

Analog Electronics

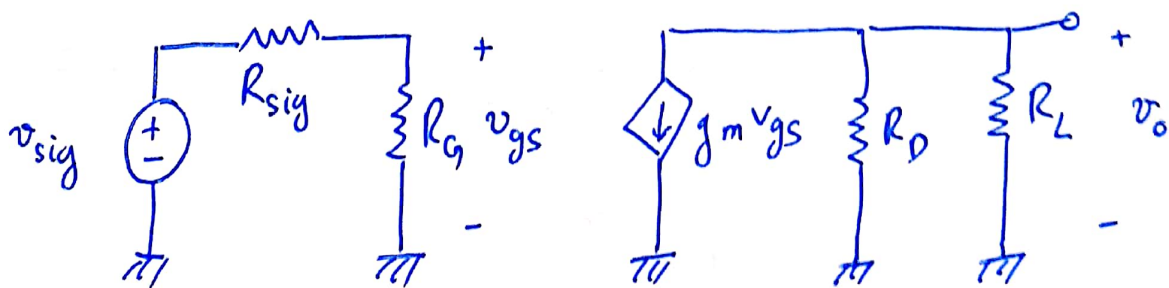
QUIZ # 4.2

$$(a) \ i) \ f_T = \frac{g_m}{2\pi(C_{gs} + C_{gd})} = \frac{2 \times 10^{-3}}{2\pi(5+2) \times 10^{-12}} \approx 45.48 \text{ MHz}$$

$$\begin{aligned} ii) \ C_{eq} &= (1 + g_m R_L') C_{gd} & (R_D \parallel R_L = 5 \text{ k}\Omega) \\ &= (1 + 2 \times 10^{-3} \times 5 \times 10^3) 2 \\ &= 22 \text{ pF} \end{aligned}$$

$$\begin{aligned} iii) \ f_H &= \frac{1}{2\pi C_{in} R_{sig}'} = \frac{1}{2\pi(C_{gs} + C_{eq}) R_{sig}'} \\ &= \frac{1}{2\pi(5+22) \text{ pF} \times 49.18 \text{ k}\Omega} & (R_{sig}' = R_{sig} \parallel R_G = 49.18 \text{ k}\Omega) \\ &\approx 120 \text{ kHz} \end{aligned}$$

$$iv) \ A_M = \frac{v_o}{v_{sig}} = -g_m \frac{R_G}{R_G + R_{sig}} R_D \parallel R_L \approx -10$$

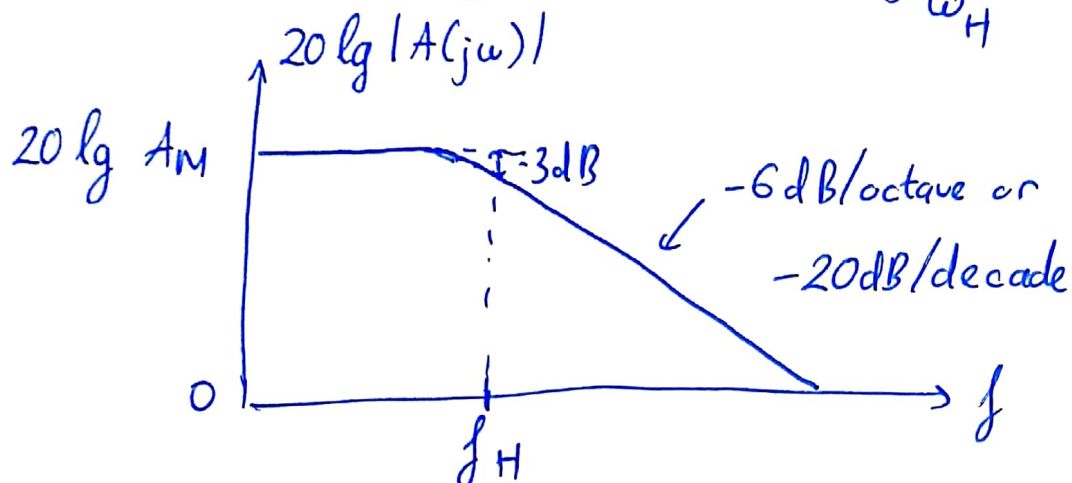


v) -6dB/octave means that at $2f_H$ the gain is:

$$20 \log |A_M| - 6 \text{ dB} = 20 \log 10 - 6 = 14 \text{ dB}$$

$$\Rightarrow A_{2f_H} = 10^{14/20} \approx 5$$

$$(vi) A(j\omega) = \frac{v_o(j\omega)}{v_{sig}(j\omega)} = -A_M \frac{1}{1 + j \frac{\omega}{\omega_H}}$$



$$(b) i) f_T = \frac{g_m}{2\pi(C_\pi + C_\mu)} \quad \begin{cases} g_m = I_c / V_T = 1/25 = 0.04 \text{ A/V} \\ C_\pi + C_\mu = 20 + 5 = 25 \text{ pF} \end{cases}$$

$$\approx 255 \text{ MHz}$$

$$ii) g_m = \frac{I_c}{V_T} = \frac{1}{25} = 0.04 \text{ (A/V)}$$

$$R_L' = R_L \parallel R_c = 2.5 \text{ (k}\Omega\text{)}$$

$$C_{eq} = (1 + g_m R_L') C_\mu = (1 + 0.04 \times 2500) 5 \text{ pF}$$

$$= 505 \text{ (pF)}$$

$$iii) R_{sig}' = r_\pi \parallel [r_x + (R_B \parallel R_{sig})] = 2.5 \parallel [0.05 + 82 \parallel 2] \approx 1.1 \text{ k}\Omega$$

$$(r_\pi = \beta / g_m = \frac{100}{0.04} = 2.5 \text{ k}\Omega)$$

$$f_H = \frac{1}{2\pi C_{in} R_{sig}'} = \frac{1}{2\pi \times 525 \text{ pF} \times 1.1 \text{ k}\Omega} \approx 276 \text{ (kHz)}$$

$$(C_{in} = C_\pi + C_{eq} = 20 + 505 = 525 \text{ pF})$$

$$\begin{aligned}
 \text{iv) } \frac{v_o}{v_{sig}} &= \frac{-R_B}{R_{sig} + R_B} \cdot \frac{r_{\pi}}{r_{\pi} + r_x + R_B \parallel R_{sig}} \cdot g_m R_L' \\
 &= \frac{-82}{2 + 82} \cdot \frac{2.5}{2.5 + 0.05 + 2 \parallel 82} \cdot 0.04 \times 2500
 \end{aligned}$$

$$A_M \approx -55$$

$$A_M(\text{dB}) = 20 \log |55| \approx 34.8 \text{ dB}$$

v) Bode plot.

