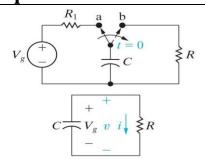
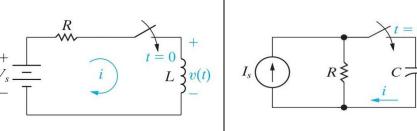
## Response of RL/RC circuit

## **Natural response**



## Step response



$$i_L(t) = i(0)e^{-t/\tau}, \tau = L/R$$

Power: 
$$p = I_s^2 R e^{-2t/\tau}$$

Energy: 
$$E = \frac{1}{2}LI_s^2(1 - e^{-2t/\tau})$$

Total Energy:  $E_t = \frac{1}{2}LI_s^2$ 

$$v_C(t) = v(0)e^{-t/\tau}, \tau = RC$$

Power: 
$$p = \frac{V_g^2}{R} e^{-2t/\tau}$$

Energy: 
$$E = \frac{1}{2}CV_g^2(1 - e^{-2t/\tau})$$

Total Energy:  $E_t = \frac{1}{2}CV_g^2$ 

$$\tau = L/R$$

$$i_L(t) = \frac{V_s}{R} + \left(I_0 - \frac{V_s}{R}\right)e^{-t/\tau}$$

$$v_L(t) = (V_S - I_0 R)e^{-t/\tau}$$

$$\tau = RC$$

$$v_C(t) = I_S R + (V_0 - I_S R) e^{-t/\tau}$$

$$i_C(t) = \left(I_S - \frac{V_0}{R}\right)e^{-t/\tau}$$

## Note that:

+ For inductor:

$$v_L(t) = L \frac{di_L}{dt} \leftrightarrow i_L(t) = \frac{1}{L} \int_{t_0}^t v_L(\tau) \, d\tau + i_L(t_0)$$

+ Parallel inductor:

$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

+ Series inductor:

$$L_{eq} = L_1 + L_2$$

+ For capacitor:

$$i_C(t) = C \frac{dv_C}{dt} \leftrightarrow v_C(t) = \frac{1}{C} \int_{t_0}^t i_C(\tau) d\tau + v_C(t_0)$$

+ Parallel capacitor:

$$C_{eq} = C_1 + C_2$$

+ Series capacitor:

$$C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$