

# An extension of the formal model for a Library System

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March 2, 2016

## 0.1 Abstract

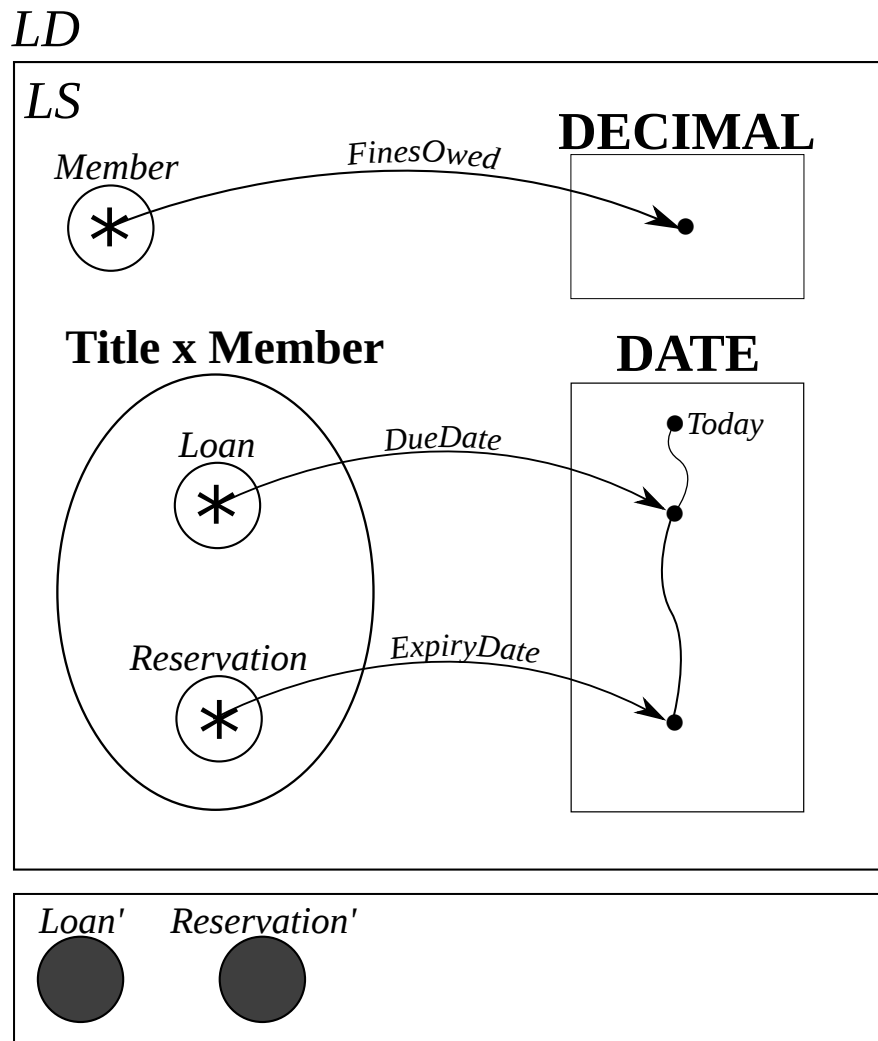
The goal of this coursework is to extend and refine the functionality of the existing library system by introducing the concept of time to it in accordance with the requirements given in the coursework document.

## 0.2 Class Invariant

### 0.2.1 Informal statement

In order to introduce the concept of time into the library system, a type named "DATE" is created and added to the class invariant. At this level, it is used to define a variable "today" which is the basis of the system's notion of time. The class invariant has also been extended to add reservations and loans by representing each as a subset of the set resulting from the cartesian product of the sets title and member. This way, each member of the loan set can be mapped to a "DATE" representing the due date and each member of the reservation subset can be mapped to another "DATE" representing the expiry date. Doing it this way also gives the system more flexibility as this set is not limited to reservations and loans, thus allowing for further extension. The invariant also contains a new addition to a member, "FinesOwned" which indicates how much money a member owes from overdue loans. In the post-condition, the Loan and Reservation set are initially empty.

### 0.2.2 Formal statement



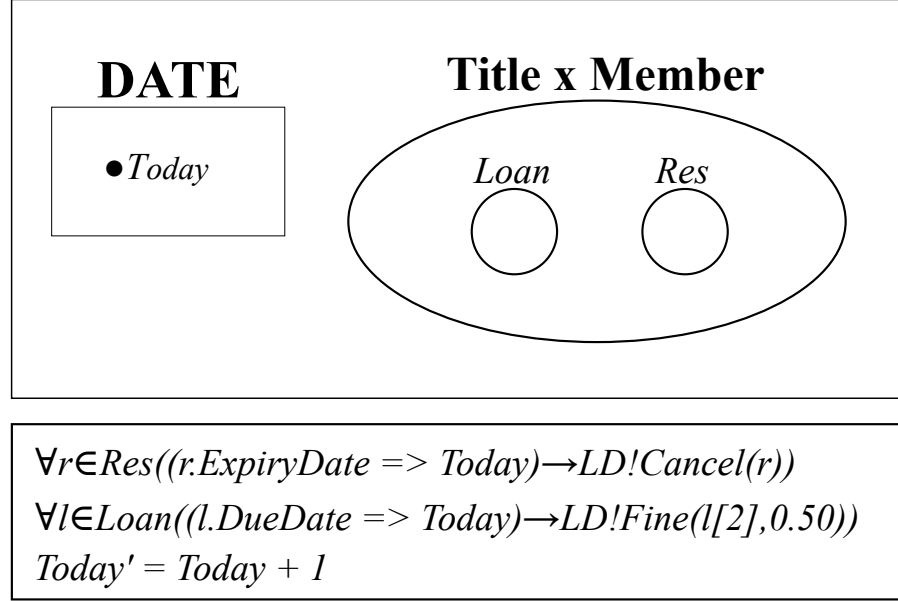
## 0.3 Move To Next Day

### 0.3.1 Informal statement

Using the "Today" variable set up in the class invariant, the next day can be derived. To do so, a new event is created that takes in today's date as a parameter. Along with this, the set of reservations and loans are passed through in order to check them for expired reservations and overdue loans. In the post-condition, every reservation is checked to see if its expiry date is equal to or after today, if it is the reservation is then passed through to the cancel event. Similarly, for each loan, the due date is checked to see if it is equal to today or more than, if it is, the member is then fined 0.50p. This fine would occur every day until the book is returned. Today is then moved to the next day by incrementing it by one.

### 0.3.2 Formal statement

***$LD!moveToNextDay(Today, Res, Loan)$***



## 0.4 Reserve

### 0.4.1 Informal statement

The reserve event has to be updated to add a expiry date when a book is reserved. To do this, it has been updated to take new parameters, "dur" (reservation duration) and "today". A new pair called *r* of type title x member is then made. To create a new reservation, a rule has been added that means a user must have currently not owe any money in fines to the library. In the post-condition, a new reservation is made by pairing title and member which is then added to the reservation set. The expiry date is then calculated and linked to this reservation by the "ExpiryDate" function.

### 0.4.2 Formal statement

$LD!reserve(title, member, dur, today \rightarrow p)$

$LS!reserve(title, member \rightarrow p)$

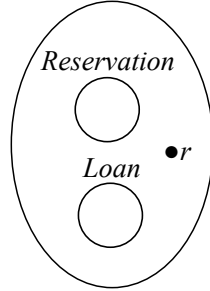
**DATE**

•*today*  
•*expiryDate*

**NAT**

•*dur*

**Title x Member**



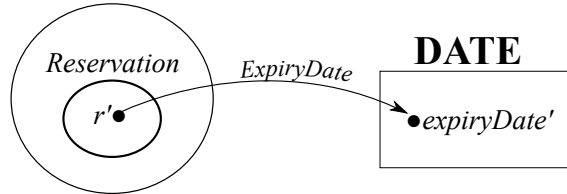
$r[1] = title$

$r[2] = member$

$member.FinesOwed \leq 0$

$expiryDate' = today + dur$

**Title x Member**



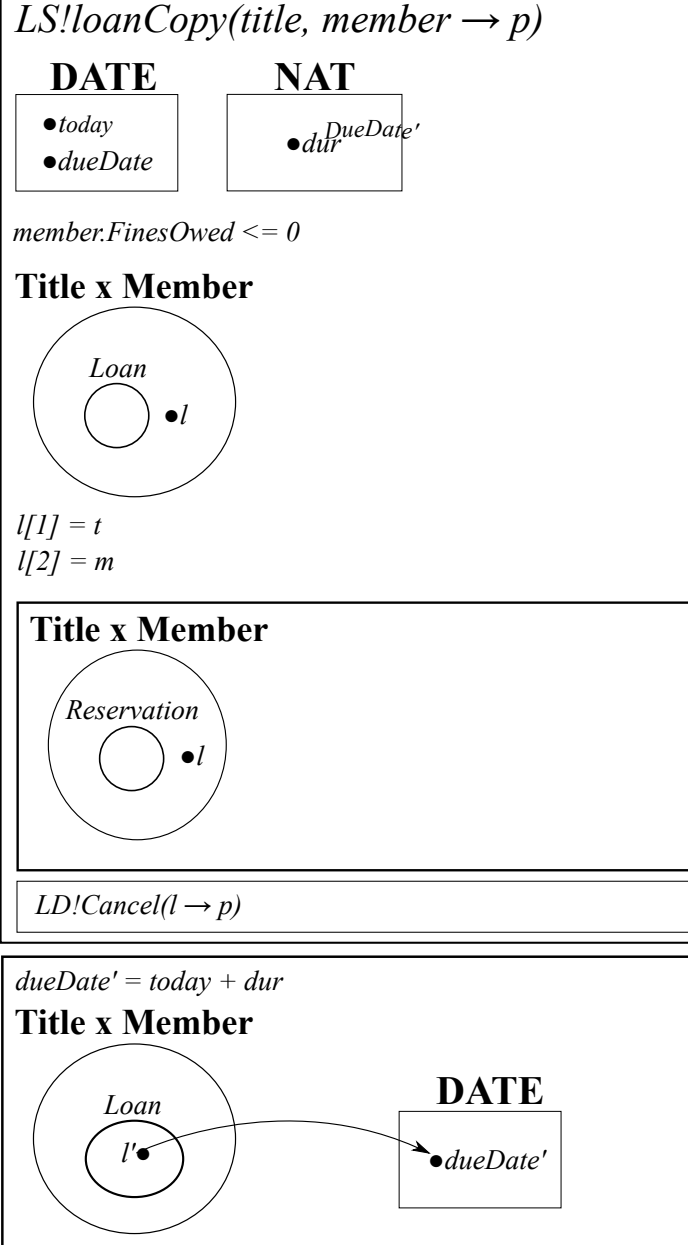
## 0.5 LoanCopy

### 0.5.1 Informal statement

Similar to reserve, the loanCopy event has to be updated to add due dates to new loans taken out. To do this, it is extended to include to new parameters, dur (loan duration) and today. To create a new loan A new Title and Member pair is made from the title and member parameters. If the loan is then found to already exist as a reservation, the cancel event is called and the reservation is cancelled. In the post-condition, the due date is calculated by adding the duration to the current date, this is then linked to the new loan by the "DueDate" function.

### 0.5.2 Formal statement

$LD!loanCopy(title, member, dur, today \rightarrow p)$



## 0.6 Cancel

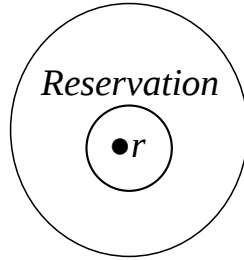
### 0.6.1 Informal statement

The cancel event is relatively simple, it takes a parameter, reservation "r". From which the title and member taken and passed through to the simple library system's cancel event in the postcondition, after this, the reservation is then removed from the set.

### 0.6.2 Formal statement

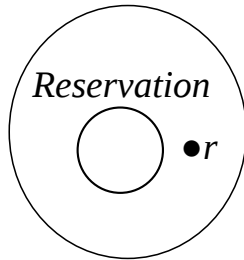
$LD!Cancel(r \rightarrow p)$

**Title x Member**



$LS!Cancel(r[1], r[2] \rightarrow p)$

**Title x Member**



## 0.7 Return

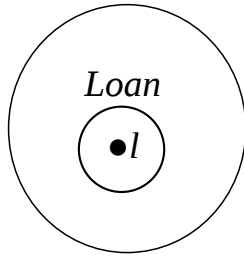
### 0.7.1 Informal statement

Again, similar to the cancel event, the new return event takes a loan as a parameter and uses the title and member with the simple library system's return event. The loan is then removed from the loan set.

### 0.7.2 Formal statement

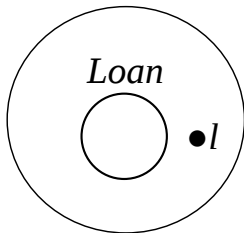
*LD!Return(l)*

**Title x Member**



*LS!Return(l[1],l[2])*

**Title x Member**



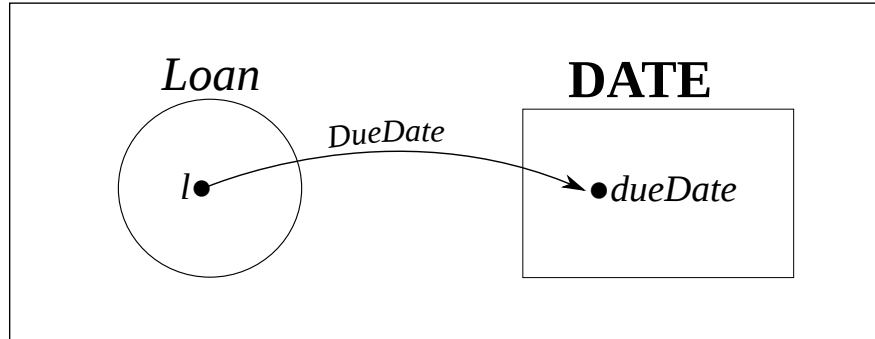
## 0.8 ShowDueDate

### 0.8.1 Informal statement

This event just takes in a loan and outputs the due date it has been associated with by the DueDate function.

### 0.8.2 Formal statement

$LD?showDueDate(l \rightarrow dueDate)$





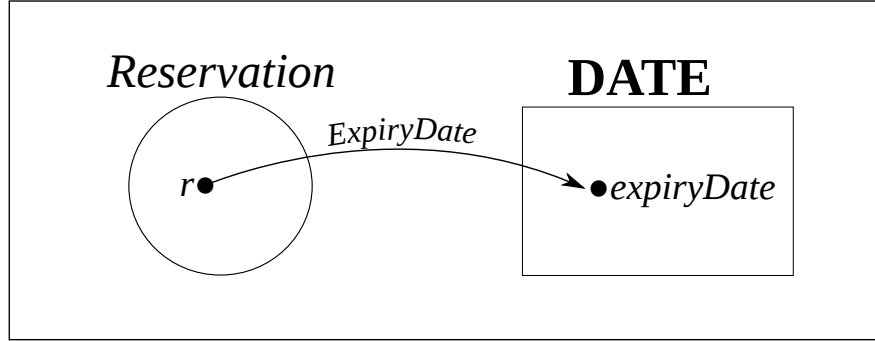
## 0.9 ShowExpiryDate

### 0.9.1 Informal statement

This event takes in a reservation and outputs the expiry date it has been associated with by the ExpiryDate function.

### 0.9.2 Formal statement

$LD?showExpiryDate(r \rightarrow expiryDate)$



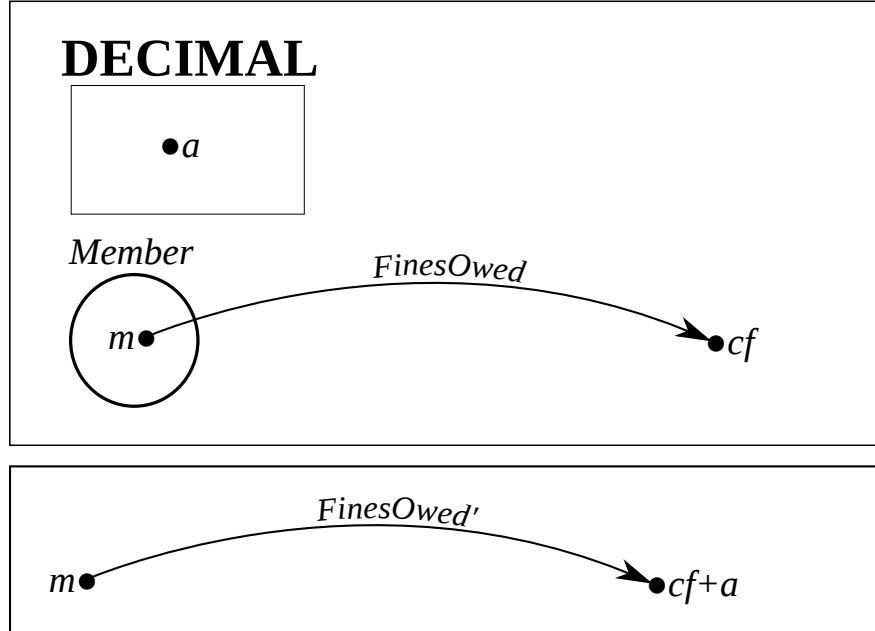
## 0.10 Fine

### 0.10.1 Informal statement

This takes in a member and an amount in the form of a decimal number. It then takes this decimal number and adds it to the current fine amount owed by the member.

### 0.10.2 Formal statement

***LD!Fine***( $m, a$ )



## 0.11 Pay Fine

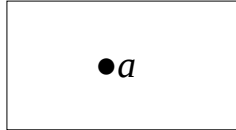
### 0.11.1 Informal statement

This allows the member to pay the fine they current owed. It takes in a member and amount. This amount has to be smaller than the or equal to the amount they currently owe, if it isn't the amount is changed to be equal to the amount they owe. It is then subtracted from the current amount they owe.

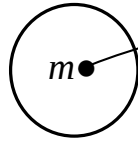
### 0.11.2 Formal statement

*LD!payFine(m, a)*

#### DECIMAL



*Member*



*FinesOwed*

$cf$

$cf > a$

$cf < a$

$a' = cf$

*FinesOwed'*

$m$

$cf-a$

## 0.12 Show Fines

### 0.12.1 Informal statement

This event takes in a member and outputs the amount of money they owe via the FinesOwned function.

### 0.12.2 Formal statement

*$LD!showFines(m \rightarrow cf)$*

