# An HDP Model for Inducing Combinatory Categorial Grammars

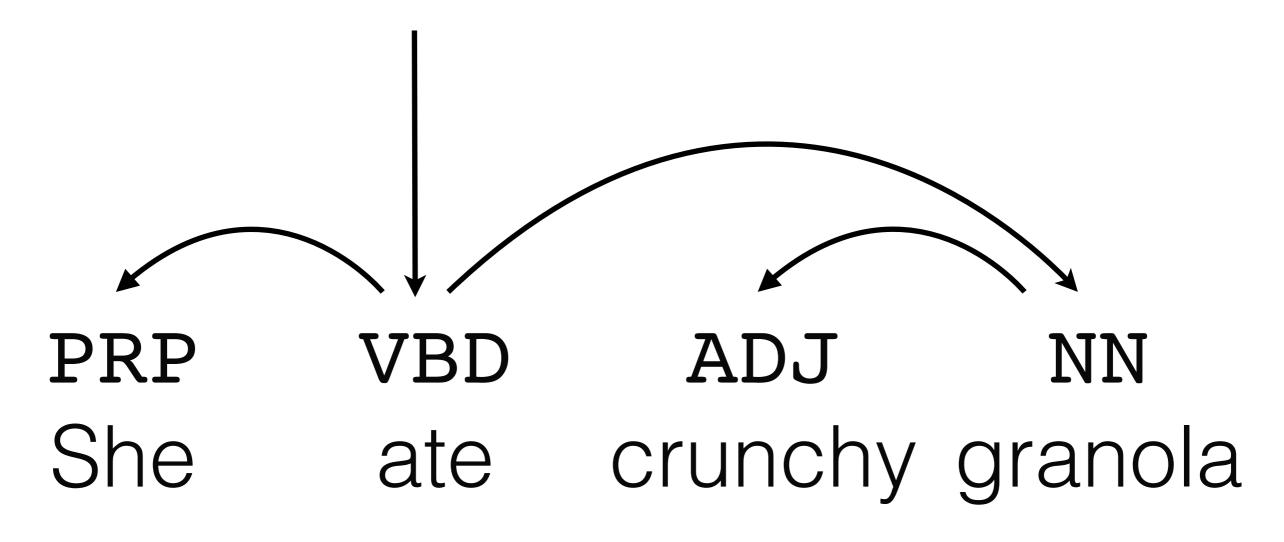
Yonatan Bisk & Julia Hockenmaier University of Illinois at Urbana-Champaign

PRP VBD ADJ NN
She ate crunchy granola

#### Dependency Grammar Induction

PRP VBD ADJ NN
She ate crunchy granola

#### Dependency Grammar Induction



#### Dependency Grammar Induction

Problem for unsupervised Dependency Grammar learner:

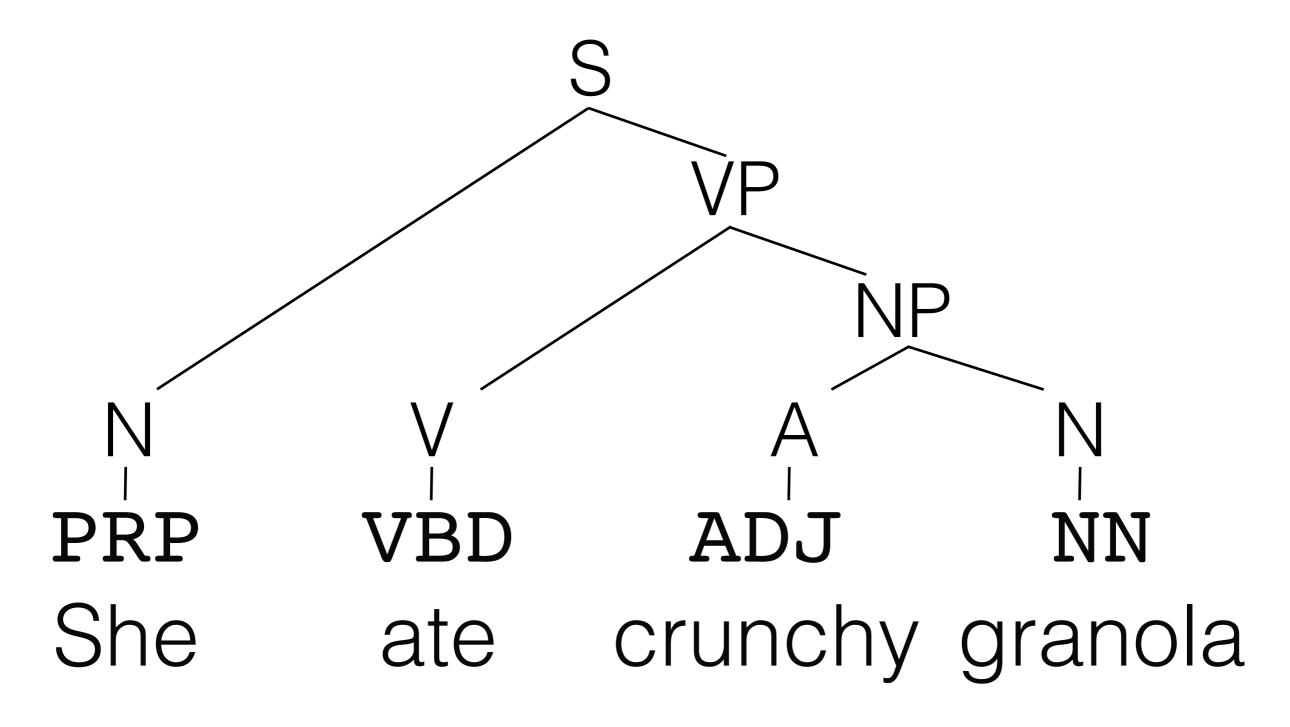
Unlabeled dependencies provide no explicit structure

nola

#### CFG Induction

PRP VBD ADJ NN
She ate crunchy granola

#### CFG Induction



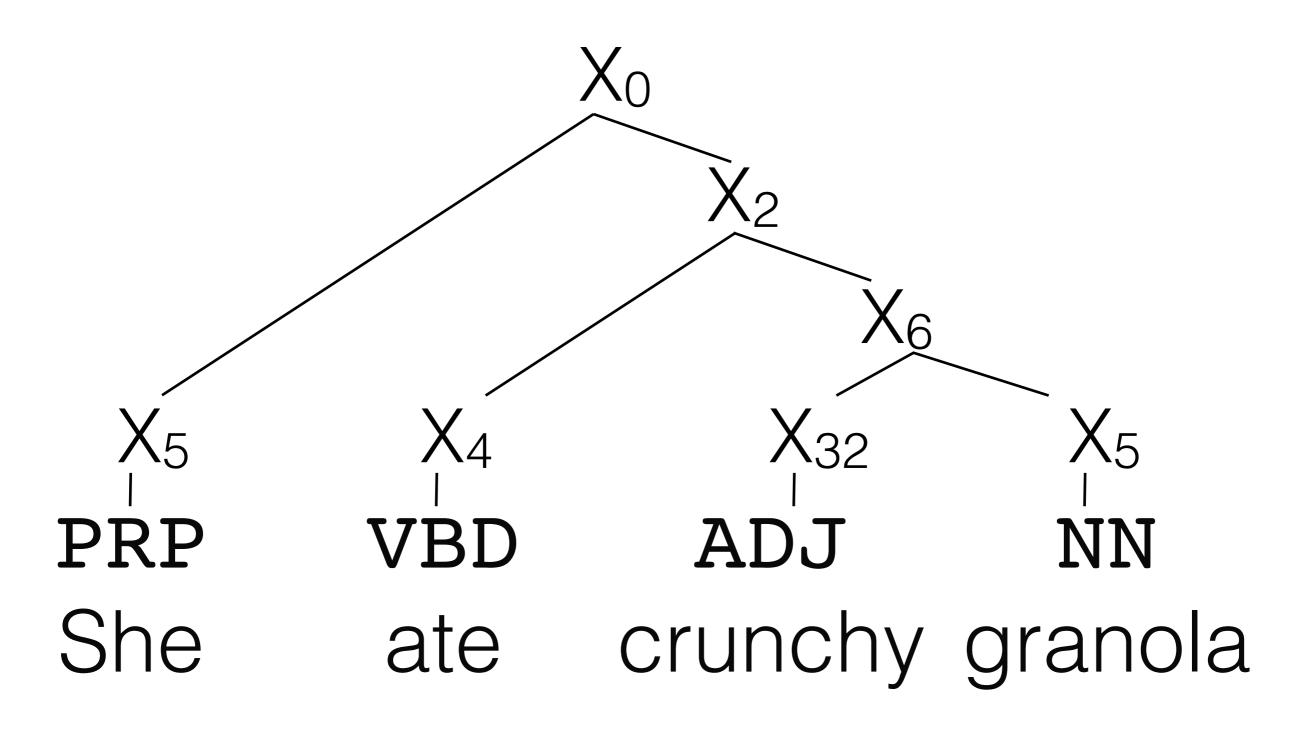
#### CFG Induction

Problem for unsupervised CFG learner:

CFG symbols and rewrite rules are arbitrary

nola

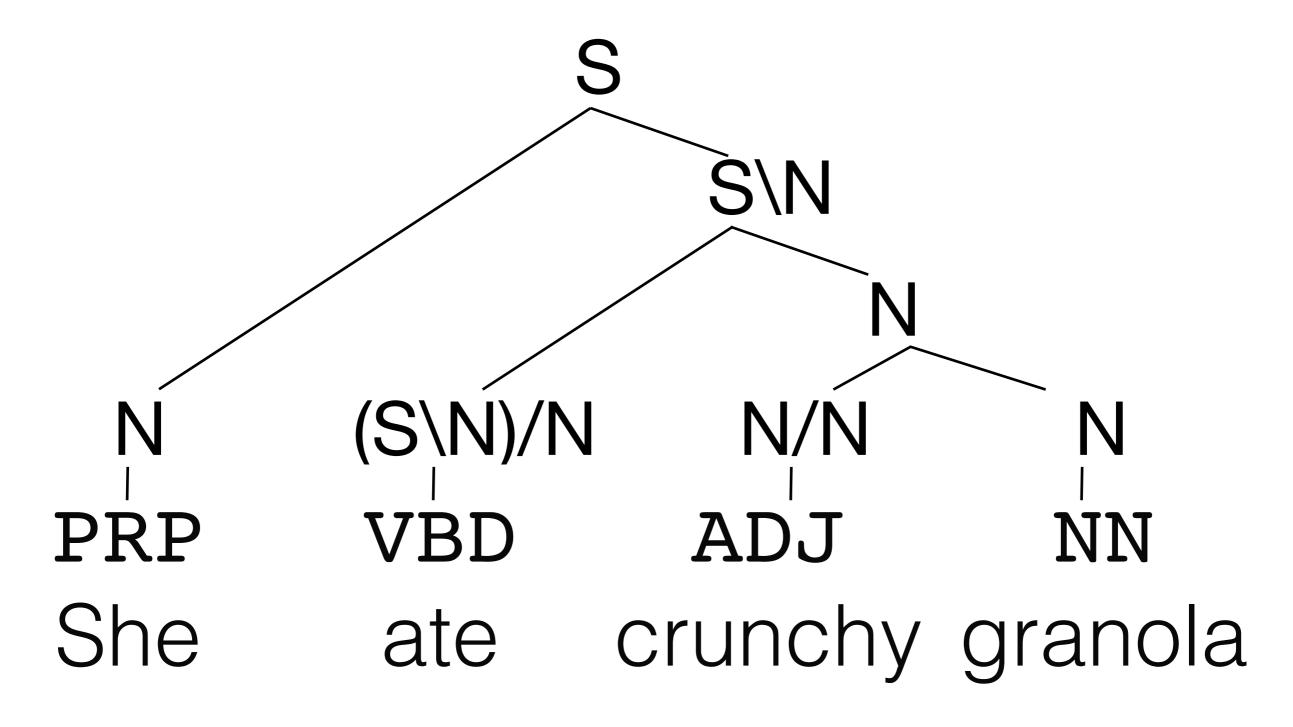
#### CFG Induction in Practice



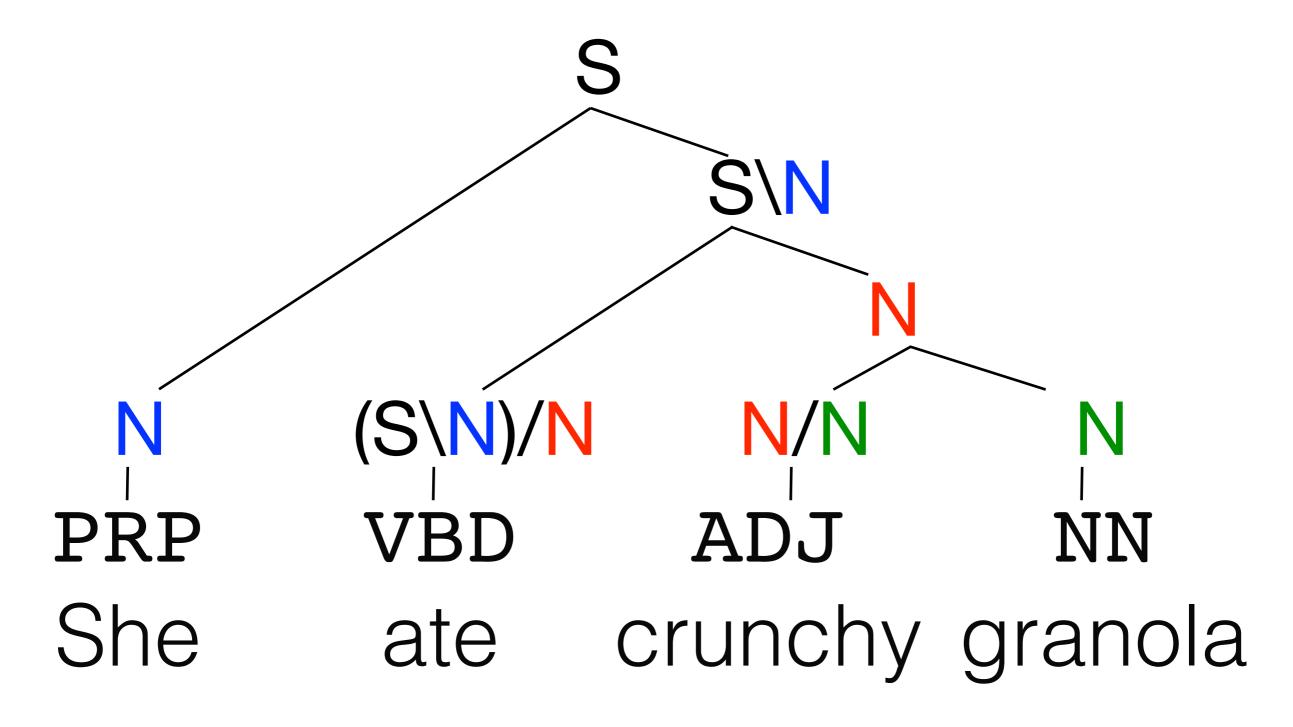
#### CFG Induction in Practice

What kind of grammatical representation is suitable for unsupervised induction?

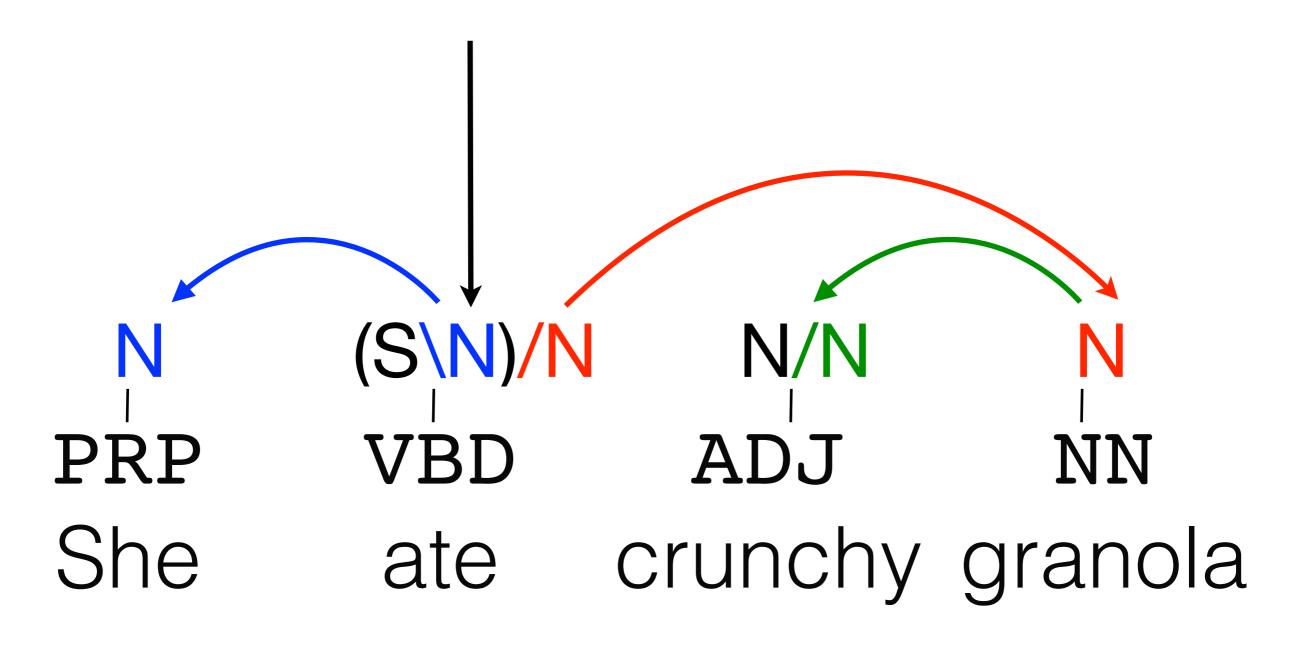
#### Categorial Grammar Induction



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Linguistically motivated symbolic representation:

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CCG captures core dependencies CCG captures basic word order

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Rules and categories are heavily constrained:

Linguistically motivated symbolic representation:

CCG captures core dependencies CCG captures basic word order

Rules and categories are heavily constrained:

CCG categories are functions CCG rules = function application & composition

## Advantages of CCG

Linguistically motivated symbolic representation:

Rules and categories are heavily constrained:

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Linguistically motivated symbolic representation:

CCG is more robust than DG on longer sentences CCG returns linguistically interpretable parses

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## Advantages of CCG

Linguistically motivated symbolic representation:

CCG is more robust than DG on longer sentences CCG returns linguistically interpretable parses

Rules and categories are heavily constrained:

CCG has a simpler probability model than CFGs CCG allows fast variational inference

## Categorial Grammar

CCG has two atomic categories:

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S, N

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All other CCG categories are functions:

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S, N

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CCG has two atomic categories:

All other CCG categories are functions:

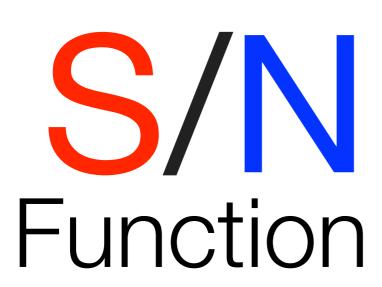
Result Argument

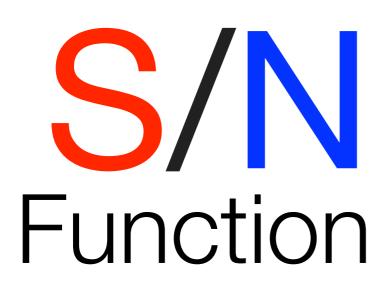
CCG has two atomic categories:

S, N

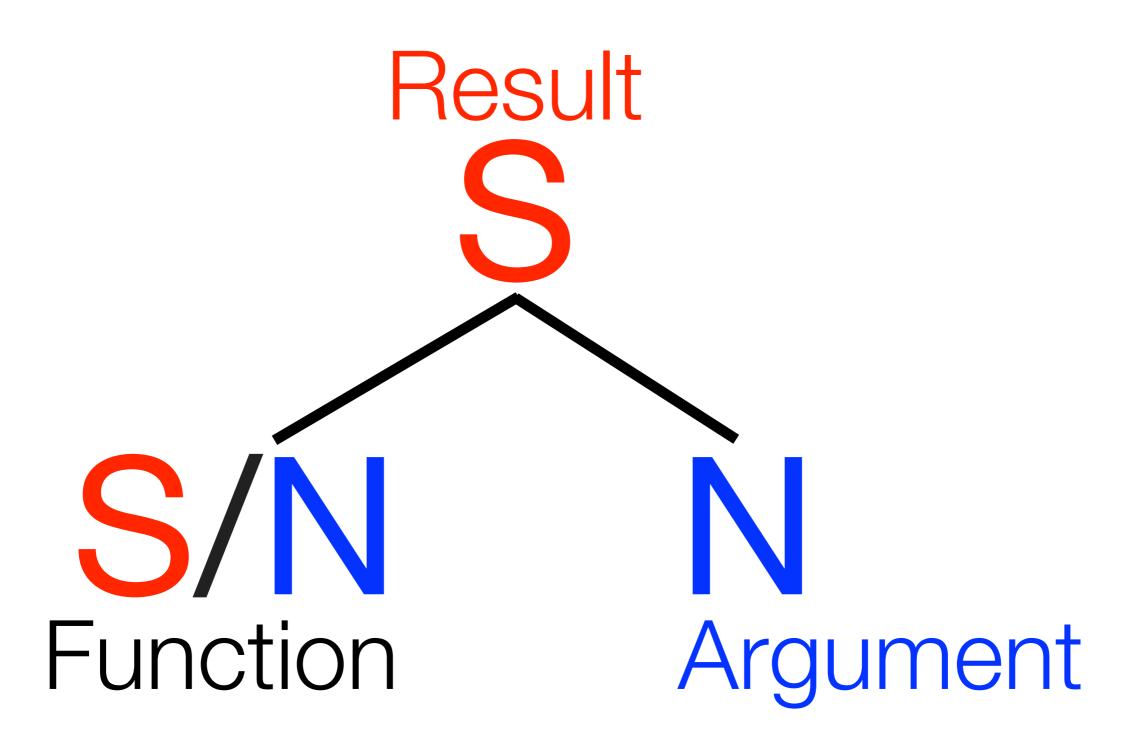
All other CCG categories are functions:

S/N Result Dir. Argument



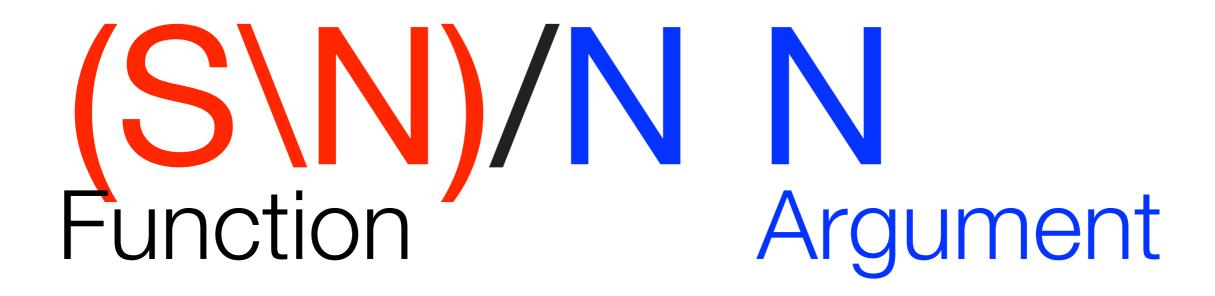




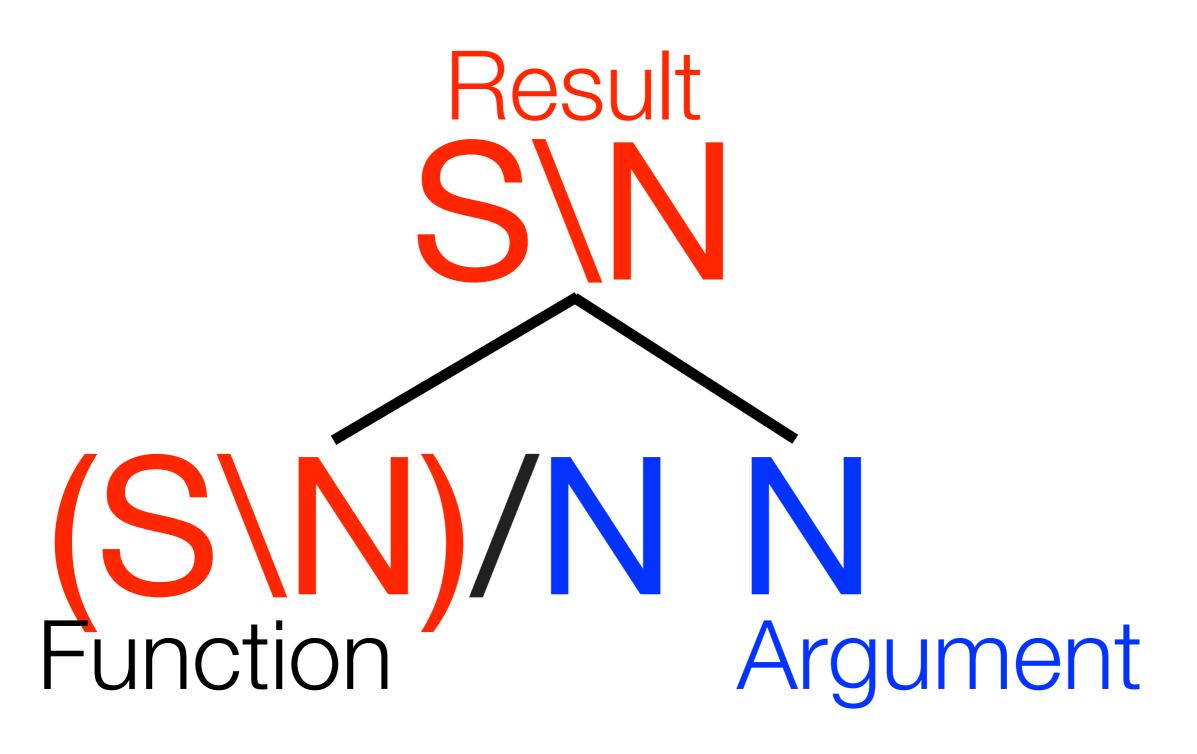




## Rules: Function application



## Rules: Function application



# Inducing CCGs

Bisk & Hockenmaier, AAAI 2012

Atomic CCG category

Part-of-speech tag class

Atomic CCG category

Part-of-speech tag class

S

Verb

Atomic CCG category

Part-of-speech tag class

S

Verb

N

Det, Noun, Pron, Num

Atomic CCG category

Part-of-speech tag class

S

Verb

N

Det, Noun, Pron, Num

conj

Conj

The man ate quickly N S

The man ate quickly N S S\N

The man ate quickly?

N S
S\N

The man ate quickly?

N S ?

S\N

The man ate quickly N S ?

The man ate quickly N/N N S?

The man ate quickly N/N N S S\N

The man ate quickly N/N N S S\S S\N

The man ate quickly N/N N S S\S S\N N\N

. . .

# An HDP Model for CCG

Nonparametric Bayesian model

#### Nonparametric Bayesian model

We do not need to fix the category inventory in advance

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#### Hierarchical model

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We do not need to fix the category inventory in advance

#### Hierarchical model

All distributions share a common base

#### Nonparametric Bayesian model

We do not need to fix the category inventory in advance

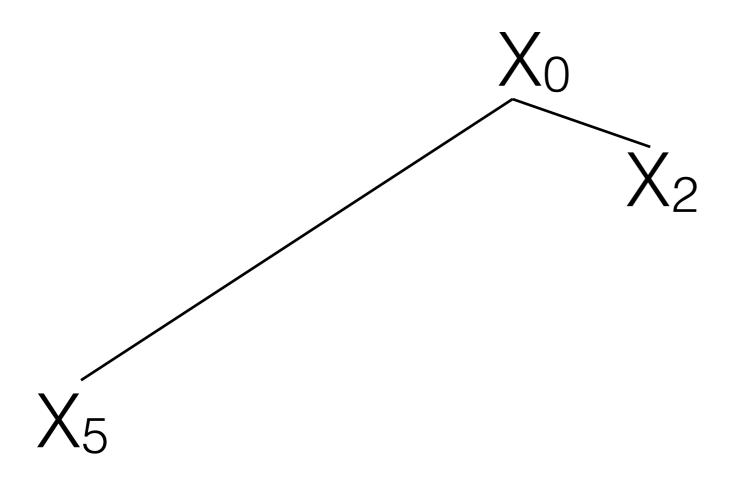
#### Hierarchical model

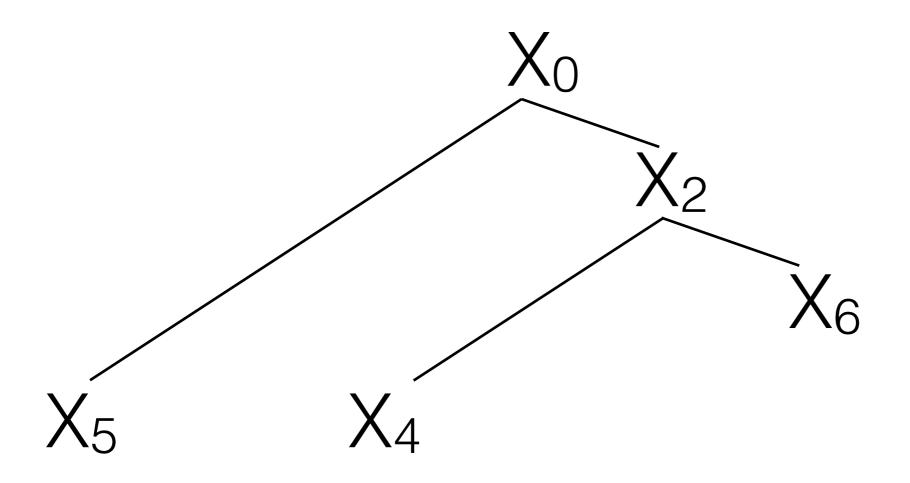
All distributions share a common base

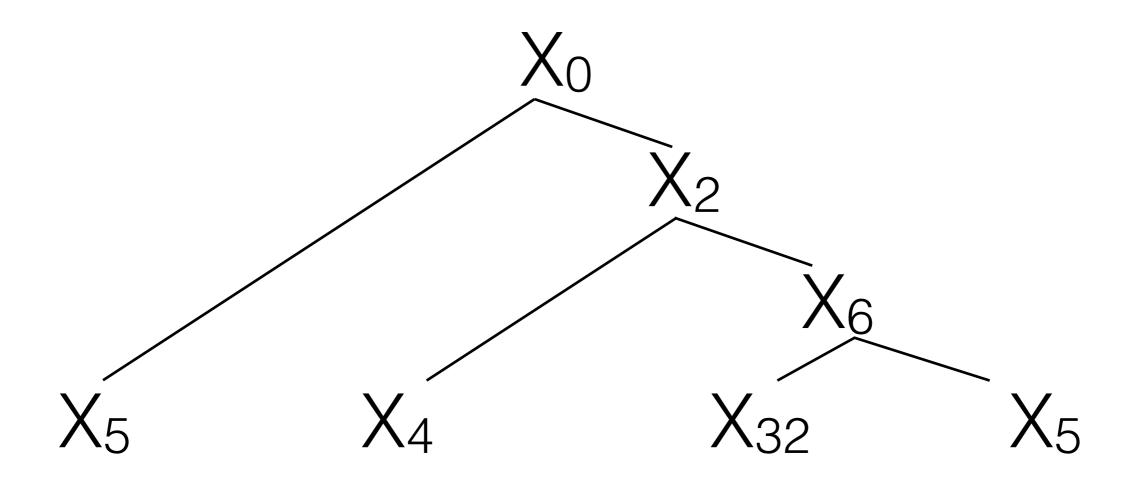
Parameter tying (smoothing)

Liang et al. 2009

 $X_0$ 





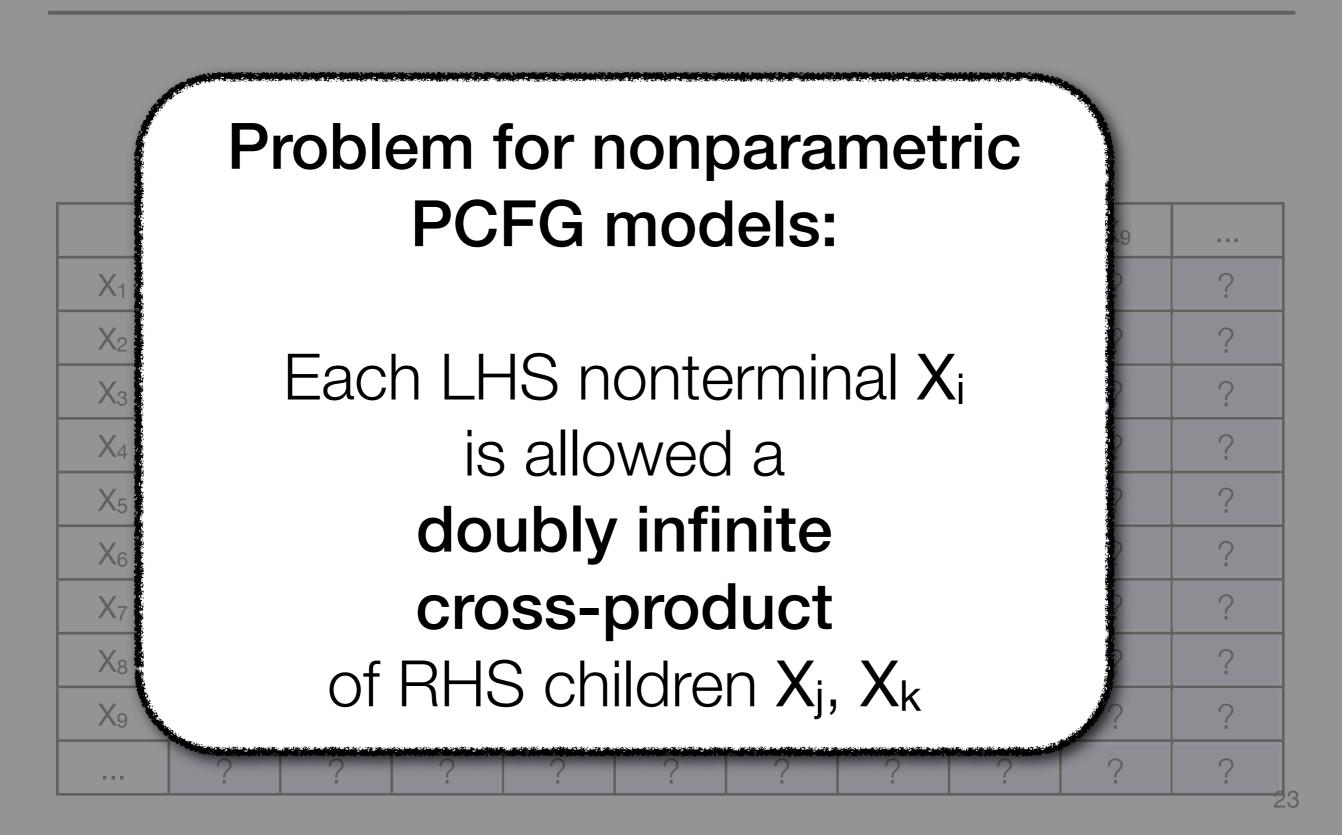


	X <sub>1</sub>	X <sub>2</sub>	<b>X</b> <sub>3</sub>	<b>X</b> <sub>4</sub>	<b>X</b> <sub>5</sub>	<b>X</b> <sub>6</sub>	<b>X</b> <sub>7</sub>	X <sub>8</sub>	<b>X</b> 9	
X <sub>1</sub>										
<b>X</b> <sub>2</sub>										
<b>X</b> <sub>3</sub>										
<b>X</b> <sub>4</sub>										
<b>X</b> <sub>5</sub>										
X <sub>6</sub>										
<b>X</b> <sub>7</sub>										
X <sub>8</sub>										
<b>X</b> 9										

	X <sub>1</sub>	X <sub>2</sub>	<b>X</b> <sub>3</sub>	$X_4$	<b>X</b> <sub>5</sub>	X <sub>6</sub>	$X_7$	X <sub>8</sub>	<b>X</b> 9	
X <sub>1</sub>	?	?-	?	?-	?-	?	?	?	?	?
$X_2$										
<b>X</b> <sub>3</sub>										
$X_4$										
<b>X</b> <sub>5</sub>										
<b>X</b> <sub>6</sub>										
<b>X</b> <sub>7</sub>										
X <sub>8</sub>										
<b>X</b> 9										

	X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	<b>X</b> <sub>4</sub>	<b>X</b> <sub>5</sub>	X <sub>6</sub>	<b>X</b> <sub>7</sub>	X <sub>8</sub>	<b>X</b> 9	
X <sub>1</sub>	?	?	?	?	?	?	?	?	?	?
$X_2$	?	?-	?	?	?	?	?	?	?	?
<b>X</b> <sub>3</sub>										
$X_4$										
<b>X</b> <sub>5</sub>										
X <sub>6</sub>										
<b>X</b> <sub>7</sub>										
X <sub>8</sub>										
<b>X</b> 9										

	X <sub>1</sub>	X <sub>2</sub>	<b>X</b> <sub>3</sub>	<b>X</b> <sub>4</sub>	<b>X</b> 5	<b>X</b> 6	$X_7$	X <sub>8</sub>	<b>X</b> 9	
X <sub>1</sub>	?	?	?	?	?	?	?	?	?	?
$\chi_2$	?	?	?	?	?	?	?	?	?	?
<b>X</b> <sub>3</sub>	?	?	?	?	?	?	?	?	?	?
$X_4$	?	?	?	?	?	?	?	?	?	?
<b>X</b> <sub>5</sub>	?	?	?	?	?	?	?	?	?	?
X <sub>6</sub>	?	?	?	?	?	?	?	?	?	?
<b>X</b> <sub>7</sub>	?	?	?	?	?	?	?	?	?	?-
X <sub>8</sub>	?	?	?	?	?	?	?	?	?	?
X <sub>9</sub>	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?



## Parameters for S\N → ....

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S	?	?	?	?	?	?	?	?	?	?
N	?	?	?	?	?	?	?	?	?	?
S/S	?	?	?	?	?	?	?	?	?	?
S\S	?	?	?	?	?	?	?	?	?	?
S/N	?	?	?	?	?	?	?	?	?	?
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N	?	?	?	?	?	?	?	?	?	?
S/S	?	?	?	?	?	?	?	?	?	?
S\S	?	?	?	?	?	?	?	?	?	?
S/N	?	?	?	?	?	?	?	?	?	?
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S	?	?	?	?	?	?	?	?	?	?
S\S	?	?	?	?	?	?	?	?	?	?
S/N	?	?	?	?	?	?	?	?	?	?
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S	?	?	?	?	?	?	?	?	?	?
S/N	?	?	?	?	?	?	?	?	?	?
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S										
S/N	?	?	?	?	?	?	?	?	?	?
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S										
S/N										
S\N	?	?	?	?	?	?	?	?	?	?
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S										
S/N										
S\N				?						
(S\N)/N	?	?	?	?	?	?	?	?	?	?
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
•••	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S										
S/N										
S\N				?						
(S\N)/N		?								
(S\N)\S	?	?	?	?	?	?	?	?	?	?
(S\N)\N	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

	S	N	S/S	S\S	S/N	S\N	(S\N)/N	(S\N)\S	(S\N)\N	
S								?		
N									?	
S/S						?				
S\S										
S/N										
S\N				?						
(S\N)/N		?								
(S\N)\S										
(S\N)\N										
	?	?	?	?	?	?	?	?	?	?

Parent Combinator Left Right

Parent	Combinato	Left	Right
(S\N)/N	$>B_0$	((S\N)/N)/Y	Y

Parent	Combinato	r Left	Right
(S\N)/N	>B <sub>0</sub>	((S\N)/N)/Y	Y
(S\N)/N	>B <sub>1</sub>	(S\N)/Y	Y/N

Parent	Combinato	r Left	Right
(S\N)/N	>B <sub>0</sub>	((S\N)/N)/Y	Y
(S\N)/N	>B <sub>1</sub>	(S\N)/Y	Y/N
(S\N)/N	$>B_2$	S\Y	( <b>Y</b> \N)/N

Parent	Combinato	r Left	Right
(S\N)/N	>B <sub>0</sub>	((S\N)/N)/Y	Y
(S\N)/N	>B <sub>1</sub>	(S\N)/Y	Y/N
(S\N)/N	$>B_2$	S\Y	(Y\N)/N
(S\N)/N	<b<sub>0</b<sub>	Y	((S\N)/N)\Y

Parent	Combinator	Left	Right
(S\N)/N	>B <sub>0</sub>	((S\N)/N)/Y	Y
(S\N)/N	>B <sub>1</sub>	(S\N)/Y	Y/N
(S\N)/N	$>B_2$	S\Y	(Y\N)/N
(S\N)/N	<b<sub>0</b<sub>	Y	((S\N)/N)\Y
(S\N)/N	<b<sub>1</b<sub>	Y/N	(S\N)\Y

Parent	Combinator	Left	Right
(S\N)/N	>B <sub>0</sub>	((S\N)/N)/Y	Y
(SN)/N	>B <sub>1</sub>	(S\N)/Y	Y/N
(S\N)/N	>B <sub>2</sub>	S\Y	( <u>Y</u> \N)/N
(S\N)/N	$<$ B $_0$	Y	((S\N)/N)\Y
(S\N)/N	<b<sub>1</b<sub>	Y/N	(S\N)\Y
(S\N)/N	<B <sub>2</sub>	(Y\N)/N	S\Y

Parent
(S\N)/N
(S\N)/N
(S\N)/N
(S\N)/N
(S\N)/N
(S\N)/N

Parent	Y
(S\N)/N	S

Parent	Y	Combinator
(S\N)/N	S	>B <sub>0</sub>
(S\N)/N	S	>B <sub>1</sub>
(S\N)/N	S	>B <sub>2</sub>
(S\N)/N	S	$<$ B $_0$
(S\N)/N	S	<b<sub>1</b<sub>
(S\N)/N	S	<B <sub>2</sub>

Parent	Y	Combinator	Left	Right
(S\N)/N	S	>B <sub>0</sub>	((S\N)/N)/S	S
(S\N)/N	S	>B <sub>1</sub>	(S\N)/S	S/N
(S\N)/N	S	>B <sub>2</sub>	S\S	(S\N)/N
(S\N)/N	S	$<$ B $_0$	S	((S\N)/N)\S
$(S\N)/N$	S	<b<sub>1</b<sub>	S/N	(S\N)\S
(S\N)/N	S	<B <sub>2</sub>	(S\N)/N	S\S

CCG rules are heavily constrained:

For a **given parent** category, the **Y category** and **combinator** determine both children

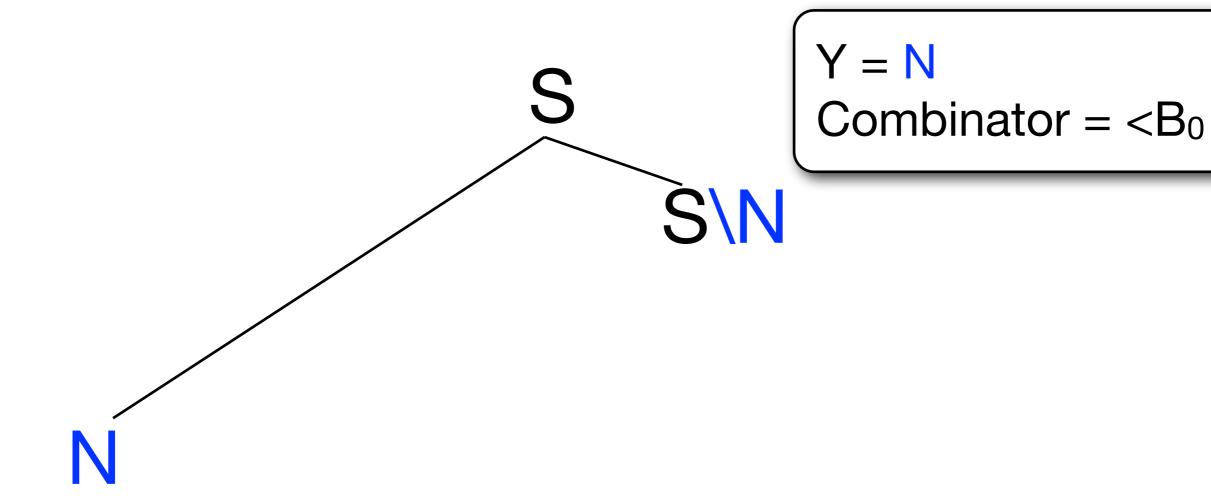
Right S/N S/N S/N)/S S/S

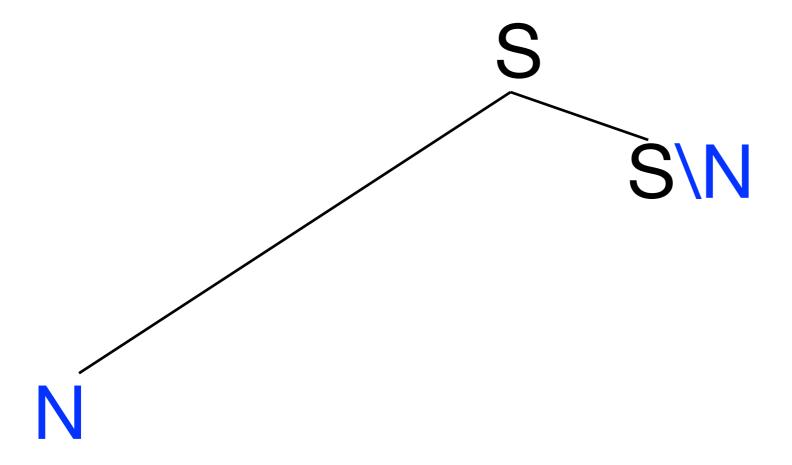
(S

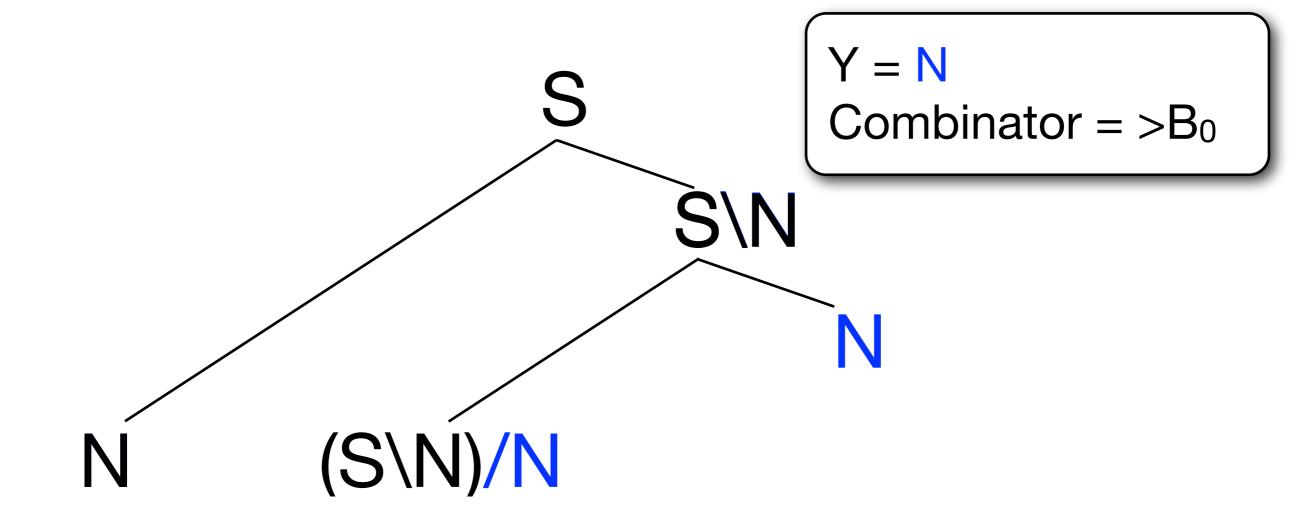
S

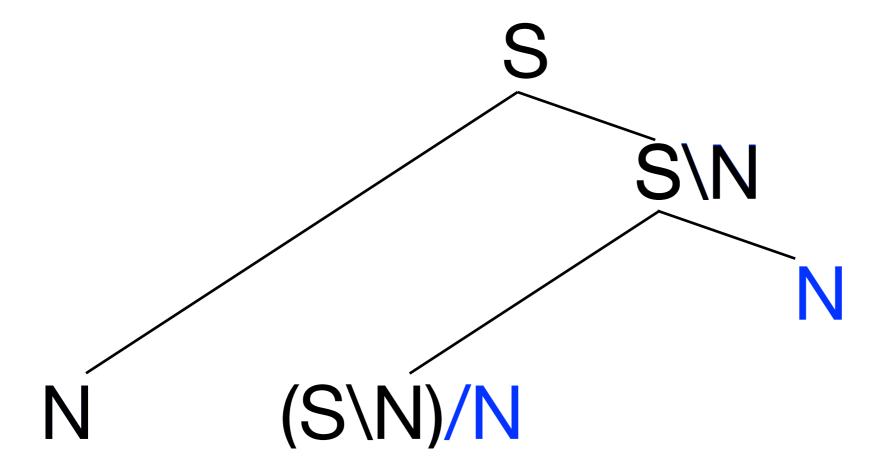
S

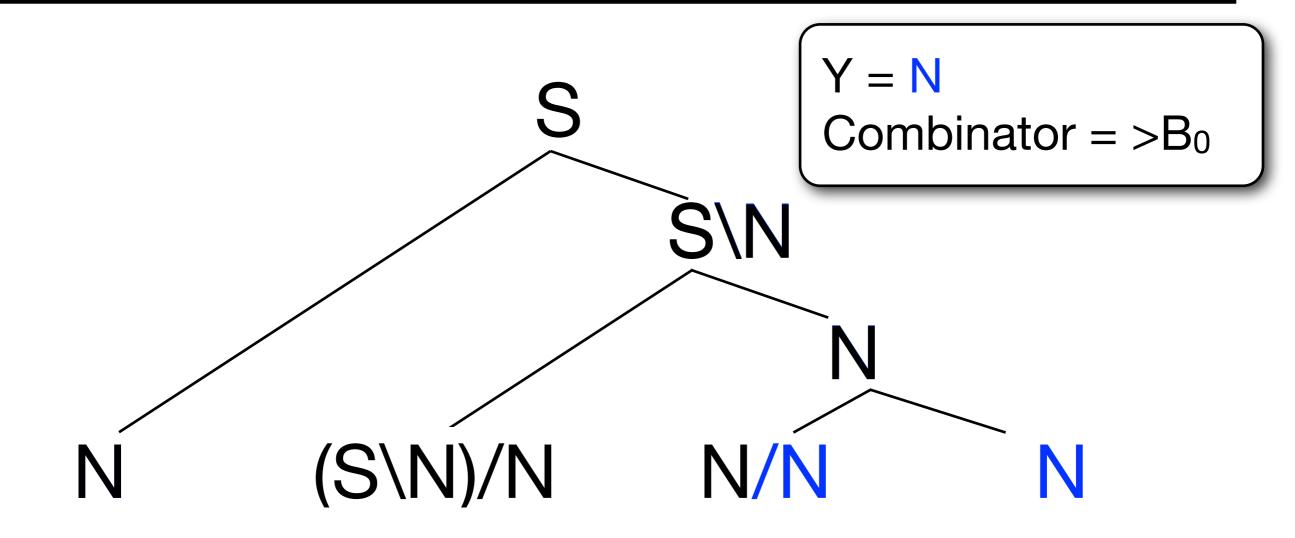
$$\begin{aligned} Y &= N \\ Combinator &= < B_0 \end{aligned}$$

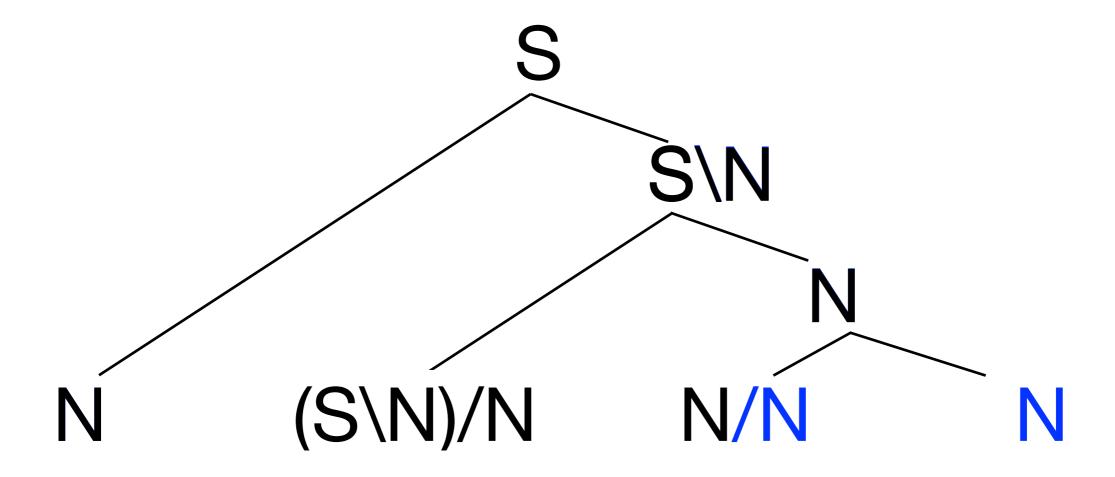












CFG: doubly infinite  $P(X_i \rightarrow X_j X_k \mid X_i)$ 

#### CFG: doubly infinite $P(X_i \rightarrow X_j X_k \mid X_i)$

	X1	X2	ХЗ	X4	X5	X6	X7	X8	X9	
X1	?	?	?	?	?	?	?	?	?	?
X2	?	?	?	?	?	?	?	?	?	?
ХЗ	?	?	?	?	?	?	?	?	?	?
X4	?	?	?	?	?	?	?	?	?	?
X5	?	?	?	?	?	?	?	?	?	?
X6	?	?	?	?	?	?	?	?	?	?
X7	?	?	?	?	?	?	?	?	?	?
X8	?	?	?	?	?	?	?	?	?	?
X9	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

#### CFG: doubly infinite $P(X_i \rightarrow X_j X_k \mid X_i)$

	X1	X2	ХЗ	X4	X5	X6	X7	X8	X9	
X1	?	?	?	?	?	?	?	?	?	?
X2	?	?	?	?	?	?	?	?	?	?
Х3	?	?	?	?	?	?	?	?	?	?
X4	?	?	?	?	?	?	?	?	?	?
X5	?	?	?	?	?	?	?	?	?	?
X6	?	?	?	?	?	?	?	?	?	?
X7	?	?	?	?	?	?	?	?	?	?
X8	?	?	?	?	?	?	?	?	?	?
Х9	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

CCG: infinite P(Y | Xi) and finite P(c | Y, Xi)

#### CFG: doubly infinite $P(X_i \rightarrow X_j X_k \mid X_i)$

	X1	X2	ХЗ	X4	X5	X6	X7	X8	X9	
X1	?	?	?	?	?	?	?	?	?	?
X2	?	?	?	?	?	?	?	?	?	?
Х3	?	?	?	?	?	?	?	?	?	?
X4	?	?	?	?	?	?	?	?	?	?
X5	?	?	?	?	?	?	?	?	?	?
X6	?	?	?	?	?	?	?	?	?	?
X7	?	?	?	?	?	?	?	?	?	?
X8	?	?	?	?	?	?	?	?	?	?
X9	?	?	?	?	?	?	?	?	?	?
	?	?	?	?	?	?	?	?	?	?

#### CCG: infinite P(Y | Xi) and finite P(c | Y, Xi)



### HDP-CFG vs HDP-CCG

The **HDP-CFG** base measure requires  $\beta\beta^T$ 

The **HDP-CCG** base measure is the standard  $\beta \sim \text{GEM}(\alpha)$  (akin to e.g. HDP-HMMs)

Computation parallels Inside-Outside:

### Computation parallels Inside-Outside:

$$\mathbf{W}_{\mathbf{P}}(Y) = \Psi(C(P, Y) + \alpha^{P}\beta_{Y}) - \Psi(C(P, *) + \alpha^{P})$$

### Computation parallels Inside-Outside:

$$W_{P}(Y) = \Psi(C(P, Y) + \alpha^{P}\beta_{Y}) - \Psi(C(P, *) + \alpha^{P})$$

Trivially parallelizeable; efficient

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- Experiments in paper:
  - 1 min 4 hrs

# Results

Trained and tested on

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 $\leq 10 \leq 20$ 

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NAACL WILS Shared Task 2012

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Average ≤10 accuracy on 10 languages

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#### NAACL WILS Shared Task 2012

Dependencies		CCG
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#### NAACL WILS Shared Task 2012

Depend	dencies	CCG	CCG: new	model
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55.2	62.3	54.2	50.9	64.5

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English

Adj Obj

Big N/N Ball N

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Adj Obj

Big N/N Ball N

**Arabic** 

كبيرة كرة

N N\N (ball) (big)

Obj Adj

### Induced Lexicons: Verbs

English
The man wrote a letter
N (S\N)/N

### Induced Lexicons: Verbs

S V O

English
The man

wrote (S\N)/N

a letter N

Child Directed Speech



write

S/N

a letter

N

### Induced Lexicons: Verbs

English
The man wrote a letter
N (S\N)/N N

Child Directed Speech

write a letter
S/N N



### Induced Lexicons: Adpositions

English

ran
on
beach
(S\N)/N

(S\S)/N

### Induced Lexicons: Adpositions

English ADP beach ran on (S\N)/N (S\S)/N Japanese ADP 浜 を 走った (S/S)\N  $(S\N)/N$ N (beach) (on) (ran)

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Thank you!