

Final Examination

Date: May 29, 2015

Duration: 120 minutes

| SUBJECT: Electromagnetic Theory | |
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| Dean of School of Electrical Engineering Signature: | Lecturer Signature: |
| Full name: Tran Van Su | Full name: Tran Van Su |

INTRODUCTIONS:

1. One sheet, A4-size paper, with your own hand-writing characters is allowed (Books are prohibited)
2. Laptop and communications devices are not allowed except calculators
3. Answer all questions

Question 1 (10 Marks)

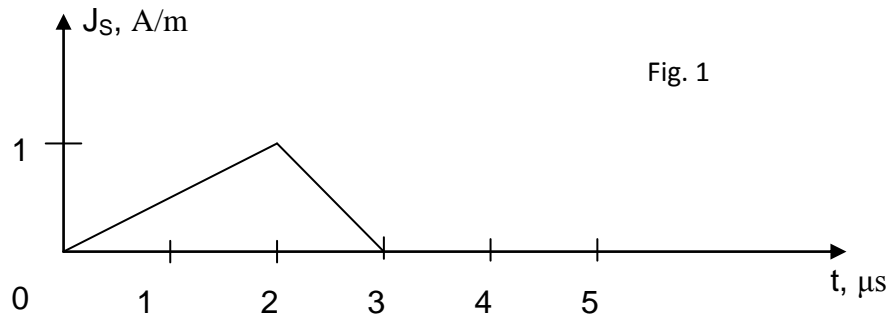
A square loop lies in the xy-plane forming the closed path C connecting the points (0,0,0), (2,0,0), (2,2,0), (0,2,0), and (0,0,0), in that order. A magnetic field \mathbf{B} exists in the region. From considerations of Lenz's law, determine whether the induced emf around the closed path C at $t = 0$ is positive, negative, or zero for each the following magnetic fields, where B_0 is a positive constant:

- $\vec{B} = B_0 \sin(3\pi t + \pi/4) \hat{z}$ [Wb/m²] (5 Marks)
- $\vec{B} = B_0 e^{-2t^2} \hat{z}$ [Wb/m²] (5 Marks)

Question 2 (20 Marks)

An infinite plane sheet lying in the $z = 0$ plane in free space ($v_p = 3 \cdot 10^8$ m/s, $\eta_0 = 120\pi \Omega$) carries a surface current of density $\vec{J}_s = -J_s \vec{a}_x$, where $J_s(t)$ is shown in Fig.1. Find and plot the waveform of:

- E_x versus t in the $z = 300$ m plane (10 Marks)
- H_y versus t for $z = 600$ m (10 Marks)



Question 3 (20 Marks)

Two sinusoidally time-varying vector fields are given by

$$\vec{F}_1 = \cos(6\pi \times 10^8 t - 2\pi z) \hat{x}$$
$$\vec{F}_2 = \cos(6\pi \times 10^8 t - 4\pi z) \hat{y}$$

Find the polarization of the sum of two given vectors at points (1, 1, 0) and (2, 2, 1/4).

Question 4 (20 Marks)

The parameters of the medium is given as follows:

$$\sigma = 10^{-4} \text{ S/m}, \epsilon = 4\epsilon_0, \mu = \mu_0, \text{ and } f = 10^6 \text{ Hz}, \epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}, \mu_0 = 4\pi \times 10^{-7} \text{ H/m}.$$

- Compute the propagation constant and intrinsic impedance. (5 Marks)
- If the magnitude of the magnetic field is E_0 . What is the magnitude of the magnetic field? (5 Marks)

- c. What is the phase difference between electric and magnetic fields? (5 Marks)
- d. Complete the expression of the electric field

$$\vec{E} = E_0 \cos(?t - ?z)\hat{x} \quad (3 \text{ Marks})$$

(Hint: Replace the question marks by proper values or functions)

- e. From the result in (d), Give the expression for magnetic field if the propagation direction is \hat{z} . (2 Marks)

Question 5 (10 Marks)

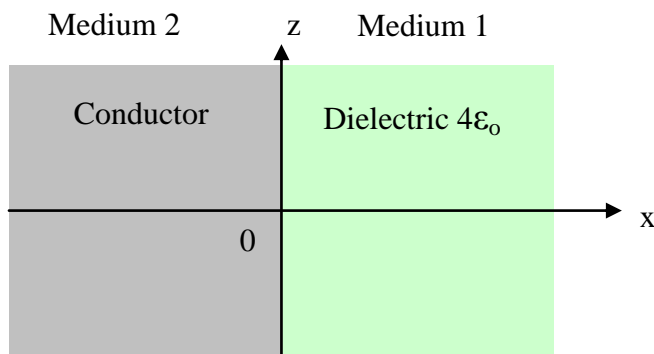
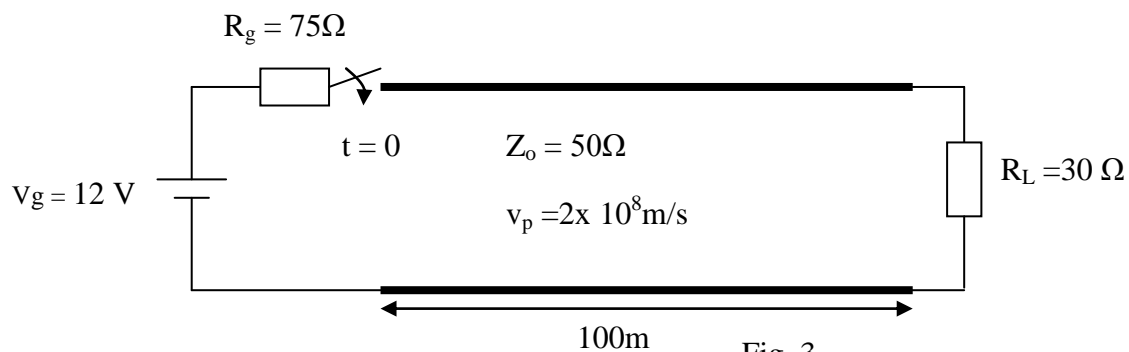


Fig. 2

Region $x \leq 0$ consists of a perfect conductor while region $x \geq 0$ is a dielectric medium as shown in the Fig. 2. If there is a surface charge of 5nC/m^2 on the boundary of the conductor and dielectric medium, determine

- The tangent components of \vec{E} and \vec{D} at the boundary.
- The normal components of \vec{E} and \vec{D} at the boundary.

Question 6 (20 Marks)



For the transmission line in Fig.3,

- Compute voltage reflection coefficients at the load and the source. (5 Marks)
- Sketch the bounce diagram of the voltage and note information on the diagram (up to $8\mu\text{s}$). (5 Marks)
- Sketch the bounce diagram of the current and note information on the diagram (up to $8\mu\text{s}$). (5 Marks)
- Calculate steady state V_{ss} and I_{ss} . (5 Marks)