

Final Examination

Date: May 31, 2013

Duration: 120 minutes

SUBJECT: Electromagnetic Theory	
Dean of School of Electrical Engineering	Lecturer: Tran Van Su, M.Eng.
Signature:	Signature:
Full name: Tran Van Su	Full name: Tran Van Su

INTRODUCTIONS:

1. One sheet, A4-size paper, with your own hand-writing characters are allowed (Books are prohibited)
2. Laptop and communications devices are not allowed
3. Answer all questions

Question 1 (10 Marks)

For a sinusoidally time-varying plane wave propagating in free space, find the following:

- a) The wavelength λ , if the phase of the field at a particular value of time is observed to change by 0.05π in a distance of 2m along the direction of propagation of the wave;
- b) The frequency f , if the phase of the field at a point is observed to change by 2π radian in $0.075\mu\text{s}$;
- c) The wavelength λ , if the frequency is 6MHz;
- d) The frequency f , if the wavelength is 20m

Question 2 (20 Marks) D4.9

The magnetic field associated with a uniform wave propagating in the $-z$ direction in a nonmagnetic ($\mu = \mu_0$) material medium is given by

$$\vec{H} = 10e^{2z} \cos(12\pi \times 10^7 t + 2\sqrt{3}z) \vec{a}_x \text{ (A/m)}$$

Find the following:

- a) The instantaneous power flow across a surface of area 1m^2 in the $z = 0$ plane at $t = 0$
- b) The time-average power flow across a surface of area 1m^2 in the $z = 0$ plane
- c) The time-average power flow across a surface of area 1m^2 in the $z = -1$ plane

Question 3 (20 Marks)

An infinite plane sheet in the plane carries a surface current of density:

$$\mathbf{J}_s = -0.2 \cos 2\pi \times 10^6 t \mathbf{a}_x \text{ A/m}$$

The medium on either side of the sheet is characterized by $\sigma = 10^{-3} \text{ S/m}$, $\epsilon = 6\epsilon_0$, and $\mu = \mu_0$. Find \mathbf{E} and \mathbf{H} on either side of the current sheet.

Question 4 (25 Marks)

The magnetic field of a uniform plane wave in the free space is given by

$$\vec{H} = H_0 \cos(6\pi \times 10^8 t - 2\pi y) \hat{z} \text{ (A/m)}$$

Find the following:

- a) unit vectors along the direction of propagation of the wave (5 Marks)

- b) unit vectors along the direction of magnetic field at $t = 0, y = 0$ (5 Marks)
- c) unit vectors along the direction of electric field at $t = 0, y = 0$ (5 Marks)
- d) the wavelength of the wave (5 Marks)
- e) the pointing vector at $t = 0, y = 0$ in terms of magnitude and direction (5 Marks)

Question 5 (10 Marks)

Explain shortly why we study Maxwell's equation not only in integral form but also differential form?