

Final Examination

Date: May 29, 2014

Duration: 120 minutes

SUBJECT: Electromagnetic Theory	
Dean of School of Electrical Engineering Signature:	Lecturer Signature:
Full name: Tran Van Su	Full name: Tran Van Su

INTRODUCTIONS:

1. One sheet, A4-size paper, with your own hand-writing characters is allowed (Books are prohibited)
2. Laptop and communications devices are not allowed except calculators
3. Answer all questions

Question 1 (15 Marks)

Given $\vec{B} = (x\hat{x} + y\hat{y}) \text{ Wb/m}^2$, find by evaluating $\vec{B} \bullet \Delta\vec{S}$ the approximate absolute value of the magnetic flux crossing from one side to the another side of an infinitesimal surface of area 0.0005 m^2 at point (1,1,1) for each of the orientations of the surface:

- In the $y = 2$ plane (8 Marks)
- Normal to the unit vector \hat{z} (7 Marks)

Question 2 (10 Marks)

Two sinusoidally time-varying, linearly polarized vector fields are given at a point by

$$\vec{F}_1 = (C\hat{x} + C\hat{y} + \hat{z}) \cos 2\pi \times 10^6 t$$

$$\vec{F}_2 = (C\hat{x} + \hat{y} - 2\hat{z}) \sin 2\pi \times 10^6 t$$

where C is a constant

- If $C = 2$, determine the polarization of the vector $\vec{F}_1 + \vec{F}_2$
- Find the value(s) of C for which the tip of the vector $\vec{F}_1 + \vec{F}_2$ traces a circle with time

Question 3 (20 Marks)

The electric field associated with a uniform plane wave propagating in the +z direction in free space is given by

$$\vec{E} = E_0 \cos(6\pi \times 10^7 t - 0.2\pi z) \vec{a}_x \text{ (A/m)}, \text{ Find the following:}$$

- The instantaneous power flow across a surface of area 2m^2 in the $z = 0$ plane at $t = 0$ (10 Marks)
- The time-average power flow across a surface of area 2m^2 in the $z = 0$ plane. (Hint: Use Phasor). (10 Marks).

Question 4 (20 Marks)

A uniform plane wave propagating in a medium has

$$\vec{E} = 10e^{-\alpha z} \cos(10^8 t - \beta z) \hat{x} \text{ [V/m]}$$

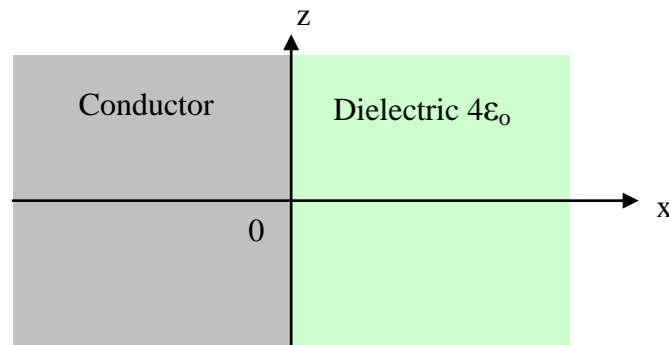
If the medium is characterized by $\epsilon_r = 1$, $\mu = 80\pi \cdot 10^{-7} \text{ (H/m)}$, and $\sigma = 3 \text{ [S/m]}$

a) The medium is considered as good conductor, find approximated values of α and β . (10 Marks)

b) Find magnetic field $\vec{H}(t, z)$ if the intrinsic impedance of the medium is

$$\bar{\eta} \approx \sqrt{\frac{\omega\mu}{\sigma}} e^{j\pi/4} \quad (10 \text{ Marks})$$

Question 5 (15 Marks)

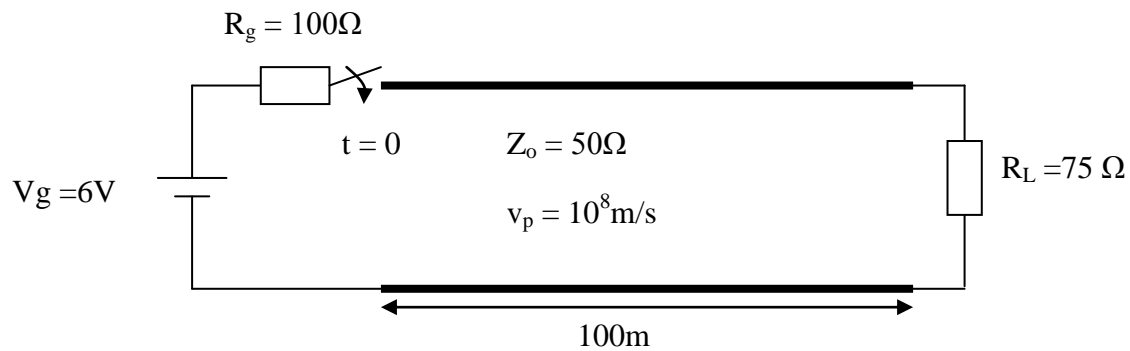


Region $x \leq 0$ consists of a perfect conductor while region $x \geq 0$ is a dielectric medium as shown in the Figure. If there is a surface charge of 5nC/m^2 on the conductor, determine \vec{E} and \vec{D} at

a) A(-31,2) (8 Marks)

b) B(10,2,5) (7 Marks)

Question 6 (20 Marks)



For the transmission line of the Figure above,

a) Sketch the bounce diagram of the voltage and give enough information on it (up to $4\mu\text{s}$). (5 Marks)

b) Sketch the bounce diagram of the current and give enough information on it (up to $4\mu\text{s}$). (5 Marks)

c) Calculate steady state V_{ss} and I_{ss} . (5 Marks)

d) Calculate steady state V_{ss}^+ , V_{ss}^- , I_{ss}^+ and I_{ss}^- . (5 Marks)