Типовик по линейной алгебре модуль 1: Задания 1 и 2

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Содержание

1	Задание 1			
		Способ №1	6	
		Способ №2	4	
	1.3	Способ №3	į	
2	Зало	иние 2		

1. Задание 1

1.1. Способ №1

$$\begin{vmatrix} 3 & 2 & 2 & 8 \\ 1 & 5 & 4 & -9 \\ 2 & 4 & 6 & -9 \\ 1 & 2 & 3 & -4 \end{vmatrix} = 1 \cdot (-1)^{2+1} \cdot \begin{vmatrix} 2 & 2 & 8 \\ 4 & 6 & -9 \\ 2 & 3 & -4 \end{vmatrix} + 5 \cdot (-1)^{2+2} \cdot \begin{vmatrix} 3 & 2 & 8 \\ 2 & 6 & -9 \\ 1 & 3 & -4 \end{vmatrix} +$$

$$4 \cdot (-1)^{2+3} \cdot \begin{vmatrix} 3 & 2 & 8 \\ 2 & 4 & -9 \\ 1 & 2 & -4 \end{vmatrix} + -9 \cdot (-1)^{2+4} \cdot \begin{vmatrix} 3 & 2 & 2 \\ 2 & 4 & 6 \\ 1 & 2 & 3 \end{vmatrix} =$$

$$-1 \begin{vmatrix} 2 & 2 & 8 \\ 4 & 6 & -9 \\ 2 & 3 & -4 \end{vmatrix} + 5 \begin{vmatrix} 3 & 2 & 8 \\ 2 & 6 & -9 \\ 1 & 3 & -4 \end{vmatrix} - 4 \begin{vmatrix} 3 & 2 & 8 \\ 2 & 4 & -9 \\ 1 & 2 & -4 \end{vmatrix} - 9 \begin{vmatrix} 3 & 2 & 2 \\ 2 & 4 & 6 \\ 1 & 2 & 3 \end{vmatrix} =$$

$$-1 \left(2 \times (-1)^{1+1} \times \begin{vmatrix} 6 & -9 \\ 3 & -4 \end{vmatrix} + 2 \times (-1)^{1+2} \times \begin{vmatrix} 4 & -9 \\ 2 & -4 \end{vmatrix} + 8 \times (-1)^{1+3} \times \begin{vmatrix} 4 & 6 \\ 2 & 3 \end{vmatrix} \right)$$

$$+5 \left(3 \times (-1)^{1+1} \times \begin{vmatrix} 6 & -9 \\ 3 & -4 \end{vmatrix} + 2 \times (-1)^{1+2} \times \begin{vmatrix} 2 & -9 \\ 1 & -4 \end{vmatrix} + 8 \times (-1)^{1+3} \times \begin{vmatrix} 2 & 6 \\ 1 & 3 \end{vmatrix} \right)$$

$$-4 \left(3 \times (-1)^{1+1} \times \begin{vmatrix} 4 & -9 \\ 2 & -4 \end{vmatrix} + 2 \times (-1)^{1+2} \times \begin{vmatrix} 2 & -9 \\ 1 & -4 \end{vmatrix} + 8 \times (-1)^{1+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} \right)$$

$$-9 \left(3 \times (-1)^{1+1} \times \begin{vmatrix} 4 & 6 \\ 2 & 3 \end{vmatrix} + 2 \times (-1)^{1+2} \times \begin{vmatrix} 2 & 6 \\ 1 & 3 \end{vmatrix} + 2 \times (-1)^{1+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} \right) =$$

$$-1 (2(-24 + 27) - 2(-16 + 18) + 8(12 - 12)) + 5 (+3(-24 + 27) - 2(-8 + 9) + 8(6 - 6))$$

$$-4 (+3(-16 + 18) - 2(-8 + 9) + 8(4 - 4)) - 9 (+3(12 - 12) - 2(6 - 6) + 2(4 - 4)) = 17$$

$$(1)$$

1.2. Способ №2

$$\begin{vmatrix} 3 & 2 & 2 & 8 \\ 1 & 5 & 4 & -9 \\ 2 & 4 & 6 & -9 \\ 1 & 2 & 3 & -4 \end{vmatrix} = 2 \times (-1)^{3+1} \times \begin{vmatrix} 1 & 5 & -9 \\ 2 & 4 & -9 \\ 1 & 2 & -4 \end{vmatrix} + 4 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 2 & 8 \\ 2 & 4 & -9 \\ 1 & 2 & -4 \end{vmatrix} + 4 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 2 & 8 \\ 2 & 4 & -9 \\ 1 & 2 & -4 \end{vmatrix} + 4 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 2 & 8 \\ 1 & 5 & -9 \\ 2 & 4 & -9 \end{vmatrix} = 2 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 & 8 \\ 1 & 5 & -9 \\ 1 & 2 & -4 \end{vmatrix} + 3 \times (-1)^{3+4} \times \begin{vmatrix} 3 & 2 & 8 \\ 1 & 5 & -9 \\ 2 & 4 & -9 \end{vmatrix} = 2 \times (-1)^{1+1} \times \begin{vmatrix} 4 & -9 \\ 2 & -4 \end{vmatrix} + 5 \times (-1)^{1+2} \times \begin{vmatrix} 2 & -9 \\ 1 & -4 \end{vmatrix} + (-9) \times (-1)^{1+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 2 \times (-1)^{1+2} \times \begin{vmatrix} 2 & -9 \\ 1 & -4 \end{vmatrix} + 8 \times (-1)^{1+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 2 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 8 \\ 1 & -9 \end{vmatrix} + 4 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 2 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 8 \\ 1 & -9 \end{vmatrix} + 4 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 2 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 8 \\ 1 & -9 \end{vmatrix} + 4 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 2 \times (-1)^{3+2} \times \begin{vmatrix} 3 & 8 \\ 1 & -9 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 3 & 2 \\ 1 & 5 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3} \times \begin{vmatrix} 2 & 4 \\ 1 & 2 \end{vmatrix} + 3 \times (-1)^{3+3}$$

1.3. Способ №3

$$\begin{vmatrix} 3 & 2 & 2 & 8 \\ 1 & 5 & 4 & -9 \\ 2 & 4 & 6 & -9 \\ 1 & 2 & 3 & -4 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 3 & 2 & 2 & 8 \\ 2 & 4 & 6 & -9 \\ 1 & 2 & 3 & -4 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -6 & -2 & 9 \\ 0 & -3 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & 0 & 0 & -1 \\ 0 & -3 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \\ 0 & 0 & 0 & -1 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -10 & 35 \\ 0 & -3 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 & 5 & 4 & -9 \\ 0 & -13 & -1 & 5 \end{vmatrix} = - \begin{vmatrix} 1 &$$

2. Задание 2

$$\begin{cases} x + 4y + 3z = 1 \\ 2x + 3y + 2z = -2 \\ 3x + y + z = -3 \end{cases}$$
 (4)

$$\Delta = \begin{vmatrix} 1 & 4 & 3 \\ 2 & 3 & 2 \\ 3 & 1 & 1 \end{vmatrix} = -4 \tag{5}$$

$$\Delta_x = \begin{vmatrix} 1 & 4 & 3 \\ -2 & 3 & 2 \\ -3 & 1 & 1 \end{vmatrix} = 6 \tag{6}$$

$$\Delta_y = \begin{vmatrix} 1 & 1 & 3 \\ 2 & -2 & 2 \\ 3 & -3 & 1 \end{vmatrix} = 8 \tag{7}$$

$$\Delta_z = \begin{vmatrix} 1 & 4 & 1 \\ 2 & 3 & -2 \\ 3 & 1 & -3 \end{vmatrix} = -14 \tag{8}$$

$$x = \frac{\Delta_x}{\Delta} = -1.5 \tag{9}$$

$$x = \frac{\Delta_x}{\Delta} = -1.5$$
 (9)

$$y = \frac{\Delta_y}{\Delta} = -2$$
 (10)

$$z = \frac{\Delta_z}{\Delta} = 3.5$$
 (11)

$$z = \frac{\Delta_z}{\Lambda} = 3.5 \tag{11}$$

(12)

Проверим:

$$\begin{cases}
-1.5 + 4 \cdot -2 + 3 \cdot 3.5 == 1 \\
2 \cdot -1.5 + 3 \cdot -2 + 2 \cdot 3.5 == -2 \\
3 \cdot -1.5 + -2 + 3.5 == -3
\end{cases}$$
(13)