#### Outline of the Course

- 1. The Learning Problem (April 3)
- 2. Is Learning Feasible? (April 5)
- 3. The Linear Model I (April 10)
- 4. Error and Noise (April 12)
- 5. Training versus Testing (April 17)
- 6. Theory of Generalization (April 19)
- 7. The VC Dimension (April 24)
- 8. Bias-Variance Tradeoff (April 26)
- 9. The Linear Model II (May 1)
- 10. Neural Networks (May 3)

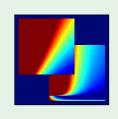
- 11. Overfitting (May 8)
- 12. Regularization (May 10)
- 13. Validation (May 15)
- 14. Support Vector Machines (May 17)
- 15. Kernel Methods (May 22)
- 16. Radial Basis Functions (May 24)
- 17. Three Learning Principles (May 29)
- 18. Epilogue (May 31)
  - theory; mathematical
  - technique; practical
  - analysis; conceptual

# Learning From Data

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Lecture 1: The Learning Problem





## The learning problem - Outline

- Example of machine learning
- Components of Learning
- A simple model
- Types of learning
- Puzzle

Example: Predicting how a viewer will rate a movie

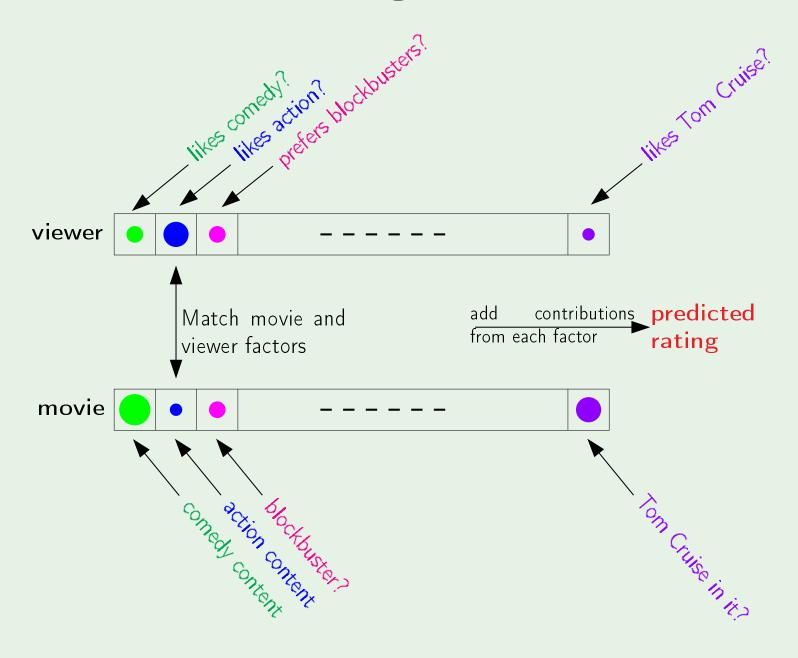
10% improvement = 1 million dollar prize

The essence of machine learning:

- A pattern exists.
- We cannot pin it down mathematically.
- We have data on it.

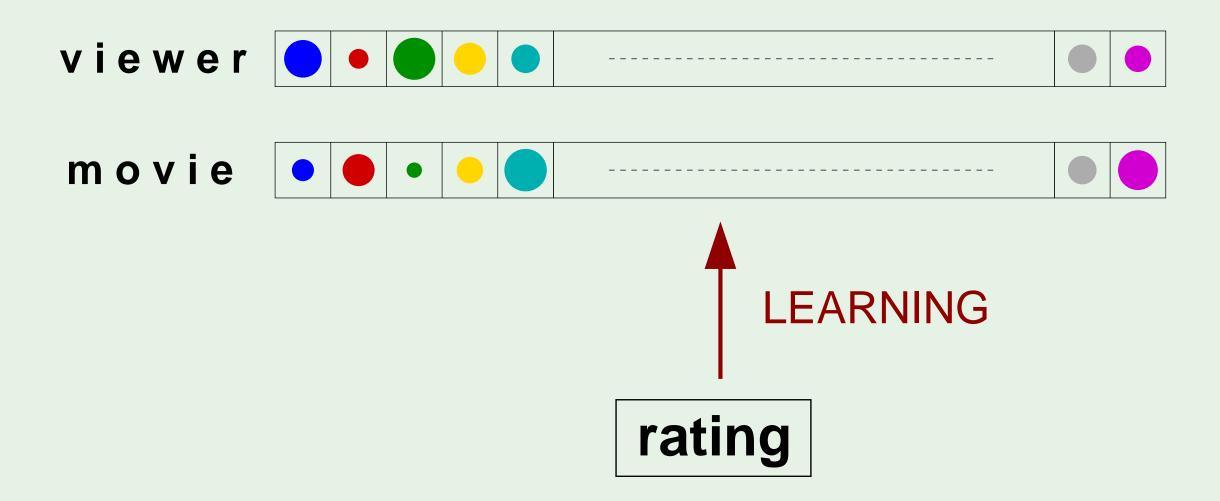
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## Movie rating - a solution



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## The learning approach



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## Components of learning

Metaphor: Credit approval

Applicant information:

age	23 years
gender	male
annual salary	\$30,000
years in residence	1 year
years in job	1 year
current debt	\$15,000
• • •	• • •

Approve credit?

### Components of learning

#### Formalization:

- Input: **x** (customer application)
- Output: y (good/bad customer?)
- Target function:  $f: \mathcal{X} \to \mathcal{Y}$  (ideal credit approval formula)
- ullet Data:  $(\mathbf{x}_1,y_1), (\mathbf{x}_2,y_2), \cdots, (\mathbf{x}_N,y_N)$  (historical records)
- Hypothesis:  $q: \mathcal{X} \to \mathcal{Y}$  (formula to be used)

We modify g to attempt to approximate f

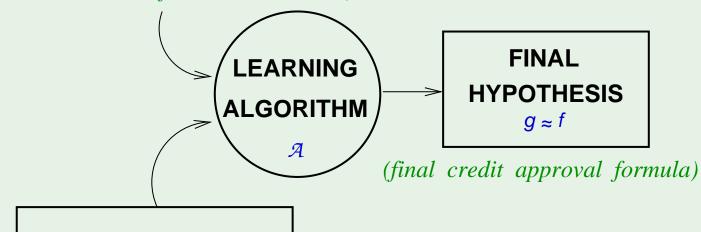
#### **UNKNOWN TARGET FUNCTION**

(ideal credit approval function)

#### TRAINING EXAMPLES

$$(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)$$

(historical records of credit customers)



HYPOTHESIS SET

 $\mathcal{H}$ 

(set of candidate formulas)

Q: why the need for set of hypotheses H, why not let A pick from all possible hypotheses?

A: There is no downside to having H since from a practical POV, you pick a Linear Model/NN/SVM at the beginning. The upside to H is that it is pivotal to if we can learn and how well we learn from the data.

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### Solution components

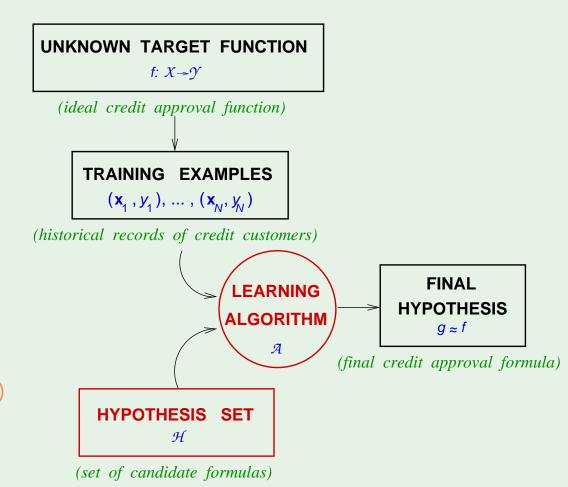
The 2 solution components of the learning problem:

• The Hypothesis Set (e.g. perceptron, NN, SVM)

$$\mathcal{H} = \{h\} \qquad g \in \mathcal{H}$$

• The Learning Algorithm (e.g. perceptron learning model, backprop., quadratic programming)

Together, they are referred to as the *learning* model.



## A simple hypothesis set - the 'perceptron'

For input  $\mathbf{x} = (x_1, \cdots, x_d)$  'attributes of a customer'

Approve credit if 
$$\sum_{i=1}^d w_i x_i > ext{threshold},$$

The linear addition of w\*x makes this a perceptron

Deny credit if 
$$\sum_{i=1}^d w_i x_i < \text{threshold.}$$

This linear formula  $h \in \mathcal{H}$  can be written as

$$m{h}(\mathbf{x}) = \operatorname{sign}\left(\left(\sum_{i=1}^d m{w_i} x_i\right) - \operatorname{threshold}\right)$$

Red parameters determine the final hypothesis - these are the aspects we change in the learning algorithm

$$h(\mathbf{x}) = \operatorname{sign}\left(\left(\sum_{i=1}^d \mathbf{w_i} \ x_i\right) + \mathbf{w_0}\right)$$

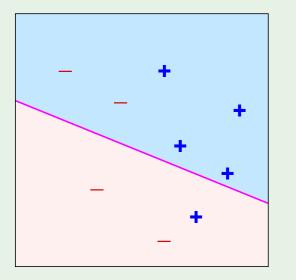
A choice of wi determines the location of the purple separation line below. (Note: change threshold to w0 and let x0 = 1 to simplify the expression)

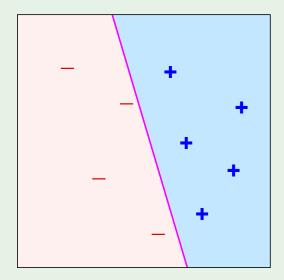
Introduce an artificial coordinate  $x_0=1$ :

$$h(\mathbf{x}) = \operatorname{sign}\left(\sum_{i=0}^{d} \mathbf{w_i} \ x_i\right)$$

In vector form, the perceptron implements

$$h(\mathbf{x}) = \operatorname{sign}(\mathbf{w}^{\mathsf{T}}\mathbf{x})$$





'linearly separable' data

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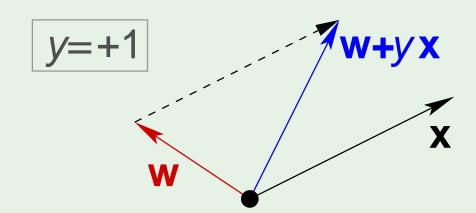
## A simple learning algorithm - PLA

The perceptron implements

$$h(\mathbf{x}) = \operatorname{sign}(\mathbf{w}^{\mathsf{T}}\mathbf{x})$$

Given the training set:

$$(\mathbf{x}_1,y_1),(\mathbf{x}_2,y_2),\cdots,(\mathbf{x}_N,y_N)$$

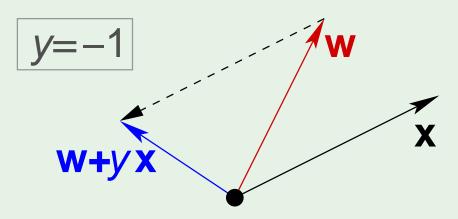


pick a misclassified point:

$$sign(\mathbf{w}^{\mathsf{T}}\mathbf{x}_n) \neq y_n$$

and update the weight vector:

$$\mathbf{w} \leftarrow \mathbf{w} + y_n \mathbf{x}_n$$



So: since yn = + or - 1, add or subtract x to w, so now the hypothesis will correctly classify this point

#### Iterations of PLA

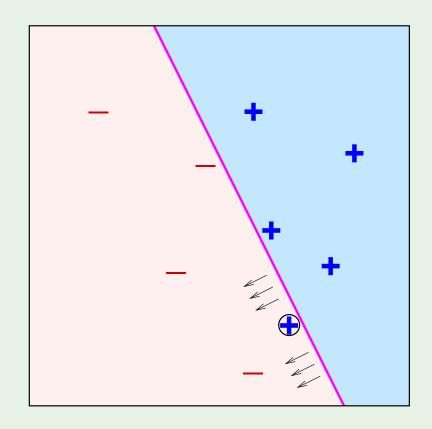
• One iteration of the PLA:

$$\mathbf{w} \leftarrow \mathbf{w} + y\mathbf{x}$$

where  $(\mathbf{x}, y)$  is a misclassified training point.

ullet At iteration  $t=1,2,3,\cdots$  , pick a misclassified point from  $(\mathbf{x}_1,y_1),(\mathbf{x}_2,y_2),\cdots,(\mathbf{x}_N,y_N)$ 

and run a PLA iteration on it.



• That's it!

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## Basic premise of learning

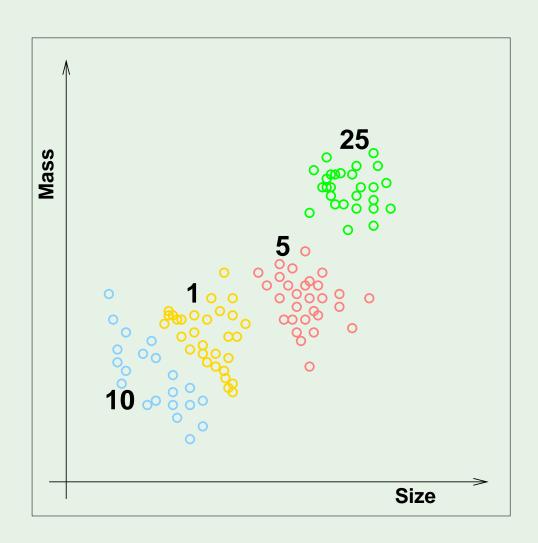
"using a set of observations to uncover an underlying process"

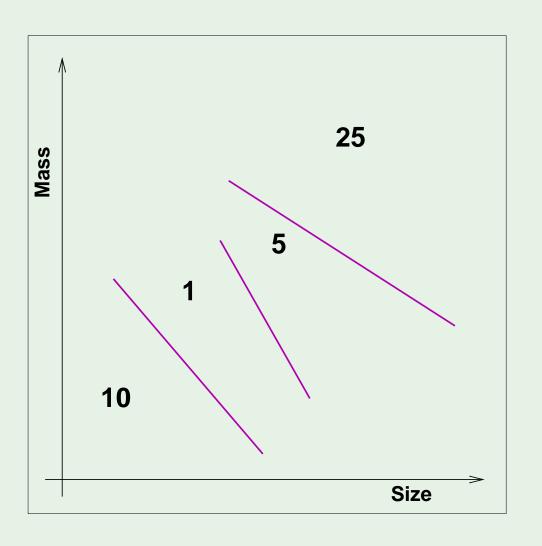
broad premise  $\implies$  many variations

- Supervised Learning
- Unsupervised Learning
- Reinforcement Learning

# Supervised learning

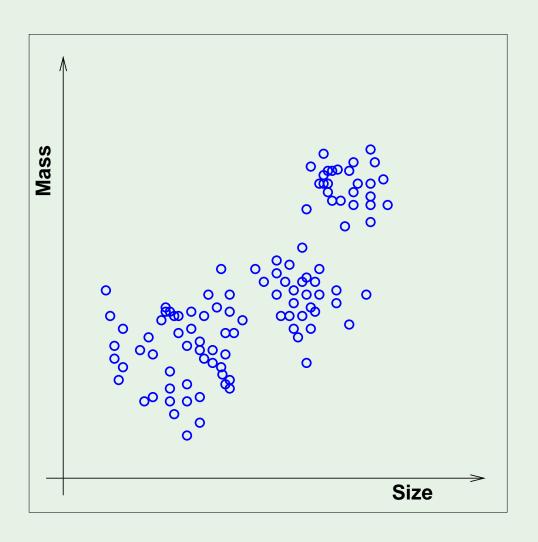
Example from vending machines - coin recognition





## Unsupervised learning

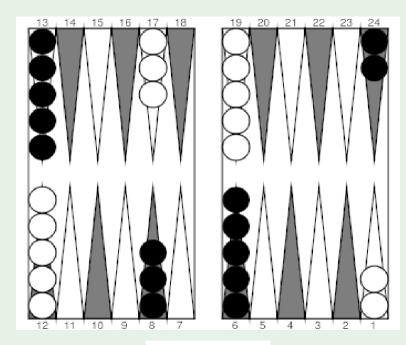
Instead of (input,correct output), we get (input,?)



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## Reinforcement learning

Instead of (input,correct output), we get (input,some output,grade for this output)

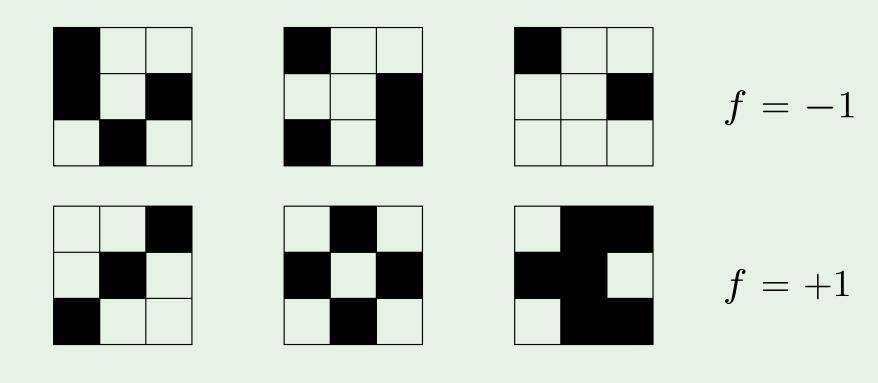


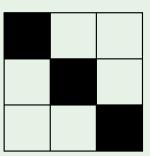
The world champion was a neural network!



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## A Learning puzzle





$$f = ?$$