

THE INTERNATIONAL UNIVERSITY (IU) - VIETNAM NATIONAL UNIVERSITY - HCMC
FINAL EXAMINATION - CLASS

Student Name: _____

Date: August 2018

Duration: 90 minutes

Student ID: _____

SUBJECT: PHYSICS 3

Chair of Department of Physics:

Signature: _____

Lecturer:

Signature: _____

Full name: Phan Bảo Ngọc

Full name: Duong Hoi Nghia

INSTRUCTIONS: This is a closed book examination. Use of cell phones, laptops, dictionaries is not allowed.

- 1) In Fig. 1, a metal wire of mass $m = 25 \text{ mg}$ can slide with negligible friction on 2 horizontal parallel rails separated by distance $d = 4 \text{ cm}$. The track lies in a vertical uniform magnetic field of magnitude 50 mT . A source is connected to the rails, producing a constant current $i = 10 \text{ mA}$ in the wire and rails. Find the magnitude and the direction of the force acting on the wire. (20 pts)

- 2) The magnitude of the electric field between the two circular parallel plates is $E = 100 \exp(-2t) \text{ V/m}$ (Fig. 2). The plate area is $A = 0.04 \text{ m}^2$. Determine

- a) The magnitude and the direction of the displacement current between the plates. (10 pts) $\mathcal{E}_i = -\frac{d\Phi_E}{dt} = -\frac{d}{dt} \int \vec{E} \cdot d\vec{A} = -\frac{d}{dt} (E A) = -A \frac{dE}{dt} = -0.04 \cdot (-200 \exp(-2t)) = 8 \exp(-2t) \text{ A}$
- b) The magnitude and the direction of the induced magnetic field between the plates. (10 pts)

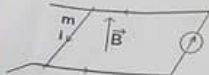


Fig. 1



Fig. 2

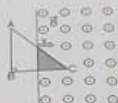


Fig. 3

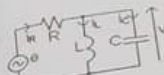


Fig. 4

- 3) In Fig. 3, the triangle ABC is moving into a magnetic field B with velocity v . If the triangle has resistance R , find the magnitude and the direction of the current i in the triangle. Let $AB = a$, $BC = b$. (20 pts)
- 4) Given the circuit in Fig. 4 with $e(t) = 100 \cos(1000t) \text{ V}$, $R = 100 \Omega$, $L = 0.1 \text{ H}$, $C = 10 \mu\text{F}$. Find the voltage v and the currents i_R , i_L , i_C . (20 pts)
- 5) The electric field component of an electromagnetic wave in vacuum is $\vec{E} = E_0 \sin(\omega t - kx) \hat{a}_y$. Find the magnetic field \vec{B} and the Poynting vector (20 pts).

END OF QUESTION PAPER

August 2018

$$\vec{F}_B = i \vec{L} \times \vec{B} \Rightarrow \begin{cases} \vec{F}_B \text{ to the left} \\ |\vec{F}_B| = 10 \times 10^{-3} \times 0.04 \times 50 \times 10^{-3} = 2 \times 10^{-5} \text{ (N)} \end{cases}$$

$$E = 100 e^{-2t}$$

$$\text{Displacement current: } i_d = \epsilon_0 \frac{d\phi_E}{dt} = \epsilon_0 A \cdot \frac{dE}{dt}$$

$$= 8.85 \times 10^{-12} \times 0.04 \times (-200) e^{-2t}$$

$$= -7.08 \times 10^{-11} \times e^{-2t} \text{ (A)}$$

\Rightarrow ~~i_d oppose the direction of \vec{E}~~
 $B_c \text{ id} < 0 \Rightarrow \vec{i}_d \text{ oppose the direction of } \vec{E} \text{ (discharge)}$
 $\hookrightarrow \text{To the left}$

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 i + \mu_0 i_d$$

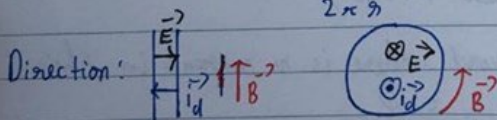
We only consider B on the plate $\Rightarrow \mu_0 i = 0$ & we ~~are~~

$$\Rightarrow \oint \vec{B} \cdot d\vec{s} = \mu_0 i_d \Rightarrow B 2\pi r = \mu_0 i_d$$

For our Algebra expression, we only care abt magnitude:

$$\hookrightarrow B 2\pi r = 7.08 \times 10^{-11} \times e^{-2t} \times \mu_0 = 8.9 \times 10^{-14} e^{-2t}$$

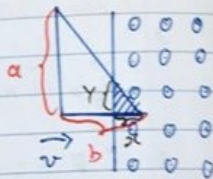
$$\Rightarrow B = \frac{8.9 \times 10^{-14} e^{-2t}}{2\pi r} \quad (0 < r < R; R \text{ being the radius of the plate})$$



$$3) \quad \mathcal{E} = \frac{d\Phi_B}{dt}; \quad i = \frac{\mathcal{E}}{R}$$

$$\mathcal{E} = \frac{dB}{dt} \cdot A = B \cdot \frac{dA}{dt} = B \cdot \frac{d(x \cdot y)}{dt}$$

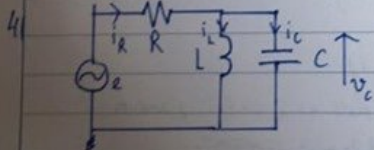
$$= B \left(x \frac{dy}{dt} + y \frac{dx}{dt} \right) \quad (1)$$



$$\frac{x}{y} = \frac{b}{a} \Rightarrow y = \frac{a}{b} x \Rightarrow \frac{dy}{dt} = \frac{a}{b} \frac{dx}{dt} = \frac{a}{b} v$$

$$\text{From (1) and (2)} \Rightarrow \mathcal{E} = B \left(\frac{a}{b} x \frac{dx}{dt} + \frac{a}{b} x \frac{dx}{dt} \right) = \frac{2 \times B a x}{b} v$$

$$\Rightarrow i \begin{cases} \text{Mag: } \frac{\mathcal{E}}{R} = \frac{2B a x v}{b R} \\ \text{Direction: Lenz's Law} \Rightarrow \text{Clockwise} \end{cases}$$



$$e(t) = 100 \cos(1000t)$$

$$= 100 \sin(1000t + 90^\circ)$$

$$R = 100 \, \Omega; \quad C = 10 \mu\text{F} \Rightarrow Z_C = 100 \, \Omega$$

$$L = 0.1 \text{ H} \Rightarrow Z_L = 100 \, \Omega$$

$$v_C = V_m \sin(1000t + \phi)$$

$$\Rightarrow i_C = \frac{V_m}{100} \sin(1000t + \phi + 90^\circ); \quad i_R = i_L + i_C = 0$$

$$i_L = \frac{V_m}{100} \sin(1000t + \phi - 90^\circ)$$

in another word, there is no current in this circuit

$$\Rightarrow i_R = i_C = i_L = 0$$