

## Mid-term Examination

**Date:** March 19, 2013

**Duration:** 90 minutes

SUBJECT: Electromagnetic Theory	
Dean of School of Electrical Engineering	Lecturer: Tran Van Su, M.Eng.
Signature:	Signature:
Full name: Trần Văn Su	Full name: Trần Văn Su

**Question 1 (20 Marks)**

A square loop lies in the xy-plane forming the closed path C connecting the points (0,0,0), (1,0,0), (1,1,0), (0,1,0), and (0,0,0), in that order and the area of this loop of  $1\text{m}^2$ . A magnetic field  $\mathbf{B}$  exists in the region. Determine  $B_0$  to obtain the induced emf of 2 [V] around the closed path C at  $t = 0$  for the following magnetic field.

$$\vec{B} = B_0 \cos(2\pi t + \pi/3) \hat{z} \text{ [Wb/m}^2\text{]}$$

**Question 2 (25 Marks)**

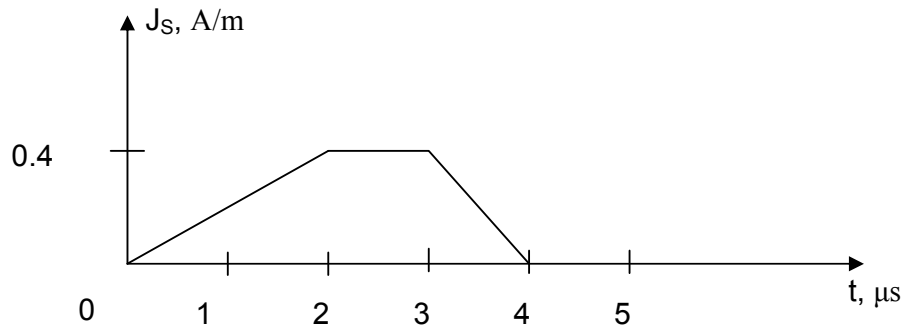
Three point charges  $Q_1(t)$ ,  $Q_2(t)$ , and  $Q_3(t)$  situated at the corners of an equilateral triangle of sides 1m are connected to each other by wires along the sides of the triangle. Current 1A flows from  $Q_1$  to  $Q_2$ . The displacement currents emanating from two spherical surfaces of radii 0.1m and centered at  $Q_1$  and  $Q_3$  are -2A and 2A, respectively. Find the following:

- the current flowing from  $Q_1$  to  $Q_3$  (10 Marks)
- the current flowing from  $Q_2$  to  $Q_3$  (10 Marks)
- the displacement current emanating from spherical surface of radius 0.1m and centered at  $Q_2$  (5 Marks)

**Question 3 (20 Marks)**

An infinite plane sheet lying in the  $z = 0$  plane in free space ( $v_p = 3.10^8\text{m/s}$ ,  $\eta_0 = 120\pi \Omega$ ) carries a surface current of density  $\vec{J}_s = -J_s \vec{a}_x$ , where  $J_s(t)$  is shown in Figure below. Find and sketch:

- $E_x$  versus  $t$  in the  $z = 600\text{m}$  plane (10 Marks)
- $H_y$  versus  $z$  for  $t = 2\mu\text{s}$  (10 Marks)

**Question 4 (25 Marks)**

The magnetic field of a uniform plane wave in the free space is given by

$$\vec{H} = H_0 \cos(6\pi \times 10^8 t - 2\pi y) \hat{z} \text{ (A/m)}$$

Find the following:

- a) unit vectors along the direction of propagation of the wave (5 Marks)
- b) unit vectors along the direction of magnetic field at  $t = 0, y = 0$  (5 Marks)
- c) unit vectors along the direction of electric field at  $t = 0, y = 0$  (5 Marks)
- d) the wavelength of the wave (5 Marks)
- e) the pointing vector at  $t = 0, y = 0$  in terms of magnitude and direction (5 Marks)

**Question 5 (10 Marks)**

Explain shortly why we study Maxwell's equation not only in integral form but also differential form?