

$$\textcircled{A} \left. \begin{aligned} p_1 &= m v_1 = F \Delta t \\ p_2 &= m v_2 = F \Delta t \end{aligned} \right\} \Rightarrow \Delta p = p_1 - p_2 = 0$$

### Assignment – Physics 1

$$K_1 = \frac{1}{2} m v_1^2 = \frac{1}{2} \frac{p^2}{m}$$

$$K_2 = \frac{1}{2} m v_2^2 = \frac{p^2}{4m}$$

1. Two carts, one twice the mass of the other, experience the same force for the same time. What is their difference in momentum? What is their difference in kinetic energy?

2. A  $12 \text{ g}$  bullet is fired horizontally into a  $96 \text{ g}$  wooden block initially at rest on a horizontal surface. After impact, the block slides  $7.5 \text{ m}$  before coming to rest. If the coefficient of kinetic friction between block and surface is  $0.60$ , what was the speed of the bullet immediately before impact?  $\rightarrow m_1 v_{1i} = (m_1 + m_2) v_f$   
 $\mu (m_1 + m_2) g = (m_1 + m_2) a \Rightarrow F_f = (m_1 + m_2) a$

3. A ball bounces upward from the ground with a speed of  $14 \text{ m/s}$  and hits a wall with a speed of  $12 \text{ m/s}$ . How high above the ground does the ball hit the wall? Ignore air resistance.

4. A  $200 \text{ g}$  mass is attached to a spring of spring constant  $k$ . The spring is compressed  $15 \text{ cm}$  from its equilibrium value. When released the mass reaches a speed of  $5 \text{ m/s}$ . What is the spring constant (in  $\text{N/m}$ )?  $\frac{1}{2} m v^2 = \frac{1}{2} k x^2$

5. A  $34\text{-g}$  bullet traveling at  $120 \text{ m/s}$  embeds itself in a wooden block on a smooth surface. The block then slides toward a spring and collides with it. The block compresses the spring ( $k=100 \text{ N/m}$ ) a maximum of  $1.25 \text{ cm}$ . Calculate the mass of the block of wood.

6. If a force of  $300 \text{ N}$  is exerted upon a  $60 \text{ kg}$  mass for  $3 \text{ seconds}$ , how much impulse does the mass experience?  $F = \frac{J}{\Delta t} \Rightarrow J = 300 \times 3 = 900 \text{ kg m/s}$

7. An  $80\text{-kg}$  man and his car are suddenly accelerated from rest to a speed of  $5 \text{ m/s}$  as a result of a rear-end collision. Assuming the time taken to be  $0.3 \text{ s}$ , find:  
 a) the impulse on the man and  $J = \Delta p = m \Delta v = 80 \times 5 = 400 \text{ (kg m/s)}$   
 b) the average force exerted on him by the back seat of his car.

8. An airplane propeller is rotating at  $1900 \text{ rev/min}$ .  
 a. Compute the propeller's angular velocity in  $\text{rad/s}$ .  $\omega = 2\pi f$   
 b. How long in seconds does it take for the propeller to turn through  $30.0$  degrees?  $F = \frac{\tau}{\Delta t} = \frac{400}{0.3} \text{ (N)}$   
 $f = 1900 \text{ rev/min} = \frac{1900}{60} \text{ Hz}$   
 $\phi = \omega t \Rightarrow t = \frac{\phi}{\omega} = \frac{30 \pi}{1900 \times \frac{1}{199}} = 0.0026 \text{ s}$

9. A disk with a  $1.0\text{-m}$  radius reaches a maximum angular speed of  $18 \text{ rad/s}$  before it stops  $30 \text{ revolutions}$  after attaining the maximum speed. How long did it take the disk to stop?  
 $d = 2\pi R \times 30 = 60\pi \text{ (m)}$   
 $v = \omega R = 18 \text{ (m/s)}$   
 $t = \frac{d}{v} = \frac{60\pi}{18} = 10.5 \text{ (s)}$

10. A net torque of  $36 \text{ N.m}$  acts on a wheel rotating about a fixed axis for  $6 \text{ s}$ . During this time the angular speed of the wheel increases from  $0$  to  $12 \text{ rad/s}$ . The applied force is then removed, and the wheel comes to rest in  $75 \text{ s}$ .

a. What is the moment of inertia of the wheel?

b. What is the magnitude of the frictional torque?

c. How many revolutions does the wheel make?

a)  $\tau = I \alpha \Rightarrow I = \frac{\tau}{\alpha} = \frac{36}{2} = 18 \text{ kg m}^2$   
 $\alpha = \frac{\Delta \omega}{\Delta t} = \frac{12}{6} = 2 \text{ rad/s}^2$   
 b)  $\tau = I \alpha = 18 \times 0.16 = 2.88 \text{ (N.m)}$   
 $\alpha_2 = \frac{12}{75} = 0.16 \text{ rad/s}^2$

c)