International University School of Electrical Engineering

Introduction to Computers for Engineers

Dr. Hien Ta

Lecturely Topics

- Lecture 1 Basics variables, arrays, matrices
- Lecture 2 Basics matrices, operators, strings, cells
- Lecture 3 Functions & Plotting
- Lecture 4 User-defined Functions
- Lecture 5 Relational & logical operators, if, switch statements
- Lecture 6 For-loops, while-loops
- Lecture 7 Review on Midterm Exam
- Lecture 8 Solving Equations & Equation System (Matrix algebra)
- Lecture 9 Data Fitting & Integral Computation
- Lecture 10 Representing Signal and System
- Lecture 11 Random variables & Wireless System
- Lecture 12 Review on Final Exam
- References: H. Moore, MATLAB for Engineers, 4/e, Prentice Hall, 2014
 - G. Recktenwald, Numerical Methods with MATLAB, Prentice Hall, 2000
 - A. Gilat, MATLAB, An Introduction with Applications, 4/e, Wiley, 2011

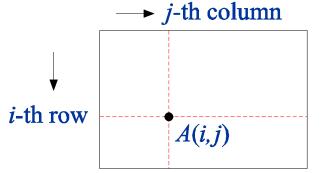
Arrays and Matrices

arrays and matrices are the most important data objects in MATLAB

Last week we discussed one-dimensional arrays, i.e., column or row vectors.

Next, we discuss matrices, which are two-dimensional arrays.

$$A = \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix}$$
 i-th row



matrix indexing convention

accessing matrix elements:

$$A = egin{bmatrix} 1 & 2 & 3 \ 2 & 0 & 4 \ 0 & 8 & 5 \end{bmatrix}$$

$$A = egin{array}{cccc} 1 & 2 & 3 \ 2 & 0 & 4 \ 0 & 8 & 5 \ \end{array}$$

$$A=egin{bmatrix}1&2&3\2&0&4\0&8&5\end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 0 & 4 \\ \hline 0 & 8 & 5 \end{bmatrix}$$

transposing a matrix: rows become columns and vice versa

transposition operation

For more information on elementary matrices see:

>> help elmat

Elementary matrices and matrix manipulation.

Elementary matrices:

```
- matrix of zeros
ones - matrix of ones
eye - identity matrix
repmat - replicate and tile an array
linspace - linearly spaced vector
logspace - logarithmically spaced vector
etc.
```

7. Operators and Expressions

operation	element-wise	matrix-wis	se	
addition subtraction multiplication division	+ - .* ./	+ - * /	fol rul	ese must low the les of linear
left division exponentiation	. ^	^	alg	gebra
transpose w/o complex conjugation transpose with complex conjugation				

```
>> help /
>> help precedence
```

```
>> a = [1 25];
>> b = [4 -5 1];
>> a+b
ans =
    5 -3 6
>> a.*b
ans =
    4 -10 5
>> a./b
ans =
   0.2500 - 0.4000 5.0000
>> a.\b
ans =
   4.0000 -2.5000 0.2000
% note: (a./b).*(a.\b) = [1,1,1]
```

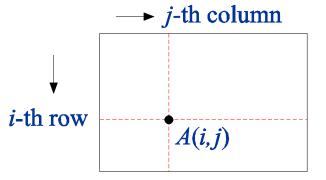
```
>> a = [2 3 4 5];
               % [2<sup>2</sup>, 3<sup>2</sup>, 4<sup>2</sup>, 5<sup>2</sup>]
>> a.^2
ans =
     4 9 16 25
               % [2^2, 2^3, 2^4, 2^5]
>> 2.^a
ans =
     4 8 16 32
>> a+10
ans =
     12 13 14 15
```

Matrix Manipulation

defining matrices accessing matrix elements colon operator, submatrices transposing a matrix changing/adding/deleting entries concatenating matrices special matrices diagonals, block-diagonal matrices replicating and reshaping matrices element-wise operations functions of matrices (element & column operations) meshgrid, ndgrid examples: DTMF keypad, Taylor series, polynomials

defining matrices

$$A = \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix}$$
 i-th row



matrix indexing convention

M N NxM matrix

% [N,M] = size(A), NxM matrix

column row
dimension dimension
no.rows no.columns

accessing matrix elements

$$A = egin{bmatrix} 1 & 2 & 3 \ 2 & 0 & 4 \ 0 & 8 & 5 \end{bmatrix}$$

$$A = egin{array}{cccc} 1 & 2 & 3 \ 2 & 0 & 4 \ 0 & 8 & 5 \ \end{array}$$

$$A=egin{bmatrix}1&2&3\2&0&4\0&8&5\end{bmatrix}$$

ans =

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 0 & 4 \\ \hline 0 & 8 & 5 \end{bmatrix}$$

concatenating columns

$$>> A = [1 2 3; 2 0 4; 0 8 5]$$

$$A =$$

$$A = egin{bmatrix} 1 \ 2 \ 0 \ 8 \end{pmatrix} egin{bmatrix} 3 \ 4 \ 5 \end{pmatrix}$$

% concatenate columns

column-wise indexing

concatenating rows

$$B = A'; B(:)$$

see also the built-in functions:

sub2ind, ind2sub

building a matrix column-wise

sub-matrices

$$A = \begin{bmatrix} 2 & 4 & 1 & 3 & 5 \\ 8 & 6 & 7 & 4 & 9 \\ 3 & 2 & 5 & 2 & 1 \\ 5 & 6 & 1 & 8 & 4 \end{bmatrix};$$

$$A(3:4, 2:4)$$
ans =
$$\begin{bmatrix} 2 & 4 & 1 & 3 & 5 \\ 4 & 9 & 2 & 1 \\ 8 & 4 & 9 & 2 \\ 1 & 8 & 4 & 9 \\ 4 & 9 & 2 & 2 \\ 1 & 8 & 4 & 9 \\ 2 & 1 & 8 & 4 \end{bmatrix};$$

$$A = \begin{bmatrix} 2 & 4 & 1 & 3 & 3 \\ 8 & 6 & 7 & 4 & 9 \\ 3 & 2 & 5 & 2 & 1 \\ 5 & 6 & 1 & 8 & 4 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 4 & 1 & 3 & 5 \\ 8 & 6 & 7 & 4 & 9 \\ 3 & 2 & 5 & 2 & 1 \\ 5 & 6 & 1 & 8 & 4 \end{bmatrix}$$

transposing a matrix

```
>> A = [1 2 3 4; 2 0 5 6; 0 8 7 9] % size 3x4
A =
                        6
     0
>> A'
                                       % size 4x3
ans =
           2
     3
            5
```

transposition operation

$$>> A = [1 2 3; 2 0 4; 0 8 5]$$

$$>> A(:,2) = []$$

% delete second column

A =

1 3

2 4

0 5

0 0

7 9

[] denotes an empty 0x0 matrix

alternatively, redefine A by omitting its second column:

$$>> A = A(:,[1,3]);$$

$$>> A = [1 2 3; 2 0 4; 0 8 5]$$

replacing rows or columns

$$A =$$

$$A =$$

```
>> A = [1 2 3; 2 0 4; 0 8 5]
                                       inserting rows
A =
                                       or columns
% insert new column between columns 2 & 3
A = [A(:,1:2), [10 20 30]', A(:,3)]
A =
                 10
                 20
                 30
% insert new row between rows 1 & 2
A = [A(1,:); [60 70 80 90]; A(2:3,:)]
A =
                 10
          70
    60
                 80
                        90
                 20
                         4
                 30
                         5
```

concatenating matrices

>> A = [1 2; 3 4];
>> B = [5 6; 7 8];
B =
$$\begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}$$

>> C = [A, B]
C =

1 2 5 6
3 4 7

A,B must have same number of rows

>> C = [A; B]

1 2 3 4 5 6

A,B must have same number of columns

appending columns or rows

```
>> b = [7; 7; 7];
>> c = [8 8 8]';
\gg B = [A,b,c]
B =
>> C = [b,A,c]
```

>>
$$\mathbf{A} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$
, $\mathbf{b} = \begin{bmatrix} 7 \\ 7 \\ 7 \end{bmatrix}$, $\mathbf{c} = \begin{bmatrix} 8 \\ 8 \\ 8 \end{bmatrix}$
>> $\mathbf{b} = \begin{bmatrix} 7 \\ 7 \end{bmatrix}$, $\mathbf{c} = \begin{bmatrix} 8 \\ 8 \\ 8 \end{bmatrix}$

```
>> D = [A; [7 7];]
>> E = [[8 8]; A]
E =
```

special matrices

```
>> help eye
>> help zeros
>> help ones
```

```
zeros(3) % 3x3 matrix of zeros
ans =
     0
     0
ones(3)
          % 3x3 matrix of ones
ans =
```

general usage:

eye(N,M)
zeros(N,M)
ones(N,M)

see also:

rand(N,M)
randn(N,M)
randi(I,N,M)

for more information on elementary matrices see:

```
>> help elmat
 Elementary matrices and matrix manipulation.
 Elementary matrices.
   zeros
              - Zeros array.
   ones
              - Ones array.
              - Identity matrix.
   eye
   repmat - Replicate and tile array.
   linspace
              - Linearly spaced vector.
   logspace
              - Logarithmically spaced vector.
   etc.
>> help gallery % various test matrices
```

diagonals

```
>> A = [1 2 3; 4 5 6; 7 8 9]
A =

1 2 3
4 5 6
7 8 9

>> help diag
```

% main diagonal

```
d =

1

5

9
```

diag(diag(A)) = what does it do?

```
>> d = diag(A,-1)
d =
4
```

>> d = diag(A,-1) % first sub-diagonal

how to make a diagonal matrix

```
>> d = [4 5 6]; % or, column d = [4 5 6]';
A = diag(d)
                     % d is main diagonal
A =
>> d = [4 5];
A = diag(d,1)
                     % d is first upper-diagonal
A =
              5
```

```
>> A = [1 2; 3 4]; B = [5 6; 7 8];
>> C = [9 8 7; 6 5 4; 3 2 1];
>> blkdiag(A,B)
                                     how to make
ans =
                                     block-diagonal
                                     matrices
                             matrix dimensions expand
>> blkdiag(A,B,C)
                             as necessary
ans
                               6
```

replicating matrices – using repmat

string

```
>> A=[1 2; 3 4]
A =
                                   repmat works also
                                   with other data types,
                                   such as strings or cell
                                   arrays
>> repmat(A, 3, 4)
ans
             2
       3
                   3
                              3
                                          3
>> s = repmat('%7.4f ', 1, 4)
S
                                       replicated
%7.4f
         %7.4f %7.4f %7.4f
```

reshaping a matrix or a vector

```
>> a = [1 2 3 4 5 6];
>> reshape(a,2,3)
ans =
                  5
>> reshape(a,3,2)
ans =
            5
```

```
B = reshape(A,P,Q)
```

reshapes an NxM matrix into a PxQ matrix (must have PxQ=NxM)

B is formed column-wise from the elements of A

reshaping a matrix or a vector

```
6
           5
         8
              4];
>> reshape (A, 3, 4)
ans
     2 5 8 0
         6
>> reshape (A, 2, 6)
ans
                           0
```

4

8

4

$$>> A = [1 2; 3 4]$$

$$A =$$



element-wise operation matrix-wise operation

% form sub-blocks

% note A.^2 ~= A^2

$$>> B = 10.^A;$$

```
>> A=[1 4; 8 2], B=[1 2; 2 1]
                                      element-wise
                                      matrix operations
A =
B =
            2
                            But note the matrix
                            operations:
>> A./B
                            >> sym(A/B) % A*inv(B)
ans =
                            ans =
                                [7/3, -2/3]
                                [-4/3, 14/3]
>> A.\B
                            >> A\B
                                        % inv(A) *B
ans =
                            ans
    1.0000
               0.5000
                                 0.2 0.0
    0.2500
               0.5000
```

0.5

element-wise matrix operations

$$A =$$

functions of matrices

```
>> X = [pi/2, pi/3; pi/4, pi/8]
X =
    1.5708 1.0472
                             many functions operate
    0.7854 0.3927
                              element-wise on matrices
                              e.g., trig, exp, log functions
>> sin(X)
ans =
                              others operate column-wise
    1.0000 0.8660
                              e.g., min, max, sort, diff,
    0.7071
               0.3827
                             mean, std, median,
                              sum, cumsum, prod, cumprod
>> sin(sym(X))
ans =
                     3^(1/2)/2]
[2^{(1/2)}/2, (2 - 2^{(1/2)})^{(1/2)}/2]
```

functions of matrices

functions that operate column-wise can also operate row-wise by using a second argument

```
\gg sum(A,2)
ans
     21
     13
     11
     10
>> cumsum (A, 2)
ans
             13
                    21
      8
             10
                    13
                    11
      6
              8
                    10
```

functions of matrices

means computed down each column

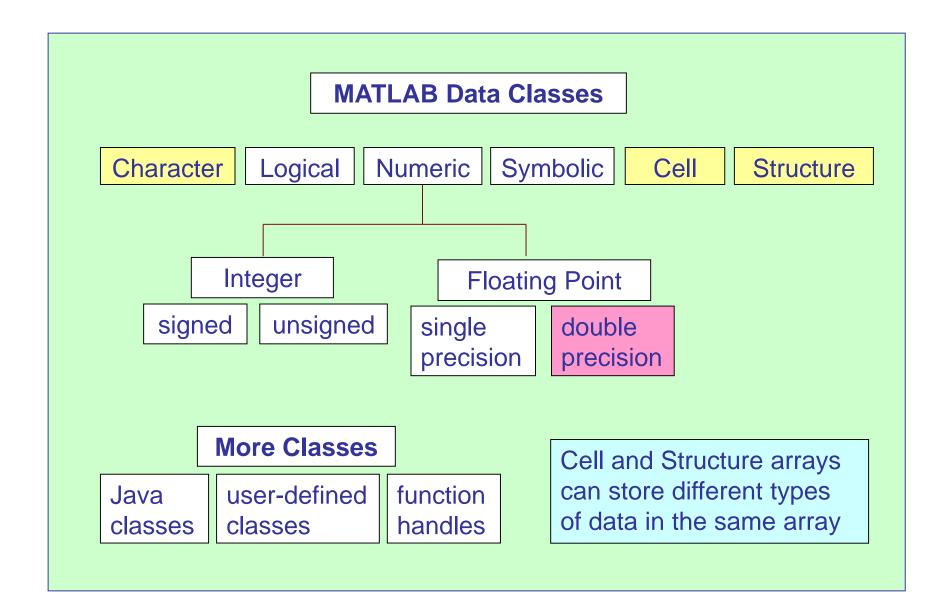
means computed across rows

min, max require a sightly different syntax for row-wise operation, similarly for diff, std

```
functions of matrices
A = [8]
                     8
                     3
      2
                     5
                                >> rot90(A)
      6
                     2];
                                ans
>> fliplr(A)
                                    5
ans
                                                           6
                     8
      8
             5
      5
                              rotate by 90 degrees
      2
                              reverse each row
>> flipud(A)
                              reverse each column
ans
      6
                              flipud(rot90(A)) and
      2
                     5
                              rot90(fliplr(A))
      9
                              are the same as A'
```

Strings, Cell Arrays, fprintf

- characters and strings
- concatenating strings
- using num2str
- comparing strings with strcmp
- cell arrays
- cell vs. content indexing
- fprintf summary & examples



Characters and Strings

```
>> c = 'A'
A
>> x = double(c)
x =
          % ASCII code for 'A'
    65
>> char(x)
ans =
A
>> class(c)
ans =
char
```

Strings are arrays of characters.

Characters are represented internally by standardized numbers, referred to as ASCII (American Standard Code for Information Interchange) codes. see Wikipedia link: ASCII table

char() creates a character string

>> doc char

>> doc class

```
>> s = 'ABC DEFG'
ABC DEFG
>> x = double(s)
x =
    65 66 67 32 68 69 70 71 ← ASCII codes
>> char(x)
                      convert ASCII codes to characters
ans =
ABC DEFG
                       s is a row vector of 8 characters
>> size(s)
ans =
                       >> s(2), s(3:5)
                       ans =
>> class(s)
                       B
ans =
                       ans =
char
```

Concatenating Strings

```
s = ['Albert', 'Einstein']
s =
AlbertEinstein
>> s = ['Albert', ' Einstein']
s =
                    preserve leading and trailing spaces
Albert Einstein
>> s = ['Albert ', 'Einstein']
s =
                             >> doc strcat
Albert Einstein
                             >> doc strvcat
                             >> doc num2str
>> size(s)
                             >> doc strcmp
ans =
                             >> doc findstr
          15
```

Concatenating Vertically

```
s = ['Apple'; 'IBM'; 'Microsoft'];
??? Error using ==> vertcat
CAT arguments dimensions are not consistent.
                              '; 'Microsoft']
s = ['Apple
                '; 'IBM
s =
Apple
                padded with spaces to the
IBM
                length of the longest string
Microsoft
>> size(s)
ans =
```

Concatenating Vertically

```
s = strvcat('Apple', 'IBM', 'Microsoft');
s = char('Apple', 'IBM', 'Microsoft');
s =
Apple
TDM
```

IBM Microsoft

```
>> size(s)
ans =
3 9
```

strvcat, char
both pad spaces as necessary

Recommendation:

use **char** to concatenate vertically,
and [] to concatenate horizontally

```
num2str
a = [143.87, -0.0000325, -7545]';
>> s = num2str(a)
s =
                      s = \text{num2str}(A)
    143.87
                      s = num2str(A, precision)
-3.25e-005
                      s = \text{num2str}(A, format)
     -7545
>> s = num2str(a, 4)
     143.9
                  max number of digits
-3.25e-005
     -7545
>> s = num2str(a, '%12.6f')
s =
  143.870000
                        format spec
   -0.000032
-7545.000000
```

Comparing Strings

Strings are arrays of characters, so the condition **s1==s2** requires both **s1** and **s2** to have the same length

```
>> s1 = 'short'; s2 = 'shore';
>> s1==s1
ans =
>> s1==s2
ans =
>> s1 = 'short'; s2 = 'long';
>> s1==s2
??? Error using ==> eq
Matrix dimensions must agree.
```

Comparing Strings

Use **strcmp** to compare strings of unequal length, and get a binary decision

```
>> s1 = 'short'; s2 = 'shore';
>> strcmp(s1,s1)
                               >> doc strcmp
ans =
                                >> doc strcmpi
>> strcmp(s1,s2)
ans =
                                   case-insensitive
>> s1 = 'short'; s2 = 'long';
>> strcmp(s1,s2)
ans =
```

Useful String Functions

```
    write formatted string

sprintf
sscanf

    read formatted string

deblank

    remove trailing blanks

            compare strings
strcmp
strcmpi - compare strings

    find possible matches

strmatch

    convert to upper case

upper

    convert to lower case

lower
blanks

    string of blanks

    left/right/center justify string

strjust
strtrim
            - remove leading/trailing spaces

    replace strings

strrep
            - find one string within another
findstr
```

Cell arrays are containers of all kinds of data: vectors, matrices, strings, structures, other cell arrays, functions.

A cell is created by putting different types of objects in curly brackets { }, e.g.,

where A,B,C,D are arbitrary objects

```
c{i,j} accesses the data in i,j cell
c(i,j) is the cell object in the i,j position
```

Cell Arrays

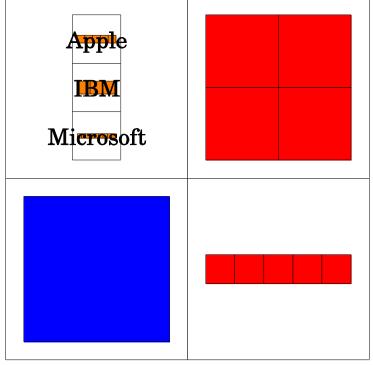
(see text Ch.11)

cell vs.
content
indexing

```
A = {'Apple'; 'IBM'; 'Microsoft'}; % cells
B = [1 \ 2; \ 3 \ 4];
                                       % matrix
C = @(x) x.^2 + 1;
                                       % function
D = [10 \ 20 \ 30 \ 40 \ 50];
                                       % row
c = {A,B;C,D} % define 2x2 cell array
  {3x1 cell} [2x2 double]
                                 Apple
  @(x)x.^2+1 [1x5 double]
                                  IBM
```

>> cellplot(c);

visual representation of the cell array



```
c\{1,1\}\{1\} =
Apple
c\{1,1\}\{2\} =
IBM
c\{1,1\}\{3\} =
Microsoft
c\{2,1\} =
     0(x)x.^2+1
c\{1,2\} =
c\{2,2\} =
     10
            20
                    30
```

```
>> c{1,1}
ans =
    'Apple'
    'IBM'
    'Microsoft'
>> c{2,1}
ans =
    0(x)x.^2+1
```

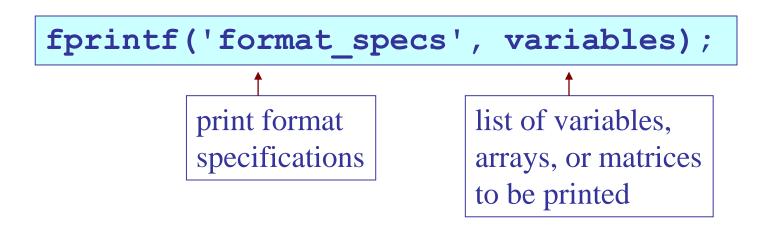
```
>> c{1,1}{3}
ans =
Microsoft
>> c{1,1}{3}(6)
ans =
S
>> x = [1 \ 2 \ 3];
>> c{2,1}(x)
ans =
                  10
>> fplot(c{2,1},[0,3]);
```

```
cell indexing ()
>> c(2,2)
                cell
                               content indexing { }
ans =
    [1x5 double]
>> class(c(2,2))
ans =
cell
>> c{2,2}
                cell contents
ans =
    10 20
                 30
                       40
                              50
>> class(c{2,2})
ans =
double
```

num2cell - converts numerical array into cell arraycell2mat - converts cell array into numerical array

```
>> D = cell2mat(c(1,2))
>> class(D)
ans =
    double
>> E = num2cell(D)
E =
   [1]
           [2]
   [3]
```

fprintf – summary & examples



- >> doc fprintf
- >> doc sprintf

see Sect.7.2 of text

```
>> fprintf('%10.6f\n', 100*pi)
                                     Example 1
>> fprintf('% 10.6f\n', 100*pi)
>> fprintf('%-10.6f\n', 100*pi)
>> fprintf('%+10.6f\n', 100*pi)
>> fprintf('%10.0f\n', 100*pi)
>> fprintf('%#10.0f\n', 100*pi)
>> fprintf('%010.0f\n', 100*pi)
314.159265
 314.159265
314.159265
                 different ways of printing 100*pi
+314.159265
       314
      314.
0000000314
10 spaces
```

```
%10.6f
  % 10.6f
  %-10.6f
  %+10.6f
  %10.0f
  %#10.0f
  %010.0f
flag
   field width
   & precision
```

```
% width 10, 6 decimal places
```

% leave space before field

% left-justify field

% print + or - signs

% no decimals

% print decimal point

% pad with zeros

conversion character:

d,	i		integer format
f			fixed-point format
e,	E,	g	exponential format
C,	S		character or string
¥			hexadecimal format

Example 2

```
>> [a, b, c]
a = [1; -2; 3; 4;];
b = [10; 20; -30; 40];
                                ans =
                                           10
                                                100
c = [100; 200; 300; -400];
                                    -2
                                          20
                                                200
                                          -30 300
      need at least %6.3f
                                           40
                                               -400
       to align first column
fprintf('%9.3f %9.3f %9.3f\n', [a, b, c]');
    1.000
              10.000
                         100.000
                                      vectorized version
                         200.000
   -2.000
              20.000
             -30.000
    3.000
                         300.000
    4.000
              40.000
                        -400.000
                                      loop version
for i=1:4,
  fprintf('%9.3f %9.3f %9.3f\n', a(i),b(i),c(i));
end
```

```
Example 3 - text & numbers
a = [1; -2; 3; 4;];
b = [10; 20; -30; 40];
s = {'a', 'bb', 'ccc', 'dddd'}; 
cell array of strings
for i=1:4,
  fprintf('%9.3f %9.3f %4s\n', a(i),b(i),s{i});
end
             10.000
    1.000
                        a
                                     note curly brackets
   -2.000 20.000
                        bb
    3.000 -30.000 ccc
    4.000
             40.000 dddd
                              max 4 characters
N = [num2cell([a';b']); s];
                                            using
fprintf('%9.3f %9.3f %-4s\n', N{:});
                                            a single
                                            fprintf
    1.000
             10.000
                      a
   -2.000
             20.000
                                            command
                     bb
                             left-justified
    3.000 -30.000 ccc
    4.000 40.000 dddd
```

```
% fprintf('%9.3f %9.3f %-4s\n', N{:});
>> N{:}
ans
                       use the three format specs to print
      10
                       each group of three entries in new row
     a
      -2
                        1.000
                                    10.000
                                               a
     20
                       -2.000
                                    20.000
                                               bb
     bb
                        3.000
                                   -30.000
                                               CCC
                        4.000
                                    40.000
                                               dddd
     3
      -30
      CCC
                       >> N
                       N
      4
                             [ 1]
                                                3]
                                                          4]
                                    [-2]
      40
                             [10]
                                    [20]
                                            [-30]
                                                         40]
     dddd
                                                        'dddd'
                             'a'
                                    'bb'
                                            'ccc'
```