

**Mid-term Examination**

Date: November , 2020

Duration: 90 minutes.

**SUBJECT: PRINCIPLES OF EE 2**

Dean of School of Electrical Engineering

Signature:

Lecturer: Mai Linh

Full name: Mai Linh

Signature:

**INSTRUCTIONS:** This is an opened-book examination.  
Laptop, tablets, & cell phones are not allowed during the exam

**A. Select the correct answer: (30 points)**

*“Step Response of an R-C Circuit with a DC voltage  $V_S$ ”.*

1. The current in the R-C circuit at a time  $t = 0^+$  is?

- a)  $V_S/R$       b)  $R/V_S$       c)  $V_S$       d)  $R$

2. In an R-C circuit, when the switch is closed, the response \_\_\_\_\_

- a) do not vary with time      b) decays with time  
c) rises with time  
d) first increases and then decreases

3. A series R-C circuit consists of resistor of  $10\ \Omega$  and capacitor of  $0.1\text{ F}$  as shown in the Fig. 1. A DC voltage  $V_S = 20\text{ V}$  is applied to the circuit at  $t = 0$ . What is the current in the circuit at  $t = 0^+$ ? Assume at  $t = 0$ , switch  $S$  is closed.

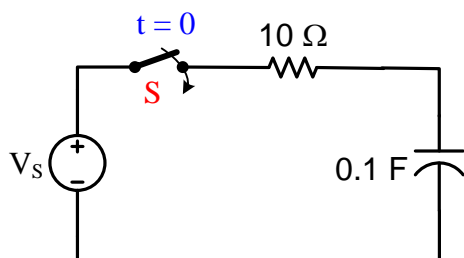


Fig. 1

- a) 1A      b) 2A      c) 3A      d) 4A

4. The current equation in the circuit shown in the question 3 is?

- a)  $i = 2(e^{-t})\text{ A}$       b)  $i = 2(e^t)\text{ A}$   
c)  $i = 2(-e^{-t})\text{ A}$       d)  $i = 2(-e^t)\text{ A}$ .

5. Determine the voltage across the capacitor in the circuit shown in the question 3 is?

- a)  $V_C = 20(1 - e^{-t})\text{ V}$       b)  $V_C = 20(1 + e^t)\text{ V}$   
c)  $V_C = 20(1 - e^t)\text{ V}$       d)  $V_C = 20(1 + e^{-t})\text{ V}$ .

*“Step Response of an R-L Circuit with a DC voltage  $V_S$ ”*

6. The value of the time constant in the R-L circuit is?

- a)  $L/R$       b)  $R/L$       c)  $R$       d)  $L$

7. After how many time constants, the transient part reaches more than 99 percent of its final value?

- a) 2      b) 3      c) 4      d) 5

8. A series R-L circuit with  $R = 30\ \Omega$  &  $L = 15\text{ H}$  has a constant voltage  $V_S = 60\text{ V}$  applied at  $t = 0$  as shown in the Fig. 2. Determine the current (A) in the circuit at  $t = 0^+$ ?

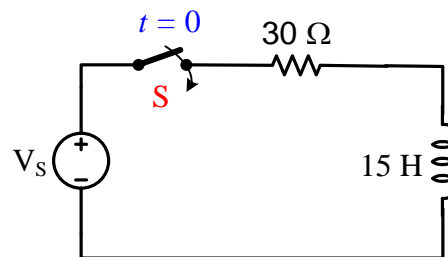


Fig. 2

- a) 1A      b) 2A      c) 3A      d) 0A

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9. The expression of current obtained from the circuit in terms of differentiation from the circuit shown in the question 8?

- a)  $\frac{di}{dt} + i = 4$                       b)  $\frac{di}{dt} + 2i = 0$   
 c)  $\frac{di}{dt} + 2i = 4$                       d)  $\frac{di}{dt} - 2i = 4$

10. Determine the voltage across the inductor in the circuit shown in the question 8 is?

- a)  $V_L = 60(-e^{-2t})$  V                      b)  $V_L = 60(e^{2t})$  V  
 c)  $V_L = 60(e^{-2t})$  V                      d)  $V_L = 60(-e^{2t})$  V

*“Step Response of an R-L-C Circuit”*

11. For an R-L-C circuit, if the roots of an equation are real and unequal, then the response will be?

- a) critically damped                      b) under damped  
 c) over damped                      d) damped

12. If the roots of an equation are complex conjugate, then the response will be?

- a) over damped                      b) critically damped  
 c) damped                      d) under damped

13. If the roots of an equation are real and equal, then the response will be?

- a) over damped                      b) damped  
 c) critically damped                      d) under damped

**B. Problems**

**Problem 1: (25 marks)** Given the circuit in Fig. 4.

- a) Construct the  $s$  – domain circuit from the given circuit?  
 b) Find the expression of voltage  $v_0(t)$  from the circuit by means of Laplace transform?

14. The circuit shown in the Fig. 3 consists of resistance, capacitance and inductance in series with a source  $V_S = 100$  V when the switch  $S$  is closed at  $t = 0$ . Find the equation obtained from the circuit in terms of current  $i$ ?

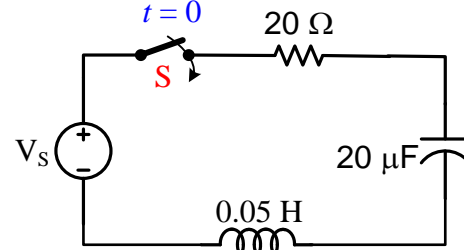


Fig. 3

- a)  $100 = 20i + 0.05 \frac{di}{dt} + \frac{1}{20 \times 10^{-6}} \int i dt$   
 b)  $100 = 20i - 0.05 \frac{di}{dt} + \frac{1}{20 \times 10^{-6}} \int i dt$   
 c)  $100 = 20i + 0.05 \frac{di}{dt} - \frac{1}{20 \times 10^{-6}} \int i dt$   
 d)  $100 = 20i - 0.05 \frac{di}{dt} - \frac{1}{20 \times 10^{-6}} \int i dt$

15. At time  $t = 0$ , the value of current in the circuit shown in the question 14 is?

- a) 1A                      b) 2A                      c) 3A                      d) 0A

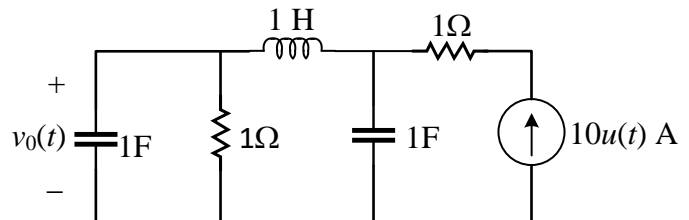


Fig. 4: Figure for Problem 1

**Problem 2: (25 marks)** The switch in the circuit (shown in Fig. 5) has been in position **a** for a long time. At  $t = 0$  it moves instantaneously to position **b**. Knowing that  $V = 24 \text{ V}$ ;  $R_1 = 3 \Omega$ ;  $R_2 = 5 \Omega$ ;  $R_3 = 20 \Omega$ ;  $C = 0.1 \text{ F}$ ;  $L = 5.625 \text{ H}$ .

a) Find  $V_0(s)$ ?

b) Find  $v_0(t)$ ?

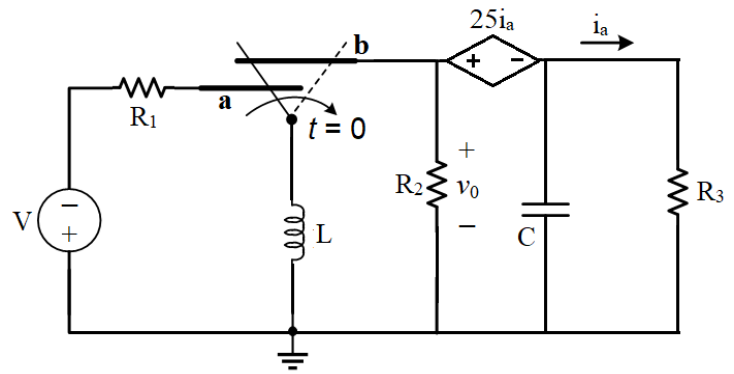


Fig. 5: Figure for Problem 2

**Problem 3: (20 marks)** For the following Laplace function  $F(s)$ , find the inverse Laplace transform  $\mathcal{L}^{-1}\{F(s)\}$ ?

$$F(s) = \frac{10s^3 + 40s^2 + 40s + 6}{s^4 + 6s^3 + 11s^2 + 6s}$$