

Modelling Static Complex Networks

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1 Introduction

Whenever one works with networks or graphs, the visualisation of connections is quite useful. Even though the computer itself doesn't benefit from the visual representation, the person working on the project may get some ideas about new modelling strategies after the visualisation, when working with networks. Networks are made up of a collection of two objects:

- Nodes: represents and entities.
- Edge: represents the connections amongst the entities.

The nodes usually have some attributes/properties, for which the whole network gives the connections amongst these. When these networks get more and more complicated, it's crucial under the modelling process to visualise them, so it showcases as much information as possible.

2 NetworkX

In the following research, I'll be analysing and modelling different networks and graphs with the NetworkX Python library. The tasks and exercises for the semester are written in a github repository, which can be found through the following link: [1]. The first task was to choose a couple data sets, which can be represented as networks. The data sets I chose are the following: The first one is about steroid usage amongst baseball players [2]. The second data set contains information about domestic flights in the UK in the year of 2003 [3].

After getting a little bit familiar with the data sets and the NetowrkX library, I tried out different layout schemes for each of these two networks. The results are interpreted in the Results and discussion section.

2.1 Baseball data set

The following graph 1 shows the 72 different players in relation to having the same steroid supplier. There is another data set in the package I downloaded, which shows all the suppliers and the different players, who bought steroid from them, however, that graph will only be presented in the second progress report. In graph 1 the common steroid suppliers can be seen for each player, where the different players are represented with numbers from 1 till 72. As it's clearly seen, most people used the same steroid supplier, while only a smaller portion of the people used different ones.

2.2 Flights data set

The other data set I chose to visualise was about domestic flights in the UK. The graph is very simple, it shows the connections between the cities, from which and to which flights flew. The visualised network can be seen in graph 2.

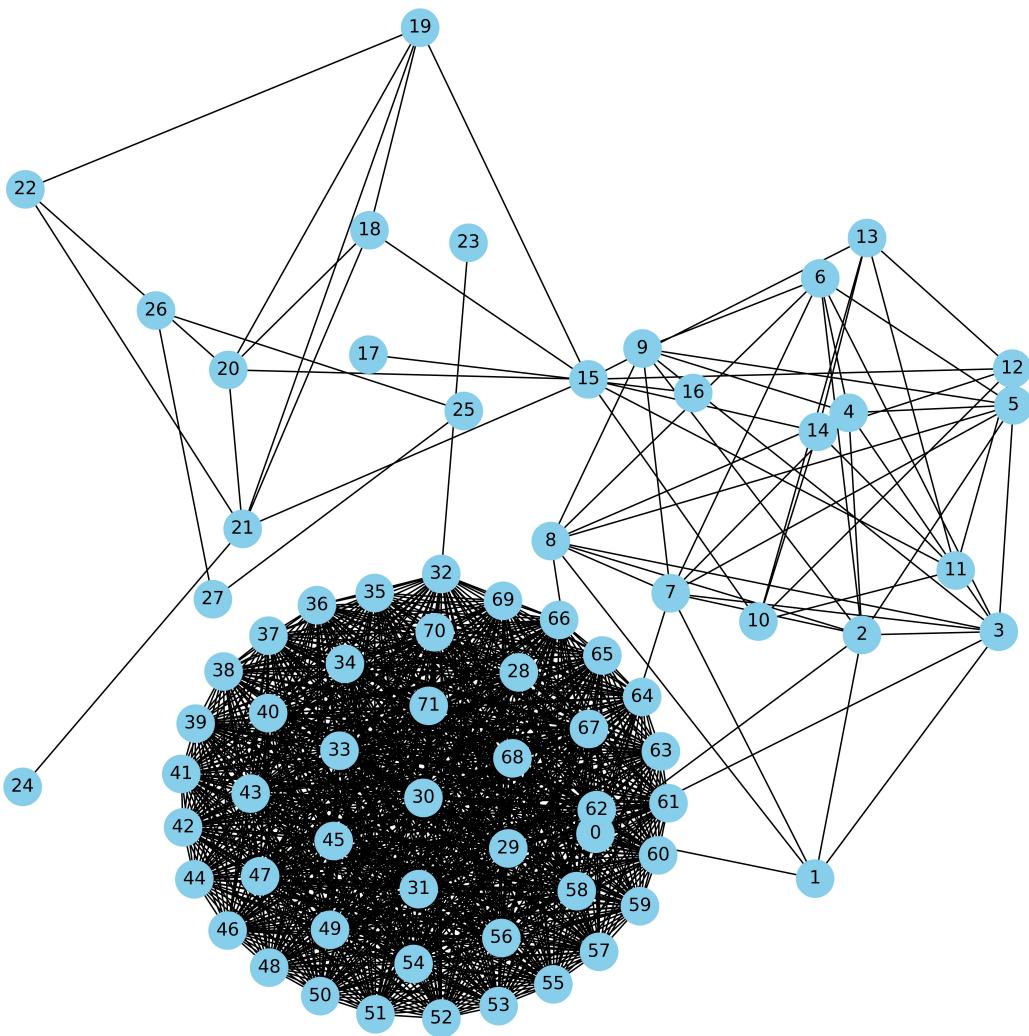


Figure 1: Common steroid suppliers of the different baseball players.

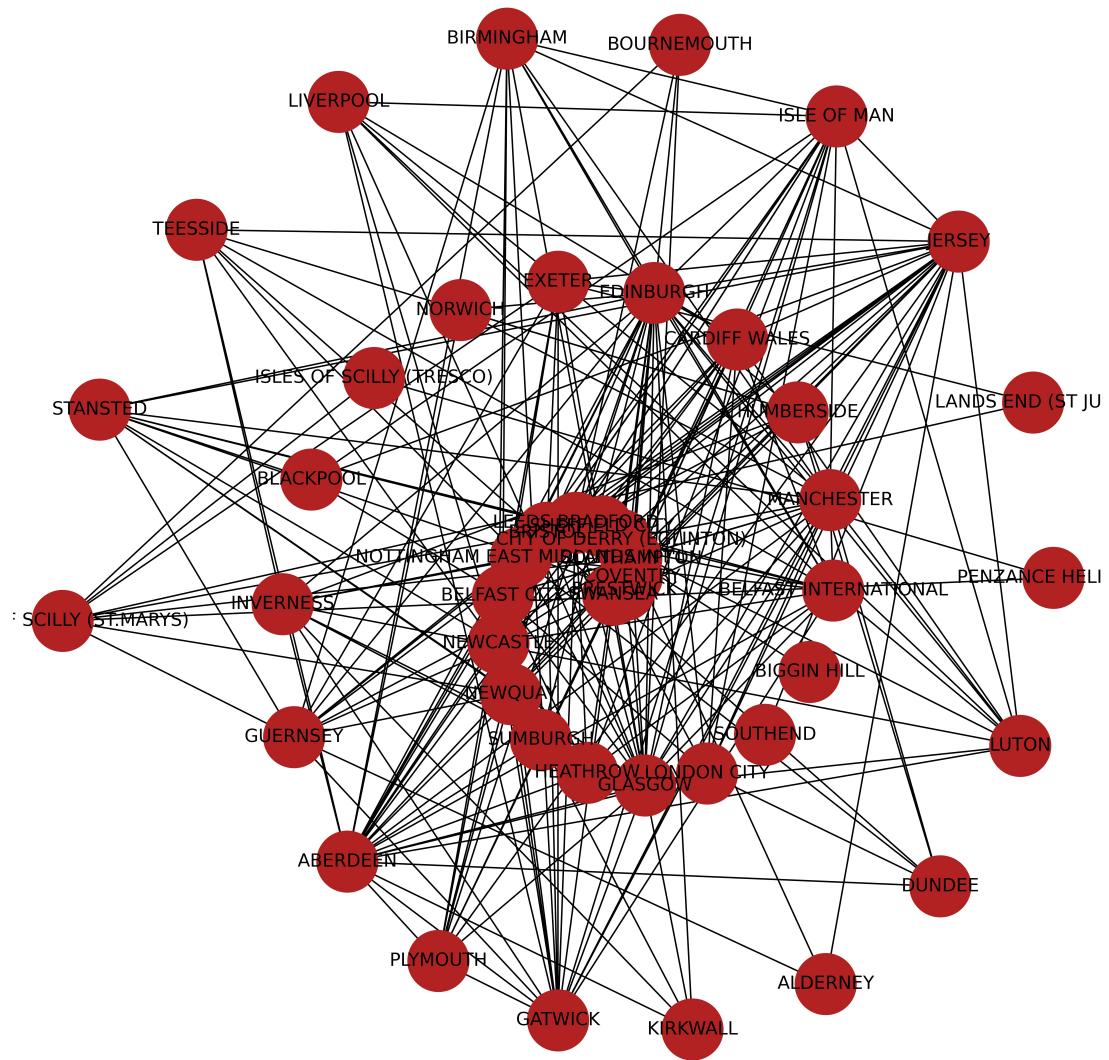


Figure 2: Domestic flights from the UK in the year of 2003.

3 Cytoscape

Cytoscape is an open source network-modelling software platform, created in 2002 at the Institute of Systems Biology in Seattle. It's mainly used for analysing and visualising networks, by creating graphs and calculating the different characteristics. One needs to load the network by giving an input consisting of the nodes and the edges [4], [5].

I was encouraged to use Cytoscape for this network visualisation project. The data set I first visualised is about protein-protein interactions. The properties of the network is the following:

- Edge Type: Co-complex association,
- Node Type: Protein Interactions,
- Avg Edges: 9,070,
- Avg Nodes: 1,622.

After importing the data set into the software, Cytoscape asks the user to choose the source- and target node, so the visualisation may begin. After selecting the nodes and edges, the graph is created. These are the steps I followed through with the protein-protein data set with the results in graph 3.

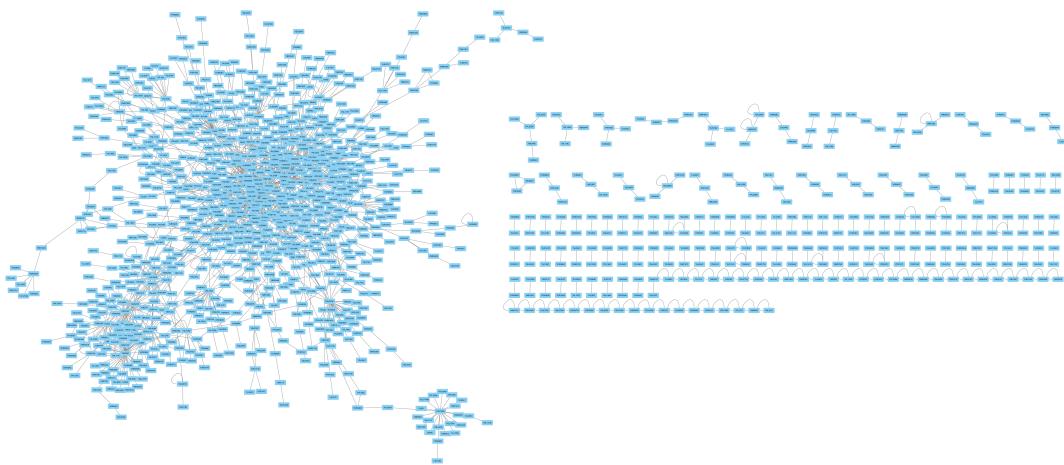


Figure 3: Protein-protein interaction graph.

As it's seen, the left part of the graph is a well connected, dense network, while the right part is consisting of proteins, which are connected to only a few other ones. This was nothing more than just loading and visualising the network. There are many more features of this software, which I'll be actively using in the rest of this network-research.

4 Theoretical Background

4.1 Degree Centrality

The investigation of centralities in networks is very important when researching connections amongst the nodes. The centrality measure indicates the importance of nodes within the graph.

Centrality measures can be crucial when for example investigating virus spreads or new friendships. It technically gives us an overview on how fast the information can spread.

One of the first centrality measures conceptually created was the degree centrality. This is a very easy measure to calculate. The degree is a basic network property, describing the connections a node has to other edges. This describes the number of link incidents upon a node. When the network is directed, the indegree and outdegree are distinguished; the indegree describes the head ends, while the outdegree describes the tail ends. The degree centrality is simply the degree of the given node. For example, a node with 10 social connections has a degree centrality of 10, while a node with only 2 edges has a degree centrality of 2 [6] [7].

Let's take a look at the following example: I chose a data set about US flights in the year of 2010 with the edge number of 5960 and node number of 500. The airports are represented by numeric codes. The degree distribution can be easily calculated by Networkx's built in functions. Since the result is given as a normalised version of the actual distribution, the values still need to be multiplied by the maximum number of edges possible. After calling the function, the results must be transformed to a specific format, so a pie chart can be created. The result can be seen in figure 4.

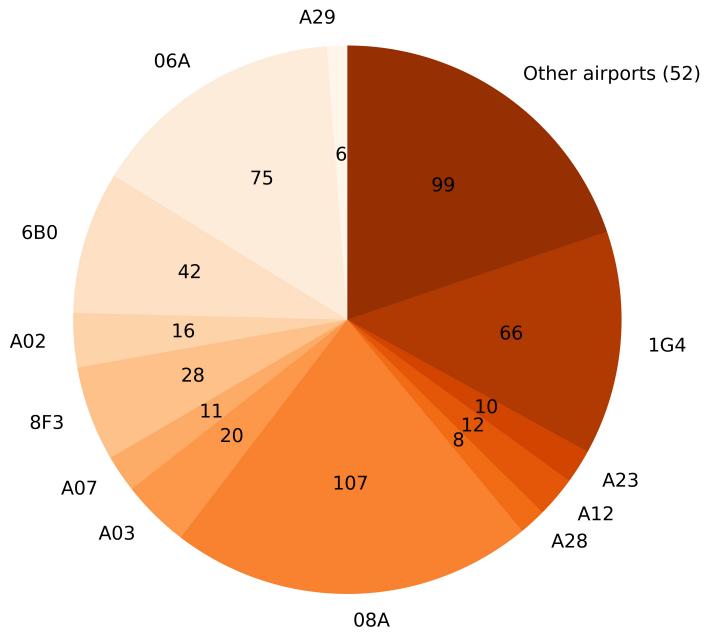


Figure 4: Degree distribution of flights in the USA in the year of 2010.

Of course, there were lots of airports which only had very small degree centralities, so they were collected in one group and are represented by the name of *Other airports* in the pie chart. As it's seen, there are three airports, which are very central. These being the 084, the 1G4 and the 06A code named airports.

4.2 Closeness Centrality

Another centrality measure to take into consideration is the closeness centrality. It indicates how close a node is to all other nodes inside of a network. This gives information about the placement of nodes, capturing the mean distance amongst all nodes in the network. When the closeness centrality has a low value, it indicates that either the network is well connected, or it is small. However, when this value is a high value, it means that the node has a less central position [8]. Let's take the following example: In figure 5 a small graph can be seen. When one wants to calculate the closeness centrality from point E , one needs to consider the average shortest path length from the node. This can be seen in the 4.2.

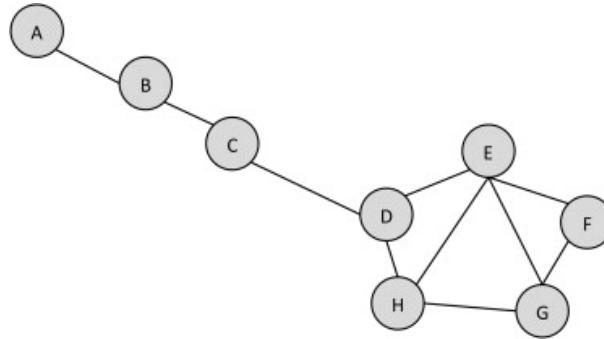


Figure 5: A small graph

Node	A	B	C	E	F	G	H
Shortest path from D	3	2	1	1	2	2	1

After calculating the path lengths, the mean value of this must be taken for the average shortest path lengths:

$$\frac{3 + 2 + 1 + 1 + 2 + 2 + 1}{7} = \frac{12}{7} = 1.71, \quad (1)$$

which concludes the calculation.

4.3 Eigenvalue Centrality

Another type of centrality measure worth mentioning is the eigenvector centrality. Let's take the following example in a social network: even though one might have not many connections, if those one has have a high degree centrality, one can be very influential in the network. The eigenvalue centrality technically describes the benefit of having a connection to a node. The more connections a node has, the more benefiting it is to connect to that node. Another social example: a person on Facebook who has 300 unpopular friends has a lower eigenvalue vector than a person with 200 very popular friends. [9]

5 Conclusion

In this part of the report, we got familiar with the Cytoscape software, which will be very useful in modelling the different networks. Moreover, the degree-, closeness- and eigenvalue centralities were defined with different network-examples.

References

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