# **Resistive Circuits**

(Chapter 3)

Textbook:

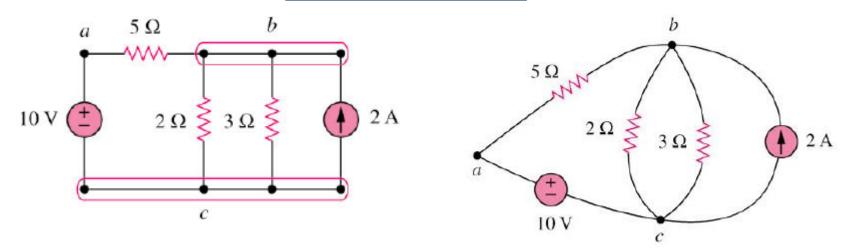
#### **Electric Circuits**

James W. Nilsson & Susan A. Riedel 9th Edition.

# Branches, Nodes, Loops

- A branch represents a single element such as a voltage source or a resistor.
- A node is the point of connection between two or more branches.
- A loop is any closed path in a circuit.
- A network with N branches, n nodes, and m independent loops will satisfy the fundamental theorem of network topology:

$$N = n + m - 1$$



# Kirchhoff's Law

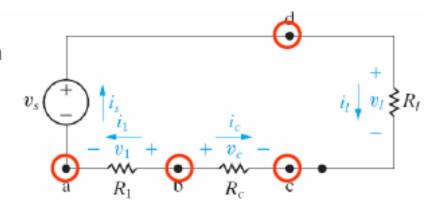


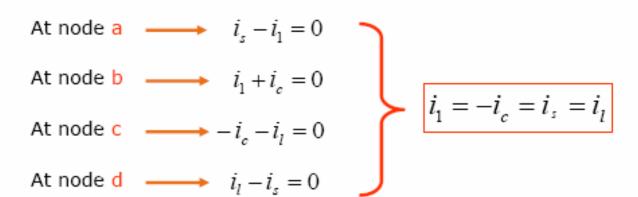
- Kirchhoff's Current Law (KCL)
- The algebraic sum of all the currents at <u>any node</u> in the circuit equals zero
- The sum of the currents entering any node must equal the sum of the currents leaving that node
- Kirchhoff's Voltage Law (KVL)
- The algebraic sum of all the voltages around <u>any closed path</u> in a circuit equals a zero
- The sum of the potential difference across all elements around any closed loop must be zero

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# Kirchhoff's Current Law

- Assign an algebraic sign corresponding to a reference direction.
  - Positive sign to a current leaving.
  - Negative sign to current entering the node.





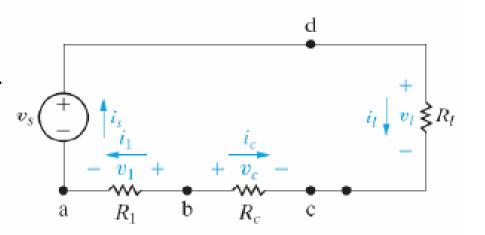
#### Note:

In any circuit with n nodes, n-1 independent current equations can be derived from Kirchhoff's current law.

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# Kirchhoff's Voltage Law

- Assign an algebraic sign (reference direction) to each voltage in the loop.
  - Positive sign to a voltage rise requires assigning a negative sign to a voltage drop.



$$-v_{s}+v_{l}-v_{c}+v_{1}=0$$

$$(a \rightarrow d \rightarrow c \rightarrow b \rightarrow a)$$

Finally, applying Ohm's law

$$v_1 = i_1 R_1$$

$$v_c = i_c R_c$$

$$v_l = i_l R_l$$

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# Ohm's Law

- Ohm's law states that the voltage across a resistor is directly proportional to the current *I* flowing through the resistor.
- Mathematical expression for Ohm's Law is as follows: v = i.R

$$R = Resistance$$

• Two extreme possible values of R:

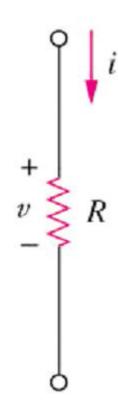
**0** (zero) and 
$$\infty$$
 (infinite)

are related with two basic circuit concepts:

short circuit and open circuit.

The power dissipated by a resistor:

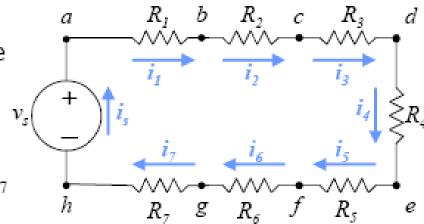
$$p = v \cdot i = i^2 \cdot R = \frac{v^2}{R}$$



### Resistors in series

- Just two elements connected at a single node are said to be in series.
- Applying KCL at all nodes.

$$i_s = i_1 = i_2 = i_3 = i_4 = i_5 = i_6 = i_7$$



Series-connected circuit elements carry the same current

Applying KVL

$$-v_s + i_s R_1 + i_s R_2 + i_s R_3 + i_s R_4 + i_s R_5 + i_s R_6 + i_s R_7 = 0$$
 or 
$$v_s = i_s \left( \underbrace{R_1 + R_2 + R_3 + R_4 + R_5 + R_6 + R_7}_{R_{eq}} \right)$$

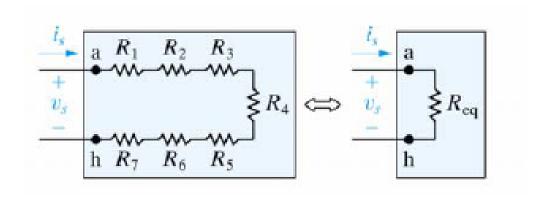
$$R_{eq} = R_1 + R_2 + R_3 + R_4 + R_5 + R_6 + R_7 \longrightarrow v_s = i_s R_{eq}$$

Constant sources are often called **dc sources**. The dc stands for direct current. Therefore, a constant voltage became known as a direct current, or dc, voltage.

# Resistors in series (cont.)

 In general, if k resistors are connected in series, the equivalent single resistor has a resistance equal to the sum of the k resistances, or

$$R_{eq} = \sum_{i=1}^{k} R_i = R_1 + R_2 + \ldots + R_k$$



# Resistors in parallel

 When two elements connect at a single <u>node</u> <u>pair</u>, they are said to be connected in parallel.

Parallel-connected circuit elements have the same voltage

across their terminals.

Applying KCL

$$---i_s = i_1 + i_2 + i_3 + i_4 - -$$

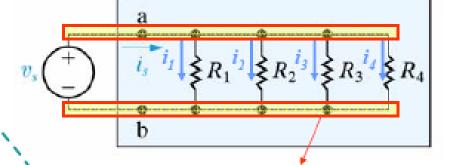
From Ohm's law

$$i_1 R_1 = i_2 R_2 = i_3 R_3 = i_4 R_4 = v_s$$

Therefore

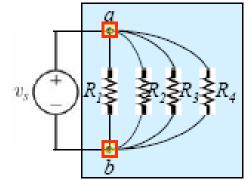
$$i_1 = \frac{v_s}{R_1}$$
,  $i_2 = \frac{v_s}{R_2}$ ,  $i_3 = \frac{v_s}{R_3} & i_4 = \frac{v_s}{R_4}$ 

$$i_s = \frac{v_s}{R_1} + \frac{v_s}{R_2} + \frac{v_s}{R_3} + \frac{v_s}{R_4}$$



Same node "No elements connected"

between nodes"

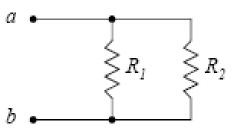


# Resistors in parallel (cont.)

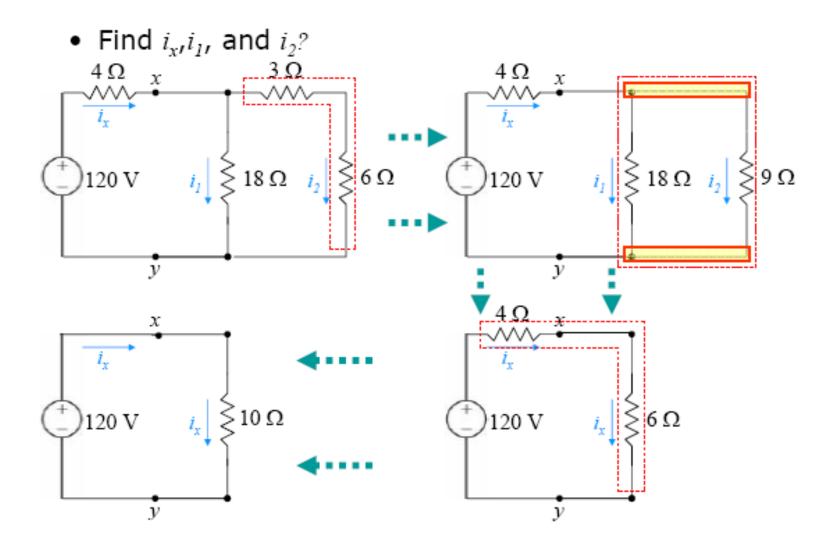
$$\begin{split} i_s &= v_s \bigg( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \bigg) \\ \frac{i_s}{v_s} &= \frac{1}{R_{eq}} = \bigg( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \bigg) \\ \frac{1}{R_{eq}} &= \sum_{i=1}^k \frac{1}{R_i} = \bigg( \frac{1}{R_1} + \frac{1}{R_2} + \ldots + \frac{1}{R_k} \bigg) \\ G_{eq} &= \sum_{i=1}^k G_i = \big( G_1 + G_2 + \ldots + G_k \big) \end{split}$$

Special Case (two resistors in parallel)

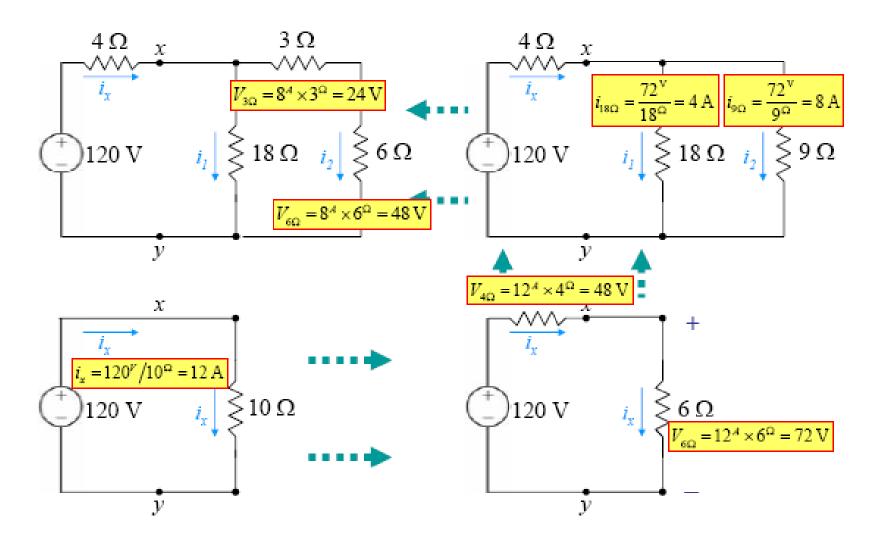
$$\begin{split} \frac{1}{R_{eq}} &= \frac{1}{R_1} + \frac{1}{R_2} = \frac{R_1 + R_2}{R_1 R_2} \\ R_{eq} &= \frac{R_1 R_2}{R_1 + R_2} \end{split}$$



# **Example 3.1**



# Example (Cont.)



# **Assessing Objective 1**

Find (a) ν, (b) power delivered to the circuit by the current source, and (c) the power dissipated in the 10 Ω resistor.

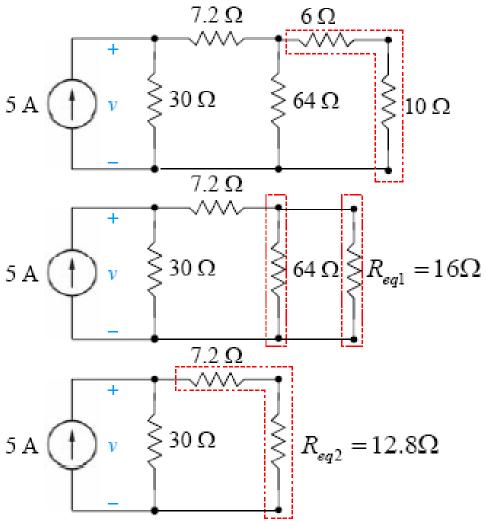


•The 6  $\Omega$  is in series with the 10  $\Omega$ ,

$$R_{eq1} = 6 + 10 = 16 \Omega$$

•The 16  $\Omega$  is in parallel with the 64  $\Omega$ ,

$$R_{eq2} = \frac{16 \times 64}{16 + 64} = 12.8 \,\Omega$$



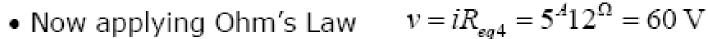
# Example (cont.)

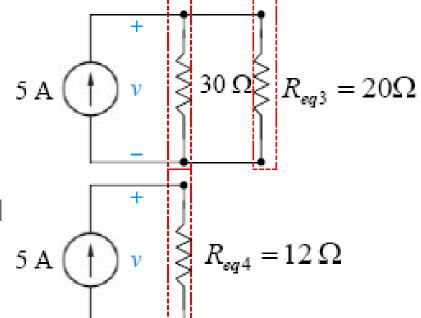
 The 12.8 O is in. series with the 7.2  $\Omega$ ,

$$R_{eq3} = 7.2 + 12.8 = 20 \Omega$$

•The 30  $\Omega$  is in parallel with the 20  $\Omega$ ,

$$R_{eq4} = \frac{30 \times 20}{30 + 20} = 12 \,\Omega$$



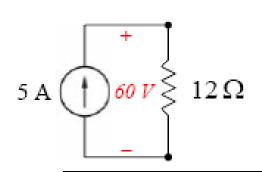


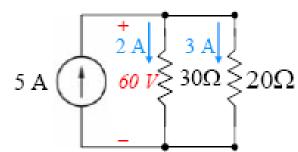
$$v = iR_{ea4} = 5^{A}12^{\Omega} = 60 \text{ V}$$

Power delivered by the current source

$$p = iv = 5^A 60^V = 300 \text{ W}$$

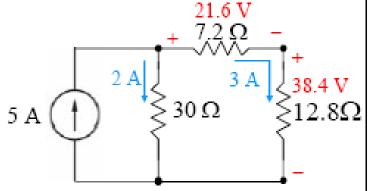
# Example (cont.)





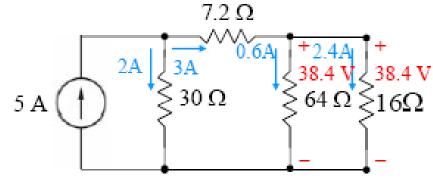
$$i_{30\Omega} = \frac{60^V}{30^{\Omega}} = 2 \text{ A}$$

$$i_{20\Omega} = \frac{60^{\nu}}{20^{\Omega}} = 3 \text{ A}$$



$$v_{7.2\Omega} = 3^A \times 7.2^{\Omega} = 21.6 \text{ V}$$

$$v_{12.8\Omega} = 3^{A} \times 12.8^{\Omega} = 38.4 \text{ V}$$



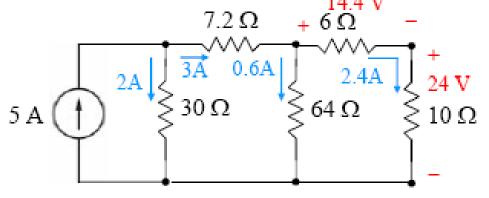
$$i_{64\Omega} = \frac{38.4^{V}}{64^{\Omega}} = 0.6 \text{ A}$$

$$i_{64\Omega} = \frac{38.4^{V}}{16^{\Omega}} = 2.4 \text{ A}$$

# Example (cont.)

$$v_{6\Omega} = 2.4^{A} \times 6^{\Omega} = 14.4 \text{ V}$$

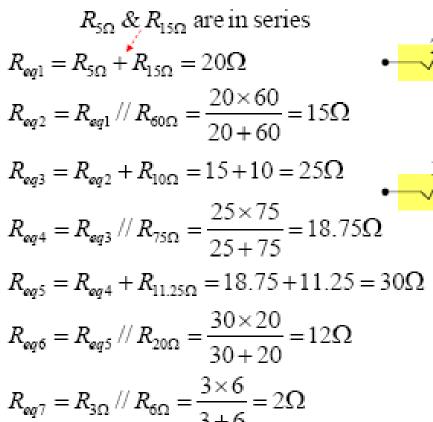
$$v_{10\Omega} = 2.4^{A} \times 10^{\Omega} = 24 \text{ V}$$

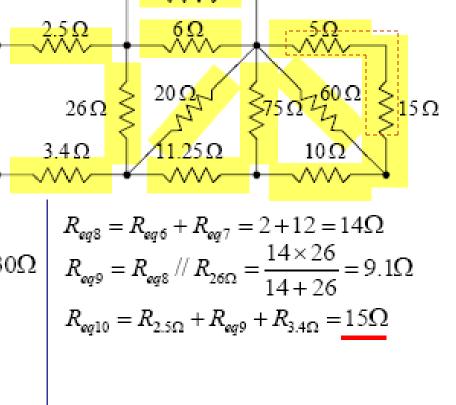


•The power dissipated in the 10  $\Omega$  resistor

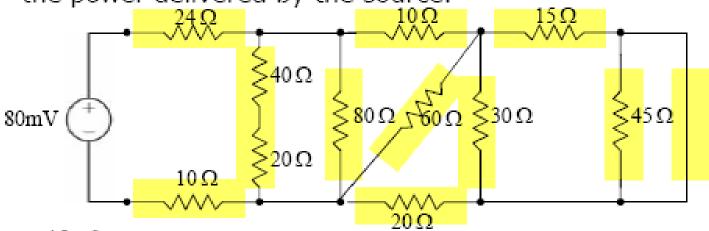
$$p_{10\Omega} = 2.4^A \times 24^V = 57.6 \text{ W}$$

Find the equivalent resistance R<sub>ab</sub> for the circuit in Figure.





 In the circuit shown, find the equivalent resistance R<sub>ab</sub>, and the power delivered by the source.



$$R_{eq1} = \frac{45 \times 0}{45 + 0} = 0\Omega \text{ (Short Circuit)}$$

$$R_{eq2} = \frac{15 \times 30}{15 + 30} = 10\Omega$$

$$R_{eq3} = 30 + 20 = 50\Omega$$

$$R_{eq4} = \frac{30 \times 60}{30 + 60} = 20\Omega$$

$$R_{eq5} = 10 + 20 = 30\Omega$$

$$R_{eq6} = \frac{1}{\frac{1}{60} + \frac{1}{80} + \frac{1}{30}} = 16\Omega$$

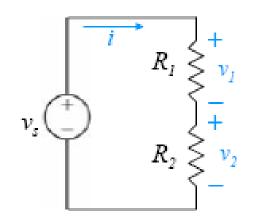
$$R_{eq7} = 24 + 16 + 10 = 50\Omega$$

$$P_{80mV} = \frac{\left(80 \times 10^{-3}\right)^2}{50} = 128\mu\text{W}$$

# The voltage-divider circuit

Apply KVL

$$\begin{aligned} v_s &= iR_1 + iR_2 \\ i &= \frac{v_s}{R_1 + R_2} \\ v_1 &= iR_1 = v_s \frac{R_1}{R_1 + R_2} \end{aligned} \quad \& \quad v_2 = iR_2 = v_s \frac{R_2}{R_1 + R_2}$$



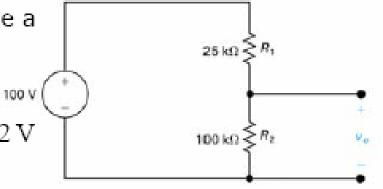
### Example:

If the resistors used in the circuit have a tolerance of  $\pm 10\%$ . Find  $v_{omax}$  and  $v_{omin}$ 

Ans.:-

$$v_o(\text{max}) = 100 \frac{100 \times 1.1}{100 \times 1.1 + 25 \times 0.9} = 83.02 \text{ V}$$

$$v_o(\text{min}) = 100 \frac{100 \times 0.9}{100 \times 0.9 + 25 \times 1.1} = 76.60 \text{ V}$$



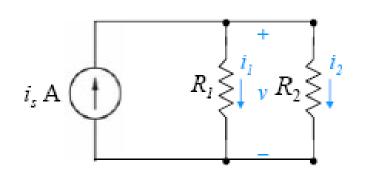
### The current-divider circuit

$$R_1 // R_2 \Longrightarrow R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

Ohm's Law

$$v = i_1 R_1 = i_2 R_2 = i_z R_{eq} = i_z \frac{R_1 R_2}{R_1 + R_2}$$

$$i_1 = \frac{R_2}{R_1 + R_2} i_s$$
 &  $i_2 = \frac{R_1}{R_1 + R_2} i_s$ 



#### Example:

Find the power dissipated in the 6  $\Omega$  resistor

$$6\Omega // 4\Omega + 1.6\Omega$$

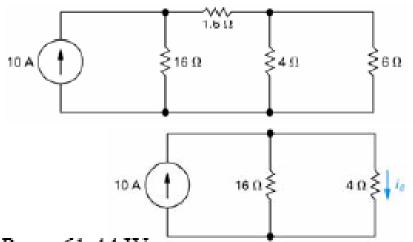
$$R_{eq} = \frac{4 \times 6}{4 + 6} + 1.6 = 4 \Omega$$

Using Current Divider

$$i_o = \frac{16}{16+4}10 = 8 \text{ A}$$

Using Current Divider

$$i_6 = \frac{4}{4+6} 8 = 3.2 \text{ A}$$
  $P_6 = i_{6\Omega}^2 R_{6\Omega} = 61.44 \text{ W}$ 



# **Assessing Objective 2**

Find (a)  $v_o$  at no load, (b)  $v_o$  when  $R_L = 150 \text{k}\Omega$ . (c) Power dissipated in 25 k $\Omega$  if the load is short circuited. (d) max. power in 75 k $\Omega$ .

Ans.:-

(a) 
$$v_o = 200 \frac{75k}{75k + 25k} = 150 \text{ V}$$

(b) 
$$R_{eq} = \frac{75k \times 150k}{75k + 150k} = 50k\Omega \implies v_o = 200 \frac{50k}{50k + 25k} = 133.33 \text{ V}$$

(c) 
$$P_{25k\Omega} = \frac{V^2}{R_{25k\Omega}} = \frac{200^2}{25k} = 1.6 \text{ W}$$

(d) 
$$P_{75k\Omega}^{\text{max}} = \frac{V^2}{R_{75k\Omega}} = \frac{150^2}{75k} = 0.3 \text{ W}$$

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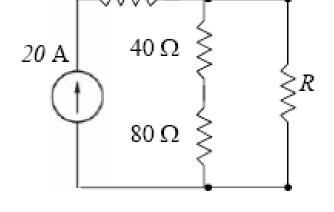
25 **k**Ω

# **Assessing Objective**

Find (a) R so 
$$i_{\delta\theta\Omega}$$
=4A, (b)  $P_{R\Omega}$ , (c)  $P_{20A}$ 

#### Ans.:-

(a) 
$$i_{80\Omega} = 4 = \frac{R}{R + 80 + 40} 20$$
  $R = 30\Omega$ 



 $60 \Omega$ 

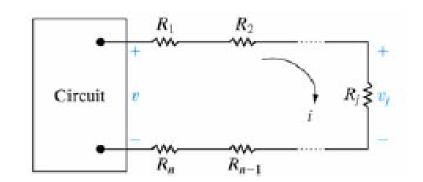
(b) 
$$P_{RO} = i_{RO}^2 R = 7680 \Omega$$

(c) 
$$V_{20A} = 20^A \times 60^\Omega + 4^A \times 120^\Omega = 1680 \text{ V}$$
  
 $P_{20A} = 20^A \times 1680^V = 33600 \text{ W}$ 

# **Voltage Division and Current Division**

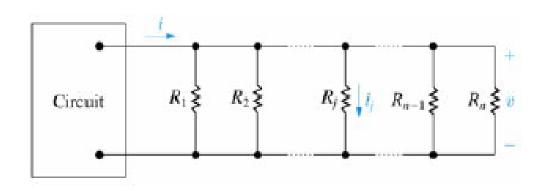
$$i = \frac{v}{R_1 + R_2 + \dots + R_n} = \frac{v}{R_{eq}}$$
$$v_j = iR_j$$

$$v_j = \frac{R_j}{R_{eq}} v$$



$$v = i(R_1 || R_2 || \dots || R_n) = iR_{eq}$$
$$v = i_j R_j$$

$$i_j = \frac{R_{eq}}{R_j}i$$



# Example 3.4

Use current division to find  $i_o$  and voltage division to find  $v_o$ 

#### Ans.:-

$$R_{eq} = \frac{1}{\frac{1}{80} + \frac{1}{10} + \frac{1}{80} + \frac{1}{24}} = 6 \Omega$$

Current Division

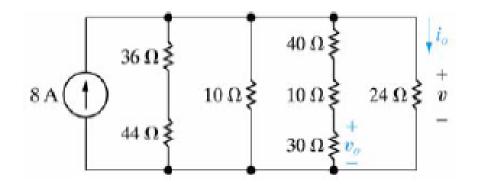
$$i_o = \frac{6}{24} 8^A = 2 \text{ A}$$

Ohm's Law

$$v_{24} = 2^{A}24^{\Omega} = 48 \text{ V}$$

Voltage Division

$$v_o = 48^{\rm V} \frac{30^{\rm \Omega}}{80^{\rm \Omega}} = 18 \,{\rm V}$$



# **Assessing Objective 3**

Use voltage division & current division to find (a)  $v_{o}$  (b)  $i_{40\Omega}$  &

$$i_{30\Omega}$$
, (c)  $P_{50\Omega}$ .

#### Ans.:-

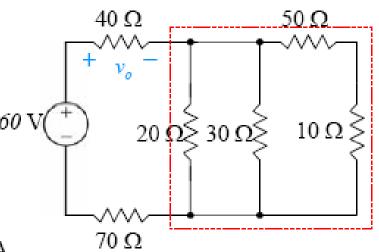
(a) 
$$R_{eq1} = \frac{1}{\frac{1}{20} + \frac{1}{30} + \frac{1}{60}} = 10 \,\Omega$$
  
 $v_o = 60^V \frac{40}{40 + 10 + 70} = 20 \,\text{V}$ 

(b) 
$$i_{40\Omega} = \frac{60^V}{120^{\Omega}} = 0.5 \text{ A}$$

$$i_{30\Omega} = i_{40\Omega} \frac{R_{eq1}}{R_{30\Omega}} = 0.5^A \frac{10}{30} = 0.1667 \text{ A}$$
(c)  $v_{R_{eq1}} = 60^V \frac{10}{40 + 10 + 70} = 5 \text{ V}$   $v_{50\Omega} = 5^V \frac{50}{50 + 10} = 4.1667 \text{ V}$ 

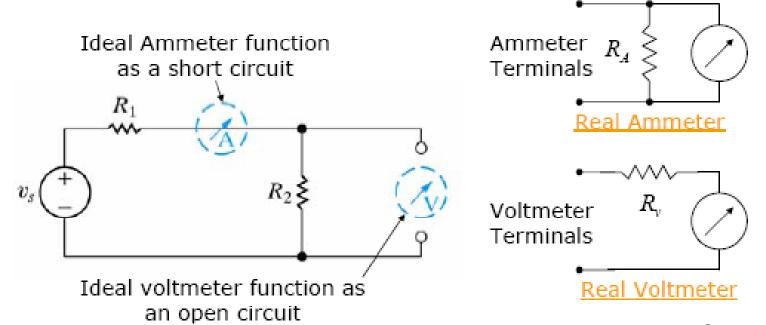
(c) 
$$v_{R_{eq1}} = 60^{V} \frac{10}{40 + 10 + 70} = 5 \text{ V}$$
  $v_{50\Omega} = 5^{V} \frac{50}{50 + 10} = 4.1667 \text{ V}$ 

$$P_{50\Omega} = \frac{V_{50\Omega}^2}{R_{50\Omega}} = 0.3472 \text{ W}$$



# **Measuring Voltage and Current**

- An ammeter is an instrument designed to measure current; it is placed in series with the circuit element whose current is being measured.
- A voltmeter is an instrument designed to measure voltage; it is placed in parallel with the element whose voltage is being measured.



An ideal ammeter has an equivalent resistance of 0  $\Omega$  An ideal voltmeter has an infinite equivalent resistance

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### **Example 3.5 & 3.6**

- (a) A 50 mV, 1 mA ammeter with a full scale of 10 mA. Determine R<sub>A</sub>.
- (b) How much resistance is added to the circuit when the 10 mA meter is inserted to measure current?
  - (a) Meaning: When 10 mA is to be measured 1 mA will be moving in the coil; accordingly 9 mA will be moving in the R<sub>A</sub>.

$$9 \times 10^{-3} R_A = 50 \times 10^{-3} \dots \qquad R_A = 50/9 = 5.555 \Omega$$
(b)  $R_m = \frac{50 \, mV}{10 \, mA} = 5 \, \Omega$ 

- (a) A 50 mV, 1 mA ammeter with a full scale of 150 V. Determine  $R_{\rm v}$ .
- (b) How much resistance is added to the circuit when the 150 V meter is inserted to measure current?

ans.:

(a) 
$$R_{movement} = \frac{50 \, mV}{1 \, mA} = 50 \, \Omega$$
,  $50 \times 10^{-3} = \frac{50}{R_v + 50} = 150 \, \Omega$ 

$$R_v = 149,950 \,\Omega$$
  
(b)  $R_m = \frac{150^v}{10^{-3}} = 150,000 \,\Omega$ 

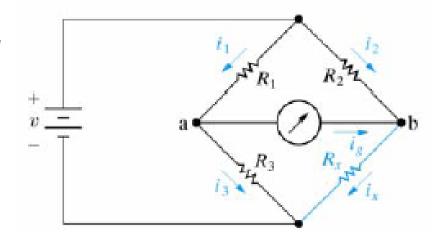
# Measuring Resistance-The Wheatstone Bridge

 To find R<sub>x</sub>, the value of R<sub>3</sub> is adjusted until there is no current in the meter.

 $i_g = 0$  Means balanced bridge.

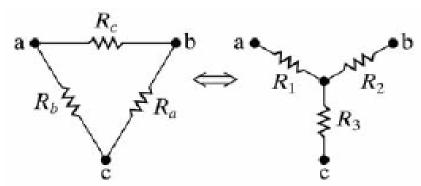
& V<sub>ab</sub>=0 "same potential at a as b"

$$\begin{array}{ll} \underline{\mathsf{KCL}} & i_1 = i_3 & \& \quad i_2 = i_x \\ \\ \underline{\mathsf{KVL}} & i_3 R_3 = i_x R_x & \& \quad i_1 R_1 = i_2 R_2 \\ \\ & i_1 R_3 = i_2 R_x \end{array}$$



$$\frac{i_1}{i_2} = \frac{R_2}{R_1} = \frac{R_x}{R_3} \qquad \square > \qquad R_x = \frac{R_2}{R_1} R_3$$

### The ∆-to-Y transformation



 The resistance between terminals a and b must be the same whether we use Δ-connected set or the Y-connected circuit.

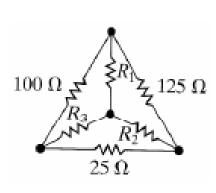
$$\begin{split} R_{ab} &= \frac{R_c \left( R_a + R_b \right)}{R_a + R_b + R_c} = R_1 + R_2 \\ R_{bc} &= \frac{R_a \left( R_b + R_c \right)}{R_a + R_b + R_c} = R_2 + R_3 \\ R_{ca} &= \frac{R_b \left( R_c + R_a \right)}{R_a + R_b + R_c} = R_1 + R_3 \\ \end{split} \qquad \begin{array}{l} R_1 &= \frac{R_b R_c}{R_a + R_b + R_c} \\ R_2 &= \frac{R_c R_a}{R_a + R_b + R_c} \\ \end{array} \qquad \begin{array}{l} R_2 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} \\ R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} \\ \end{array} \qquad \begin{array}{l} R_2 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} \\ \end{array} \qquad \begin{array}{l} R_2 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_a R_b}{R_a + R_b + R_c} \\ \end{array} \qquad \begin{array}{l} R_2 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_2 + R_3 R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_1}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_3 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_1 &= \frac{R_1 R_3 R_3 R_3}{R_3} \\ \end{array} \qquad \begin{array}{l} R_1 &= \frac{R_$$

# Example 3.7

Find the current and power supplied by the 40 V source.

#### Ans.:

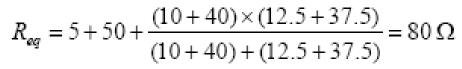
We can convert  $\Delta(100, 125, 25 \Omega)$ or  $\Delta(25,40,37.5 \Omega)$ 



$$R_1 = \frac{100 \times 125}{100 + 125 + 25} = 50 \Omega$$

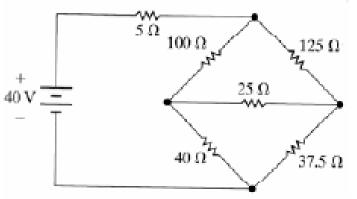
$$R_2 = \frac{125 \times 25}{100 + 125 + 25} = 12.5 \,\Omega$$

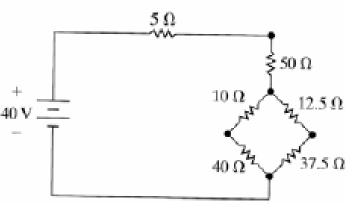
$$R_2 = \frac{100 \times 25}{100 + 125 + 25} = 10 \Omega$$

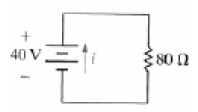


$$i = \frac{40^V}{80^\Omega} = \underline{0.5 \text{ A}}$$
  $P = 0.5^A \times 80^\Omega = \underline{40 \text{ W}}$ 

$$P = 0.5^{\text{A}} \times 80^{\Omega} = 40 \text{ W}$$







# **Assessing Objective 6**

Use Y-to- $\Delta$  transformation to find  $\nu$ .

#### Ans.:

$$R_a = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{5} = 70 \,\Omega$$

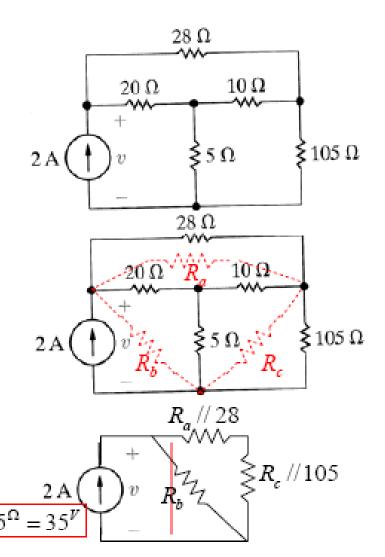
$$R_b = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{10} = 35 \,\Omega$$

$$R_c = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{20} = 17.5 \,\Omega$$

$$R_{eq1} = \frac{28 \times 70}{28 + 70} = 20 \,\Omega$$

$$R_{eq2} = \frac{17.5 \times 105}{17.5 + 105} = 15 \,\Omega$$

$$R_{eq3} = \frac{35 \times (20 + 15)}{35 + (20 + 15)} = 17.5 \,\Omega \quad v = 2^{A} \times 17.5^{\Omega} = 35^{A}$$



Select  $R_1$ ,  $R_2 \otimes R_3$  in the circuit to meet the following design requirements:

- a) The total power supplied is 36 W.
- b)  $v_1 = 12 \text{ V}, v_2 = 6 \text{ V}, \text{ and } v_3 = -12 \text{ V}.$

Ans.:-

(a) 
$$P_{24^{V}} = \frac{V^2}{R_{eq}} = \frac{(24)^2}{R_1 + R_2 + R_3} = 36$$
  
 $R_1 + R_2 + R_3 = 16 \Omega$ ....

(b) Using Voltage dividers

$$v_{1} = 24^{V} \frac{R_{1} + R_{2}}{R_{1} + R_{2} + R_{3}} = 12^{V}, R_{1} + R_{2} = \frac{12}{24} \times (R_{1} + R_{2} + R_{3}) = 8 \Omega, R_{1} + R_{2} = 8 \Omega$$

$$v_{2} = 24^{V} \frac{R_{2}}{R_{1} + R_{2} + R_{3}} = 6^{V}, R_{2} = \frac{6}{24} \times (R_{1} + R_{2} + R_{3}) = 4 \Omega$$

$$R_{1} + R_{2} = 8 \Omega$$

$$R_{2} = 4 \Omega$$

$$R_{1} = 4 \Omega$$

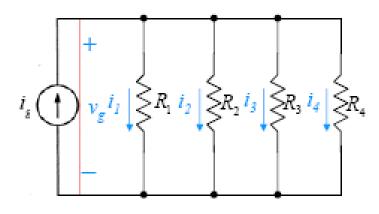
$$v_3 = -24^V \frac{R_3}{R_1 + R_2 + R_3} = -12^V \implies R_3 = 8 \Omega$$

Specify the value of the resistors in the circuit to meet the following design criteria:  $i_g=8$  mA;  $v_g=4$  V,  $i_1=2i_2$ ;  $i_2=10i_3$ ; and  $i_z = i_d$ 

Ans.:- 
$$v_{g} = i_{g} R_{eq}$$
,  $\frac{1}{R_{eq}} = \frac{1}{R_{1}} + \frac{1}{R_{2}} + \frac{1}{R_{3}} + \frac{1}{R_{4}}$ 

$$4^{V} = 8 \times 10^{-3} \left( \frac{1}{\frac{1}{R_{1}} + \frac{1}{R_{2}} + \frac{1}{R_{3}} + \frac{1}{R_{4}}} \right)$$

$$\frac{1}{R_{1}} + \frac{1}{R_{2}} + \frac{1}{R_{3}} + \frac{1}{R_{4}} = 2 \times 10^{-3}$$



$$i_j = \frac{v}{R_j} = \frac{R_{eq}}{R_j}i$$
  $i_1 = 2i_2 = \frac{R_{eq}}{R_1}i_g = 2\frac{R_{eq}}{R_2}i_g$ ,  $R_2 = 2R_1$ 

$$i_2 = 10i_3 \longrightarrow R_3 = 10R_2$$
  
 $i_3 = i_4 \longrightarrow R_3 = R_4$   
 $R_1 = 800 \Omega$ 

$$i_2 = 10i_3 \longrightarrow R_3 = 10R_2$$
  
 $i_3 = i_4 \longrightarrow R_3 = R_4$   
 $\frac{1}{R_1} + \frac{1}{2R_1} + \frac{1}{20R_1} + \frac{1}{20R_1} = \frac{32}{20R_1} = 2 \times 10^{-3}$ 

$$R_2 = 1.6 \,\mathrm{k}\Omega$$
  $R_3 = R_4 = 1.6 \,\mathrm{k}\Omega$ 

Find v<sub>o</sub>?

Ans.:-

Using current dividers

$$i_1 = \frac{200 + 1000}{300 + 300 + 200 + 1000} 15 \text{mA}$$

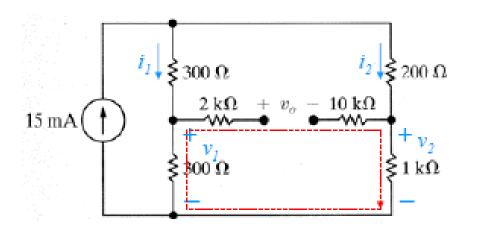
$$i_1 = 10 \text{mA}$$

$$i_2 = \frac{300 + 300}{300 + 300 + 200 + 1000} 15 \text{mA}$$

$$i_2 = 5 \text{mA}$$

$$v_1 = 10 \times 10^{-3} \times 300 = 3 \text{ V}$$
,  $v_2 = 5 \times 10^{-3} \times 1000 = 5 \text{ V}$ 

Applying KVL 
$$v_o + v_2 - v_1 = 0$$
  $v_o = v_1 - v_2 = 3 - 5$   $v_o = -2 \text{ V}$ 

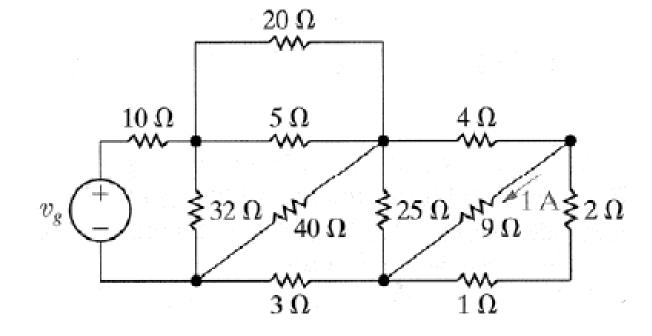


Find (a)  $v_g$ , (b) power dissipated in 20  $\Omega$ .

### Ans:-

$$v_g = 144 \text{ V}$$

$$P_{20\Omega} = 28.8 \text{ W}$$



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Find ν<sub>τ</sub> when the device in (b) is connected to the circuit.

#### Ans.:

$$R_{eq_i} = \frac{40 \times 10}{40 + 10} = 8 \Omega$$

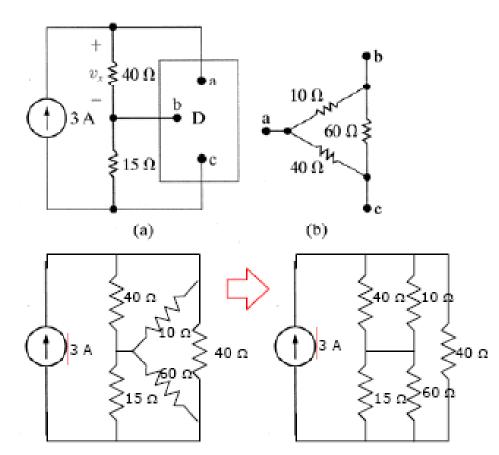
$$R_{eq2} = \frac{60 \times 15}{60 + 15} = 12 \,\Omega$$

$$R_{eq3} = 8 + 12 = 20 \Omega$$

$$i_{\text{Re}q3} = 3\frac{40}{20+40} = 2 \text{ A}$$

$$i_{40\Omega} = 2\frac{10}{10 + 40} = 0.4 \text{ A}$$

$$v_x = 0.4^A 40^\Omega = 16 \text{ V}$$



- (a) Find the resistance seen by the ideal voltage source in the circuit.
- (b) If  $v_{ab}$  equals 400 V, how much power is dissipated in the 31  $\Omega$  resistor.

#### Ans.:

$$R_{eq_{ab}}=80\,\Omega$$

$$P_{31\Omega} = 279 \text{ W}$$

