

## Awkward example like proof.

For target language.

Assume assert loops and no flags.

We ignore malloc and pretend memory magically appears.

• We do not have a way to generate a fresh seal for the closure.

• The  $R$  relation is tailored for the call semantics, but we do not know that the adversary uses call, so when we return, we fail to use the continuation relation.

## Proof

Pick

$$W = \begin{bmatrix} L^{sta} & ms_{link} \\ L^{stk} & dom(ms_{stk}) \\ L^{adv} & dom(ms_{adv}) \\ L^{sta} & dom(ms_{gr}^{gr}) \end{bmatrix}$$

contains  $g1$  and  $R4$ .

where

$L^{sta}$  is a normal region

$L^{stk}$  is a spatial-owned region

$L^{adv}$  is a normal region

(in particular the standard region).

For

$$\text{reg} = \text{reg}_0 [ \text{pc} \mapsto c_{\text{adv}}, c_{\text{data}} \mapsto c_{\text{adv},d}, r_{\text{stk}} \mapsto c_{\text{stk}}, r_1 \mapsto c_{g_1}, r_2 \mapsto c_{g_2, \text{data}} ]$$

where  $c_{g_1}$  and  $c_{g_2,d}$  is a sealed capability pair.

$c_{\text{stk}}$  is a linear capability for the stack.

$c_{\text{adv}}$  is the adversary code capability and  $c_{\text{adv},d}$  is the data capability for the adversary.

Show

$$(\text{reg}, \text{ms}) \in \mathcal{O}(W)$$

(for ms like in the prev. lemma).

To this end we use the FTLR ... (?) to get

$$(c_{\text{adv}}, c_{\text{adv},d}) \in \mathcal{E}(W_p) \quad \text{No owned regions}$$

Now if we can show

$$(c_{\text{adv}}, c_{\text{adv},d}) \in \mathcal{P}(W_p)$$

okay because the capabilities not linear.

$$(0, 0) \in \mathcal{R}(W_k)$$

nothing owned

okay because it always fails.

$$(1) \text{ reg} \in \mathcal{R}(W_{\text{stk}})$$

$$(2) \text{ ms} : W_M$$

owns nothing

then we are done by the conclusion of  $\mathcal{E}$ .

In other words, we need to show (1) and (2).

(2) is here okay because ..., so it remains to show (1).

(1) Show

(a)  $c_{gk} \in \mathcal{V}(W_k)$

(b)  $c_{g1} \in \mathcal{V}(W')$

(c)  $c_{g1,d} \in \mathcal{V}(W')$

~~W' has no owned regions.~~  
We can pick the owned stack region, and the rest should be ok.

where  $W'$  has no owned regions.

We need to show (b) and (c)

At this point we need a proper def. of  $\mathcal{V}$  for sealed capabilities, but for arguments sake assume it amounts to the following (in this case):

Say  $c_{g1} \stackrel{\text{sealed}}{=} (sc_{g1}, \sigma)$   
 $c_{g1,d} = \text{sealed}(sc_{g1,d}, \sigma)$

then we need to show

$$(sc_{g1}, sc_{g1,d}) \in \mathcal{E}(W_1)$$

for  $W_1 \supseteq^{\text{priv}} W'$

This means that the stack region may have been revoked in  $W_1$ .

to this end let  $W_R, W_M, W_K$  be given s.t.

$W_R \oplus W_M \oplus W_K \oplus W_1$  is defined. Further assume

$$\text{reg}_R \in \mathcal{R}(W_R), \quad (sc_{g1}, sc_{g1,d}) \in \mathcal{P}(W_1)$$

$$\text{ms}_M : W_M, \quad \text{and}$$

$$(c_K, c_{K,d}) \in \mathcal{R}(W_K)$$

and show

$$(\text{reg}_R, \text{ms}_M) \in \mathcal{O}(W_R \oplus W_M \oplus W_K \oplus W_1)$$

where

$$\text{reg}_1' = \text{reg}_1 [p \mapsto sc_{g_1}, \text{data} \mapsto sc_{g_1.d}, \text{retcode} \mapsto c_k, \text{retdata} \mapsto c_{k.d}]$$

We use the anti-reduction lemma w/ the following observations

$$(\text{reg}_1', \text{ms}_1) \longrightarrow^* (\text{reg}_2, \text{ms}_2)$$

where

$$\text{reg}_2(r_3) = c_{f_4}$$

$$\text{ms}_2(x) = 0$$

$$\text{reg}_2(r_3) = ((RW, \text{normal}), x, x, x)$$

$$\text{reg}_2(r_1) = \text{sealed}(c_x, \sigma)$$

$$\text{reg}_2(r_2) = \text{sealed}(c_{f_4}, \sigma)$$

$$c_{f_4} = ((RX, \text{normal}), \underline{c_k}, \underline{c_{k.d}}, -) \quad \leftarrow \text{Points to f4 code.}$$

$$\text{reg}_2(p_c) = sc_k$$

$$\text{reg}_2(\text{data}) = sc_{k.d}$$

otherwise like reg<sub>1</sub>

} unsealed  $c_k$  and  $c_{k.d}$  respectively.

Now show

$$(\text{reg}_2, \text{ms}_2) \in \mathcal{O}(W_2) \quad \text{where} \quad W_2 = W_1[L_x]$$

To this end, we need to use

$$(c_k, c_{k.d}) \in R(W_k)$$

$$A \rightarrow W_k \subseteq^{p_{\text{th}}} W_k[L_x], \text{ we need to show}$$

$$\text{ms}_2: W_k[L_x] \xrightarrow{\text{Hopefully follows from previous shift}}$$

$$* \text{ reg}_2 \in R(W_k[L_x])$$

$$c_k, c_{k.d} \in P(W_p)$$

normal region w/  
transition system



\* Remains to be shown.

Here, the most interesting case is showing  
 $\text{sealed}(c_{\text{pc}}) \in V(W_2 \cup \dots)$  w/ no owned regions.

which (like previously) hopefully amounts to  
 $(c_{\text{pc}}, c_x) \in E(W_2)$  for  $W_2 \supseteq^{\text{priv}} W_1$

To this end let  $W_{2R}, W_{2M}, W_{2K}$  be given s.t.  
 $W_{2R} \oplus W_{2M} \oplus W_{2K} \oplus W_2$  is defined. Further, assume

$$\text{reg}_3 \in R(W_{2R})$$

$$(c'_k, c_{k,d}) \in R(W_{2K})$$

$$\text{ms}_3: W_{2M}$$

and show

$$(\text{reg}_3[\text{pc} \mapsto c_{\text{pc}}, \text{rdata} \mapsto c_s, \text{retcode} \mapsto c'_k, \text{retdata} \mapsto c_{k,d}], \text{ms}_3) \in O(W_{2R} \oplus W_{2M} \oplus W_{2K} \oplus W_2)$$

Use anti-reduction. Execution goes as follows:

$$(\text{reg}_3[\text{pc} \mapsto \dots], \text{ms}_3) \xrightarrow{*} (\text{reg}_4, \text{ms}_4)$$

where  $\text{reg}_4(\text{rstk}) = ((w_1, \dots), \text{base}, \dots)$  ← base of stack checked

$\text{ms}_4(x) = 0$   $\text{ms}_4$  otherwise has a changed stack (see next page) - otherwise unchanged.

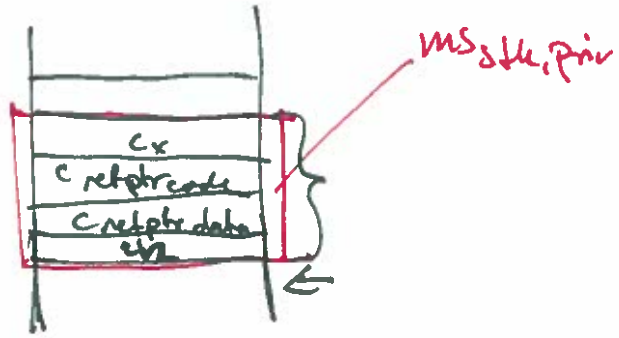
$\text{reg}_4(\text{pc}) = s_{\text{cbs}}$   
 $\text{reg}_4(\text{rdata}) = s_{\text{cbs,d}}$  } these capabilities come from the callstack given to us.

$\text{reg}_4(\text{retcode}) = c_{\text{bu,ret}}$  ← sealed capability that points to the appropriate place in memory.

$\text{reg}_4(\text{retdata}) = c_{\text{fu,dade}}$  ← sealed capability that contains the linear capability for the private part of the stack.

$\text{reg}_4(\text{rtemp}, \dots) = 0$ . The rest of reg as before.

The private stack:



Now argue

$$(reg_4, ms_4) \in \mathcal{O}(W_3)$$

the region for the stack.  
spatial owned

where  $W_3 = \text{revolveRegion}(i, W_2) [ \begin{matrix} sth \\ ms\_stk\_priv \end{matrix} ]$

$W_3$  ~~is~~  $W_2$   $\leftarrow$  does this even matter?

$[ \begin{matrix} sth \\ ms\_unused \end{matrix} ]$   $\leftarrow$  spatial owned sub. region.

To this end pick  $W_{SR}^{scb} = \text{revolveRegion}(i, W_{2R}) [ \begin{matrix} sth, spatial \\ ms\_stk\_priv \end{matrix} ]$

$[ \begin{matrix} sth, spatial \\ ms\_unused \end{matrix} ]$   $\leftarrow$  Not owned.

Now notice  $W_{2R}^{scb} \subseteq^{priv} W_{SR}^{scb}$  as:

$W_{2R}(i)$  is a spatial region as it must be owned by  $W_{2R}$ . It is thus ok to revoke it. Further, we add new regions, so all in all we are good.

This gives us that

$$(scb, scb.d) \in \Sigma(W_{scb}^{scb})$$

and show

$ms_4: W_{4R}$  for a <sup>world</sup> region that owns none of the new spatial regions.

(i)  $reg_4 \in W_{4R}$  for a world that owns the region for ~~the stack~~ the unowned stack.

(ii)  $(c_{func}, c_{data}) \in R(W_{4R})$  for a region that owns the region for the private stack.

To show (i) the most interesting case is  $rstk$  for which we use the stack region which is spatially-owned in  $W_{4R}$ .

To show (ii) let  $W_{5K} \supseteq W_{4K}$  and let  $W_{5R}, W_{5M}$  be given s.t.  $W_{5K} \circ W_{5R} \circ W_{5M}$  is defined and assume

$$(c_{func}, c_{data}) \in P(W_{5K})$$

$$reg_5 \in R(W_{5R})$$

$$ms_5 \in W_{5M}$$

and show

Here I used the unary  $K$  from local cap. work. so no  $stk$ .

$$(reg_5[p \mapsto sc_{func}, data \mapsto sc_{data}], ms_5) \in \mathcal{O}(W_{5M})$$

To this end use anti-red lemma.

$$W_{5K} \circ W_{5R} \circ W_{5M}$$

Based on the program, the execution either fails or step to a configuration  $(reg_0, ms_0)$  s.t.

$reg_0(rs_k) = reg_3(rs_k) \leftarrow$  i.e. the old stack pointer.

$reg_0(pc) = \text{[scribbled out]}$   
 $SC_k'$

We skip the second call and return

$reg_0(rdata) = SC_{kid}' \leftarrow$  the unsealed versions of the return capability pair. (circled on p. 5).

In order to use the continuation/return pointer, we need to take a look at the  $R(W_{2K})$  relation. Here we need to use ~~this~~ a where  $W_{6K} \supseteq^{priv} W_{2K}$ . At the world  $W_{6K}$

same time, we need to ~~add~~ construct  $W_{6K}$  based on  ~~$W_{5K}$~~  so we can revoke regions that are no longer needed.

$W_{6K}$  contains an owned spatial region for the private stack. We need to be able to revoke this in order to give up the stack.

Not this one, but one of the other

$W_5$  regions. Ignoring this, revoke the two stack regions and add the old stack region from  $W_{2K}$ .

We want to make sure

$W_6 \supseteq^{priv} W_{5K}$  and

$W_6 \supseteq^{priv} W_{5M}$ , so

we can argue the validity of  $reg_0$  and  $ms_0$ .

Is the problem perhaps in R? Should the P be ~~on~~ before H.