

HW 4

43) $W = \int p dV$

a) $W = p \Delta V + 0$

$= 40 \times 3 = 120 \text{ J}$

b) $W = \frac{1}{2} (10 + 40) \times 3 = 75 \text{ J}$

or you can see

$W = \int p dV = \int (50 - 10) dV$

$= (50V - 5V^2) \Big|_0^3 = 75 \text{ J}$

c) $W = 0 + p \Delta V = 10 \times 3 = 30 \text{ J}$

45) $Q = W$, $p = a + bV$

$W_{AB} = \int_{V_A}^{V_B} p dV = \int_{V_A}^{V_B} (a + bV) dV$

$= a(V_B - V_A) + \frac{1}{2} b(V_B^2 - V_A^2)$

the work done by the gas is

$W_{BC} = p_B \Delta V_{BC} = p_B (V_C - V_B)$

the pressure function can be written as

$p = \frac{20}{3} \text{ Pa} + \left(\frac{20}{3} \text{ Pa/m}^3 \right) V$

$p = 10 \text{ Pa}$

$V = 1 \text{ m}^3$ and $p = 30 \text{ Pa}$ when $V = 4 \text{ m}^3$

$$49) \Delta E_{in} = Q - W$$

for a closed cycle

$$\Delta E_{int} = 0$$

$$\Delta E_{abc} + \Delta E_{cd} + \Delta E_{da} = 0$$

$$\Delta E_{abc} = -200 \text{ J}$$

for process da:

$$\Delta E_{da} = Q_{da} - W_{da} = 80 - 0 = 80 \text{ J}$$

$$\Delta E_{cd} = -\Delta E_{abc} - \Delta E_{da} = 200 - 80 = 120 \text{ J}$$

$$\Rightarrow W_{cd} = Q_{cd} - \Delta E_{cd} = 180 - 120 = 60 \text{ J}$$

$$50) \Delta E_{int} = Q - W$$

a) the process a \rightarrow b is an expansion ($V_b > V_a$)

$W > 0$ and $W = 5 \text{ J}$

$$Q_{ab} = \Delta E_{int} + W = 3 + 5 = 8 \text{ J}$$

b) We consider a closed cycle abca

$$\Delta E_{in} = Q - W = 0$$

$$Q_{ab} + Q_{bc} + Q_{ca} = W_{net}$$

$$Q_{bc} = W_{net} - Q_{ab} - Q_{ca} \\ = 1.5 - 8 - 2.5 = -9.0 \text{ J}$$

$$W_{AB} = a(V_B - V_A) + \frac{1}{2}b(V_B^2 - V_A^2)$$

$$= \left(\frac{10}{3} \text{ Pa}\right)(4 \text{ m}^3 - 1 \text{ m}^3) + \frac{1}{2} \left(\frac{20}{3}\right)(4)^2 - (1)^2$$

$$= 6 \text{ J}$$

we have

$$W_{BC} = P_B(V_C - V_B) = (60)(1 - 4) = -90 \text{ J}$$

$$\Rightarrow W = W_{AB} + W_{BC} + W_{CA}$$

$$= 60 - 90 + 0 = -30 \text{ J}$$

$$46) W_{\text{on}} = 200 \text{ J}$$

$$W_{\text{on}} = +W$$

$$a) \Rightarrow W = -W_{\text{on}} = -200 \text{ J}$$

b) the gas released energy as heat

$$Q = -20 = -80, 4, 19 = -335, 2 \text{ J}$$

$$c) \Delta E_{\text{int}} = Q - W$$

$$= -335, 2 - (-200) = -135, 2 \text{ J}$$

48)

$$\Delta E_{\text{int}} = Q - W$$

For the ABCA closed cycle

$$\Delta E_{\text{int}} = 0$$

$$Q_{AB} + Q_{BC} + Q_{CA} = W$$

$$\Rightarrow Q_{CA} = W - Q_{AB} - Q_{BC}$$

$$= 15 - 25 - 0 = -10 \text{ J}$$