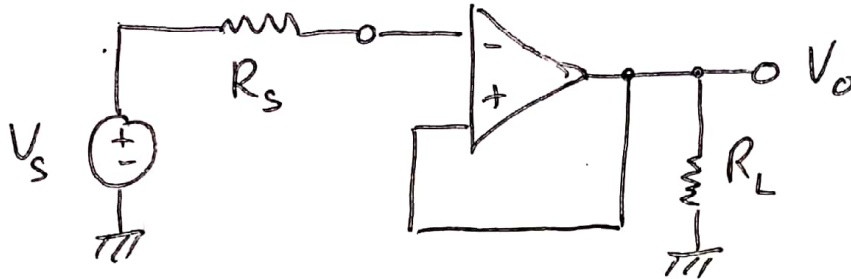


# ANALOG ELECTRONICS

## Homework #5

### Problem 1.



- Open loop gain  $A = 1000$ . Output voltage fully fed back to the input so  $\beta = 1$

$$A_f = \frac{A}{1 + A\beta} = \frac{1000}{1 + 1000} \approx 0.999$$

- The amount of feedback =  $20 \log (1 + A\beta) \approx 59 \text{ dB}$

- Output voltage  $V_o = V_s A_f = 1.5 \times 0.999 \approx 1.499 \text{ V}$

- Input voltage  $V_i = V_s - V_o \beta = 1 \text{ mV}$

- $A_n = 0.85 A = 765 \text{ V} \Rightarrow A_{f_n} = \frac{A_n}{1 + A_n \beta} \approx 0.9987$

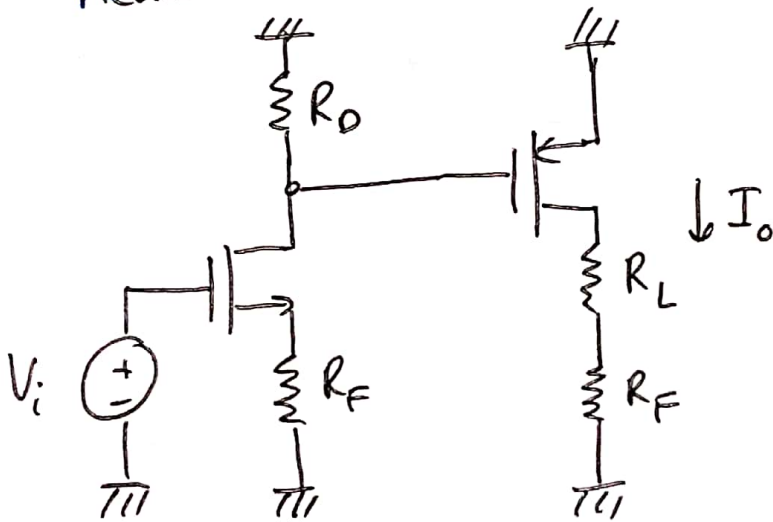
$$\frac{\Delta A_f}{A_f} = \frac{0.999 - 0.9987}{0.999} \approx 0.03 \%$$

## Problem 2.

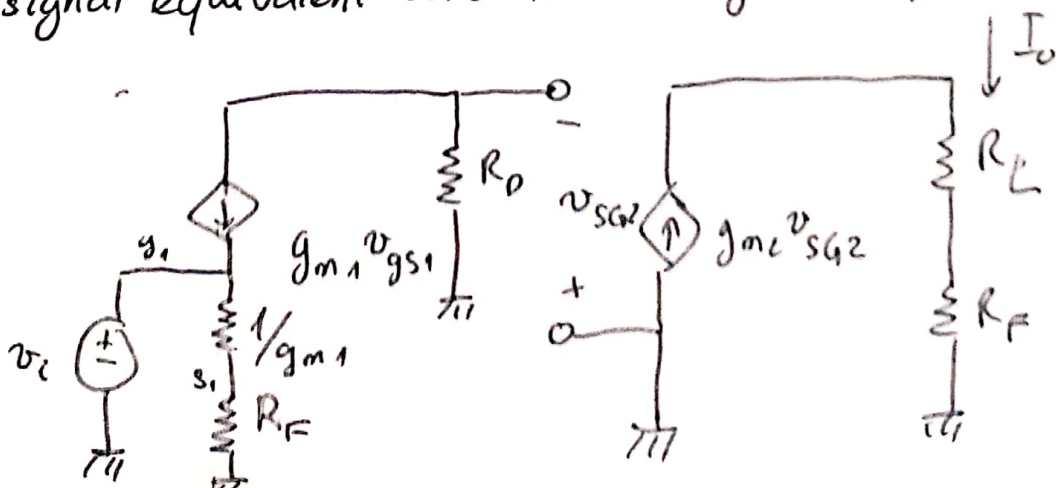
- We have:  $\frac{A_M}{1 + A_M \beta} = 20$   
 $\Leftrightarrow \frac{900}{1 + A_M \beta} = 20 \Leftrightarrow 1 + A_M \beta = 45$
- $f_{Hg} = f_H (1 + A_M \beta) = 20 \times 45 = 900 \text{ (kHz)}$
- $f_{Lg} = f_L / (1 + A_M \beta) = 200 / 45 \approx 4.44 \text{ (Hz)}$

## Problem 3.

Redraw the circuit to include  $R_F$  in each of the loops



Small signal equivalent circuit: (disregard  $r_{o1}, r_{o2}$ )



- Open loop gain  $A = \frac{I_o}{V_i} = g_{m1} g_{m2} \frac{R_D}{1 + g_{m1} R_F}$

$$\left\{ \begin{aligned} \text{with } I_o &= +g_{m2} V_{SG2} = +g_{m2} (V_{S2} - V_{G2}) \\ &= +g_{m2} [0 - (-g_{m1} V_{GS1} R_D)] \\ &= g_{m2} g_{m1} V_i \frac{1/g_{m1}}{1/g_{m1} + R_F} R_D \\ &= g_{m1} g_{m2} \frac{V_i R_D}{1 + g_{m1} R_F} \end{aligned} \right.$$

- Feedback gain  $\beta = \frac{V_f}{I_o} = R_f$

- Loop gain  $A\beta = \frac{g_{m1} g_{m2} R_D R_f}{1 + g_{m1} R_f} = \frac{5^m \times 5^m \times 30^k \times 0.2^k}{1 + 5^m \times 0.2^k} = 75$

- $A_f = \frac{A}{1 + A\beta} = \frac{g_{m2} g_{m1} R_D}{1 + g_{m1} R_F (1 + g_{m2} R_D)}$   
 $= \frac{5^m \times 5^m \times 30^k}{1 + 5^m \times 0.2^k (1 + 5^m \times 30^k)}$   
 $\approx 0.005 \text{ (A/V)} = 5^{\text{mA/V}}$

- $R_o = r_{o2} + R_L + R_F = 30^k + 1.5^k + 0.2^k = 31.7^k (\text{k}\Omega)$

- $R_{of} = R_o (1 + A\beta) = 31.7^k (1 + 75)$   
 $\approx 2.4 \text{ (M}\Omega)$