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In This Issue

### How To Determine The Drag Coefficient of Your Rockets

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# **How To Determine The Drag Coefficient of Your Rockets**

By Tim Van Milligan

As the members of the TARC teams become more knowledgable about rocketry, the event is becoming more and more competitive. Everyone is looking for that extra edge that will get them to the finals in Virginia.

The one question I get every year is how to determine the  $Drag\ Coefficient\ (C_d)$  of the rocket more accurately. The reason this is a big question is because with an accurate value for the Drag Coefficient, teams can reduce the number of test flights they need to make. That really helps lower the cost to the students.

### Making RockSim Better

Because it accounts for so many of the variables associated with flight, people really have a pretty good understanding of just how accurate RockSim can be. The one Achilles heel is determining the Drag Coefficient of the rocket.

This is a problem that even plagues NASA. While software has gotten better, and it will continue to get better, there is still an uncertainty of just what is the actual Drag Coefficient of the flying object.

But still, people want to know how RockSim can be made more accurate at predicting the Drag Coefficient. That will be the topic of this article.

### Altitude Back-Tracking

The method that most people use to get a better value on the Drag Coefficient is called back-tracking. It is pretty easy to do, and here is the procedure:

- 1. Put an altimeter in the rocket. Measure the actual height of the rocket. For example, in your test flight, the altimeter says the rocket went to a height of 1000 feet.
- 2. Input the design into RockSim. Run a simple simulation, using a fixed  $\rm C_d$  value. A good starting point is to set the  $\rm C_d$  at 0.75.
- 3. Compare the altitude that RockSim predicts against the altitude measured by the altimeter.
- 4. Adjust the  $\rm C_d$  value in the software (make it higher if the previous simulation went higher than the measured al-

titude from the altimeter, and lower if it didn't simulate high enough). Run a new simulation.

Go back to step 3. Repeat this process until the altitudes match.

The final  $\rm C_d$  entered into RockSim that was used to match the actual altitude from the Altimeter is now your "back-tracked"  $\rm C_d$  value.

This process does involve a little bit of effort. But you can usually zero-in the  $\rm C_d$  value within 5 or 6 iterations of the process.

We used to sell a program called SMARTSim that sped up the process. But unfortunately, the programmer got tired of repairing it every time Microsoft created a Windows OS update. Our long-term goal is to get that program back, and maybe even incorporated directly into RockSim. We have lots of ideas on how to make it better...

### How Good Is Altitude Back-Tracking?

That is the million-dollar question, isn't it?

It should be pretty good. And many successful TARC teams have proved that it does work well.

But, the big assumption is that the rocket flew the same trajectory as predicted by RockSim. In RockSim, you probably set the conditions to try to match the actual flight conditions, but it may not be "perfect." And, as a lot of TARC teams know, there is some variability between rocket motors. So while RockSim assumes the motor may have put out exactly 80 N-s of total power, in real life, you might have gotten to the altitude with just 75 N-s of power.

So on your next real-life flight, if you have a motor with 79 N-s of power, it is going to go a bit higher, and now you're thinking that your back-tracked  $C_{\rm d}$  is too low.

The solution to this, of course, is to fly a high number of test flights and back-track the  $\rm C_d$  value for each of them so that you average out the variability of the motors. Then you'd average them so that you'd get a better approximation of the actual  $\rm C_d$  value for the rocket.

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### **Determine A Rocket's Drag Coefficient**

This is where it starts getting a little expensive, because you're burning a lot of rocket motors. But it is actually the right thing to do.

### We Need More Data

As you can tell, we need to gather a lot of flight data, so that we can dial-in on that elusive  $C_{\rm d}$  value. The more data you can get, the quicker you can find that  $C_{\rm d}$  value.

One additional piece of data that we can get on the flight is the velocity of the rocket, either through the recording altimeter, or through the AltimeterTwo altimeter (<a href="https://www.ApogeeRockets.com/AltimeterTwo.asp">www.ApogeeRockets.com/AltimeterTwo.asp</a>). It is better to use a device that has an accelerometer on board, as you'll get more accurate readings.

A pressure-sensing altimeter can give you rougher speed readings on velocity, but it isn't quite as accurate. For one thing, it has a little lag in sensing the air pressure inside the rocket. To understand this, think of the electronics bay as a balloon filled with air. There are holes in the balloon, so air is escaping. Air continues to flow out until the pressure inside the balloon equals the outside air pressure. It doesn't change instantly, as you know. It takes a few moments for the air pressure to equalize.

The same thing happens in a rocket. On the ground, the pressure inside the e-bay is the same as the outside. As the rocket ascends, the outside air pressure decreases. So the air inside the e-bay has to flow out until they equalize. When it is equalized, that is the point where you want to take the pressure reading. The big problem comes when the rocket is moving really fast, since the outside air pressure is rapidly changing because the altitude changes quickly.

The most accurate readings for a pressure sensor oc-

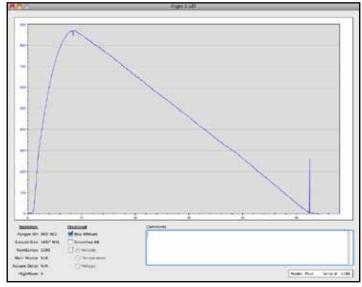


Figure 1: Altimeter data from a recording altimeter. The curve is nice and smooth indicating good data.

cur when the rocket is moving slow – such as when it nears the apogee point in the flight (see Figure 1). At this point, there is no upward velocity, so it is a great time to make a pressure reading. There is plenty of time for the air pressure to equalize when the outside pressure is staying constant. And that is exactly why pressure sensors are used to measure height.

But unfortunately, when it is moving slow, even subtle changes in pressure readings can indicate fast *speed* changes. If you look at the speed chart from a recording Barometric altitude sensor, they fluctuate wildly when the rocket is moving at a slow speed. For example, in Figure 2, notice how jagged the graph is when the rocket is descending under the parachute. Also note, that even before the rocket is launched, the speed is rapidly changing. And you know that can't be right, since the rocket is actually station-

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### **Determine A Rocket's Drag Coefficient**

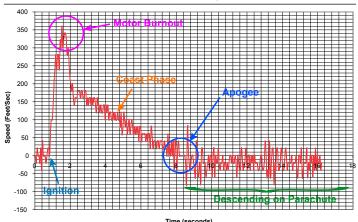


Figure 2: Speed graph created from barometric altitude data. Notice the data is more jumpy at slow speeds.

ary prior to launch.

Pressure sensors are great for measuring peak altitude, but not so great when the rocket is moving rapidly upward.

That is why you want to use an accelerometer-based sensor to measure speed. It reacts much quicker.

For your reference, the payloads Apogee Components sells that have accelerometers on them are: AltimeterTwo, G-Wiz Flight Computer (<a href="www.ApogeeRockets.com/G-Wiz\_flight\_computers.asp">www.ApogeeRockets.com/G-Wiz\_flight\_computers.asp</a>), and the TeleMetrum (<a href="www.ApogeeRockets.com/Altus\_Metrum\_GPS.asp">www.ApogeeRockets.com/Altus\_Metrum\_GPS.asp</a>).

Now you have this extra velocity data, what do you do with it?

Basically, you treat it the same way as you'd treat peak altitude. You back-track out a  $\rm C_d$  based on that velocity.

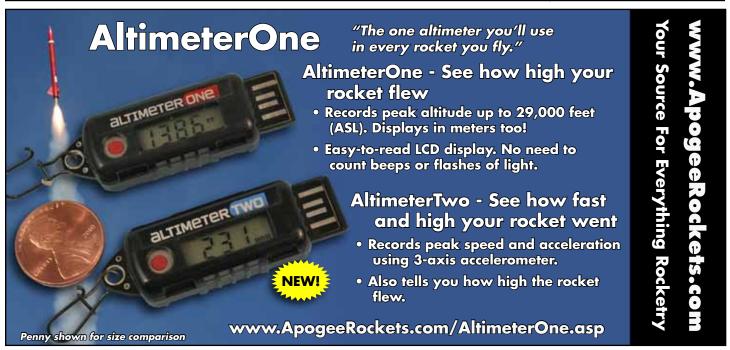
- 1. Put an accelerometer in the rocket. Measure the maximum speed of the rocket. For example, in your test flight, the accelerometer says the rocket went to a speed of 250 miles per hour.
- 2. Input the design into RockSim. Run a simple simulation, using a fixed  $\rm C_d$  value. A good starting point is to set the  $\rm C_d$  at 0.75.
- 3. Compare the maximum speed that RockSim predicts against the speed measured by the accelerometer.
- 4. Adjust the  $C_d$  value in the software (make it higher if the previous simulation went faster than the measured speed from the accelerometer, and lower if it didn't simulate fast enough). Run a new simulation.
- 5. Go back to step 3. Repeat this process until the maximum speeds match.

The final  $C_d$  entered into RockSim that was used to match the actual maximum speed from the accelerometer is now your "back-tracked"  $C_d$  value.

If you use any of the accelerometer-based electronic payloads that also have a barometric sensor included (like the AltimeterTwo), the advantage is that you have two

What Do You Do With Velocity?

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### **Determine A Rocket's Drag Coefficient**

independant sources of data. So you can back-track out a  $\rm C_d$  value based on the maximum speed, and a  $\rm C_d$  based on the peak altitude. You've now doubled the amount of data for the same cost of the rocket motor!

With this extra data, you can average out the  $\rm C_d$  values and get to a final value in a faster amount of time.

### **Eliminating Motor Variation**

As mentioned previously, the one big unknown we still have is the rocket motor variability.

First of all, why is there some variability in the thrust produced by the rocket motors? There are two factors.

First is the chemical formulation of the propellant. As you know, there are different chemicals that make up the final propellant. These are weighed out and mixed together. Unfortunately, errors creep into the manufacturing process. Are the weights exactly equal down to the micro-gram? Probably not. Are they mixed perfectly together so that the chemicals are evenly distributed throughout the entire volume? Probably not. Are the purity of the chemicals used the same from batch to batch? Again, probably not.

The second way errors creep into the motors is through the geometric properties of the motors. For example, are the propellant grains exactly the same length from motor to motor? Are the slots or the holes in the propellant exact from motor to motor? Are there voids (air bubbles) in the propellant? And are those voids in the same place from motor to motor? Nope.

The motor manufacturers are really good at trying to limit the variability by extensive quality assurance procedures in place during production. But the errors still creep in, and that means the thrust of each motor is going to be slightly different.

That means that your back-tracked  $C_{\rm d}$  is going to be off. The reason is that RockSim is assuming the motors are perfect from one flight to the next. But they are actually off a little bit.

What would be ideal is if we could eliminate the motor from the determination of the Drag Coefficient. And there is a couple of ways to do this.

### Wind Tunnels

The obvious method is to use a wind tunnel to measure the drag forces on the rocket. And this is a great way to do it. In fact, this is the way that NASA does it. If you have a good wind tunnel with perfectly smooth airflow, and good measuring equipment, you can get highly accurate values for the Drag Coefficient.

Unfortunately, most TARC teams nor average hobbyists have access to such test equipment.

But there is a second way to get  $C_d$  values that eliminate the effects of the rocket motors.

### **Terminal Velocity Measurements**

In the February 1970 issue of <u>Model Rocketry Magazine</u>. Tom Milkie wrote an article on how to determine the drag coefficient of your rocket by dropping them out of a window. It was actually that article that sparked the idea for this one.

The reason for dropping the rocket out the window is to get the rocket to reach its terminal velocity. This is good, because it eliminates most all the variables except the one important one. That is the *Drag Coefficient*.

When the rocket falls, the two forces acting on the rocket pull in opposite directions. Gravity pulls harder at first and the falling rocket gains speed. As the speed increases,

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### **Determine A Rocket's Drag Coefficient**

the Drag force increases. When it gains enough speed, the two forces eventually equal out. This is the terminal velocity speed.

Terminal velocity occurs when the downward force of gravity  $(F_g)$  equals the upward force of drag  $(F_d)$ . This causes the net force on the object to be zero, resulting in

Force due to gravity =  $F_g = m g$ 

Force due to Drag = 
$$F_d = \frac{1}{2} \rho v^2 A C_d$$

an acceleration of zero.

Where:

v = velocity (m/s)

m = mass of the falling object - (kg)

g = acceleration due to gravity = 9.80665 m/s<sup>2</sup>

C<sub>d</sub> = drag coefficient

 $\rho$  = density of the air = 1.225 kg/m<sup>3</sup> at 15°C

A = projected area of the object - Typically this is the cross-sectional area at the base of the nose cone, or the largest diameter of the rocket. You have a choice in RockSim, but make sure you use the one that RockSim is using when you work through the equations.

Now let's set the two to be equal:

$$m g = \frac{1}{2} \rho v^2 A C_d$$

Gravity Force = Drag Force

Solving for this equation for the Drag Coefficient (C<sub>d</sub>)

$$C_{d} = \frac{2 \text{ m g}}{\rho \text{ v}^2 \text{ A}}$$

yields.

Note that this is the same equation we use when finding the drag coefficient of a descending parachute. The only thing that changes is the *Area*.

At this point, when you find the terminal velocity, you can simply plug it into this equation.

### Watch your UNITS!

When you solve this equation, you have to be sure to watch your units. It is a lot easier to solve this using metric units, so make sure all your numbers are in metric before solving it.

### How do you get the rocket to reach terminal

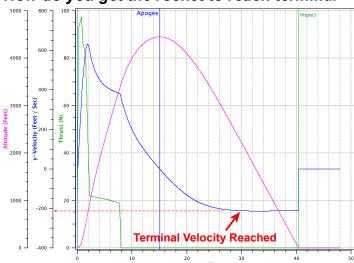


Figure 3: Terminal velocity is reached when the speed curve flattens out.

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Quick-

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### **Determine A Rocket's Drag Coefficient**

### velocity?

Simple. Drop it from a very great height. In our case, we'll launch the rocket to a very great height, let it arc over and come screaming down. Obviously, that isn't too safe if the rocket impact the grounds at a high velocity. So you'll want to do two things.

First, select a motor with a very long delay, so that it ejects before it hits the ground.

Second, make the rocket as lightweight as possible. The lower the weight, the slower the terminal velocity. Slower is safer.

### Here are some other things to consider:

First, you have to use a recording accelerometer, because you'll be getting the downward portion of the trajectory. This currently eliminates all but the G-Wiz Flight Computer and the TeleMetrum (always check the Apogee Components web site for *new* payloads - technology is always improving). But at the present time, this means you're flying something larger than a typical model rocket.

The Drag Coefficient is dependant on the shape of the rocket, so instead of using a full-size rocket, use a smaller one (but with the same shape). Not only is it going to be lighter weight, but you can use a smaller motor to launch it into the air. In other words, smaller equals cheaper! You want to save money doing this, right? Make it just large enough to use the recording accelerometer.

Also make sure that your recovery device can withstand a high-speed deployment. You'll probably want to switch over to a streamer instead of a parachute, at least for the expensive part of the altimeter.

If I were to do this myself, here is the procedure that I'd use:

- 1. Start with a few RockSim simulations to dial in on the delay to use in the rocket motor. You want to initially set the Drag Coefficient to a low number (such as 0.5), so that the rocket will come down faster. Why? Because I'd rather deploy a little too early than have the rocket impact into the ground. In RockSim, pick a really long delay (at least 15 seconds on a typical size rocket). You're going to *TYPE* this number into RockSim's delay field. Hit the **ENTER** key (not the **RETURN**) to force RockSim to accept the new value for the delay.
- 2. Remember, you also want to select a motor that is powerful enough to put the rocket to a sufficient height, that when it arcs over and comes down, it can reach that terminal velocity before it impacts the ground.
- 3. Launch the real rocket straight up, with as little wind as possible. You want the downward trajectory to be perfectly straight. Collect the terminal velocity speed from the recording accelerometer.
- 4. Compare the terminal velocity speed that RockSim predicts against the speed measured by the accelerometer.
  - 5. Adjust the C<sub>d</sub> value in the software (make it higher Continued on page 8)



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### **Determine A Rocket's Drag Coefficient**

if the previous simulation went faster than the measured speed from the accelerometer, and lower if it didn't simulate fast enough). Run a new simulation.

6. Go back to step 4. Repeat this process until the terminal velocity speeds match.

The last C<sub>d</sub> value is now the "back-tracked" C<sub>d</sub> value of the rocket.

The advantage of this method, as we said, is that it completely eliminates the random effects of the motor. That's cool, huh? That means it will only take a few flights to dial in on the actual C<sub>d</sub> of the design.

### What if The Rocket Doesn't Reach Terminal Velocity?

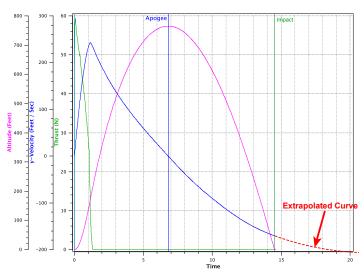


Figure 4: If you can't get the curve to flatten out, just extrapolate the end portion. Your eyeball is good at smoothing out the curve! Compare this to Figure 3.

You launch the rocket into the air, and it doesn't quite reach terminal velocity as it descends. What do you do then?

You do what all good engineers do. You cheat.

What you do is look at the curve, and extrapolate out where it levels out to zero. You can see how this is done in Figure 4, as compared to Figure 3 on page 6. You may be off a little bit, but it won't be much. The longer the curve that you captured in the data, the more accurate your results will be.

In the simulations I did here, when this particular rocket did reach Terminal Velocity, the speed according to Rock-

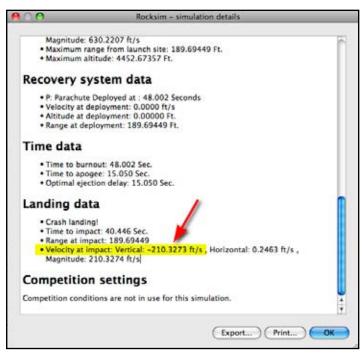


Figure 5: The terminal velocity can be read directly from the Simulation Details Report in RockSim.

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### **Determine A Rocket's Drag Coefficient**

Sim's detailed flight report was 210.32 ft/sec. See Figure 5. From the graph in Figure 4, I would estimate that the extrapolation would show a terminal velocity around 208 ft/sec. That's an error of just 1%!

### Where The Error Creeps In

Now we didn't eliminate all the variables, but we got pretty close. What variables might we reduce if you want even greater accuracy?

First, the rocket has to come down perfectly straight. If it wobbles at all, the Drag Coefficient is going to fluctuate wildly. That is because the rocket is presenting the side of the tube to the airstream, instead of just the top of the nose cone. In other words, the surface area term has changed. But we actually see this in the  $\rm C_d$  changing, since we assumed the reference area was a constant value.

Secondly, the density of the air is changing on us too. The rocket starts at a high altitude where the air is thin, and descends into thicker air as it comes down. This means that as it descends, the Terminal Velocity is going to be a little lower. You see this subtle change in Figure 3 where the velocity begins to fall again as the rocket gets closer to the ground.

The good news is that if you launch on a calm wind day, you can probably eliminate most of the wobble. And that is about as good as you'll get.

### Is There a Safer Way?

Having your rockets come streamlining down to the ground at a high speed is not something that I want to do either. It carries a high risk. If the ejection charge doesn't deploy at the right time – SMACK! Or if the chute strips off because of the high-speed deployment – CRACK! It is a brutal deployment situation, and I would worry about the

electronics surviving this kind of trajectory.

I would only do it if I was in a remote area further away from spectators and property. You must be extremely careful.

Is there a safer way?

Not quite yet. But we're not too far from the day. In fact, if you're a computer programmer, you might speed that day along by writing a program to do what I'm about to describe.

Consider this situation...

Why did we want to get the rocket to come in ballistically to reach terminal velocity? Right. To eliminate the variability of the motor's performance. We had to wait until the motor burned out to start making measurements.

Furthermore, we had to wait until the rocket's speed evened out so that there was no net forces acting on the rocket – where the drag force equaled the gravity force.

The question I have for you is "why even wait for the drag force to equal the gravity force?" Can we deduce the drag force directly in another manner?

The answer is yes.

We already are calculating the drag force in RockSim (assuming we know the Drag Coefficient). The result is that you can predict the speed and acceleration of the rocket as it ascends.

You may be confused by this, so let me try to explain. What I'm saying is, we should be able to predict how fast the rocket starts to decelerate after the motor burns out. Why? Because, the only thing that controls this is the force of gravity (which is known), and the force of drag – the deceleration is the sum of drag plus the gravity force.

For example, Figure 6 shows the deceleration curves

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### **Determine A Rocket's Drag Coefficient**

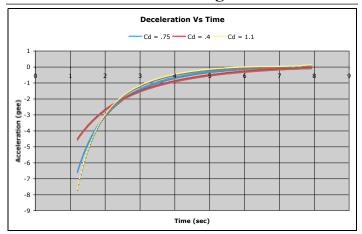


Figure 6: Deceleration curves of the rocket from burnout to apogee for three different  $C_a$  values.

of a rocket after motor burnout, and before it reaches Apgoee for three different  $C_{\rm d}$  values. In other words, this is just a snipet of the flight during coast, but before the rocket reaches apogee.

Do you see in Figure 6 that each Cd gives us a different deceleration curve? This shape is important!

Before I go on, I want to point out that this is something that can actually be measured using the accelerometer data!

Doing it this way, we can back-track out the  $C_d$  of the rocket, not by comparing a single point on the curve (like just peak altitude, burnout speed, or Terminal Velocity), but

by comparing the "SHAPE" of the curve itself.

There is only one  $C_d$  value that can create a specific-shape deceleration curve.

What you see in Figure 6 are three different deceleration-curves based on different Drag Coefficients. You can definitely see that they are different. But unfortunately, they are a little hard to make comparisons in this format. They need to be separated out so that it is easier to distinguish the different shapes for the different drag coefficient values.

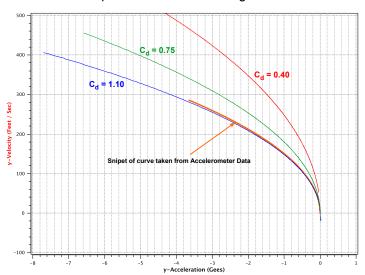
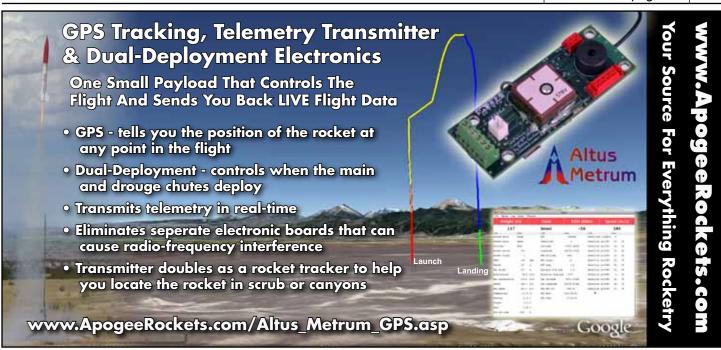


Figure 7: Just by plotting out the data a little differently, (Deceleration vs Speed), you get much greater separation of the curves for the three different  $C_d$  values.

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### **Determine A Rocket's Drag Coefficient**

I did this in Figure 7 by plotting out the deceleration values versus Speed. Now you can definitely distinguish the different shapes of the curves.

### How would you use this procedure for finding the Cd value of the rocket?

- 1. Here is the part where we need some new software. The first thing we need to do is to create a chart like Figure 7, with different deceleration curves for the various values of Drag Coefficients. It has to use the rocket design we intend to fly, just like we do with the other back-tracking methods. We still need an accurate shape and mass, plus all the launch conditions accounted for.
- 2. After running these simulations, now go out and launch the real rocket straight up on a windless day. We always need windless, because we don't want the rocket to wobble or arc over as it takes off. Record the acceleration data from lift-off to apogee.
- 3. From the acceleration data, create a new plot showing the acceleration versus speed. You can toss out that part of the plot during the motor's thrust phase. It will be skewed by the variations in thrust anyway.
- 4. Overlay the actual plot on top of the deceleration curves. Make sure the scales on the X-Y axes are the same. In Figure 7, I placed a snipet of acceleration data on the graph so you can get an idea of how you're going to overlay the curves.

5. The  $C_{\rm d}$  value is one that best matches the curve from the launch.

### The Advantages of This Method

There are several major advantages to this method.

First, it is safe. We can prep the rocket like any normal flight. We're not going to have it come streamlining toward the ground at a high rate of speed.

Second, it eliminates the variation in motor thrust between launches. So it will take fewer test flights to dial in on the  $\rm C_{\rm d}$  value.

Third, we can use the actual rocket to make the measurements. We don't have to make a scale model just to keep the weight low - like you have to do when making Terminal Velocity measurements.

Fourth, it should be highly accurate because it is easy to distinguish how the curves overlay each other.

Fifth, if you look at the chart in Figure 7, one thing should pop right out at you: the higher the speed of the rocket, the further the lines are apart for each  $C_{\rm d}$  value. What this means is that you actually want to use a high-thrust motor when you measure the  $C_{\rm d}$  value. You want your rocket to go REAL fast, so it has a longer amount of time to decelerate. That way, you'll get a longer curve, which makes matching up on the overlay a lot easier.

Also, the accelerometers are more accurate when there are larger forces to measure, which means that going faster

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### **Determine A Rocket's Drag Coefficient**

makes the accuracy higher.

So what you'd do is make your Drag Coefficients with high thrust motors, and then fly your actual launches (like TARC qualification flights), with any motor you'd like.

### One last thing...

Notice that the snipet of deceleration data in Figure 7 does not match perfectly up with the  $\rm C_d$  curves. The reason is that we're seeing some of the affects of density variation in the flight.

The curves were generated with a high thrust motor (I used an E30 in the simulations). The snipet of deceleration data was generated using a lower thrust motor (an E15). The E15, because it has lower thrust, is more efficient in fighting drag because it keeps the speed of the rocket lower. Remember, drag is proportional to the square of velocity (double the velocity, the drag goes up four times).

So the E15 was higher in the sky when the motor burned out. At higher altitudes, the air is less dense, so it acts like the rocket has a lower Drag Coefficient. That is why the curve bends slightly upward and isn't a perfect match for the Drag Coefficient of 1.1. But the shape is so close, that you can easily tell what the  $\rm C_d$  value was.

In this article, I described four different ways to back-track out the  $C_d$  value of your rocket based on flight data.

- 1. Peak Altitude back-tracking
- 2. Maximum velocity back-tracking
- 3. Terminal velocity back-tracking
- 4. Deceleration-versus-Speed back-tracking

This final method of determining the  $\rm C_d$  values is still off in the future, but it will eventually come as software becomes available to process the flight data. And it will give us our best and easiest way to determine that elusive  $\rm C_d$  value.

I hope you found this article useful. If you did, please send me a note.

### Additional Information

Maximum Simulation Accuracy from RockSim, Peak-of-Flight Newsletter 45 (www.ApogeeRockets.com/Education/Downloads/Newsletter45.pdf).

Smarter Guessing and Simulating With RockSim 5, Peak-of-Flight Newsletter 60 (www.ApogeeRockets.com/Education/Downloads/Newsletter60.pdf).

Optimizing Your Design Using SMARTSim, Peak-of-Flight Newsletter 130 (www.ApogeeRockets.com/Educa-

Conclusion

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tion/Downloads/Newsletter130.pdf).

*SMARTSim Tips for design Optimization,* Peak-of-Flight Newsletter 134 (<a href="www.ApogeeRockets.com/Education/Downloads/Newsletter134.pdf">www.ApogeeRockets.com/Education/Downloads/Newsletter134.pdf</a>).

Sleuthing Altimeter Data for Critical Answers, Peak-of-Flight Newsletter 208 (<a href="www.ApogeeRockets.com/Education/Downloads/Newsletter208.pdf">www.ApogeeRockets.com/Education/Downloads/Newsletter208.pdf</a>).

How To Zero In on The TARC Altitude and Duration Objectives, Peak-of-Flight Newsletter 249 (www.ApogeeRockets.com/Education/Downloads/Newsletter249.pdf).

### About The Author:

Tim Van Milligan (a.k.a. "Mr. Rocket") is a real rocket scientist who likes helping out other rocketeers. Before he started writing articles and books about rocketry, he worked on the Delta II rocket that launched satellites into orbit. He has a B.S. in Aeronautical Engineering from Embry-Riddle Aeronautical University in Daytona Beach, Florida, and has worked toward a M.S. in Space Technology from the Florida Institute of Technology in Melbourne, Florida. Currently, he is the owner of Apogee Components (<a href="http://www.apogeerockets.com/education/">http://www.apogeerockets.com/education/</a>.

He is also the author of the books: "Model Rocket Design and Construction," "69 Simple Science Fair Projects with Model Rockets: Aeronautics" and publisher of a FREE ezine newsletter about model rockets. You can subscribe to the e-zine at the Apogee Components web site or by sending an e-mail to: ezine@apogeerockets.com with "SUB-

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