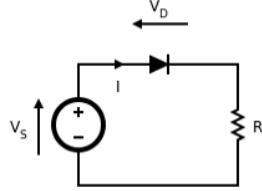
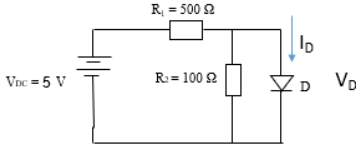
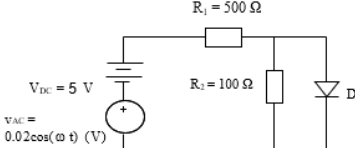
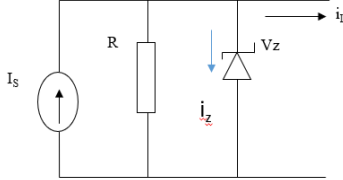


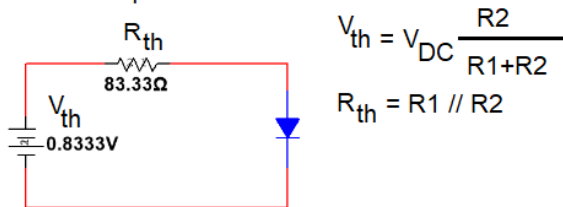
Lecture 3-3&3-4 Quiz Solution

March 2020

	Lecture 3-3
Q:	<p>Question 3.3</p> <p>a) Compute I_1, (V_{D2}, I_2), (V_{D3}, I_3) in Fig. 1 using Iterative analysis with initial $V_{D1} = 0.65\text{V}$, $n = 1$, $I_S = 10^{-15}\text{A}$, $V_S = 3\text{V}$, and $R = 1.6\text{K}\Omega$.</p> <p>b) The circuit is depicted in Fig. 2.</p> <p>(i) Use Ideal-diode model to determine I_D and V_D.</p> <p>(ii) Use Constant voltage drop model to determine I_D and V_D. Given $V_{D0} = 0.7\text{V}$</p> <p>(iii) Use Piece-wise linear model to determine I_D and V_D. Given $V_{D0} = 0.7\text{V}$ and $r_D = 15\Omega$.</p> <p>Hint: Use Thevenin equivalent circuit for V_{DC}, R_1 and R_2 before applying the models.</p> <p>c) The constant-voltage-drop model is used for the diode (D) in Fig. 3 with $V_{D0} = 0.7\text{V}$. The ideality factor $n = 1$.</p> <p>(i) Find the current i_D.</p> <p>(ii) Find the voltage v_D.</p> <p>d) A zener diode exhibits a constant voltage $V_{Z0} = 6.8\text{V}$ for current not less than $I_{Zmin} = 6\text{mA}$. It is to be used in the design of a shunt regulator shown in Fig. 4. The load current is i_L and $r_{Zmin} = 0$.</p> <p>(i) If I_S varies from 30mA to 40mA and I_L varies from 5mA to 20mA. Determine minimum value of R.</p> <p>(ii) Compute maximum power dissipated by the Zener diode with I_S, I_L and R given in (a).</p> <p>Hint: You use $i_Z \geq i_{Zmin}$</p>  <p>Fig. 1</p>  <p>Fig. 2</p>  <p>Fig. 3</p>  <p>Fig. 4</p>
Ans:	
a.	<p>• $V_{D1} = 0.65\text{V}$</p> <p>$I_1 = (V_S - V_{D1})/R = (3 - 0.65)/(1.6 \times 10^3) = 1.47\text{mA}$</p> <p>• $V_{D2} = nV_T \ln \frac{I_1}{I_S} = 1 \times 25 \times 10^{-3} \ln \frac{1.47 \times 10^{-3}}{10^{-15}} = 0.7004\text{V}$</p> <p>$I_2 = (V_S - V_{D2})/R = (3 - 0.7004)/(1.6 \times 10^3) = 1.4373\text{mA}$</p> <p>• $V_{D3} = nV_T \ln \frac{I_2}{I_S} = 1 \times 25 \times 10^{-3} \ln \frac{1.4373 \times 10^{-3}}{10^{-15}} = 0.6998\text{V}$</p> <p>$I_3 = (V_S - V_{D3})/R = (3 - 0.6998)/(1.6 \times 10^3) = 1.4376\text{mA}$</p>

b.

Thevenin equivalent circuit:



- (i) $V_D = 0\text{ V}$
 $I_D = \frac{0.8333}{83.33} = 0.01\text{ A} = 10\text{ mA}$
- (ii) $V_D = V_{D0} = 0.7\text{ V}$
 $I_D = \frac{0.8333 - 0.7}{83.33} = 1.6\text{ mA}$
- (iii) $I_D = \frac{0.83 - 0.7}{83.3 + 15} = 1.322\text{ mA}$
 $V_{D0} = 0.7 + 15 \times 1.322 \times 10^{-3} = 0.72\text{ V}$

c

- DC analysis:

$$V_D = 0.7\text{ V}$$

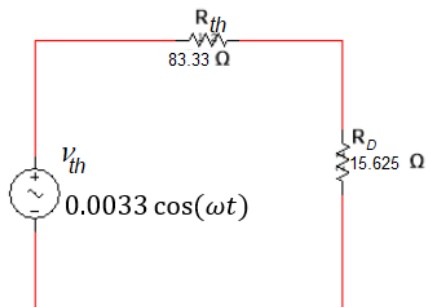
$$I_D = 1.6\text{ mA}$$

From question b (ii)

- AC analysis:

$$r_D = \frac{nV_T}{I_D} = \frac{25 \times 10^{-3}}{1.6 \times 10^{-3}} = 15.625\ \Omega$$

$$v_{th} = 0.02 \cos(\omega t) * \frac{100}{500 + 100} = 0.0033 \cos(\omega t)$$



$$i_d = \frac{v_{th}}{R_{th} + R_D} = 0.0337 \cos(\omega t) [mA]$$

$$v_d = i_d * R_D = 0.526 \cos(\omega t) [mV]$$

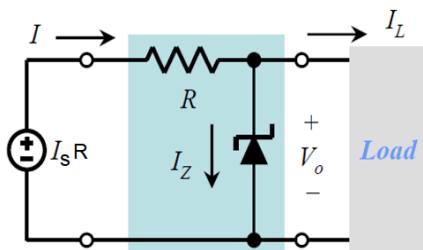
Finally:

$$(i) i_D = I_D + i_d = 1.6 + 0.0337 \cos(\omega t) [mA]$$

$$(ii) v_D = V_D + v_d = 0.7 + 0.526 \cos(\omega t) [mV]$$

d.

Using source transformation, we get:



$$\begin{aligned}
 (i) \quad I_Z &\geq I_{Zmin} \rightarrow \frac{I_s R - V_{Z0}}{R} - I_L \geq I_{Zmin} \\
 &\rightarrow I_s - \frac{V_{Z0}}{R} \geq I_{Zmin} + I_L \\
 &\rightarrow \frac{V_{Z0}}{R} \leq I_s - I_{Zmin} - I_L \\
 &\rightarrow R \geq \left(\frac{V_{Z0}}{I_s - I_{Zmin} - I_L} \right)_{max}
 \end{aligned}$$

Then:

$$\begin{aligned}
 (I_s - I_{Zmin} + I_L) &\text{ must be minimum} \\
 \rightarrow R &= \frac{V_{Z0}}{I_{s_min} - I_{Zmin} + I_{L_max}} \\
 &= \frac{6.8}{30m - 6m - 20m} = 1700 \, \Omega
 \end{aligned}$$

$$\begin{aligned}
 (ii) \quad P_{Z_max} &= V_{Z0} * I_{Z_max} \\
 &= V_{Z0} * \left(I_s - \frac{V_{Z0}}{R} - I_L \right)_{max} \\
 &= V_{Z0} * \left(I_{s_max} - \frac{V_{Z0}}{R} - I_{L_min} \right) \\
 &= 6.8 * \left(40m - \frac{6.8}{1700} - 5m \right) \\
 &= 0.21 \, W
 \end{aligned}$$

Lecture 3.4

Question 3.4

- a) An AC input $20\sin(100\pi t)$ volts is at the primary winding of the 2:1 transformer as shown in Fig.1. The secondary winding connects to a half-wave rectifier with an ideal diode. Determine DC equivalent (or average voltage) at the output V_{out} .

Hint: You use *integral over one period* of the output waveform $V_{av} = \frac{1}{T} \int_0^T V_{out} dt$

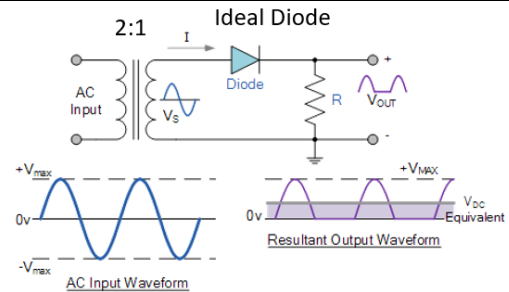
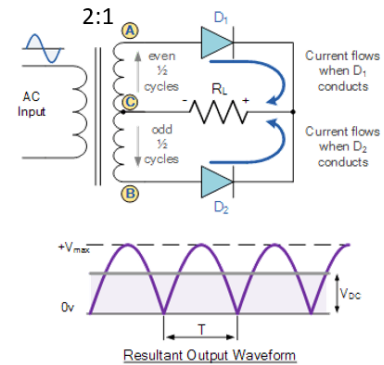


Fig. 1

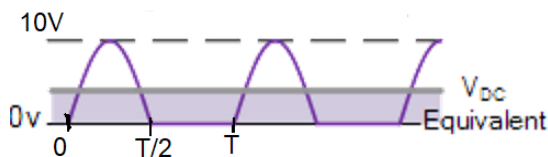
- b) An AC input $20\sin(100\pi t)$ volts is at the primary winding of the 2:1 transformer as shown in Fig.2. The secondary winding connects to a full-wave rectifier with ideal diodes. Determine DC equivalent (or average voltage) at the output V_{out} (voltage drop on R_L).

Hint: You use *integral over one period* of the output waveform $V_{av} = \frac{1}{T} \int_0^T V_{out} dt$



Ans

a.



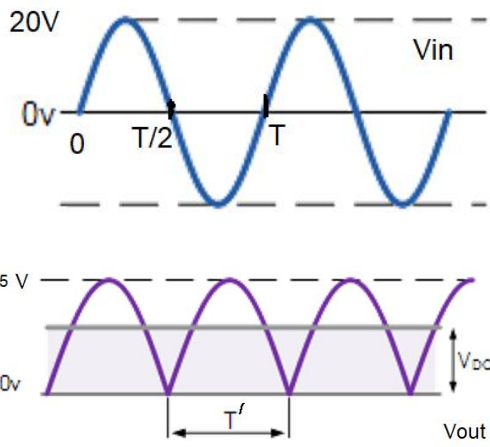
$$\omega = 100\pi \rightarrow T = 0.02$$

Using 2:1 transformer

$$\rightarrow V_s = \frac{V_{ac_input}}{2} = 10\sin(\omega t) \, [V]$$

$$\begin{aligned}
 V_{out_average} &= \frac{1}{T} \int_0^T V_{out} dt \\
 &= \frac{1}{T} \int_0^{T/2} 10\sin(\omega t) dt + \frac{1}{T} \int_{T/2}^T 0 dt = \frac{10}{\pi} \, [V]
 \end{aligned}$$

b.



$$T' = \frac{T}{2} = 0.01$$

Using 2:1 transformer and center-tap rectifier

$$\rightarrow V_{out} = \frac{V_{ac_input}}{4} = 5\sin(\omega t) [V]$$

$$V_{out_average} = \frac{1}{T'} \int_0^{T'} V_{out} dt = \frac{1}{T'} \int_0^{T'} 5\sin(\omega t) dt = \frac{10}{\pi} [V]$$