

**Final Examination**

**Date:** June 9<sup>th</sup>, 2011

**Duration:** 120 minutes

<b>SUBJECT: Electromagnetic Theory</b>	
Dean of School of Electronics & Telecommunications Engineering  Signature:          Full name:	Lecturer: Tran Van Su, M.Eng.  Signature:          Full name:

**INTRODUCTIONS:**

1. This is a closed-book examination
2. One sheet of notes allowed during examination period.
3. Communications devices are prohibited
4. Answer all questions

### Question 1 (25 Marks)

The time variation for  $z = 0$  of a function  $f(z,t)$  representing a traveling wave propagating in the  $+z$ -direction with velocity 150 m/s is shown in Fig. 1. Find the value of the function for each of the following case:

- a)  $z = 300\text{m}$ ,  $t = 2.5\text{s}$  (15 Marks)
- b)  $z = -150\text{m}$ ,  $t = 0.5\text{s}$  (10 Marks)

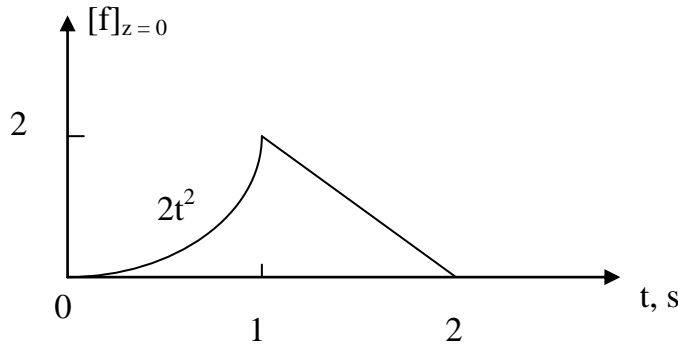


Fig. 1

### Question 2 (25 Marks)

Two sinusoidally time-varying, linear vector fields are given at a point by

$$\vec{F}_1 = (C\hat{x} + C\hat{y} + \hat{z})\cos 2\pi \times 10^6 t$$
$$\vec{F}_2 = (C\hat{x} + \hat{y} - 2\hat{z})\sin 2\pi \times 10^6 t$$

where  $C$  is a constant

- a) Determine the polarization of vector  $\vec{F}_1 + \vec{F}_2$  for  $C = 2$  (10 Marks)

(Hint: 1. Are  $\mathbf{F}_1$  and  $\mathbf{F}_2$  in phase? Are  $\mathbf{F}_1$  and  $\mathbf{F}_2$  opposite phase? is  $\mathbf{F}_1$  perpendicular to  $\mathbf{F}_2$ )

- b) Find the values of  $C$  for which the tip of the vector  $\vec{F}_1 + \vec{F}_2$  traces a circle with time (15 Marks)

(Hint: (i) Compute the modulus of  $\vec{F}_1 + \vec{F}_2$  and determine  $c$  to obtain constant magnitude (ii) Check 3 conditions for circular polarization)

### Question 3 (25 Marks)

The plane  $z = 0$  forms the boundary between free space ( $z > 0$ ) and another medium.

- a) Write four equations of boundary conditions (5 Marks)

b) Find  $\vec{J}_s(0,0,0)$  at  $t = 0$  if  $z < 0$  is a perfect conductor and

$$\vec{H}(0,0,0^+) = H_0(3\hat{x} - 4\hat{y})\cos\omega t. \text{ (10 Marks)}$$

c) Find  $\vec{H}(0,0,0^+)$  at  $t = 0$  if  $z < 0$  is a magnetic material of  $\mu = 20\mu_0$  and

$$\vec{H}(0,0,0^-) = H_0(10\hat{x} + \hat{z})\cos\omega t. \text{ (10 Marks)}$$

#### Question 4 (25 Marks)

For the transmission line of the following Figure

- Calculate and sketch the bounce diagram of voltages for  $0 < t < 5\mu\text{s}$ . (5 Marks)
- Calculate and sketch the bounce diagram of currents for  $0 < t < 5\mu\text{s}$ . (5 Marks)
- Determine  $V_{ss}$  and  $I_{ss}$  (5 Marks)
- Determine  $V_{ss}^+$  and  $I_{ss}^+$  (5 Marks)
- If  $R_L$  is substituted by a capacitor  $C$ , compute the voltage reflection coefficient at the capacitor for  $t = 1\mu\text{s}$  and  $t \rightarrow \infty$  (5 Marks)

