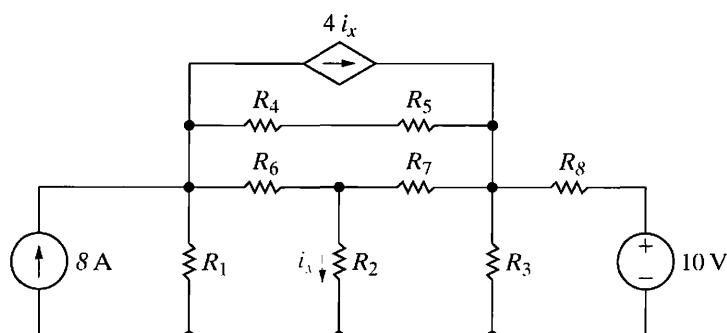


# Problems

## Section 4.1

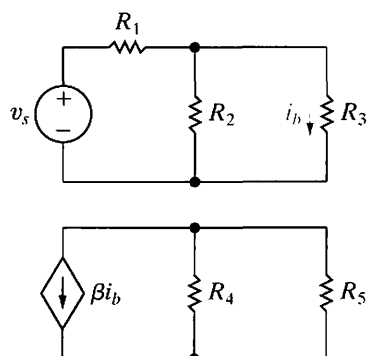
- 4.1** For the circuit shown in Fig. P4.1, state the numerical value of the number of (a) branches, (b) branches where the current is unknown, (c) essential branches, (d) essential branches where the current is unknown, (e) nodes, (f) essential nodes, and (g) meshes.

Figure P4.1



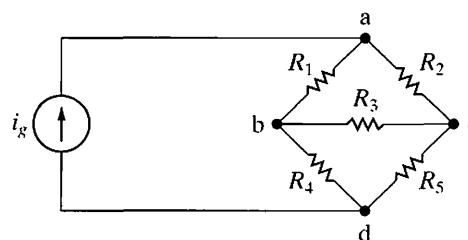
- 4.2** a) If only the essential nodes and branches are identified in the circuit in Fig. P4.1, how many simultaneous equations are needed to describe the circuit?  
 b) How many of these equations can be derived using Kirchhoff's current law?  
 c) How many must be derived using Kirchhoff's voltage law?  
 d) What two meshes should be avoided in applying the voltage law?
- 4.3** a) How many separate parts does the circuit in Fig. P4.3 have?  
 b) How many nodes?  
 c) How many branches are there?  
 d) Assume that the lower node in each part of the circuit is joined by a single conductor. Repeat the calculations in (a)–(c).

Figure P4.3



- 4.4** Assume the current  $i_g$  in the circuit in Fig. P4.4 is known. The resistors  $R_1 - R_5$  are also known.  
 a) How many unknown currents are there?  
 b) How many independent equations can be written using Kirchhoff's current law (KCL)?  
 c) Write an independent set of KCL equations.  
 d) How many independent equations can be derived from Kirchhoff's voltage law (KVL)?  
 e) Write a set of independent KVL equations.

Figure P4.4



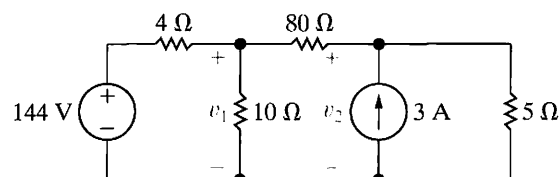
- 4.5** A current leaving a node is defined as positive.  
 a) Sum the currents at each node in the circuit shown in Fig. P4.4.  
 b) Show that any one of the equations in (a) can be derived from the remaining three equations.

## Section 4.2

- 4.6** Use the node-voltage method to find  $v_1$  and  $v_2$  in the circuit in Fig. P4.6.

PSPICE  
MULTISIM

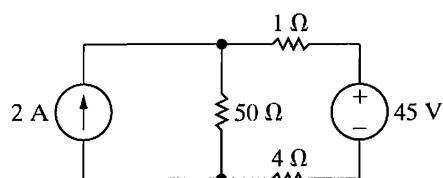
Figure P4.6



- 4.7** Use the node-voltage method to find how much power the 2 A source extracts from the circuit in Fig. P4.7.

PSPICE  
MULTISIM

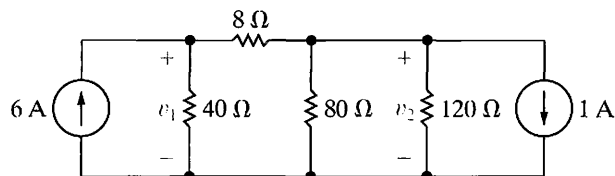
Figure P4.7



- 4.8** Use the node-voltage method to find  $v_1$  and  $v_2$  in the circuit shown in Fig. P4.8.

PSPICE  
MULTISIM

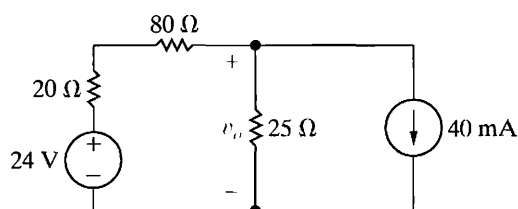
Figure P4.8



- 4.9** Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.9.

PSPICE  
MULTISIM

Figure P4.9



- 4.10** a) Find the power developed by the 40 mA current source in the circuit in Fig. P4.9.

PSPICE  
MULTISIM

- b) Find the power developed by the 24 V voltage source in the circuit in Fig. P4.9.  
c) Verify that the total power developed equals the total power dissipated.

- 4.11** A 50 Ω resistor is connected in series with the 40 mA current source in the circuit in Fig. P4.9.

PSPICE  
MULTISIM

- a) Find  $v_o$ .  
b) Find the power developed by the 40 mA current source.  
c) Find the power developed by the 24 V voltage source.  
d) Verify that the total power developed equals the total power dissipated.  
e) What effect will any finite resistance connected in series with the 40 mA current source have on the value of  $v_o$ ?

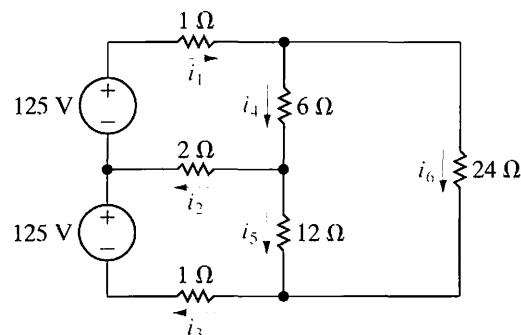
- 4.12** The circuit shown in Fig. P4.12 is a dc model of a residential power distribution circuit.

PSPICE  
MULTISIM

- a) Use the node-voltage method to find the branch currents  $i_1 - i_6$ .

- b) Test your solution for the branch currents by showing that the total power dissipated equals the total power developed.

Figure P4.12

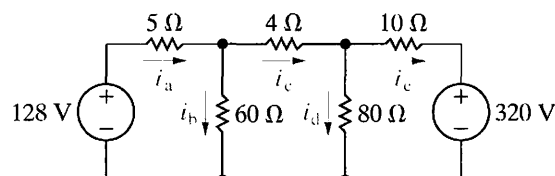


- 4.13** a) Use the node-voltage method to find the branch currents  $i_a - i_e$  in the circuit shown in Fig. P4.13.

PSPICE  
MULTISIM

- b) Find the total power developed in the circuit.

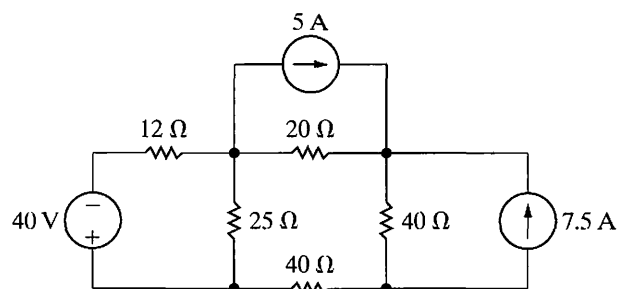
Figure P4.13



- 4.14** Use the node-voltage method to find the total power dissipated in the circuit in Fig. P4.14.

PSPICE  
MULTISIM

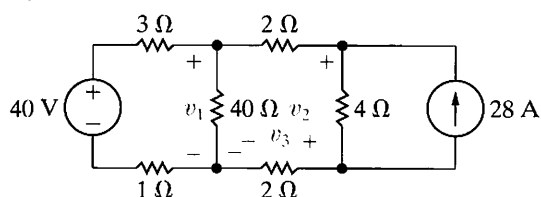
Figure P4.14



- 4.15** a) Use the node-voltage method to find  $v_1$ ,  $v_2$ , and  $v_3$  in the circuit in Fig. P4.15.  
 b) How much power does the 40 V voltage source deliver to the circuit?

PSPICE  
MULTISIM

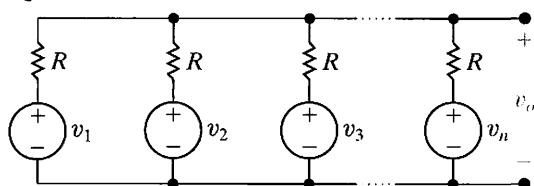
Figure P4.15



- 4.16** a) Use the node-voltage method to show that the output voltage  $v_o$  in the circuit in Fig. P4.16 is equal to the average value of the source voltages.  
 b) Find  $v_o$  if  $v_1 = 100$  V,  $v_2 = 80$  V, and  $v_3 = -60$  V.

PSPICE  
MULTISIM

Figure P4.16

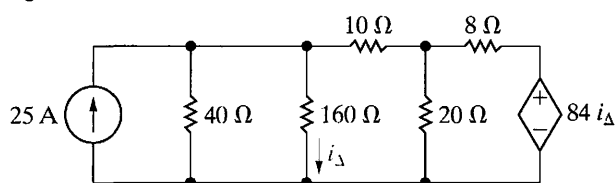


## Section 4.3

- 4.17** a) Use the node-voltage method to find the total power developed in the circuit in Fig. P4.17.  
 b) Check your answer by finding the total power absorbed in the circuit.

PSPICE  
MULTISIM

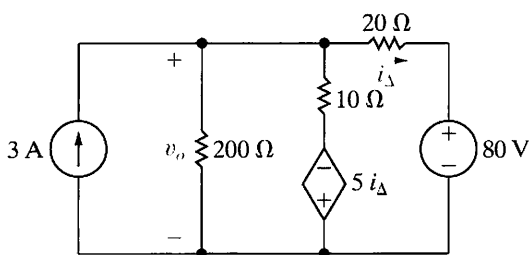
Figure P4.17



- 4.18** a) Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.18.  
 b) Find the power absorbed by the dependent source.  
 c) Find the total power developed by the independent sources.

PSPICE  
MULTISIM

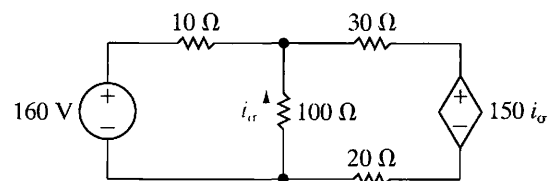
Figure P4.18



- 4.19** Use the node-voltage method to calculate the power delivered by the dependent voltage source in the circuit in Fig. P4.19.

PSPICE  
MULTISIM

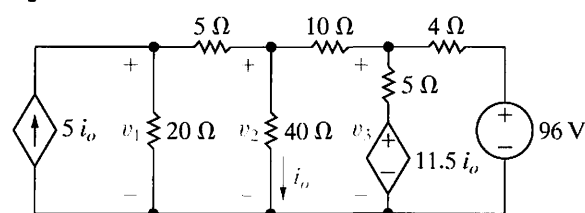
Figure P4.19



- 4.20** a) Find the node voltages  $v_1$ ,  $v_2$ , and  $v_3$  in the circuit in Fig. P4.20.  
 b) Find the total power dissipated in the circuit.

PSPICE  
MULTISIM

Figure P4.20

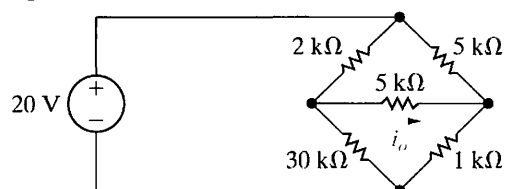


## Section 4.4

- 4.21** Use the node-voltage method to find  $i_o$  in the circuit in Fig. P4.21.

PSPICE  
MULTISIM

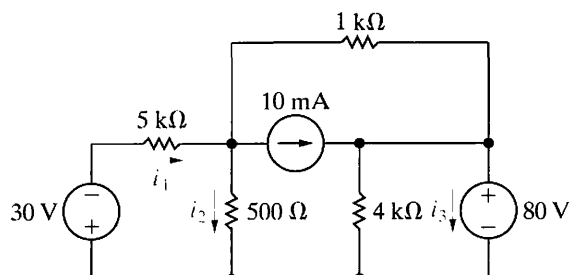
Figure P4.21



- 4.22** a) Use the node-voltage method to find the branch currents  $i_1$ ,  $i_2$ , and  $i_3$  in the circuit in Fig. P4.22.  
 b) Check your solution for  $i_1$ ,  $i_2$ , and  $i_3$  by showing that the power dissipated in the circuit equals the power developed.

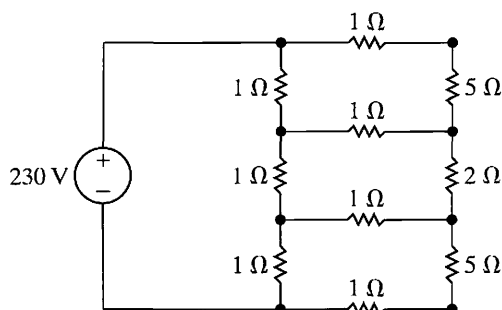
PSPICE  
MULTISIM

Figure P4.22



- 4.23 a) Use the node-voltage method to find the power dissipated in the  $2\ \Omega$  resistor in the circuit in Fig. P4.23.  
b) Find the power supplied by the  $230\text{ V}$  source.

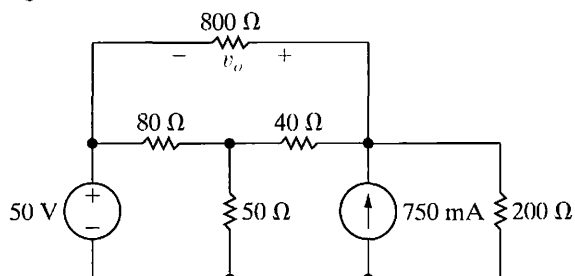
Figure P4.23



- 4.24 Use the node-voltage method to find the value of  $v_o$  in the circuit in Fig. P4.24.

PSPICE  
MULTISIM

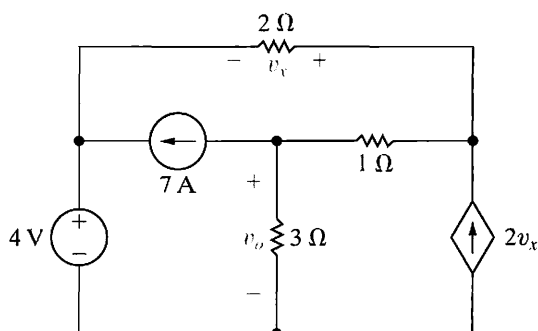
Figure P4.24



- 4.25 Use the node-voltage method to find the value of  $v_o$  in the circuit in Fig. P4.25.

PSPICE  
MULTISIM

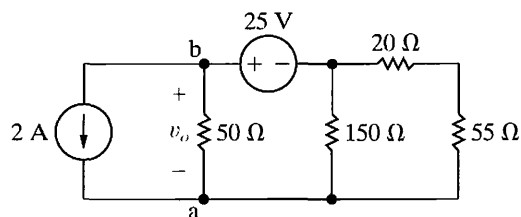
Figure P4.25



- 4.26 a) Use the node-voltage method to find  $v_o$  and the power delivered by the  $2\text{ A}$  current source in the circuit in Fig. P4.26. Use node a as the reference node.  
b) Repeat part (a), but use node b as the reference node.  
c) Compare the choice of reference node in (a) and (b). Which is better, and why?

PSPICE  
MULTISIM

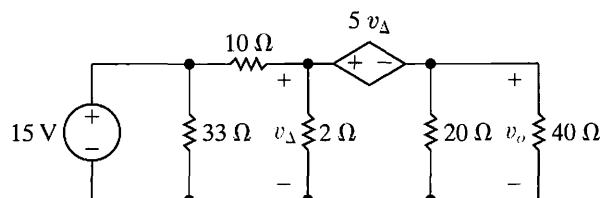
Figure P4.26



- 4.27 Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.27.

PSPICE  
MULTISIM

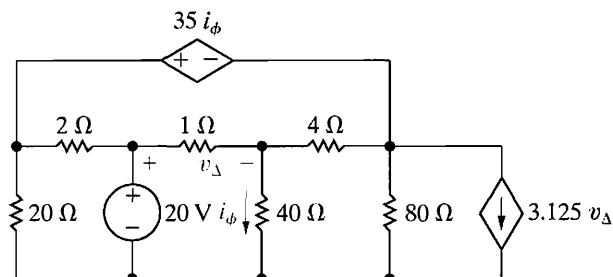
Figure P4.27



- 4.28 Use the node-voltage method to find the power developed by the  $20\text{ V}$  source in the circuit in Fig. P4.28.

PSPICE  
MULTISIM

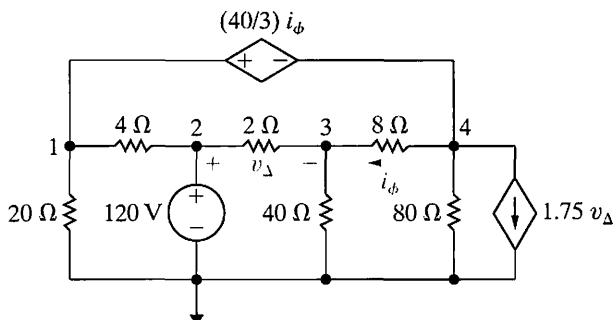
Figure P4.28



- 4.29 Assume you are a project engineer and one of your staff is assigned to analyze the circuit shown in Fig. P4.29. The reference node and node numbers given on the figure were assigned by the analyst. Her solution gives the values of  $v_3$  and  $v_4$  as  $108\text{ V}$  and  $81.6\text{ V}$ , respectively.

Test these values by checking the total power developed in the circuit against the total power dissipated. Do you agree with the solution submitted by the analyst?

Figure P4.29



- 4.30** Show that when Eqs. 4.16, 4.17, and 4.19 are solved for  $i_B$ , the result is identical to Eq. 2.25.

### Section 4.5

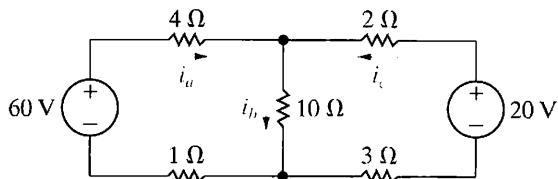
- 4.31** Solve Problem 4.12 using the mesh-current method.

- 4.32** Solve Problem 4.13 using the mesh-current method.

- 4.33** a) Use the mesh-current method to find the branch currents  $i_a$ ,  $i_b$ , and  $i_c$  in the circuit in Fig. P4.33.  
b) Repeat (a) if the polarity of the 60 V source is reversed.

PSPICE  
MULTISIM

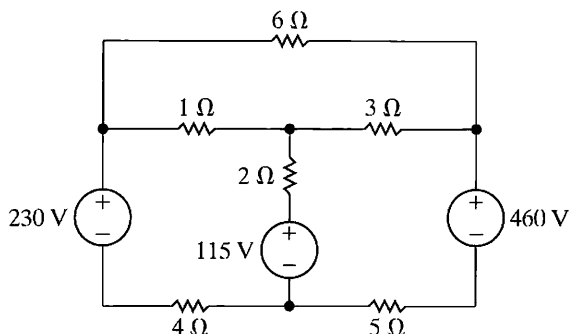
Figure P4.33



- 4.34** a) Use the mesh-current method to find the total power developed in the circuit in Fig. P4.34.  
b) Check your answer by showing that the total power developed equals the total power dissipated.

PSPICE  
MULTISIM

Figure P4.34



- 4.35** Solve Problem 4.21 using the mesh-current method.

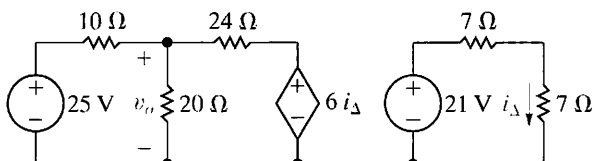
- 4.36** Solve Problem 4.23 using the mesh-current method.

### Section 4.6

- 4.37** a) Use the mesh-current method to find  $v_o$  in the circuit in Fig. P4.37.  
b) Find the power delivered by the dependent source.

PSPICE  
MULTISIM

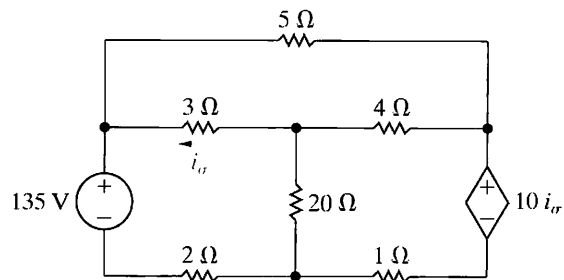
Figure P4.37



- 4.38** Use the mesh-current method to find the power dissipated in the 20 Ω resistor in the circuit in Fig. P4.38.

PSPICE  
MULTISIM

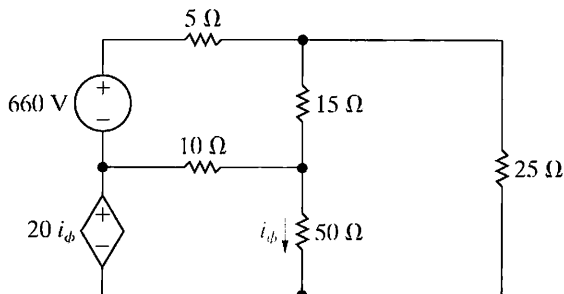
Figure P4.38



- 4.39** Use the mesh-current method to find the power delivered by the dependent voltage source in the circuit seen in Fig. P4.39.

PSPICE  
MULTISIM

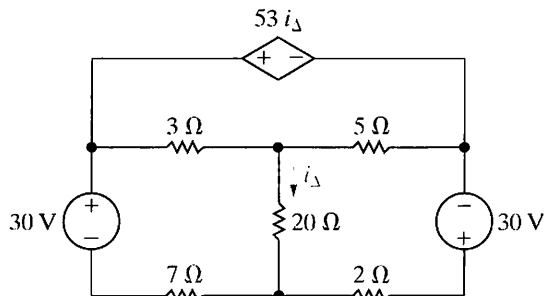
Figure P4.39



- 4.40** Use the mesh-current method to find the power developed in the dependent voltage source in the circuit in Fig. P4.40.

PSPICE  
MULTISIM

Figure P4.40



### Section 4.7

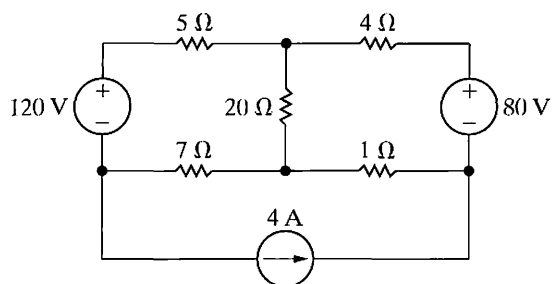
- 4.41** Solve Problem 4.8 using the mesh-current method.

- 4.42** a) Use the mesh-current method to find how much power the 4 A current source delivers to the circuit in Fig. P4.42.

- b) Find the total power delivered to the circuit.

- c) Check your calculations by showing that the total power developed in the circuit equals the total power dissipated

Figure P4.42

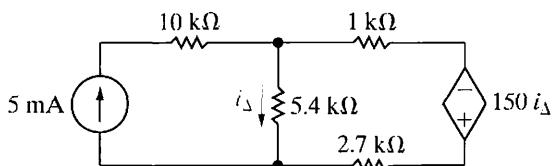


4.43 Solve Problem 4.20 using the mesh-current method.

- 4.44 a) Use the mesh-current method to solve for  $i_\Delta$  in the circuit in Fig. P4.44.  
 b) Find the power delivered by the independent current source.  
 c) Find the power delivered by the dependent voltage source.

PSPICE  
MULTISIM

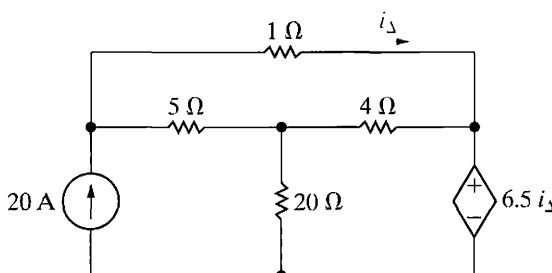
Figure P4.44



4.45 Use the mesh-current method to find the total power developed in the circuit in Fig. P4.45.

PSPICE  
MULTISIM

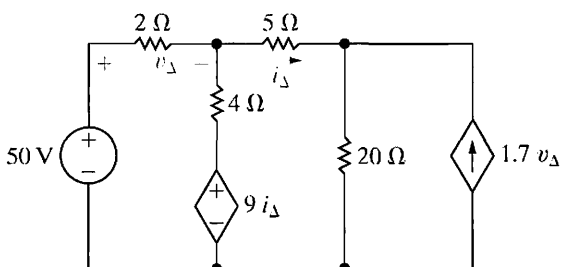
Figure P4.45



- 4.46 a) Use the mesh-current method to determine which sources in the circuit in Fig. P4.46 are generating power.  
 b) Find the total power dissipated in the circuit.

PSPICE  
MULTISIM

Figure P4.46

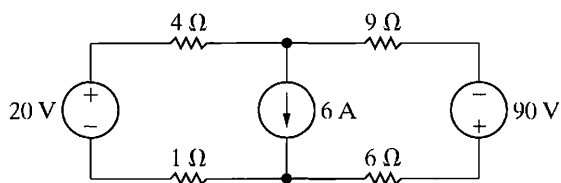


4.47 Solve Problem 4.22 using the mesh-current method.

4.48 Use the mesh-current method to find the total power dissipated in the circuit in Fig. P4.48.

PSPICE  
MULTISIM

Figure P4.48



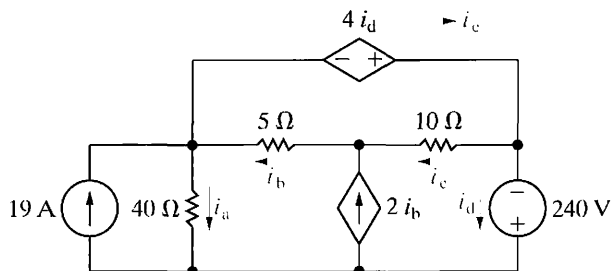
- 4.49 a) Assume the 20 V source in the circuit in Fig. P4.48 is changed to 60 V. Find the total power dissipated in the circuit.  
 b) Repeat (a) if the 6 A current source is replaced by a short circuit.  
 c) Explain why the answers to (a) and (b) are the same.

4.50 a) Find the branch currents  $i_a - i_c$  for the circuit shown in Fig. P4.50.

PSPICE  
MULTISIM

- b) Check your answers by showing that the total power generated equals the total power dissipated.

Figure P4.50

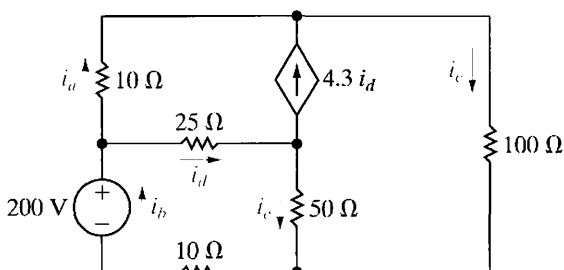


4.51 a) Use the mesh-current method to find the branch currents in  $i_a - i_e$  in the circuit in Fig. P4.51.

PSPICE  
MULTISIM

- b) Check your solution by showing that the total power developed in the circuit equals the total power dissipated.

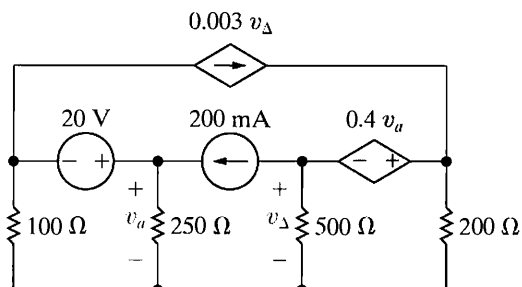
Figure P4.51



## Section 4.8

- 4.52** a) Would you use the node-voltage or mesh-current method to find the power absorbed by the 20 V source in the circuit in Fig. P4.52? Explain your choice.  
 b) Use the method you selected in (a) to find the power.

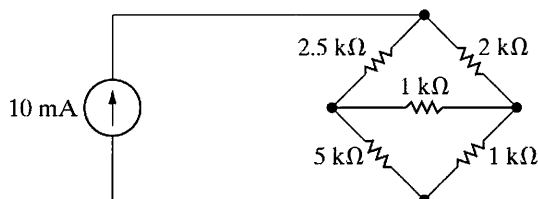
Figure P4.52



- 4.53** Assume you have been asked to find the power dissipated in the 1 kΩ resistor in the circuit in Fig. P4.53.

- a) Which method of circuit analysis would you recommend? Explain why.  
 b) Use your recommended method of analysis to find the power dissipated in the 1 kΩ resistor.  
 c) Would you change your recommendation if the problem had been to find the power developed by the 10 mA current source? Explain.  
 d) Find the power delivered by the 10 mA current source.

Figure P4.53



- 4.54** A 4 kΩ resistor is placed in parallel with the 10 mA current source in the circuit in Fig. P4.53. Assume you have been asked to calculate the power developed by the current source.

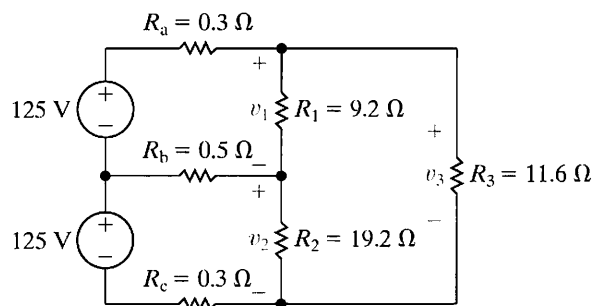
- a) Which method of circuit analysis would you recommend? Explain why.  
 b) Find the power developed by the current source.

- 4.55** The circuit in Fig. P4.55 is a direct-current version of a typical three-wire distribution system. The resistors  $R_a$ ,  $R_b$ , and  $R_c$  represent the resistances of the three conductors that connect the three loads  $R_1$ ,  $R_2$ , and  $R_3$  to the 125/250 V voltage supply. The

resistors  $R_1$  and  $R_2$  represent loads connected to the 125 V circuits, and  $R_3$  represents a load connected to the 250 V circuit.

- a) What circuit analysis method will you use and why?  
 b) Calculate  $v_1$ ,  $v_2$ , and  $v_3$ .  
 c) Calculate the power delivered to  $R_1$ ,  $R_2$ , and  $R_3$ .  
 d) What percentage of the total power developed by the sources is delivered to the loads?  
 e) The  $R_b$  branch represents the neutral conductor in the distribution circuit. What adverse effect occurs if the neutral conductor is opened? (Hint: Calculate  $v_1$  and  $v_2$  and note that appliances or loads designed for use in this circuit would have a nominal voltage rating of 125 V.)

Figure P4.55

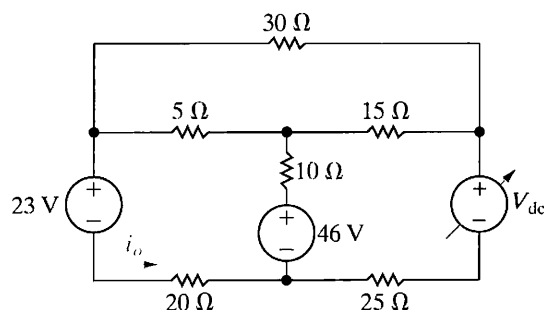


- 4.56** Show that whenever  $R_1 = R_2$  in the circuit in Fig. P4.55, the current in the neutral conductor is zero. (Hint: Solve for the neutral conductor current as a function of  $R_1$  and  $R_2$ .)

- 4.57** The variable dc voltage source in the circuit in Fig. P4.57 is adjusted so that  $i_o$  is zero.

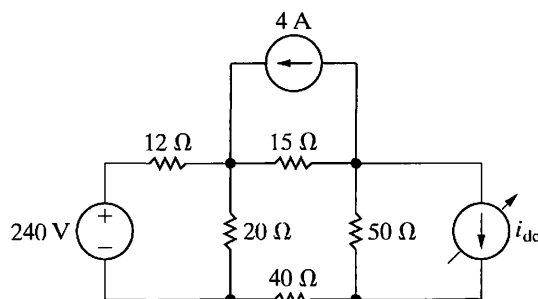
- a) Find the value of  $V_{dc}$ .  
 b) Check your solution by showing the power developed equals the power dissipated.

Figure P4.57



- 4.58** The variable dc current source in the circuit in Fig. P4.58 is adjusted so that the power developed by the 4 A current source is zero. Find the value of  $i_{dc}$ .

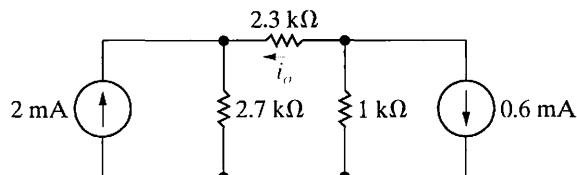
Figure P4.58



## Section 4.9

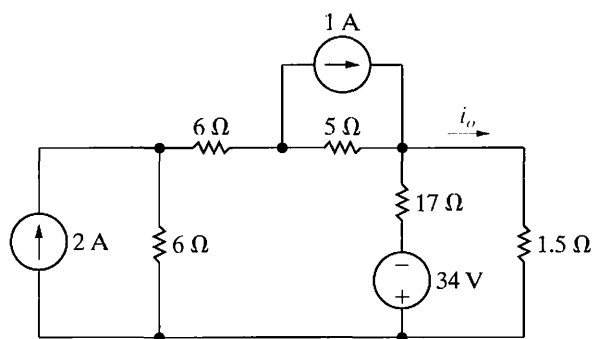
- 4.59** a) Use a series of source transformations to find the current  $i_o$  in the circuit in Fig. P4.59.  
b) Verify your solution by using the node-voltage method to find  $i_o$ .

Figure P4.59



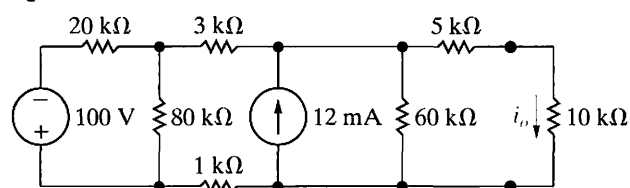
- 4.60** a) Use a series of source transformations to find  $i_o$  in the circuit in Fig. P4.60.  
b) Verify your solution by using the mesh-current method to find  $i_o$ .

Figure P4.60



- 4.61** a) Find the current in the 10 kΩ resistor in the circuit in Fig. P4.61 by making a succession of appropriate source transformations.  
b) Using the result obtained in (a), work back through the circuit to find the power developed by the 100 V source.

Figure P4.61

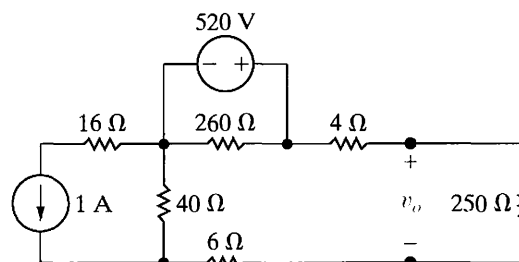


- 4.62** a) Use source transformations to find  $v_o$  in the circuit in Fig. P4.62.

PSPICE  
MULTISIM

- b) Find the power developed by the 520 V source.  
c) Find the power developed by the 1 A current source.  
d) Verify that the total power developed equals the total power dissipated.

Figure P4.62

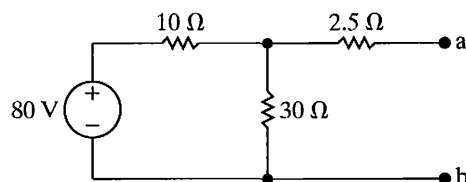


## Section 4.10

- 4.63** Find the Thévenin equivalent with respect to the terminals a,b for the circuit in Fig. P4.63.

PSPICE  
MULTISIM

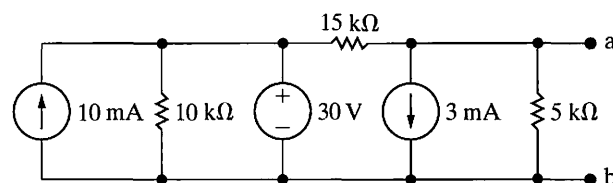
Figure P4.63



- 4.64** Find the Norton equivalent with respect to the terminals a,b in the circuit in Fig. P4.64.

PSPICE  
MULTISIM

Figure P4.64



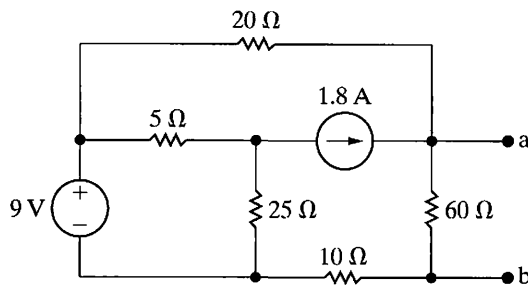
- 4.65** a) Find the Thévenin equivalent with respect to the terminals a,b for the circuit in Fig. P4.65 by finding the open-circuit voltage and the short-circuit current.

PSPICE  
MULTISIM

- b) Solve for the Thévenin resistance by removing the independent sources. Compare your result to the Thévenin resistance found in (a).



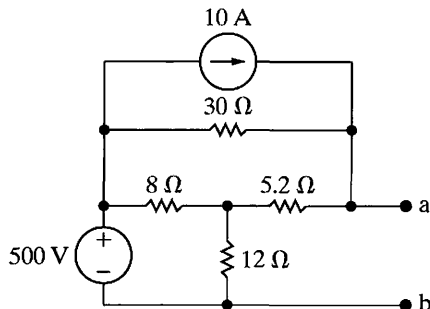
Figure P4.65



- 4.66** Find the Thévenin equivalent with respect to the terminals a,b for the circuit in Fig. P4.66.

PSPICE  
MULTISIM

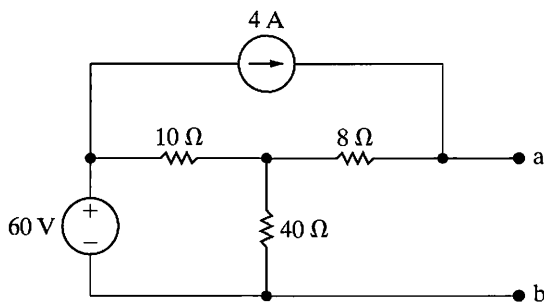
Figure P4.66



- 4.67** Find the Norton equivalent with respect to the terminals a,b for the circuit in Fig. P4.67.

PSPICE  
MULTISIM

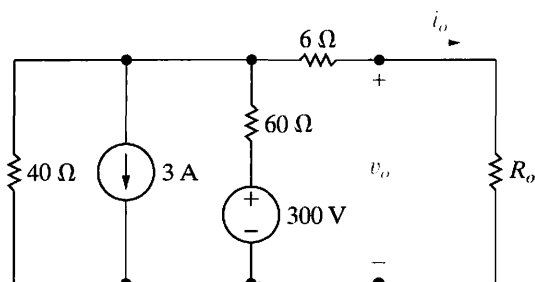
Figure P4.67



- 4.68** Determine  $i_o$  and  $v_o$  in the circuit shown in Fig. P4.68 when  $R_o$  is a resistor from Appendix H whose value is less than  $100\ \Omega$ .

PSPICE  
MULTISIM

Figure P4.68



- 4.69** An automobile battery, when connected to a car radio, provides 12.5 V to the radio. When connected to a set of headlights, it provides 11.7 V to the headlights. Assume the radio can be modeled as a  $6.25\ \Omega$  resistor and the headlights can be modeled as a  $0.65\ \Omega$  resistor. What are the Thévenin and Norton equivalents for the battery?

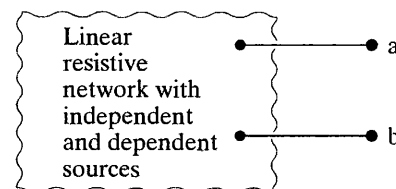
- 4.70** A Thévenin equivalent can also be determined from measurements made at the pair of terminals of interest. Assume the following measurements were made at the terminals a,b in the circuit in Fig. P4.70.

When a  $20\ \Omega$  resistor is connected to the terminals a,b, the voltage  $v_{ab}$  is measured and found to be 100 V.

When a  $50\ \Omega$  resistor is connected to the terminals a,b, the voltage is measured and found to be 200 V.

Find the Thévenin equivalent of the network with respect to the terminals a,b.

Figure P4.70

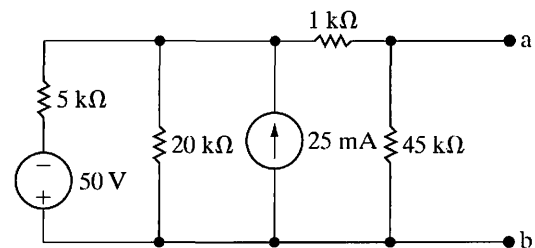


- 4.71** A voltmeter with a resistance of  $85.5\ \text{k}\Omega$  is used to measure the voltage  $v_{ab}$  in the circuit in Fig. P4.71.

PSPICE  
MULTISIM

- a) What is the voltmeter reading?  
b) What is the percentage of error in the voltmeter reading if the percentage of error is defined as  $[(\text{measured} - \text{actual})/\text{actual}] \times 100$ ?

Figure P4.71

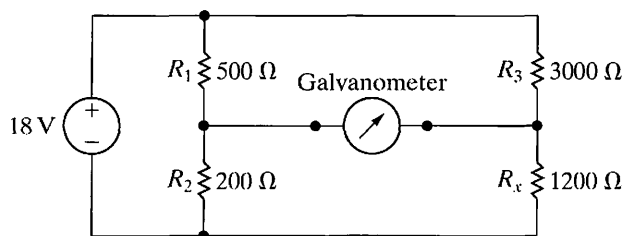


- 4.72** The Wheatstone bridge in the circuit shown in Fig. P4.72 is balanced when  $R_3$  equals  $3000\ \Omega$ . If the galvanometer has a resistance of  $50\ \Omega$ , how much current will the galvanometer detect, when the bridge is unbalanced by setting  $R_3$  to  $3003\ \Omega$ ? (Hint: Find the Thévenin equivalent with respect to the galvanometer terminals when  $R_3 = 3003\ \Omega$ . Note that once we have found this Thévenin equivalent, it is easy to find the amount of unbalanced

PSPICE  
MULTISIM

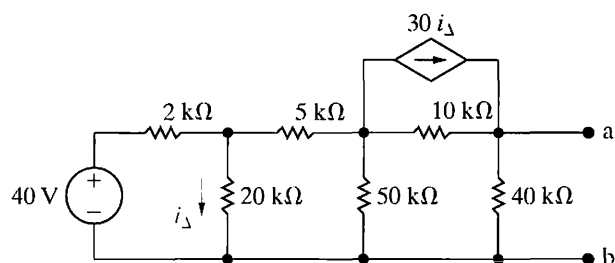
current in the galvanometer branch for different galvanometer movements.)

Figure P4.72



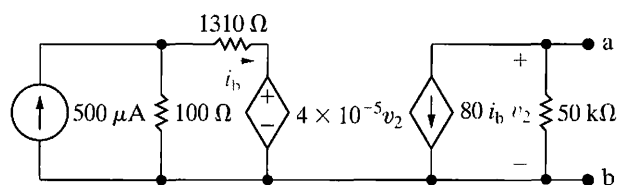
- 4.73** Find the Norton equivalent with respect to the terminals a,b for the circuit seen in Fig. P4.73.

Figure P4.73



- 4.74** Determine the Thévenin equivalent with respect to the terminals a,b for the circuit shown in Fig. P4.74.

Figure P4.74

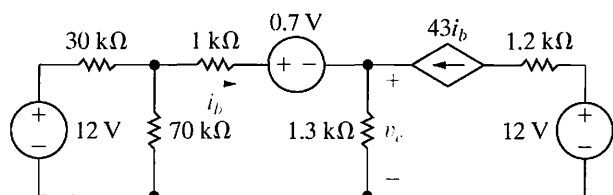


- 4.75** When a voltmeter is used to measure the voltage  $v_e$  in Fig. P4.75, it reads 5.5 V.

PSPICE  
MULTISIM

- What is the resistance of the voltmeter?
- What is the percentage of error in the voltage measurement?

Figure P4.75

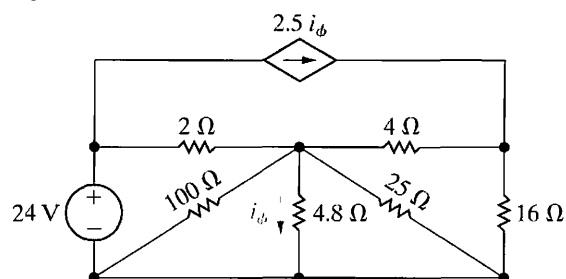


- 4.76** When an ammeter is used to measure the current  $i_\phi$  in the circuit shown in Fig. P4.76, it reads 6 A.

PSPICE  
MULTISIM

- What is the resistance of the ammeter?
- What is the percentage of error in the current measurement?

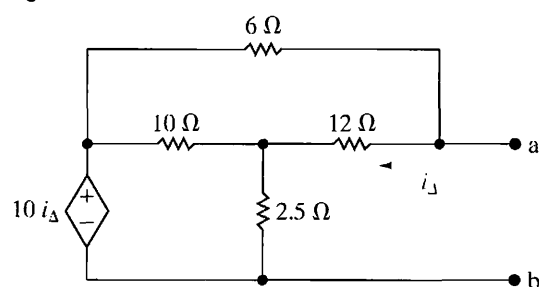
Figure P4.76



## Section 4.11

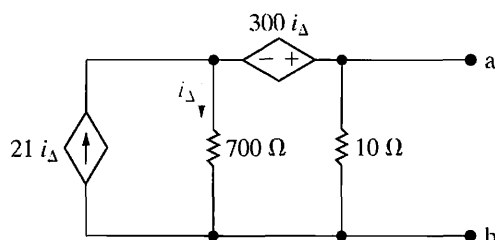
- 4.77** Find the Thévenin equivalent with respect to the terminals a,b in the circuit in Fig. P4.77.

Figure P4.77



- 4.78** Find the Norton equivalent with respect to the terminals a,b for the circuit seen in Fig. P4.78.

Figure P4.78



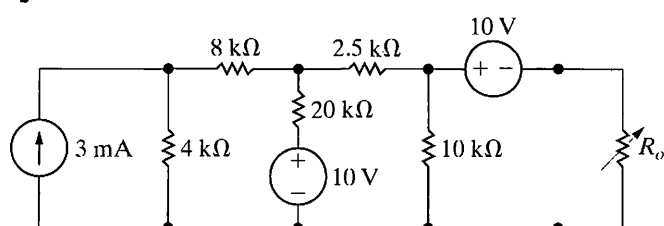
## Section 4.12

- 4.79** The variable resistor in the circuit in Fig. P4.79 is adjusted for maximum power transfer to  $R_o$ .

PSPICE  
MULTISIM

- Find the value of  $R_o$ .
- Find the maximum power that can be delivered to  $R_o$ .
- Find a resistor in Appendix H closest to the value in part (a). How much power is delivered to this resistor?

Figure P4.79

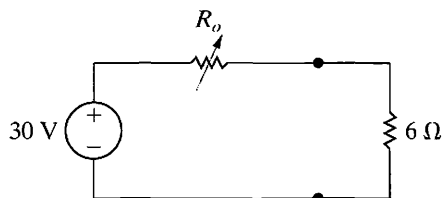


**4.80** What percentage of the total power developed in the circuit in Fig. P4.79 is delivered to  $R_o$  when  $R_o$  is set for maximum power transfer?

PSPICE  
MULTISIM

- 4.81** a) Find the value of the variable resistor  $R_o$  in the circuit in Fig. P4.81 that will result in maximum power dissipation in the  $6\ \Omega$  resistor. (Hint: Hasty conclusions could be hazardous to your career.)  
b) What is the maximum power that can be delivered to the  $6\ \Omega$  resistor?

Figure P4.81

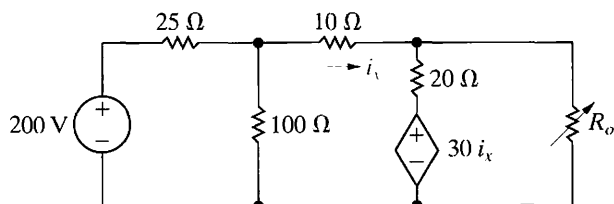


- 4.82** a) Calculate the power delivered for each value of  $R_o$  used in Problem 4.68.  
b) Plot the power delivered to  $R_o$  versus the resistance  $R_o$ .  
c) At what value of  $R_o$  is the power delivered to  $R_o$  a maximum?

**4.83** The variable resistor ( $R_o$ ) in the circuit in Fig. P4.83 is adjusted until the power dissipated in the resistor is 250 W. Find the values of  $R_o$  that satisfy this condition.

PSPICE  
MULTISIM

Figure P4.83



**4.84** A variable resistor  $R_o$  is connected across the terminals a,b in the circuit in Fig. P4.73. The variable resistor is adjusted until maximum power is transferred to  $R_o$ .

PSPICE  
MULTISIM

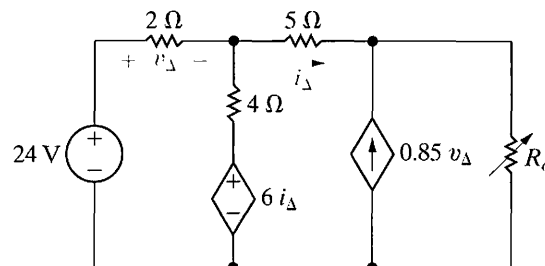
- a) Find the value of  $R_o$ .  
b) Find the maximum power delivered to  $R_o$ .  
c) Find the percentage of the total power developed in the circuit that is delivered to  $R_o$ .  
d) Find the resistor from Appendix H closest in value to the  $R_o$  from part (a).  
e) Find the percentage of the total power developed in the circuit that is delivered to the resistor in part (d).

**4.85** The variable resistor ( $R_o$ ) in the circuit in Fig. P4.85 is adjusted until it absorbs maximum power from the circuit.

PSPICE  
MULTISIM

- a) Find the value of  $R_o$ .  
b) Find the maximum power.  
c) Find the percentage of the total power developed in the circuit that is delivered to  $R_o$ .

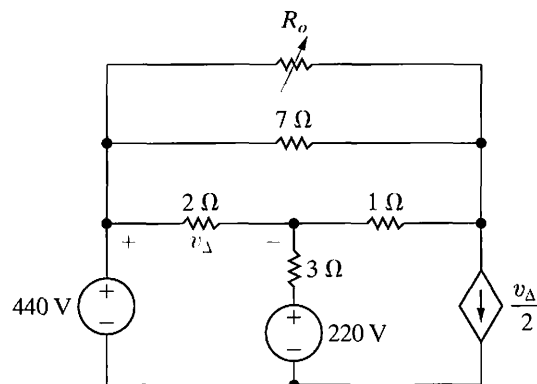
Figure P4.85



**4.86** The variable resistor ( $R_o$ ) in the circuit in Fig. P4.86 is adjusted for maximum power transfer to  $R_o$ . What percentage of the total power developed in the circuit is delivered to  $R_o$ ?

PSPICE  
MULTISIM

Figure P4.86

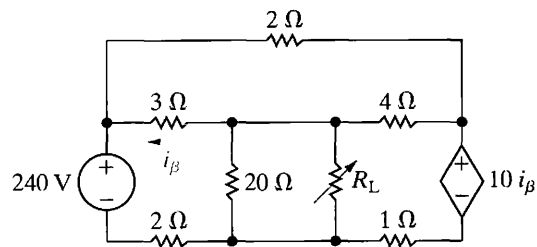


**4.87** The variable resistor ( $R_L$ ) in the circuit in Fig. P4.87 is adjusted for maximum power transfer to  $R_L$ .

PSPICE  
MULTISIM

- a) Find the numerical value of  $R_L$ .  
b) Find the maximum power transferred to  $R_L$ .

Figure P4.87

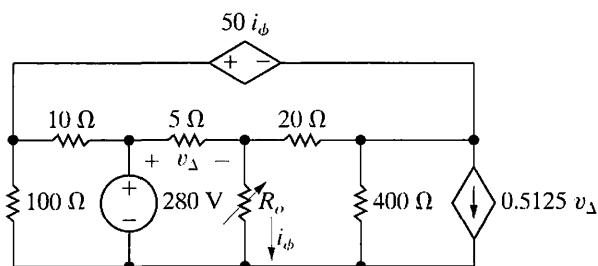


**4.88** The variable resistor in the circuit in Fig. P4.88 is adjusted for maximum power transfer to  $R_o$ .

PSPICE  
MULTISIM

- Find the numerical value of  $R_o$ .
- Find the maximum power delivered to  $R_o$ .
- How much power does the 280 V source deliver to the circuit when  $R_o$  is adjusted to the value found in (a)?

Figure P4.88

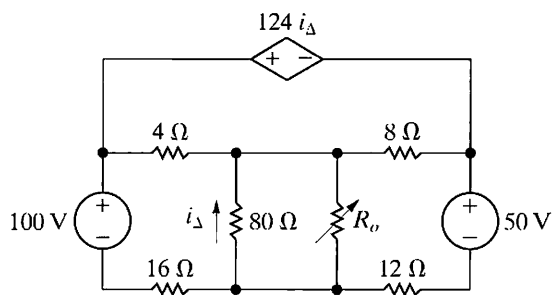


**4.89** The variable resistor ( $R_o$ ) in the circuit in Fig. P4.89 is adjusted for maximum power transfer to  $R_o$ .

PSPICE  
MULTISIM

- Find the value of  $R_o$ .
- Find the maximum power that can be delivered to  $R_o$ .
- If  $R_o$  is selected from Appendix H, which resistor value will result in the greatest amount of power delivered to  $R_o$ ?

Figure P4.89



**4.90** What percentage of the total power developed in the circuit in Fig. P4.89 is delivered to  $R_o$  found in Problem 4.89(a)?

PSPICE  
MULTISIM

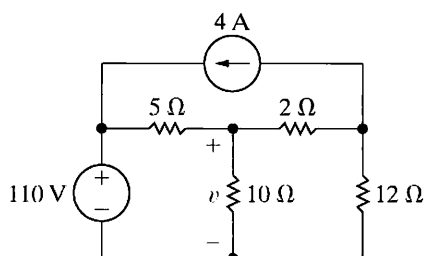
### Section 4.13

**4.91** a) Use the principle of superposition to find the voltage  $v$  in the circuit of Fig. P4.91.

PSPICE  
MULTISIM

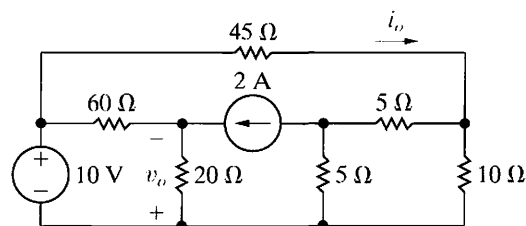
- Find the power dissipated in the 10 Ω resistor.

Figure P4.91



**4.92** Use superposition to solve for  $i_o$  and  $v_o$  in the circuit in Fig. P4.92.

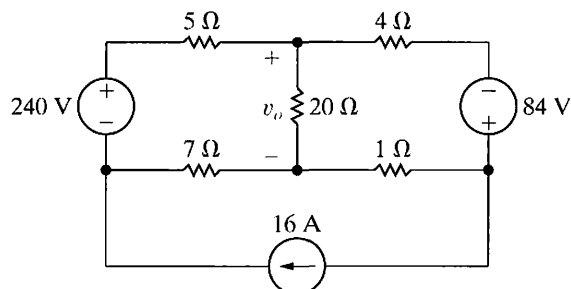
Figure P4.92



**4.93** Use the principle of superposition to find the voltage  $v_o$  in the circuit in Fig. P4.93.

PSPICE  
MULTISIM

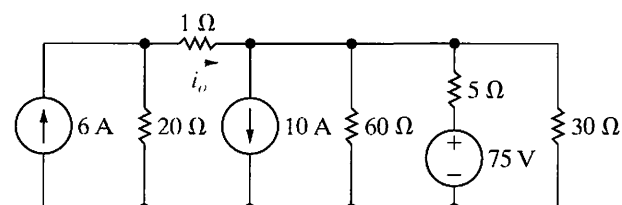
Figure P4.93



**4.94** Use the principle of superposition to find the current  $i_o$  in the circuit shown in Fig. P4.94.

PSPICE  
MULTISIM

Figure P4.94

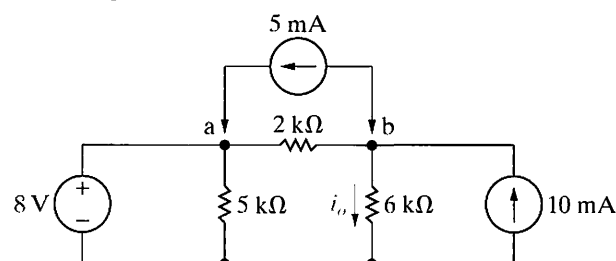


**4.95** a) In the circuit in Fig. P4.95, before the 5 mA current source is attached to the terminals a,b, the current  $i_o$  is calculated and found to be 3.5 mA. Use superposition to find the value of  $i_o$  after the current source is attached.

PSPICE  
MULTISIM

- Verify your solution by finding  $i_o$  when all three sources are acting simultaneously.

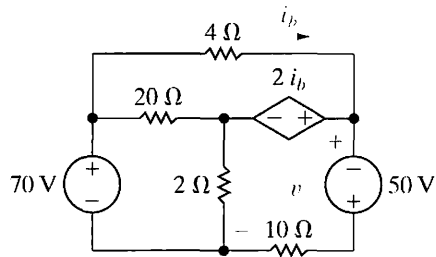
Figure P4.95



- 4.96** Use the principle of superposition to find the voltage  $v$  in the circuit of Fig. P4.96.

PSPICE  
MULTISIM

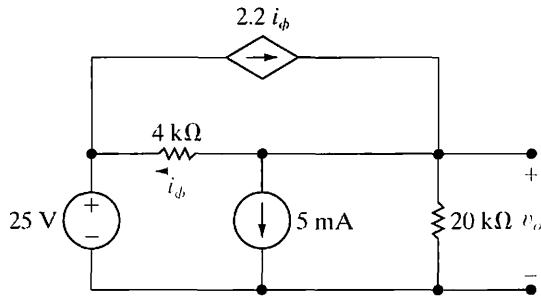
Figure P4.96



- 4.97** Use the principle of superposition to find  $v_o$  in the circuit in Fig. P4.97.

PSPICE  
MULTISIM

Figure P4.97

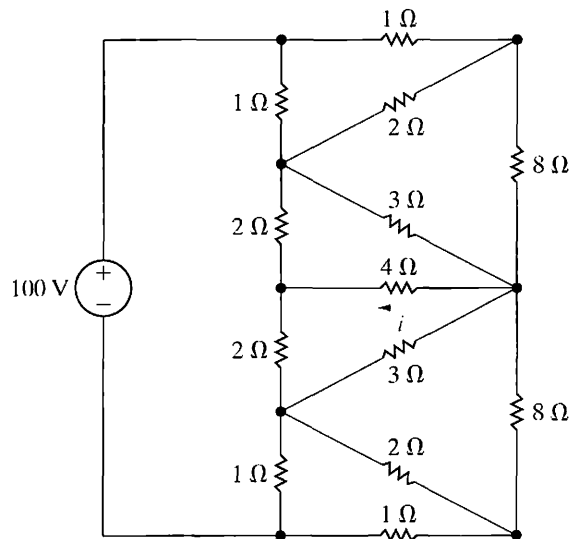


## Sections 4.1–4.13

- 4.98** Find  $i$  in the circuit in Fig. P4.98.

PSPICE  
MULTISIM

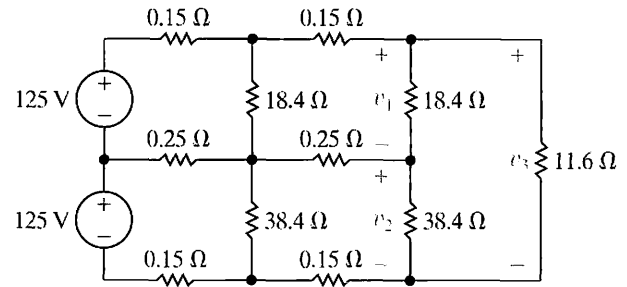
Figure P4.98



- 4.99** Find  $v_1$ ,  $v_2$ , and  $v_3$  in the circuit in Fig. P4.99.

PSPICE  
MULTISIM

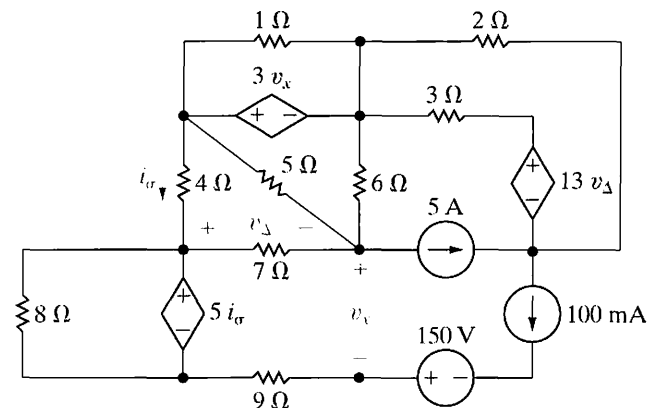
Figure P4.99



- 4.100** Find the power absorbed by the 5 A current source in the circuit in Fig. P4.100.

PSPICE  
MULTISIM

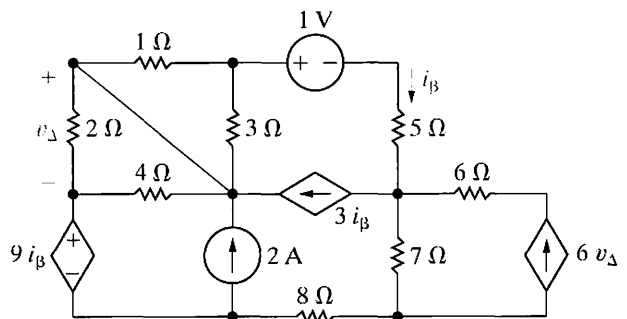
Figure P4.100



- 4.101** Assume your supervisor has asked you to determine the power developed by the 1 V source in the circuit in Fig. P4.101. Before calculating the power developed by the 1 V source, the supervisor asks you to submit a proposal describing how you plan to attack the problem. Furthermore, he asks you to explain why you have chosen your proposed method of solution.

- Describe your plan of attack, explaining your reasoning.
- Use the method you have outlined in (a) to find the power developed by the 1 V source.

Figure P4.101



# Problems

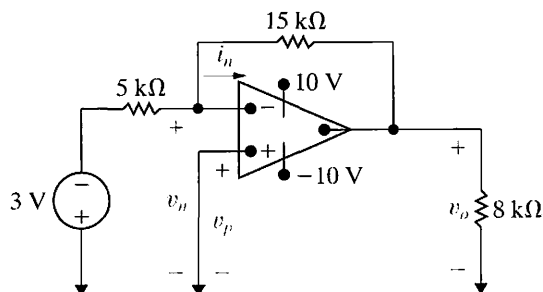
## Sections 5.1–5.2

**5.1** The op amp in the circuit in Fig. P5.1 is ideal.

PSPICE  
MULTISIM

- Label the five op amp terminals with their names.
- What ideal op amp constraint determines the value of  $i_n$ ? What is this value?
- What ideal op amp constraint determines the value of  $(v_p - v_n)$ ? What is this value?
- Calculate  $v_o$ .

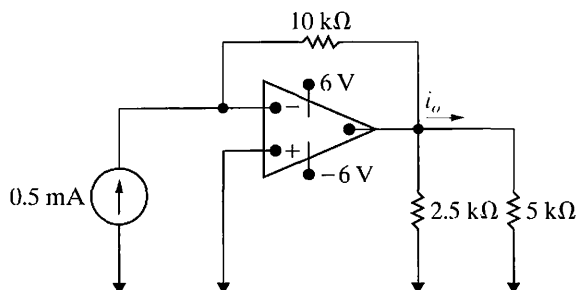
Figure P5.1



**5.2** Find  $i_o$  in the circuit in Fig. P5.2 if the op amp is ideal.

PSPICE  
MULTISIM

Figure P5.2

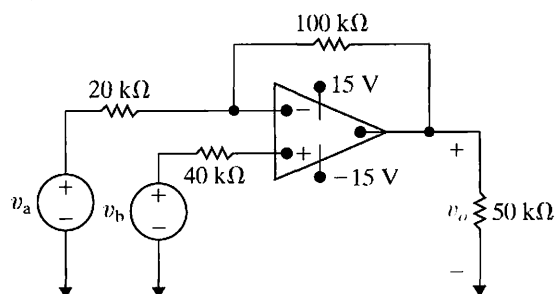


**5.3** The op amp in the circuit in Fig. P5.3 is ideal.

PSPICE  
MULTISIM

- Calculate  $v_o$  if  $v_a = 4$  V and  $v_b = 0$  V.
- Calculate  $v_o$  if  $v_a = 2$  V and  $v_b = 0$  V.
- Calculate  $v_o$  if  $v_a = 2$  V and  $v_b = 1$  V.
- Calculate  $v_o$  if  $v_a = 1$  V and  $v_b = 2$  V.
- Calculate  $v_o$  if  $v_a = 1.5$  V and  $v_b = 4$  V.
- If  $v_b = 1.6$  V, specify the range of  $v_a$  such that the amplifier does not saturate.

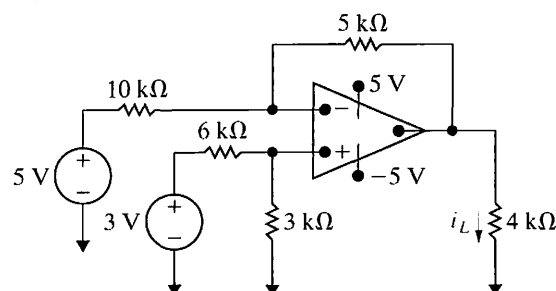
Figure P5.3



**5.4** Find  $i_L$  (in microamperes) in the circuit in Fig. P5.4.

PSPICE  
MULTISIM

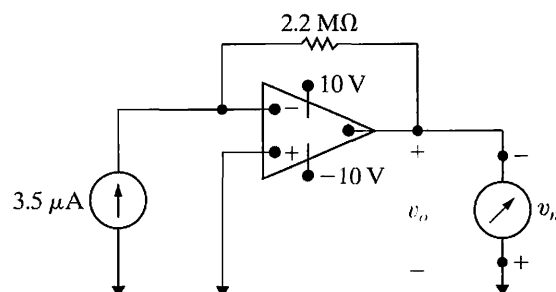
Figure P5.4



**5.5** A voltmeter with a full-scale reading of 10 V is used to measure the output voltage in the circuit in Fig. P5.5. What is the reading of the voltmeter? Assume the op amp is ideal.

PSPICE  
MULTISIM

Figure P5.5

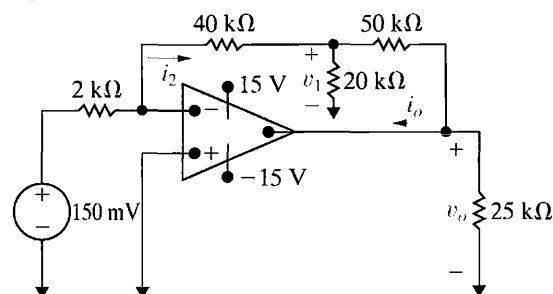


**5.6** The op amp in the circuit in Fig. P5.6 is ideal. Calculate the following:

PSPICE  
MULTISIM

- $v_1$
- $v_o$
- $i_2$
- $i_o$

Figure P5.6

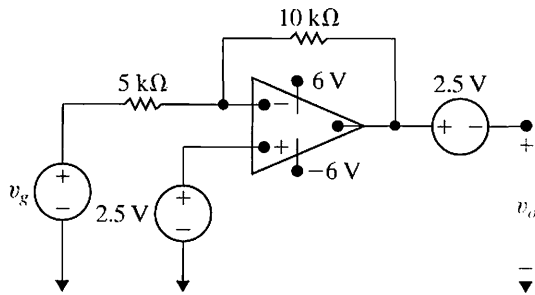


**5.7** A circuit designer claims the circuit in Fig. P5.7 will produce an output voltage that will vary between  $\pm 5$  as  $v_g$  varies between 0 and 5 V. Assume the op amp is ideal.

PRACTICAL  
PERSPECTIVE  
PSPICE  
MULTISIM

- Draw a graph of the output voltage  $v_o$  as a function of the input voltage  $v_g$  for  $0 \leq v_g \leq 5$  V.
- Do you agree with the designer's claim?

Figure P5.7



## Section 5.3

**5.8** a) Design an inverting amplifier using an ideal op amp that has a gain of 3. Use a set of identical resistors from Appendix H.

DESIGN PROBLEM

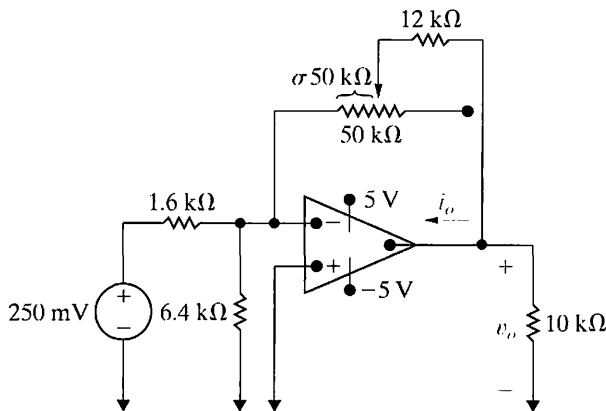
b) If you wish to amplify a 5 V input signal using the circuit you designed in part (a), what are the smallest power supply signals you can use?

**5.9** The op amp in the circuit in Fig. P5.9 is ideal.

PSPICE MULTISIM

- a) Find the range of values for  $\sigma$  in which the op amp does not saturate.  
b) Find  $i_o$  (in microamperes) when  $\sigma = 0.272$ .

Figure P5.9

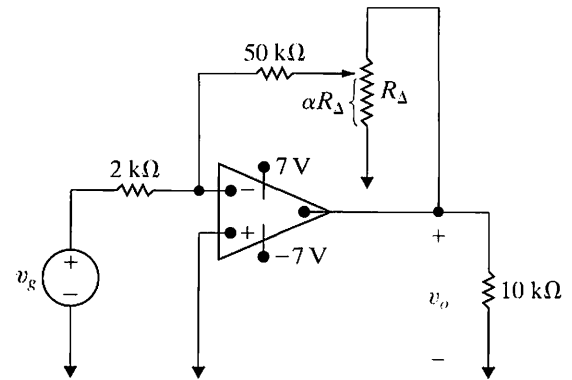


**5.10** a) The op amp in the circuit shown in Fig. P5.10 is ideal. The adjustable resistor  $R_\Delta$  has a maximum value of 100 kΩ, and  $\alpha$  is restricted to the range of  $0.2 \leq \alpha \leq 1$ . Calculate the range of  $v_o$  if  $v_g = 40$  mV.

PSPICE MULTISIM

b) If  $\alpha$  is not restricted, at what value of  $\alpha$  will the op amp saturate?

Figure P5.10



## Section 5.4

**5.11** Refer to the circuit in Fig. 5.12, where the op amp is assumed to be ideal. Given that  $R_a = 4$  kΩ,  $R_b = 5$  kΩ,  $R_c = 20$  kΩ,  $v_a = 200$  mV,  $v_b = 150$  mV,  $v_c = 400$  mV, and  $V_{CC} = \pm 6$  V, specify the range of  $R_f$  for which the op amp operates within its linear region.

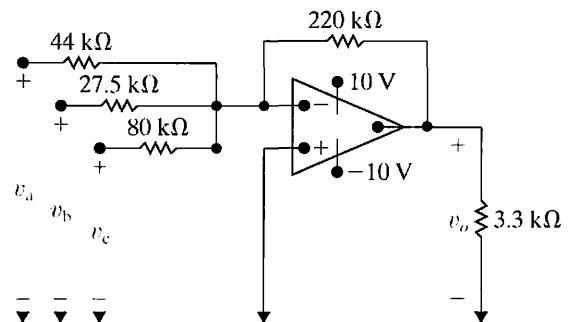
PSPICE MULTISIM

**5.12** The op amp in Fig. P5.12 is ideal.

PSPICE MULTISIM

- a) What circuit configuration is shown in this figure?  
b) Find  $v_o$  if  $v_a = 1$  V,  $v_b = 1.5$  V, and  $v_c = -4$  V.  
c) The voltages  $v_a$  and  $v_c$  remain at 1 V and  $-4$  V, respectively. What are the limits on  $v_b$  if the op amp operates within its linear region?

Figure P5.12



**5.13** Design an inverting-summing amplifier so that

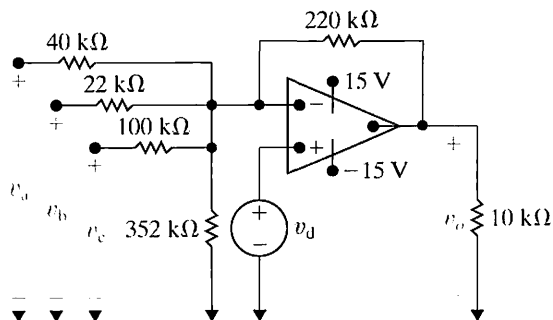
DESIGN PROBLEM  
PSPICE MULTISIM

$$v_o = -(3v_a + 5v_b + 4v_c + 2v_d).$$

Start by choosing a feedback resistor ( $R_f$ ) from Appendix H. Then choose single resistors from Appendix H or construct resistor networks from resistors in Appendix H to satisfy the design values for  $R_a$ ,  $R_b$ ,  $R_c$ , and  $R_d$ . Draw your final circuit diagram.

- 5.14** a) The op amp in Fig. P5.14 is ideal. Find  $v_o$  if  $v_a = 4$  V,  $v_b = 9$  V,  $v_c = 13$  V, and  $v_d = 8$  V.  
 b) Assume  $v_a$ ,  $v_c$ , and  $v_d$  retain their values as given in (a). Specify the range of  $v_b$  such that the op amp operates within its linear region.

Figure P5.14



- 5.15** The 220 kΩ feedback resistor in the circuit in Fig. P5.14 is replaced by a variable resistor  $R_f$ . The voltages  $v_a - v_d$  have the same values as given in Problem 5.14(a).

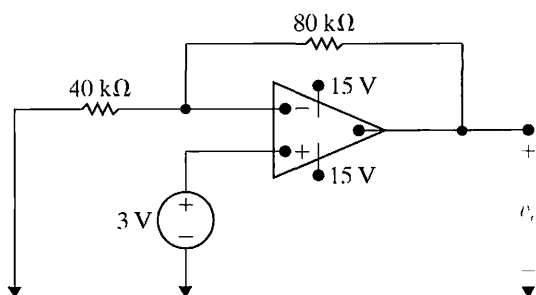
- a) What value of  $R_f$  will cause the op amp to saturate? Note that  $0 \leq R_f \leq \infty$ .  
 b) When  $R_f$  has the value found in (a), what is the current (in microamperes) into the output terminal of the op amp?

## Section 5.5

- 5.16** The op amp in the circuit of Fig. P5.16 is ideal.

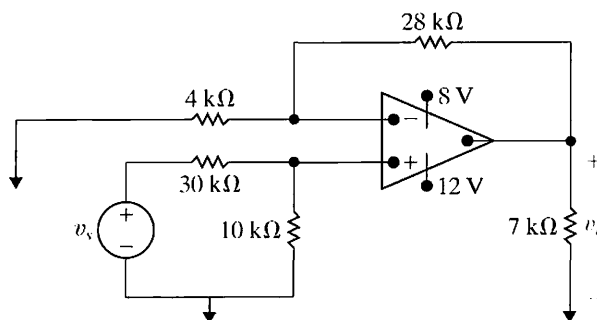
- a) What op amp circuit configuration is this?  
 b) Calculate  $v_o$ .

Figure P5.16



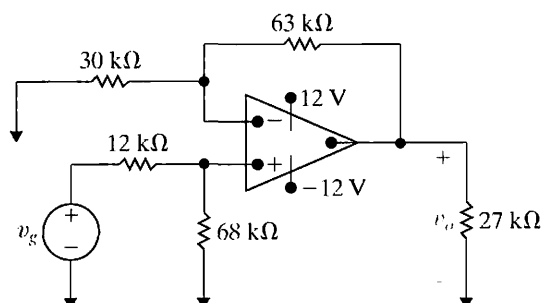
- 5.17** The op amp in the circuit of Fig. P5.17 is ideal.  
 a) What op amp circuit configuration is this?  
 b) Find  $v_o$  in terms of  $v_s$ .  
 c) Find the range of values for  $v_s$  such that  $v_o$  does not saturate and the op amp remains in its linear region of operation.

Figure P5.17



- 5.18** The op amp in the circuit shown in Fig. P5.18 is ideal.  
 a) Calculate  $v_o$  when  $v_g$  equals 4 V.  
 b) Specify the range of values of  $v_g$  so that the op amp operates in a linear mode.  
 c) Assume that  $v_g$  equals 2 V and that the 63 kΩ resistor is replaced with a variable resistor. What value of the variable resistor will cause the op amp to saturate?

Figure P5.18

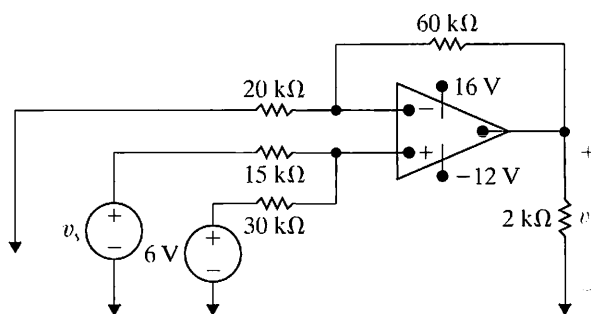


- 5.19** a) Design a non-inverting amplifier with a gain of 4. Use resistors from Appendix H. You might need to combine resistors in series and in parallel to get the desired resistance. Draw your final circuit.  
 b) If you use  $\pm 12$  V power supplies for the op amp, what range of input values will allow the op amp to stay in its linear operating region?

- 5.20** The op amp in the circuit of Fig. P5.20 is ideal.

- a) What op amp circuit configuration is this?  
 b) Find  $v_o$  in terms of  $v_s$ .  
 c) Find the range of values for  $v_s$  such that  $v_o$  does not saturate and the op amp remains in its linear region of operation.

Figure P5.20



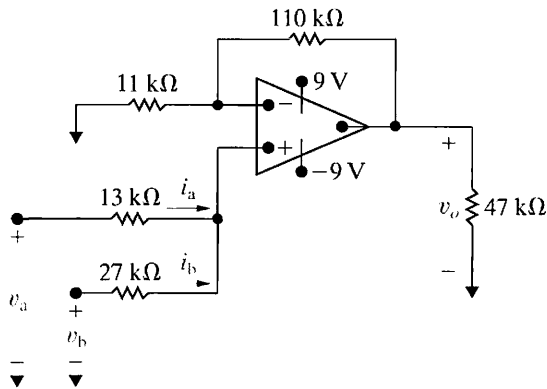


**5.21** The op amp in the circuit shown in Fig. P5.21 is ideal. The signal voltages  $v_a$  and  $v_b$  are 800 mV and 400 mV, respectively.

PSPICE  
MULTISIM

- What circuit configuration is shown in the figure?
- Calculate  $v_o$  in volts.
- Find  $i_a$  and  $i_b$  in microamperes.
- What are the weighting factors associated with  $v_a$  and  $v_b$ ?

Figure P5.21



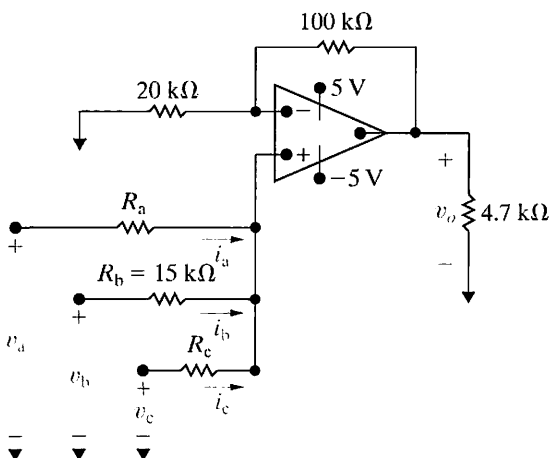
**5.22** The circuit in Fig. P5.22 is a noninverting summing amplifier. Assume the op amp is ideal. Design the circuit so that

DESIGN  
PROBLEM  
PSPICE  
MULTISIM

$$v_o = v_a + 2v_b + 3v_c.$$

- Specify the numerical values of  $R_a$  and  $R_c$ .
- Calculate  $i_a$ ,  $i_b$ , and  $i_c$  (in microamperes) when  $v_a = 0.7$  V,  $v_b = 0.4$  V, and  $v_c = 1.1$  V.

Figure P5.22



**5.23** The op amp in the noninverting summing amplifier of Fig. P5.23 is ideal.

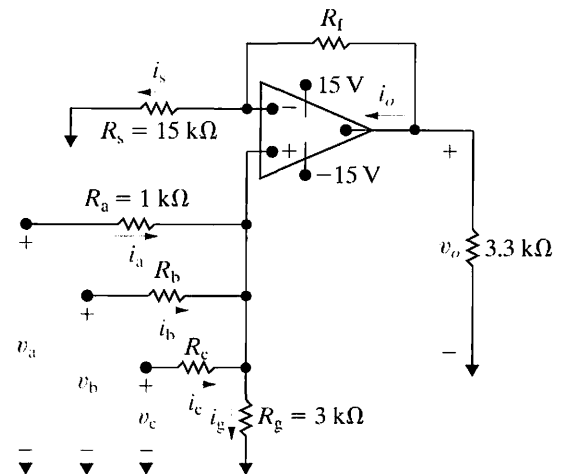
PSPICE  
MULTISIM

- Specify the values of  $R_f$ ,  $R_b$ , and  $R_c$  so that

$$v_o = 6v_a + 3v_b + 4v_c.$$

- Using the values found in part (a) for  $R_f$ ,  $R_b$ , and  $R_c$ , find (in microamperes)  $i_a$ ,  $i_b$ ,  $i_c$ ,  $i_g$ , and  $i_s$  when  $v_a = 0.5$  V,  $v_b = 2.5$  V, and  $v_c = 1$  V.

Figure P5.23



## Section 5.6

**5.24** a) Use the principle of superposition to derive Eq. 5.22.

- Derive Eqs. 5.23 and 5.24.

**5.25** The resistors in the difference amplifier shown in Fig. 5.15 are  $R_a = 24$  kΩ,  $R_b = 75$  kΩ,  $R_c = 130$  kΩ and  $R_d = 120$  kΩ. The signal voltages  $v_a$  and  $v_b$  are 8 and 5 V, respectively, and  $V_{CC} = \pm 20$  V.

PSPICE  
MULTISIM

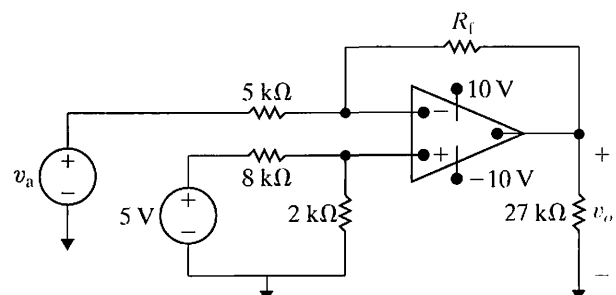
- Find  $v_o$ .
- What is the resistance seen by the signal source  $v_a$ ?
- What is the resistance seen by the signal source  $v_b$ ?

**5.26** The op amp in the circuit of Fig. P5.26 is ideal. What value of  $R_f$  will give the equation

$$v_o = 5 - 4v_a,$$

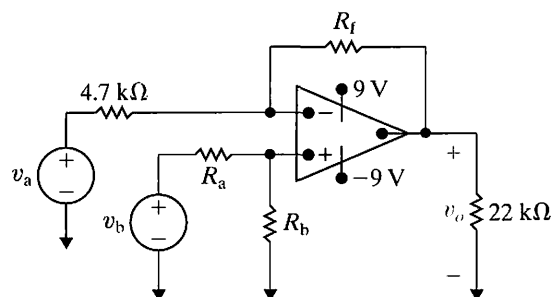
for this circuit?

Figure P5.26



- 5.27** Design the difference-amplifier circuit in Fig. P5.27 so that  $v_o = 10(v_b - v_a)$ , and the voltage source  $v_b$  sees an input resistance of  $220\text{ k}\Omega$ . Specify the values of  $R_a$ ,  $R_b$ , and  $R_f$  using single resistors or combinations of resistors from Appendix H. Use the ideal model for the op amp.

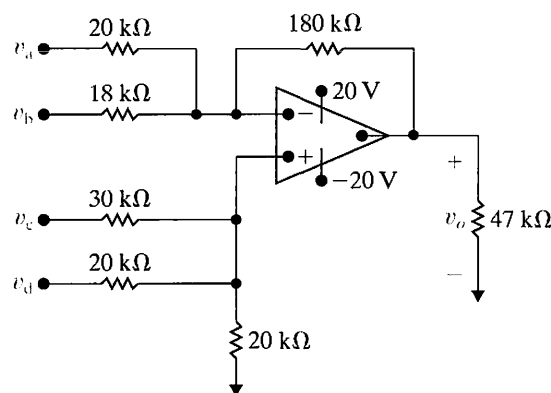
Figure P5.27



- 5.28** The op amp in the adder-subtractor circuit shown in Fig. P5.28 is ideal.

- Find  $v_o$  when  $v_a = 1\text{ V}$ ,  $v_b = 2\text{ V}$ ,  $v_c = 3\text{ V}$ , and  $v_d = 4\text{ V}$ .
- If  $v_a$ ,  $v_b$ , and  $v_d$  are held constant, what values of  $v_c$  will not saturate the op amp?

Figure P5.28

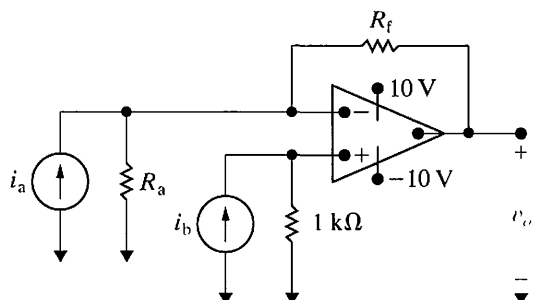


- 5.29** Select the values of  $R_a$  and  $R_f$  in the circuit in Fig. P5.29 so that

$$v_o = 5000(i_b - i_a).$$

Use single resistors or combinations of resistors from Appendix H. The op amp is ideal.

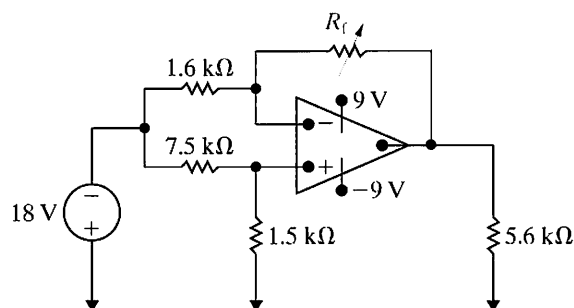
Figure P5.29



- 5.30** Design a difference amplifier (Fig. 5.15) to meet the following criteria:  $v_o = 3v_b - 4v_a$ . The resistance seen by the signal source  $v_b$  is  $470\text{ k}\Omega$ , and the resistance seen by the signal source  $v_a$  is  $22\text{ k}\Omega$  when the output voltage  $v_o$  is zero. Specify the values of  $R_a$ ,  $R_b$ ,  $R_c$ , and  $R_d$  using single resistors or combinations of resistors from Appendix H.

- 5.31** The resistor  $R_f$  in the circuit in Fig. P5.31 is adjusted until the ideal op amp saturates. Specify  $R_f$  in kilohms.

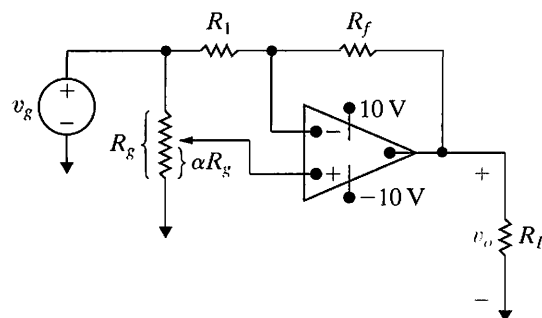
Figure P5.31



- 5.32** The op amp in the circuit of Fig. P5.32 is ideal.

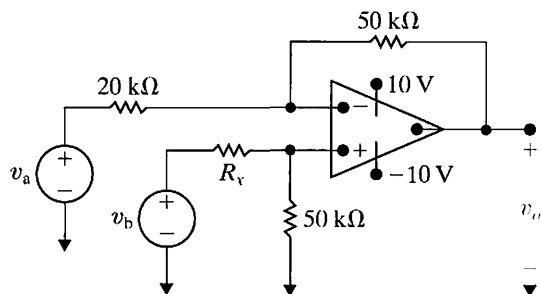
- Plot  $v_o$  versus  $\alpha$  when  $R_f = 4R_1$  and  $v_g = 2\text{ V}$ . Use increments of 0.1 and note by hypothesis that  $0 \leq \alpha \leq 1.0$ .
- Write an equation for the straight line you plotted in (a). How are the slope and intercept of the line related to  $v_g$  and the ratio  $R_f/R_1$ ?
- Using the results from (b), choose values for  $v_g$  and the ratio  $R_f/R_1$  such that  $v_o = -6\alpha + 4$ .

Figure P5.32



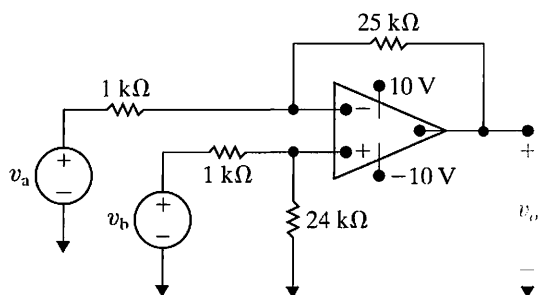
- 5.33 In the difference amplifier shown in Fig. P5.33, what range of values of  $R_x$  yields a CMRR  $\geq 1000$ ?

Figure P5.33



- 5.34 In the difference amplifier shown in Fig. P5.34, compute (a) the differential mode gain, (b) the common mode gain, and (c) the CMRR.

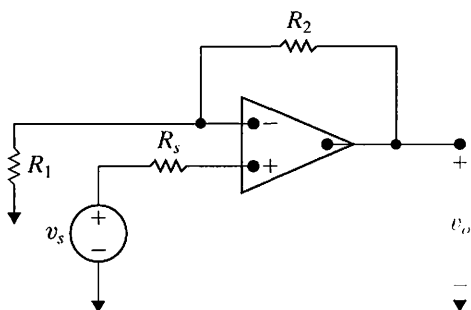
Figure P5.34



### Sections 5.1–5.6

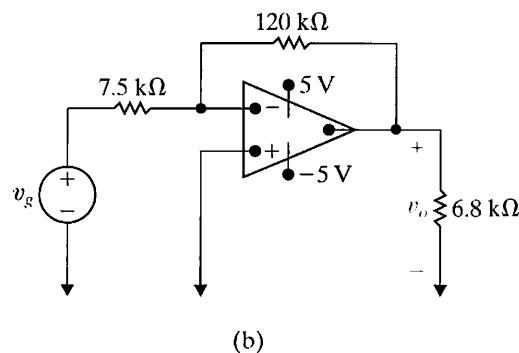
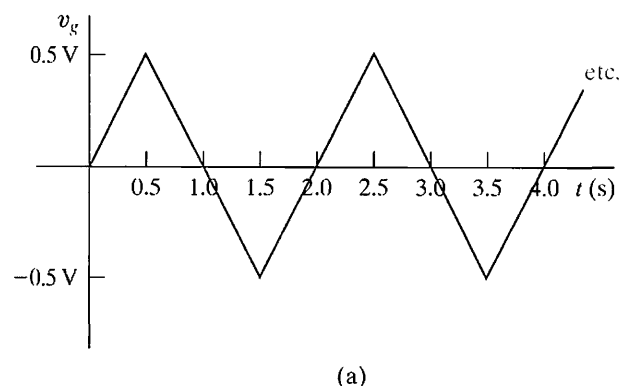
- 5.35 Assume that the ideal op amp in the circuit seen in Fig. P5.35 is operating in its linear region.
- Show that  $v_o = [(R_1 + R_2)/R_1]v_s$ .
  - What happens if  $R_1 \rightarrow \infty$  and  $R_2 \rightarrow 0$ ?
  - Explain why this circuit is referred to as a voltage follower when  $R_1 = \infty$  and  $R_2 = 0$ .

Figure P5.35



- 5.36 The voltage  $v_g$  shown in Fig. P5.36(a) is applied to the inverting amplifier shown in Fig. P5.36(b). Sketch  $v_o$  versus  $t$ , assuming the op amp is ideal.

Figure P5.36



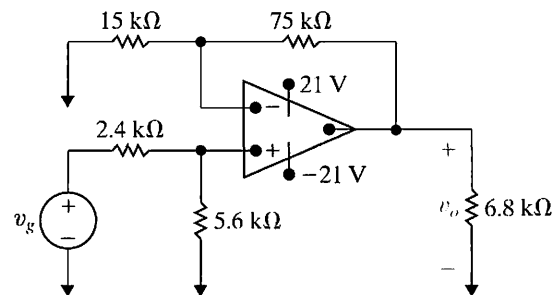
- 5.37 The signal voltage  $v_g$  in the circuit shown in Fig. P5.37 is described by the following equations:

$$v_g = 0, \quad t \leq 0,$$

$$v_g = 10 \sin(\pi/3)t \text{ V}, \quad 0 \leq t \leq \infty.$$

Sketch  $v_o$  versus  $t$ , assuming the op amp is ideal.

Figure P5.37



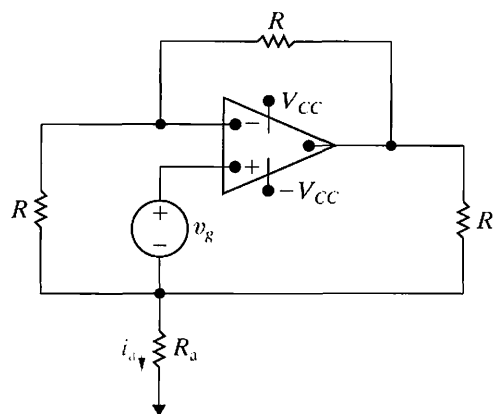
- 5.38 a) Show that when the ideal op amp in Fig. P5.38 is operating in its linear region,

$$i_a = \frac{3v_g}{R}.$$

- b) Show that the ideal op amp will saturate when

$$R_a = \frac{R(\pm V_{CC} - 2v_g)}{3v_g}.$$

Figure P5.38

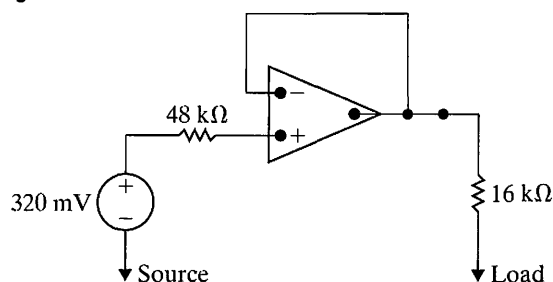


**5.39** Assume that the ideal op amp in the circuit in Fig. P5.39 is operating in its linear region.

PSPICE  
MULTISIM

- Calculate the power delivered to the  $16\text{ k}\Omega$  resistor.
- Repeat (a) with the op amp removed from the circuit, that is, with the  $16\text{ k}\Omega$  resistor connected in the series with the voltage source and the  $48\text{ k}\Omega$  resistor.
- Find the ratio of the power found in (a) to that found in (b).
- Does the insertion of the op amp between the source and the load serve a useful purpose? Explain.

Figure P5.39

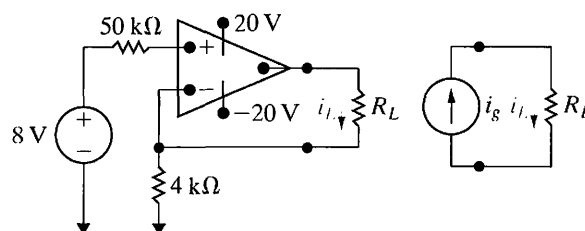


**5.40** The circuit inside the shaded area in Fig. P5.40 is a constant current source for a limited range of values of  $R_L$ .

PSPICE  
MULTISIM

- Find the value of  $i_L$  for  $R_L = 4\text{ k}\Omega$ .
- Find the maximum value for  $R_L$  for which  $i_L$  will have the value in (a).
- Assume that  $R_L = 16\text{ k}\Omega$ . Explain the operation of the circuit. You can assume that  $i_n = i_p \approx 0$  under all operating conditions.
- Sketch  $i_L$  versus  $R_L$  for  $0 \leq R_L \leq 16\text{ k}\Omega$ .

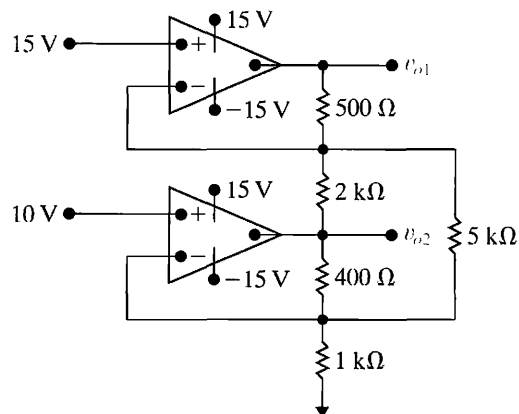
Figure P5.40



**5.41** The two op amps in the circuit in Fig. P5.41 are ideal. Calculate  $v_{o1}$  and  $v_{o2}$ .

PSPICE  
MULTISIM

Figure P5.41

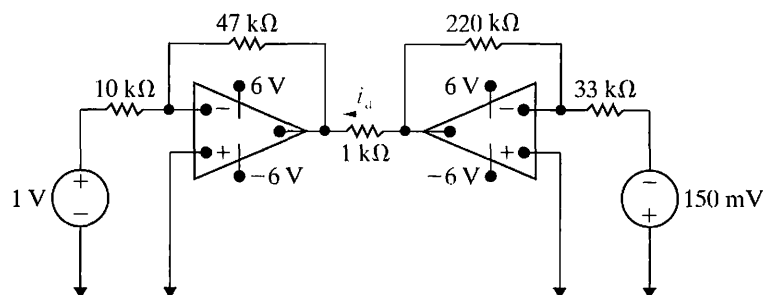


**5.42** The op amps in the circuit in Fig. P5.42 are ideal.

PSPICE  
MULTISIM

- Find  $i_a$ .
- Find the value of the left source voltage for which  $i_a = 0$ .

Figure P5.42



## Section 5.7

**5.43** Repeat Assessment Problem 5.6, given that the inverting amplifier is loaded with a  $500\ \Omega$  resistor.

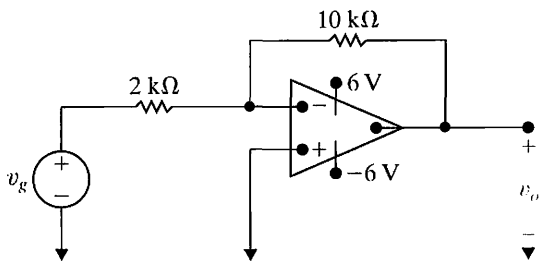
PSPICE  
MULTISIM

**5.44** Assume the input resistance of the op amp in Fig. P5.44 is infinite and its output resistance is zero.

PSPICE  
MULTISIM

- Find  $v_o$  as a function of  $v_g$  and the open-loop gain  $A$ .
- What is the value of  $v_o$  if  $v_g = 1\text{ V}$  and  $A = 150$ ?
- What is the value of  $v_o$  if  $v_g = 1\text{ V}$  and  $A = \infty$ ?
- How large does  $A$  have to be so that  $v_o$  is 99% of its value in (c)?

Figure P5.44

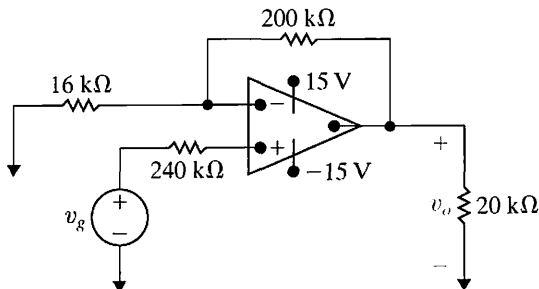


**5.45** The op amp in the noninverting amplifier circuit of Fig. P5.45 has an input resistance of  $560\text{ k}\Omega$ , an output resistance of  $8\text{ k}\Omega$ , and an open-loop gain of 50,000. Assume that the op amp is operating in its linear region.

PSPICE  
MULTISIM

- Calculate the voltage gain ( $v_o/v_g$ ).
- Find the inverting and noninverting input voltages  $v_n$  and  $v_p$  (in millivolts) if  $v_g = 1\text{ V}$ .
- Calculate the difference ( $v_p - v_n$ ) in microvolts when  $v_g = 1\text{ V}$ .
- Find the current drain in picoamperes on the signal source  $v_g$  when  $v_g = 1\text{ V}$ .
- Repeat (a)–(d) assuming an ideal op amp.

Figure P5.45

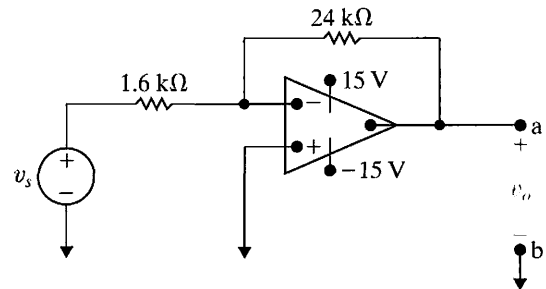


**5.46** a) Find the Thévenin equivalent circuit with respect to the output terminals a,b for the inverting amplifier of Fig. P5.46. The dc signal source has a value of 880 mV. The op amp has an input resistance of  $500\text{ k}\Omega$ , an output resistance of  $2\text{ k}\Omega$  and an open-loop gain of 100,000.

PSPICE  
MULTISIM

- What is the output resistance of the inverting amplifier?
- What is the resistance (in ohms) seen by the signal source  $v_g$  when the load at the terminals a,b is  $330\ \Omega$ ?

Figure P5.46



**5.47** Repeat Problem 5.46 assuming an ideal op amp.

PSPICE  
MULTISIM

**5.48** Derive Eq. 5.60.

**5.49** Suppose the strain gages in the bridge in Fig. 5.21 have the value  $120\ \Omega \pm 1\%$ . The power supplies to the op amp are  $\pm 15\text{ V}$ , and the reference voltage,  $v_{\text{ref}}$ , is taken from the positive power supply.

PRACTICAL  
PERSPECTIVE

- Calculate the value of  $R_f$  so that when the strain gage that is lengthening reaches its maximum length, the output voltage is 5 V.
- Suppose that we can accurately measure 50 mV changes in the output voltage. What change in strain gage resistance can be detected in milliohms?

### Sections 5.1–5.7