

Final Examination

Date: May 21, 2016

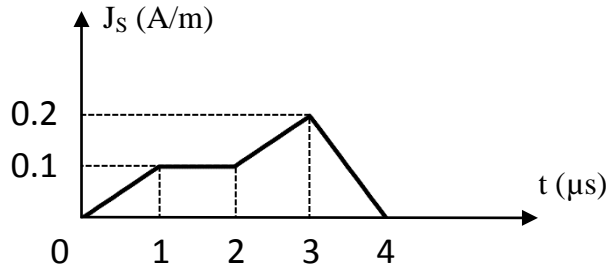
Duration: 120 minutes

SUBJECT: Electromagnetic Theory	
Dean of School of Electrical Engineering Signature:	Lecturer Signature:
Full name: Tran Van Su	Full name: Tran Van Su

Question 1 (20 Marks)

An infinite plane sheet of current density $\vec{J}_S = -J_S(t)\hat{x}$ (A/m), where $J_S(t)$ is as shown in *Figure* below, lie in the $z = 0$ in free space. Find and sketch:

- a) E_x versus t in the $z = 600\text{m}$ plane (10 Marks)
 b) E_x versus z for $t = 2\mu\text{s}$ (10 Marks)

**Question 2 (15 Marks)**

The electric field of a uniform plane wave propagating in the $+z$ direction in a nonmagnetic ($\mu = \mu_o = 4\pi \times 10^{-7}$) material medium is given by

$$\vec{E} = 8.4e^{-0.0432z} \cos(4\pi \times 10^6 t - 0.1829z) \vec{a}_x (\text{V/m})$$

Find the magnetic field of the wave (*Hint: $\vec{\gamma}\vec{\eta} = j\omega\mu_o$*)

Question 3 (10 Marks)

The plane $z = 0$ forms the boundary between free space ($z > 0$) and perfect conductor ($z < 0$)

- a) Find $\vec{J}_S(0,0,0)$ at $t = 0$ and $\vec{H}(0,0,0^+) = H_o(\hat{x} + 2\hat{y}) \cos \omega t$ (5 Marks)
 b) Find $\rho_S(0,0,0)$ at $t = 0$ and $\vec{D}(0,0,0^+) = E_o \cos \omega t \hat{z}$ (5 Marks)

Question 4 (15 Marks)

The sinusoidally time-varying, linearly polarized vector fields are given at a point by

$$\vec{F}_1 = \cos(2\pi \times 10^6 t + 30^\circ) \hat{x}, \quad \vec{F}_2 = \cos(2\pi \times 10^6 t + 30^\circ) \hat{z}, \quad \vec{F}_3 = \sqrt{2} \sin(2\pi \times 10^6 t + 30^\circ) \hat{y}$$

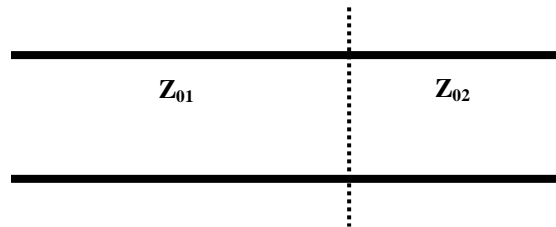
Determine the polarizations of the following vectors:

- a) $\vec{F}_1 + \vec{F}_2$ (7 Marks)
 b) $\vec{F}_1 + \vec{F}_2 + \vec{F}_3$ (8 Marks)

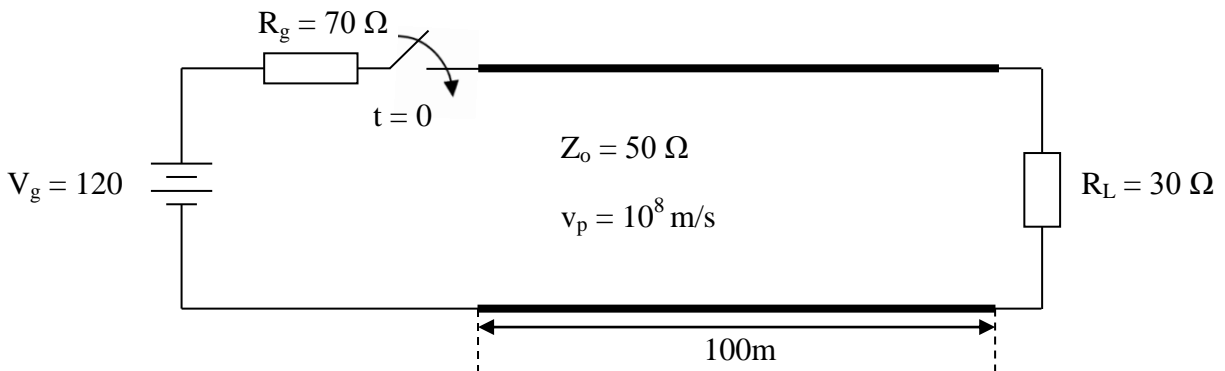
Question 5 (15 Marks)

For the Transmission line of the following *Figure*:

- a) The reflected wave voltage is $1/5$ times the incident wave voltage **(5 Marks)**
- b) The transmitted wave voltage is $1/5$ times the incident wave voltage **(5 Marks)**
- c) The reflected wave voltage is $1/5$ times the transmitted wave voltage **(5 Marks)**



Question 6 (25 Marks)



For the transmission line in *Figure* shown:

- a) Sketch the bounce diagram of the voltage and give enough information on it (up to $5\mu\text{s}$) **(5 Marks)**
- b) Sketch the bounce diagram of the current and give enough information on it (up to $5\mu\text{s}$) **(5 Marks)**
- c) Determine the voltage at the middle of the line at $t = 2.8\mu\text{s}$ **(5 Marks)**
- d) Calculate steady state V_{ss} and I_{ss} **(5 Marks)**
- e) Calculate steady state V_{ss}^+ , V_{ss}^- , I_{ss}^+ and I_{ss}^- **(5 Marks)**