

REVIEW FOR FINAL PHYSICS 1

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CHAPTER 3

$$\text{Work: } W = (F \cos \theta) \Delta x = \vec{F} \cdot \overrightarrow{\Delta x} \text{ (J)}$$

$$\text{Power: } P = \frac{W}{\Delta t} = \vec{F} \cdot \vec{v} \text{ (J/s or W)}$$

Energy: $E = K + U_g + U_{el}$

- Kinetic energy: $K = \frac{1}{2}mv^2 (J)$
- Potential energy: $U_g = mgh (J)$
 - With h is the distance from potential origin to obj position.
- Elastic energy: $U_{el} = \frac{1}{2}kx^2 (J)$
 - k is force constant or spring constant (N/m)
 - x is spring deformation (m)
 - Equilibrium position: $x = 0$

Kinetic Energy Theorem: (Định lý biến thiên động năng)

$$W_{net} = \Delta K = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

Potential Energy: (Định lý thế năng trọng trường)

$$W_{gravity} = -\Delta U_g = U_{gi} - U_{gf}$$

Work done by spring:

$$W = -\Delta U_{el} = \frac{1}{2}kx_1^2 - \frac{1}{2}kx_2^2$$

Conservative VS Nonconservative

- Conservative force: gravity, elastic
- Nonconservative force: friction, resistance,...

Note: Work of resistive forces are always negative

Conservation of energy theorem: (Định luật bảo toàn cơ năng)
(use for conservative system)

$$E_i = E_f$$
$$\Rightarrow K_i + U_{gi} + U_{eli} = K_f + U_{gf} + U_{elf}$$

Energy with nonconservative force

$$W_{nc} = \Delta E = (K_f + U_f) - (K_i + U_i)$$

CHAPTER 4

Linear momentum: (động lượng)

$$\vec{p} = m\vec{v}$$

Impulse:

$$I = \Delta\vec{p} = \int d\vec{p} = \int_{t_i}^{t_f} \vec{F} \Delta t$$

Conservation of linear momentum:

$$\vec{p}_i = \vec{p}_f$$

Two types of collisions:

Inelastic collision: Kinetic energy is not conserved

$$E_{lost} = \Delta K$$

Elastic collision: both momentum and kinetic energy are conserved

$$K_i = K_f$$

CHAPTER 5

| Notation | Linear Translational | Angular Rotational |
|---------------------|---|--|
| Basic quantities | x (m) v (m/s) a (m/s ²) | θ (rad) ω (rad/s) α (rad/s ²) |
| Basic formula | a const $v = v_0 + at$ $x = x_0 + v_0t + \frac{1}{2}at^2$ $v^2 - v_0^2 = 2a\Delta x$ | α const $\omega = \omega_0 + \alpha t$ $\theta = \theta_0 + \omega_0t + \frac{1}{2}\alpha t^2$ $\omega^2 - \omega_0^2 = 2\alpha\Delta\theta$ |
| Inertia | mass: m (kg) | Moment of inertia } Rotational inertia } ❖ $I = \sum mR^2$ (kg×m ²) ❖ $I = \dots$ |

| Notation | Linear Translational | Angular Rotational |
|--------------------------------|---|---|
| Speeding up Slowing down | $\mathbf{a} \cdot \mathbf{v}$ $\vec{\mathbf{a}} \cdot \vec{\mathbf{v}}$ | $\boldsymbol{\alpha} \cdot \boldsymbol{\omega}$ $\vec{\boldsymbol{\alpha}} \cdot \vec{\boldsymbol{\omega}}$ |
| Force vs Torque | Newton's 2 nd law: $\vec{\mathbf{F}} = m\vec{\mathbf{a}}$ (N) | $\vec{\boldsymbol{\tau}} = \vec{\mathbf{r}} \times \vec{\mathbf{F}}$ or $\tau = Fd$ (d: moment/lever arm) Newton's 2 nd law: $\vec{\boldsymbol{\tau}} = I \times \vec{\boldsymbol{\alpha}}$ (N·m) |
| Convention of (+) direction | y up x to the right | Counterclockwise |

| Notation | Linear Translational | Angular Rotational |
|------------------------------|---|---|
| Energy $E = K + U$ | $K = \frac{1}{2}mv^2 \text{ (J)(eV)}$ $U_g = mgh \text{ (y up, 0 at ...)}$ $U_{el} = \frac{1}{2}kx^2 \text{ (J)(eV)}$ | $K = \frac{1}{2}I\omega^2 \text{ (J)(eV)}$ |
| Work | $W = \vec{F} \cdot \Delta \vec{x} \text{ or } \int_{x_i}^{x_f} \vec{F}(x) \cdot d\vec{x}$ (J)(eV) | $W = \vec{\tau} \cdot \Delta \vec{\theta} \text{ or } \int_{\theta_i}^{\theta_f} \vec{\tau}(\theta) \cdot d\vec{\theta}$ (J)(eV) |
| Power | $P = \frac{W}{\Delta t} = \vec{F} \cdot \vec{v}$ (J/s)(W) | $P = \frac{W}{\Delta t} = \vec{\tau} \cdot \vec{\omega}$ (J/s)(W) |
| Momentum | $\vec{p} = m\vec{v} \text{ (kg} \cdot \text{m/s)}$ | $\vec{L} = \vec{r} \times \vec{p}$ $\vec{L} = I\vec{\omega} \text{ (kg} \cdot \text{m}^2/\text{s)}$ |

| Notation | Linear Translational | Angular Rotational |
|--------------------------|--|--|
| Impulse | $\vec{I} = \Delta \vec{p} = \vec{F} \Delta t = \int_{t_i}^{t_f} \vec{F}(t) dt$ $\diamond \vec{F}_{\text{net}} = \frac{\Delta \vec{p}}{\Delta t} \text{ or } \frac{d\vec{p}}{dt}$ | $\vec{I} = \Delta \vec{L} = \vec{\tau} \Delta t = \int_{t_i}^{t_f} \vec{\tau}(t) dt$ $\diamond \vec{\tau}_{\text{net}} = \frac{\Delta \vec{L}}{\Delta t} \text{ or } \frac{d\vec{L}}{dt}$ |
| Momentum conservation | $\color{blue}{+} \vec{F}_{\text{net}} = \vec{0} \Rightarrow \Delta \vec{p} = \vec{0}$ $\Rightarrow \sum \vec{p}_i = \sum \vec{p}_f$ $\Rightarrow \sum m_i v_i = \sum m_f v_f$ | $\color{blue}{+} \vec{\tau}_{\text{net}} = \vec{0} \Rightarrow \Delta \vec{L} = \vec{0}$ $\Rightarrow \sum \vec{L}_i = \sum \vec{L}_f$ $\Rightarrow \sum I_i \omega_i = \sum I_f \omega_f$ |

Pure rotation relationship:

$$s=R\theta$$

$$v=R\omega$$

$$a_T=R\alpha$$

$$a_R=\frac{v^2}{R}$$

$$a=\sqrt{a_T^2+a_R^2}$$

Rolling motion relationship:

$$s_{cm}=R\theta$$

$$v_{cm}=R\omega$$

$$a_{cm}=R\alpha$$

Total kinetic energy (translation + rotation)

$$K=\frac{1}{2}I_{cm}\omega^2+\frac{1}{2}Mv_{cm}^2$$