

30/08/2024  
Final Sem 03

## QUESTIONS

$h = 6.63 \times 10^{-34} \text{ Js}$ ;  $c = 3 \times 10^8 \text{ m/s}$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ; rest mass of electron:  $9.1 \times 10^{-31} \text{ kg}$

Avogadro number:  $N_A = 6.02 \times 10^{23} \text{ particle/mol}$

**Q1. (20 marks)** A 1.50-cm-high object is placed 20.0 cm from a concave mirror with focal length 15.0 cm.

(a) Determine the position of the image and its size.  $q = 60 \text{ cm}$ ,  $4.5 \text{ cm}$

(b) Draw a ray diagram.

**Q2. (20 marks)** The x-coordinate of an electron is measured with an uncertainty of 0.20 mm  $\Delta p = m \Delta v$

(a) What is the x-component of the electron's velocity if the minimum percentage uncertainty in a simultaneous measurement of this velocity is 1.0%?

(b) What is your observation about the precision of the measurement of this electron's position? What is the result in the precision of the velocity's measurement?

**Q3. (20 marks)** Consider a box with width  $L$  centered at  $x = 0$ , so that it extends from  $x = -L/2$  to  $x = +L/2$  (Fig. 1). Consider possible wave functions of the form:

$\psi(x) = A \sin(kx)$  where  $k = \frac{2\pi}{\lambda} = \frac{h}{p}$  is the wave number and  $p = mv$  is the linear

momentum.

(a) Apply the boundary conditions at the wall:  $\psi(L/2) = \psi(-L/2) = 0$  to obtain the allowed energy levels.

(b) Show that the energy levels are not equidistant.

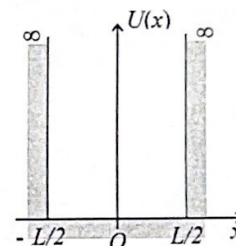


Fig. 1

**Q4. (20 marks)** Knowing that the energy of hydrogen atom is given by:  $E_n = -\frac{13.6}{n^2} \text{ eV}$ .

In which region of electromagnetic spectrum does the Lyman series fall? Explain your answer.  $\lambda_{\text{short}} = 91.35 \text{ nm}$   
 $\rightarrow 121.803 \text{ nm}$  (longest)  
ultraviolet.

**Q5. (20 marks)** World War II aircraft had instruments with glowing radium-painted dials. The activity of one such instrument was  $1.0 \times 10^5 \text{ Bq}$  when it was new. Knowing that the half life of Ra is 1600 years.

(a) What mass of  $^{226}_{88}\text{Ra}$  was present?  $m = N \cdot \frac{m}{N_A}$   
 $m = 2.73 \times 10^{-6} \text{ (kg)}$

(b) What is the activity of this instrument 57.0 years after it was made?

$$97.56 \times 10^3 \text{ (Bq)}$$

END OF QUESTION PAPER

$$N = N_0 \left( \frac{1}{2} \right)^{\frac{t}{T_{1/2}}}$$

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$