

Mid-term Examination

Date: March , 2016

Duration: 90 minutes

SUBJECT: Electromagnetic Theory	
Dean of School of Electrical Engineering	Lecturer: Tran Van Su, M.Eng.
Signature:	Signature:
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Question 1 (25 Marks)

A conducting cylinder (M) which is depicted in Fig. 1 has radius of a (m) and charge density of ρ_s (C/m²), respectively. In the free space, determine:

- Total displacement flux crossing the concentric cylinder which has the radius $r > a$ and length of 2 (m). (10 Marks)
- The displacement flux $D(r)$. (5 Marks)

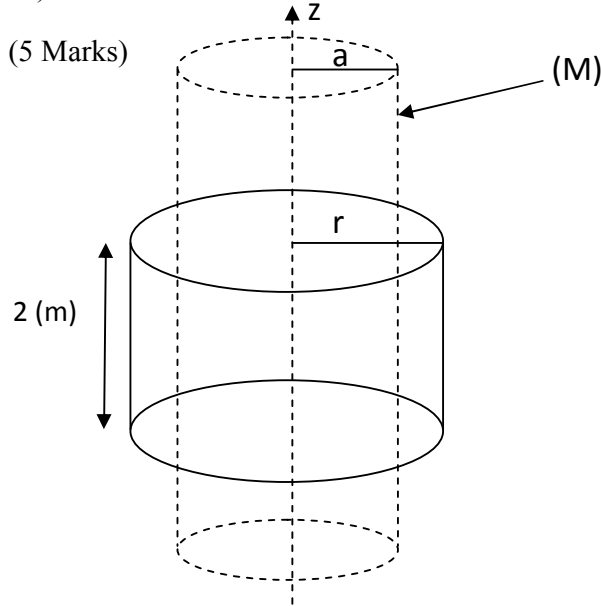


Fig. 1

- If $a = 0$ and $\rho_s = \rho_L$ (C/m), Repeat question a and b. (10 Marks)

Question 2 (25 Marks)

Given $\vec{A} = x^2 yz\hat{x} + y^2 zx\hat{y} + z^2 xy\hat{z}$,

- Evaluate $\oint_S \vec{A} \cdot d\vec{S}$, where S is the surface of the cubical box bounded by the planes $x = 0$, $x = 1$, $y = 0$, $y = 1$, $z = 0$, and $z = 1$. (15 Marks)
- Show that the divergence theorem is also satisfied with \vec{A} and the cubical box in question (a). (10 Marks)

Question 3 (25 Marks)

An infinite plane sheet of current density $\vec{J}_s = -J_s(t)\hat{x}$ (A/m) where $J_s(t)$ is shown in Fig. 2, lies in the $z = 0$ plane in free space. If The phase velocity is $3 \cdot 10^8$ m/s. Plot

- E_x versus t in the $z = -300$ m plane. (10 Marks)
- H_y versus t in the $z = 600$ m plane. (10 Marks)
- E_x versus z at $t = 1\mu s$. (5 Marks)

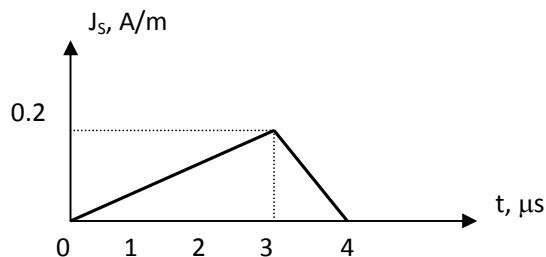


Fig. 2

Question 4 (25 Marks)

For the plane wave in free space, the electric field is defined as follows

$$\vec{E} = E_o \cos(6\pi \times 10^8 t + 2\pi x) \hat{z} \text{ (V/m)}$$

Compute:

- a) velocity of the wave. (3 Marks)
- b) the wavelength of the wave. (2 Marks)
- c) Magnetic field \vec{H} . (5 Marks)
- d) Vector poynting. (5 Marks)
- e) $\nabla \times \vec{E}$. (5 Marks)
- f) $\nabla \times \vec{H}$. (5 Marks)