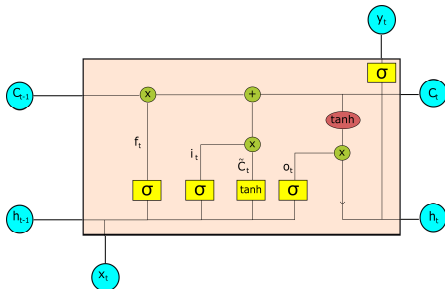
FRIEDRICH-ALEXANDER-  
UNIVERSITÄT  
ERLANGEN-NÜRNBERG  
SCHOOL OF ENGINEERING

# Long Short-Term Memory



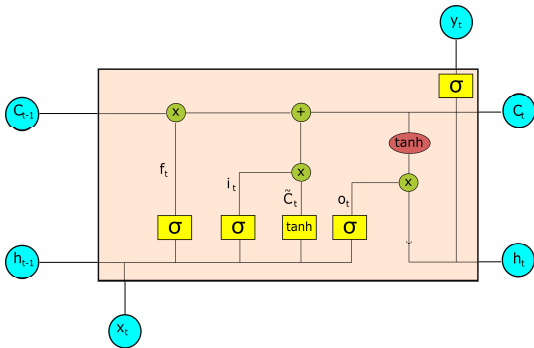


## Forward



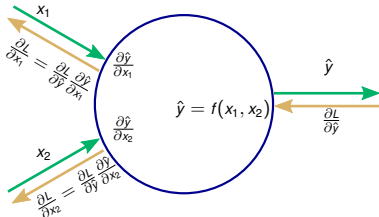
- We can reuse a **fully connected** layer again to for the **output**
- The **concatenation** is also **analogous** to the RNN
- The gates  $\sigma$  and the yellow  $\tanh$  can be a single **fully connected** layer with an output size of  $4 \cdot \text{dim}(\text{hidden state})$
- Remember that we have to pass the vectors of the input tensor **sequentially**

## Backward



- Most gradients are again handled by the **embedded layers**
- Again **store and feed the values for backprop externally** to the embedded layers because of **multiple calls to forward**
- We need gradients through **summation, multiplication and copying**

## Backward



Sum

Multiply

Copy

$$f(x_1, x_2) = x_1 + x_2$$

$$\frac{\partial \hat{y}}{\partial x_1} = 1$$

$$f(x_1, x_2) = x_1 \cdot x_2$$

$$\frac{\partial \hat{y}}{\partial x_1} = x_2$$

Backward pass of sum  
So the gradient is a sum!

Gradient is **copying**  $\frac{\partial L}{\partial \hat{y}}$

Gradient is  $\cdot$  with **switched**  
**inputs**



Thanks for listening.  
**Any questions?**