Homework: 42, 44, 46, 54, 56, 78 (p. 533-535)

42. What is the internal energy of 2.0 mol of an ideal monatomic gas

at 273 K2

$$E = nC_V T$$

$$C_V = \frac{3}{2}R = 12.5 \text{ J mol}^{-1} \text{ K}^{-1}$$

$$E = 2.0 \times 12.5 \times 273 = 6825 \text{ (J)}$$

$$E \approx 6.8 \, (kJ)$$

The change in internal energy of the gas:

$$\Delta E_{int} = \frac{3}{2} nR\Delta T = \frac{3}{2} nRT_2 - \frac{3}{2} nRT_1 = \frac{3}{2} (378,75 - 252,5) = 189,375 (J)$$

$$e=5 \leftarrow adiatomic gas: C_V = \frac{5}{2}R$$

46. Under constant pressure, the temperature of 3.0 mol of an ideal monatomic gas is raised 15.0 K. What are (a) the work W done by the gas, (b) the energy transferred as heat Q, (c) the change ΔE_{int} of the gas, and (d) the change ΔK in the average KE per atom?

(a) At constant pressure:
$$8.31$$
 $Cp = Cv + R$

$$W = p\Delta V = nR\Delta T = 3.0 \times 8.31 \times 15.0 \approx 374$$
 (J)

$$Q = nC_p \Delta T = n \times \frac{5}{2} R \times \Delta T = \frac{5}{2} W \approx 935 \text{ (J)}$$

$$Q = nC_p \Delta T = n \times \frac{5}{2} R \times \Delta T = \frac{5}{2} W \approx 935 \text{ (J)}$$

$$\Delta E_{\text{int}} = Q - W \quad \text{(or } \Delta E_{\text{int}} = nC_V \Delta T = \frac{3}{2} nR \Delta T)$$

$$\Delta E_{\rm int} = 935 - 374 = 561 \text{ (J)}$$

$$\Delta E_{\rm int} = 935 - 374 = 561 \, ({\rm J})$$
(d) For a monatomic gas: $K_{\rm avg} = \frac{3}{2} kT \Rightarrow \Delta K_{\rm avg} = \frac{3}{2} k\Delta T$
(38×10⁻²³

$$\Delta K_{\rm avg} = \frac{3}{2} \times 1.38 \times 10^{-23} \times 15.0 \approx 3.1 \times 10^{-22} \, ({\rm J}) \times \Delta K_{\rm avg}$$

54. We know that for an adiabatic process $pV^{\gamma}=\text{constant}$. Evaluate "constant" for an adiabatic process involving exactly 2.0 mol of an ideal gas passing through the state having exactly p=1.5 atm and T=300 K. Assume a diatomic gas whose molecules rotate but do not oscillate.

Equation of state:
$$pV = nRT$$

$$V = \frac{nRT}{p} = \frac{2.0 \times 8.31 \times 300}{1.5 \times 1.01 \times 10^5} \approx 0.033 \text{ (m}^3)$$

$$\gamma = \frac{C_p}{C_V} = \frac{C_V + R}{C_V} = \frac{\frac{f}{2}R + R}{\frac{f}{2}R}$$
For a diatomic gas, f=5:
$$\gamma = \frac{7}{5}$$

constant= $pV^{\gamma} = 1.5 \times 1.01 \times 10^5 \times 0.033^{\frac{7}{5}} = 1.28 \times 10^3 (\text{N/m}^2 \times (\text{m}^3)^{\frac{1.4}{1.4}})$ constant= $1.28 \times 10^3 (\text{N m}^{\frac{2.2}{1.4}})$ 56. Suppose 1.0L of a gas with $\gamma=1.30$, initially at 285 K and 1.0 atm, is suddenly compressed adiabatically to half its initial volume. Find its final (a) pressure and (b) temperature. (c) If the gas is then cooled to 273 K at constant pressure, what is its final volume?

$$p_{i}V_{i}^{\gamma} = p_{f}V_{f}^{\gamma}; \quad V_{f} = \frac{1}{2}V_{i}$$

$$p_{f} = p_{i}\left(\frac{V_{i}}{V_{f}}\right)^{\gamma}$$

$$T_{f} = T_{i}\left(\frac{V_{i}}{V_{f}}\right)^{\gamma-1}$$

$$pV = nRT, p = \text{constant} \Rightarrow \frac{V'_{f}}{V_{f}} = \frac{T'_{f}}{T_{f}}$$

78. (a) An ideal gas initially at pressure p_0 undergoes a free expansion until its volume is 3.0 times its initial volume. What then is the ratio of its pressure to p_0 ? (b) The gas is next slowly and adiabatically compressed back to its original volume. The pressure after compression is $(3.0)^{1/3}p_0$. Is the gas monatomic, diatomic, or polyatomic? (c) What is the ratio of the average kinetic energy per molecule in this final state to that in the initial state?

(a)
$$p_0V_0 = p_1V_1; V_1 = 3V_0 \Rightarrow p_1 = \frac{1}{3}p_0$$

(b) $p_1V_1^{\gamma} = p_1'V_0^{\gamma}$
 $p_1'_1 = p_1\left(\frac{V_1}{V_0}\right)^{\gamma} = \frac{1}{3}p_03^{\gamma} = 3^{\gamma-1}p_0$
 $\Rightarrow \gamma - 1 = \frac{1}{3} \Rightarrow \gamma = \frac{4}{3} = \frac{C_p}{C_V} = \frac{C_V + R}{C_V} = \frac{\frac{f}{2} + 1}{f} = \frac{f + 2}{f}$
 $f = 6$: polyatomic

$$K_{avg} = \frac{3}{2}kT$$

$$r = \frac{K'_{avg}}{K_{avg}} = \frac{T'_1}{T_0}$$

$$r = \frac{T'_1}{T_0} = \frac{p'_1 V'_1}{p_0 V_0} = \frac{p'_1}{p_0} = 3^{1/3} = 1.44 \text{ (since } V'_1 = V_0)$$

$$P_0 V_0 T_0 \xrightarrow{\text{Rel e-lownsign}} P_1 V_1 T_1 \xrightarrow{\text{Production}} P_2 V_2 T_2$$

$$P_0 V_0 = P_1 V_1 \qquad P_1 V_1 = P_2 V_2$$

$$T_0 = T_1 \qquad P_2 = 3^{1/3} P_0$$

$$V_1 = 3 V_0$$

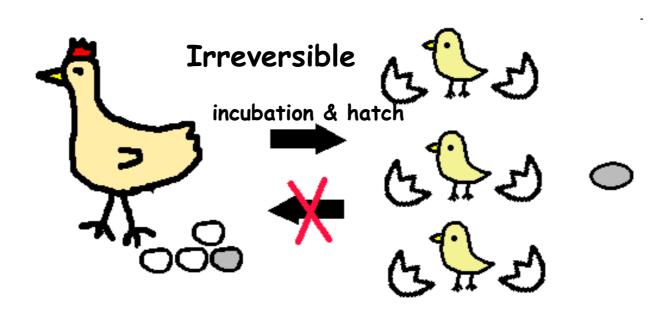
Chapter 4 Entropy and the Second Law of Thermodynamics

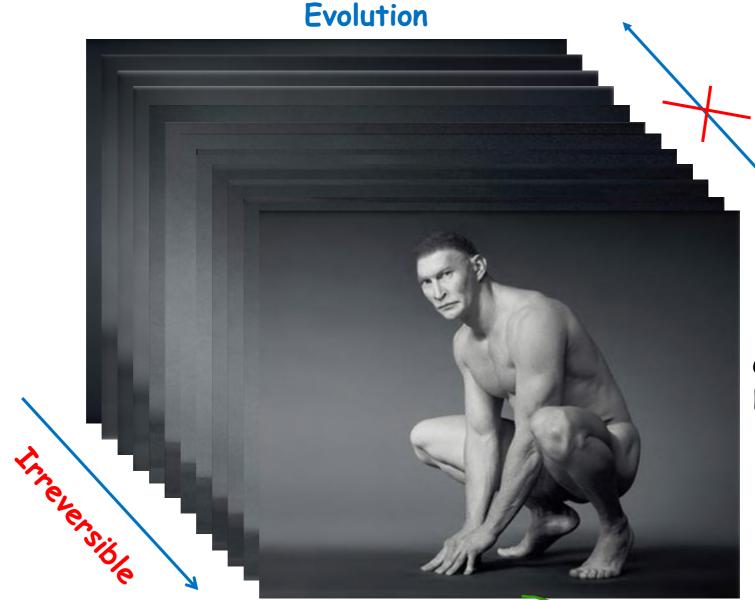
- 4.1. Reversible, Irreversible Processes and Entropy
- 4.2. The Second Law of Thermodynamics
- 4.3. Entropy in the Real World: Engines
- 4.4. A Statistical View of Entropy

What is Physics?

- · Time has direction, from the past to the future
- One-way processes that can occur only in a certain sequence and never in the reverse sequence are irreversible, meaning that they can not be reversed.

Examples: a pizza is baked, water flows from high level to low level, current moves from high potential to low potential, etc.



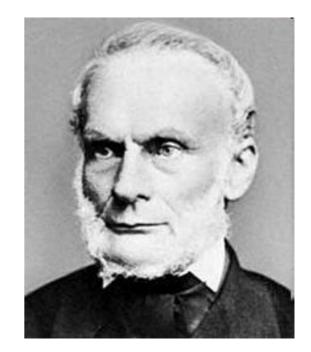


Credit:
Daniel Lee

- In this chapter, we study why one-way processes are irreversible
- The key to understand why one-way processes cannot be reversed involves a quantity known as Entropy

What is Entropy?

Entropy is the extensive property of the system (depends on the mass of the system) and its unit of measurement is J/K. Entropy is heat or energy change per degree Kelvin temperature. Entropy is denoted by '5'.



Clausius - author of the entropy concept

Interdisciplinary applications of entropy

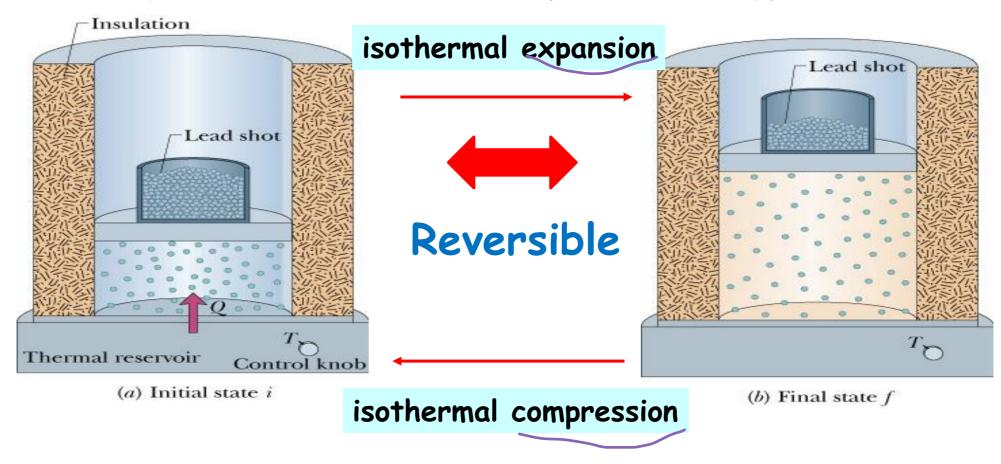
Although the concept of entropy was originally a thermodynamic construct, it has been adapted in the other following fields of study:

- √ information theory
- √ psychodynamics
- √ thermoeconomics
- √ evolution

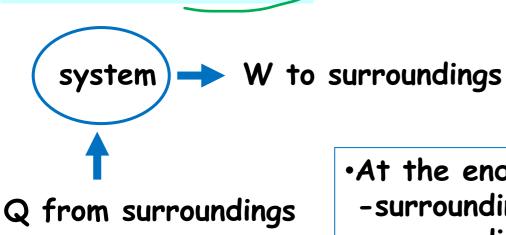
4.1. Reversible, Irreversible Processes and Entropy

a. Reversible processes:

A reversible process is a process that, after it has taken place, can be reversed and causes no change in either the system or its surroundings (i.e. without loss or dissipation of energy)



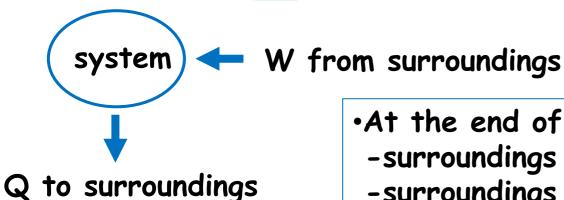
isothermal expansion



$$Q = W = nRT \ln \frac{V_f}{V_i}$$

- ·At the end of the isothermal expansion:
 - -surroundings have received work
 - -surroundings have given up heat

isothermal compression



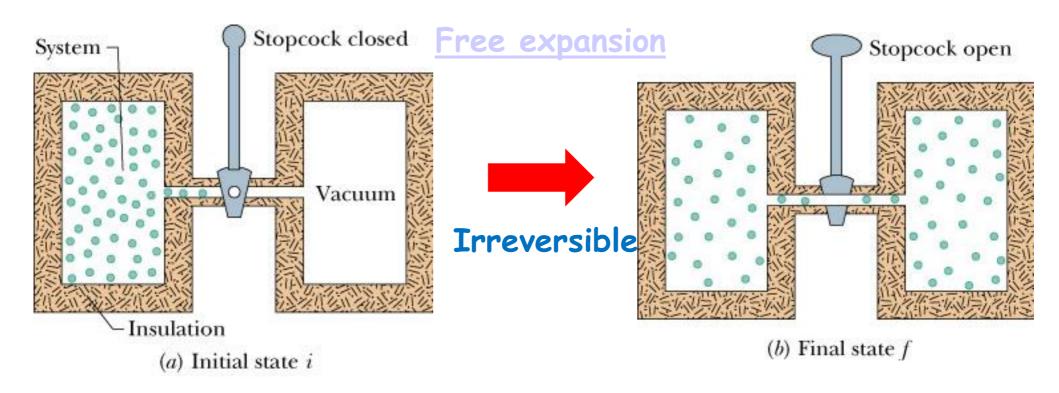
- •At the end of the isothermal compression:
 - -surroundings have done work
 - -surroundings have received heat

Net result: the system and the surroundings back to the initial state without any change \Rightarrow the process is reversible

• However, the presence of friction always results in the output work of the system being smaller than the work transferred into the system. Therefore, it is practically impossible to realize reversible processes (i.e. ideal ones). But the concept of a reversible process proves to be very useful in studying irreversible processes.

b. Irreversible processes:

- A process that is not reversible is called irreversible.
- In irreversible processes, both the system and the surroundings can not return to their initial state on their own.

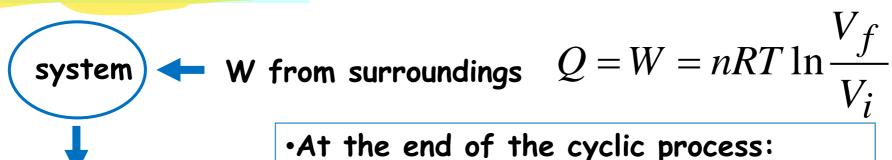


Free expansion

$$\begin{array}{c} \text{system} \\ \mathbf{V_1, T_1} \end{array} \longrightarrow \begin{array}{c} \text{system} \\ \mathbf{V_2, T_1} \end{array} \qquad T = \text{constant}; \Delta E_{\text{int}} = Q = W = 0 \end{array}$$

 To restore the system to the initial state at constant T, we compress isothermally by some external agency:

isothermal compression



- Q to surroundings
- •At the end of the cyclic process:
 - -the system is back in the initial state
 - -surroundings have done work
 - -surroundings have received heat

Net result: the system is the same and the surroundings have changed (W converted to Q)

 \Rightarrow the universe has changed \Rightarrow the process is irreversible

·For irreversible processes, the entropy S of a closed system always increases, because of this property, the change in entropy ΔS is sometimes called "the arrow of time".

Examples: eggs \Rightarrow chickens: $\Delta S > 0$

chickens \Rightarrow eggs: $\Delta S < 0$: it never happens

d. Change in Entropy:

There are two equivalent ways to define the change in entropy of a system:

- (1) in terms of the system's temperature and the energy the system gains or loses as heat (next slide)
- (2) by counting the ways in which the atoms or molecules that make up the system can be arranged (see next lecture)

Mot in Einal

$$\Delta S = S_f - S_i = \int_i^f \frac{dQ}{T}$$

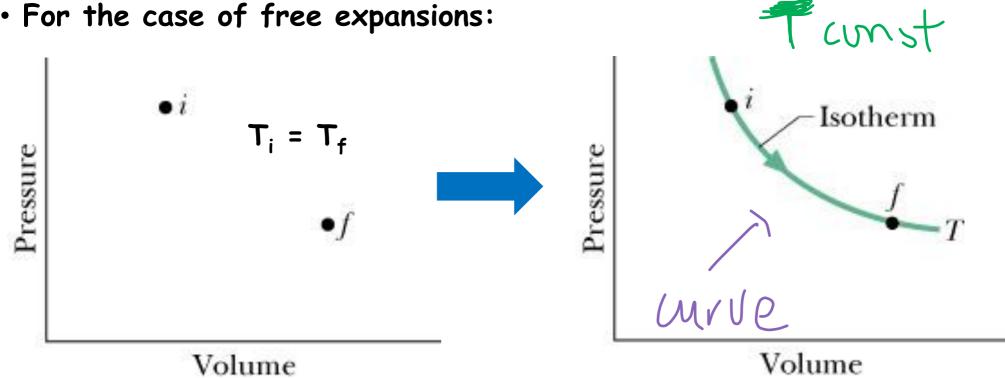
Q: energy transferred as heat to or from the system during the process; T(K): temperature of the system; Unit: J/K

• For free expansions: p, V and T fluctuate unpredictably, so we cannot find a relation between Q and T to calculate ΔS .

♣ Method to calculate ∆S:

- The difference in entropy only depends on the initial and final states, we can therefore replace an irreversible process occurring in a closed system with any reversible one that connects the same initial and final states to calculate the entropy change.

For the case of free expansions:



$$\Delta S = \int_{i}^{f} \frac{dQ}{T} = \frac{1}{T} \int_{i}^{f} dQ = \frac{Q}{T}$$

· For isotherms:

$$Q = W = nRT \ln \frac{V_f}{V_i}$$

$$\Delta S = nR \ln \frac{V_f}{V_i}$$

• Special Case: If the temperature change ΔT of a system is small relative to the temperature (in K) before and after the process, the change in entropy can be computed:

$$\Delta S = S_f - S_i \approx \frac{Q}{T_{avg}}$$

Checkpoint 1 (p. 539): Water is heated on a stove. Rank the entropy changes of the water as its temperature rises (a) from 20°C to 30°C, (b) from 30°C to 35°C, and (c) from 80°C to 85°C, greatest first.

$$\Delta S = S_f - S_i \approx \frac{Q}{T_{avg}} = \frac{cm\Delta T}{T_{avg}} \Rightarrow (a), (b), (c)$$

Homework: Read Sample Problems page 540 and page 541