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Comparative Analysis of Nearest Neighbor Query Processing Techniques

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Abstract

The goal of Nearest Neighbour (NN) search is to find the objects in a dataset A that are closest to a query point q. Existing algorithms presume that the dataset is indexed by an R-tree and searching a query point q in a large volume of a dataset, is a tedious task that effects the quality and usefulness of the NNQ processing algorithms which determined by the time as well as space complexity. The simplest solution to the NNS problem is to compute the distance from the query point to every other point in the database. However, due to these complexities issue, the various research techniques have been proposed. It is a technique which has applications in various fields such as pattern recognition, moving object recognition etc. In this paper, a comprehensive analysis on data structures, processing techniques and variety of algorithms in this field is done along with different way to categorize the NNS techniques is presented. This different category such as weighted, additive, reductional, continuous, reverse, principal axis, which are analyzed and compared in this paper. Complexity of different data structures used in different NNS algorithms is also discussed.

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1. Introduction

Originally nearest neighbour decision rule and pattern classification was proposed by P. E. Hart and T. M. Cover in 1966 – 67, and now it is very popular in application and research field. Its simplicity is one of the main reason of its popularity and efficient in programming. Earlier using the nearest neighbour rule, the searching result needs high memory and computation requirements. But after several year of research, it's already modify a lot and used in different field of high computations field such as robotics, industrial management, telematics system, etc., along with advantage over high volume dataset. There are number of research paper where the NN rule is widely discussed and used such as pattern recognition, application for predicting economic events, vehicle telematics, and robotics.

The query processing technique is applied generally small dataset, but when the dataset is large (in high volume), high dimensions and uncertain, then the nearest neighbour decision rule come into vital role. There is numerous numbers of k-nearest neighbour algorithms available and recent development is lead to it in fast processing.

A NNS problem can be defined in two ways, metric and non-metric. The focus of this research paper is on the problems defined on a metric space. The distance formula in non-metric space is converted to a distance in metric space. Different metric distance functions can be defined on the searching space. Table 1 shows a list of formulas along with space that have presented different categorizing and analyzed of NNS.

Table 1. Distance Equations

Distance Name	Space	Equation
Manhattan	Vector	$\sum x_i - y_i $
Euclidean	Vector	$\sqrt{\sum x_i - y_i ^2}$
Minkowski	Vector	$\sqrt[p]{\sum x_i - y_i ^p}$
Chebychev	Vector	$\max x_i - y_i $
Canberra	Vector	$\sum_{i=1}^n (x_i - y_i / (x_i + y_i))$
Hamming	String	$\sum x_i \oplus y_i$
Edit	String	$ A + B - 2 \times LCS(A,B) $
Jaccard	Set	$1 - (A \cap B / A \cup B)$

2. NNS Data Structures

One of the main parts in NNS is data structure which used in each technique. Now there are different data structures that can use for solving this problem. By paying attention to different applications and data, each of these techniques has to use structure for maintaining, indexing points and searching. Some of these structures are techniques for NNS such as LSH, Ball-Tree, kd-Tree and etc.[2]; and the other are infrastructures in some techniques such as R-tree, R* Tree, B-Tree, X-Tree and etc. A brief overview about some of these data structures is presented as follow.

LSH (Locality Sensitive Hashing) is one of the best algorithms that can be used as a technique. The LSH algorithm is probably the one that has received most attention in practical context. Its main idea is to hash the data points using several hash function so as to ensure that, for each function the probability of collision is much higher for points which are close to each other than for those which are far apart.

In LSH algorithm at first preprocessing should have been done. In preprocessing all data points hash by all functions and determine their buckets. In searching step query point q is hashed and after determining buckets all of its data points retrieve as the answer [2,5].

One of the other structures that use as a technique is kd-Tree that creates for a set with n points in d-dimensional space recursive. kd-Tree and its variance remain probably the most popular data structure used for searching in multidimensional space at least in main memory. In this structure, in each step the existence space is divided by paying attention to points dimensions.

This division is continued recursively until that in each zone just a point is remained. Finally the data structure that produced is a binary tree with n level and depth. For searching nearest neighbor a circle is drawn with query point q as center and $|p - q|$ as radius that p is in query point q zone. With assisting of points that are interfered with the circle, the radius and p are updated. This operation is continued until up to dating is possible and finally NN is reported [6-9].

Table 2. Computational Complexity of Data Structures

Data Structure Name	Idea	Search Complexity (Query Time)	Search Complexity (Space)
LSH	Mapping data point by using hash function-search based on hash function.	$O(n)$	$O(1)$
KD-Tree	Making binary tree recursively based on the mean of points- search based on nearest query region	$O(n + k)$	$O(1)$
Quad-Tree	Making Quad-tree recursively based on same zones (or based on the place of points)-search based on nearest query region	$O(n)$	$O(1)$
Oct-Tree	Making Oct-tree recursively based on axis-search based on nearest query region	$O(n)$	$O(1)$
Ball-Tree	Making binary tree recursively based on axis-search based on data pruning and the distance from the axis.	$O(n)$	$O(1)$
R-Tree	Making R-tree into down to up based on MBR-search based on data pruning and MBR	$O(n)$	$O(\log n)$
M-Tree	Making M-tree into down to up based on the radius of adjacent data. Search based on data pruning and the radius of nodes.	$O(\log n)$	$O(\log n)$

Quad-Tree and Oct-Tree act similar to kd-Tree, as Quad-Tree used in two dimensional spaces and for creating tree in it, each zone in each repetition is divided to four parts. Oct-Tree used in 3D and each zone in each repetition is divided to eight parts. Searching operation in these two structures are similar to kd-Tree [10 – 14].

Also we can point to Ball-Tree [15, 16]. A Ball-Tree is a binary tree where each node represents a set of points, called $Pts(N)$. Given a data set, the root node of a Ball-Tree represents the full set of points in the data set. A node can be either a leaf node or a non-leaf node. A leaf node explicitly contains a list of the points represented by the node. A non-leaf node has two children nodes: $N.child1$ and $N.child2$.

$$Pts(N.child1) \cap Pts(N.child2) = \phi$$

$$Pts(N.child1) \cup Pts(N.child2) = Pts(N)$$

Points are organized spatially. Each node has a distinguished point called a Pivot. Depending on the implementation, the Pivot may be one of the data points, or it may be the centroid of $Pts(N)$. Each node records the maximum distance of the points it owns to its pivot.

For searching in this tree, the algorithms such as KNS1, KNS2, KNS3 and KNSV can be used. As these algorithms have rules for pruning points. One of the other important extant structures is R-Tree that also named

spatial access method. R-trees are a generalized B-tree. R-trees can handle multidimensional data. R-Trees can be used in Temporal and Spatial Data and also in commercial database management systems such as Oracle, MySQL and Postgre SQL. Furthermore in spaces which points are moveable, R-Tree is one of the most usable structures. This tree one of data structures which operate based on local indexing. This local indexing is defined as rectangular vicinity named MBR (Minimum Bounding Rectangle). MBR is the smallest local rectangle that contains its all points and subset nodes. R-Tree uses three concept distance for searching: *MinDist*, *MaxDist* and *MinMaxDist*. Also this tree is a balance tree and all of its leaves are in the same level. For R-Tree there are two algorithms for searching nearest neighbor to HS and RKV that HS is a breadth search Algorithm and RKV is a branch and bound algorithm that use depth search [17 - 21].

Another structure that can be used for NNS is M-Tree that is inspired from R-Tree and B-Tree with the difference that pay more attention to memory and I/O. M-Tree is defined by paying attention to different situation and tries to prune more points. Searching in this is similar to R-Tree but with priority queue searching algorithm is optimum. For indexing points in metric space M-Tree is used such as VP-Trees, Cover-Trees, MVP-Trees and BK-Trees [22, 23]. And another structures for NNS that is created by R-Tree idea are R*-Tree, R+-Tree, TPR-Tree, X-Tree, SS-Tree, SR-Tree, A-Tree and BD-Tree. At the end of this section the complexity of some of the structures are compared in table 2.

3. Nearest Neighbor Search Technique

One of the most important reasons that have made it pervasive is widespread of application and its extent. This wide spreading caused heterogeneous data, conditions and system environment and made the solution hard. So it is necessary to create a technique that has the best result. With this reason for solving NNS problem, different technique with different approach has been created. Each of these techniques can be divided to two parts. The first part consists suitable structure for indexing and maintaining data points that is discussed in the last section. It is necessary to mention that some of these structures itself can be used as a technique for NNS, such as KD-Tree, Ball-Tree and LSH.

The second part consists a suitable algorithm for finding the nearest points to query point q . linear searching and kNN can be mentioned as simple and first techniques [2]. In linear searching for each query point q , its distance from all points in S is calculated and each point that has the lowest distance is chosen as a result. The main problem in this technique is unsalable that in high dimensional or by increasing the points in space, the speed of searching is really decreased.

kNN technique for the first time in T. M. Cover et. al. [24] has been presented for classification and used simple algorithm. A naive solution for the NNS problem is using linear search method that computes distance from the query to every single point in the dataset and returns the k closest points. This approach is guaranteed to find the exact nearest neighbors. However, this solution can be expensive for massive datasets. By paying attention to this initial algorithm, different techniques have been presented that each of them tries to improve kNN's performance. In present study, a new, suitable and comparable categorizing from these techniques is presented. By paying attention to this, these techniques have been categorized to different groups that are discussed as follow.

3.1. Weighted techniques

In such these groups of techniques, by give weight to points the effect of each of them on final result is denoted that one of the main applications of this group is its usage in information classification. Some of these techniques are mentioned as follow: Weighted k-Nearest Neighbor (Weighted-kNN), Modified k-Nearest Neighbor (Modified-kNN) and Pseudo k-Nearest Neighbor (Pseudo-kNN).

Surveying the position of each point compare to other points for query point q is one of the most application methods which Weighted-kNN use it. In this technique if distance is defined as weight, it names distance Weighted-kNN. Usually each of the points has different distance from query point q , so nearer points have more effects. In this technique calculating weight based on distance of points S . A. Dudani et. al [25, 26].

If space has imbalance data, it is better to use Neighbor Weighted-kNN instance of Weighted-kNN. If in a set of data same of the classes have many members in compare to others, its score very high and so more query belong to this class. For solving this problem it is necessary that the classes with more members gain low weight and the classes with less members gain high weight. The weight for each class calculated in S. Tan et. al [27, 28].

For example in point classification for presenting better answer instead of distance, product of distance and weight must be used. Here by paying attention to space weight is calculated by one of these techniques. In more problems choosing neighbors based on distance have some problems such as low Accuracy and incorrect answers. Modified-kNN method which use for classification, tries to solve these problems. At first a preprocessing is done on all of the points and gives a validity value to each point. This value defines based on each point H nearest neighbor.

3.2. Reductional techniques

One of the necessary needs in data processing is extra data and its suitable summarize. This is introduced in spaces which has massive data or data that need high memory. These techniques caused improving performance of systems by decreasing data. Condensed k-Nearest Neighbor (Condensed-kNN), Reduced k-Nearest Neighbor (Reduced-kNN), Model Based k-Nearest Neighbor (ModelBased-kNN) and Clustered k-Nearest Neighbor (Clustered-kNN) are discussed in this section [29 – 35].

Data that are considered as unnecessary information, identical with other data, are deleted in Condensed-kNN. There are two approaches, A) It is assumed that the data are labeled. Then instead of saving the data along with their classes, sample data is saved so that there will be no duplicate data in the dataset. B) Data might be without label; thus the desired cluster can be found by clustering and sample data is obtained from the center of the cluster. kNN operation then, is carried out on the remainder of the data [29 – 31].

Another approach, which uses the nearest neighbor to reduce information volume, is Reduced-kNN (a developed version of condensed-kNN). In addition to removing identical data, null data is also deleted. This even shrinks more the data volume and facilitates the system response to queries. Moreover, smaller memory space is required for processing. One of the drawbacks is increase in complexity of computations and costs of execution of the algorithm consequently. In general, these two approaches are time consuming [29, 32].

The next technique to reduce information volume is ModelBased-kNN. As the technique dictates, a data model is first extracted from the information and replaces the data. This removes a great portion of the information volume. It is noticeable, however, that the data model needs to resemble well the whole data. In place of the whole data, for instance, one may use the data that show the points (usually the central point), number of the member, distance of the farthest data from the resemblance and the class label in some cases. Modelbased-kNN employs “largest local neighborhood” and “largest global neighborhood” to create a simpler structure and definition of the model so that the data are modeled step by step [33, 34].

3.3. Additive Techniques

In this group of techniques it is tried to increase system operation accuracy by increasing data volume. Another aim of these techniques is paying attention to all of points together that can affect each other. Nearest Feature Line (NFL), Local Nearest Neighbor (Local-kNN), Center Based Nearest Neighbor (CenterBased-kNN) and Tunable Nearest Neighbor (Tunable-kNN) are discussed in this section [36 – 41].

When the number of points for classification is not enough, accuracy of the final result is unacceptable. It is necessary to have another technique for increasing data volume and the accuracy consequently. One answer, Euclidean and 2D spaces, is NFL technique. By converting each two points in a class (future points) into a line, not only NFL increases the data volume but it adds to effect of the points in each class. Future points (FP) symbolize features of a class and there are two FPs at least in each class. The lines drawn between the two FPs are called future lines (FL). Instead of calculating distance between q and other data points, perpendicular distance between q and each FL is measured (Figure 1a).

With high efficiency of the technique in small dataset, by increasing size of dataset the computation complexities is increased. There is a risk of wrong determination of nearest FL in NFL for distant q and FPs (Figure 1b). Figure 1b shows that x_3x_4 is wrongly adopted [36, 37].

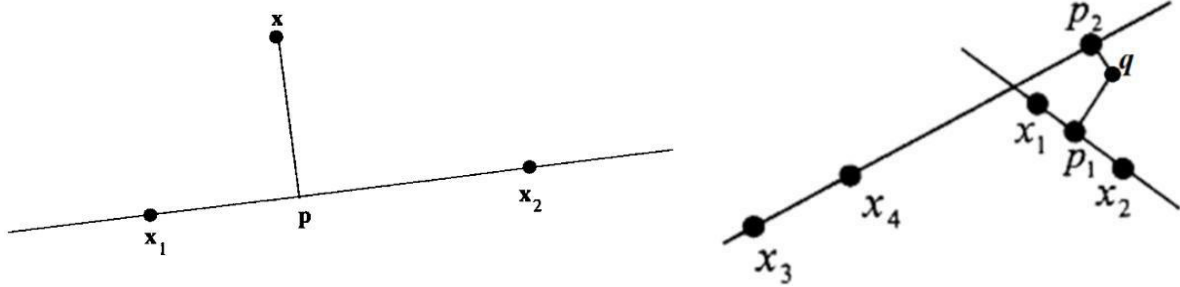


Fig. 1. (a) Mapping Query Point on Future Line [36],

(b) Nearest Future Line Drawback in Classification [38]

To deal with the drawback, Local-kNN was introduced, so that FPs are chosen among k nearest neighbors of q in each class. This ensures accurate determination of nearest FL, though great deal of computation is required. For classification, first kNN for each class is computed.

If $k=2$, distance between q and the FL is created from 2NN of each class and if $k=3$, distance between q to future plane created from 3NN of each class are obtained. Finally, the class with shortest distance to q is taken as the result

3.4. Reverse Techniques

Reverse techniques are the most important and most application techniques in NNS. This group is variety that in present paper some of them are discussed. In this group of techniques the approach of problem is changed and data points are taken more attention than query points. Reverse Nearest Neighbor (Reverse-kNN) and Mutual Nearest Neighbor (Mutual-kNN) are described in this section [42 – 48].

The straightest way to find reserve-kNN of query point q is to calculated the nearest point in the dataset based on the distance equation of each p ; this creates regions centered by p with radius of r . Then, when point q is located in one of the regions, the point p in the regions is the answer. Noticeably, the for L_2 -norm and L_∞ -norm are circle and rectangular respectively. In spite of kNN, Reserve-kNN technique may have empty set as answer and given the distance function and dimension of the data, number of points in the set is limited. If L_2 -norm is the case, for instance, we have 6 and 12 points at most under 3D and 2D spaces respectively. For L_∞ -norm there are equal points. A comparison between kNN and Reserve-kNN is carried out in follow [42-47].

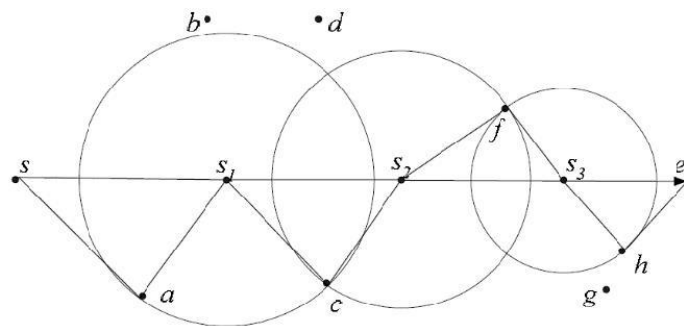


Fig. 2. Continuous Nearest Neighbor Sample [49]

3.5. Continuous Techniques

Techniques that are presented in this section are suitable for points that are introduced in continuous space instead of discrete space. In this section continuous Nearest Neighbor (Continuous -kNN) and Range Nearest Neighbor (Range-kNN) are evaluated [49, 50].

3.6. Principal Axis Techniques

In this group of techniques data environment is divided in several subset. Each these sets have an Axis which data are mapped on them. In this section Principal Axis Nearest Neighbor (Principal Axis-kNN) and Orthogonal Nearest Neighbor (Orthogonal-kNN) are introduced [51-54].

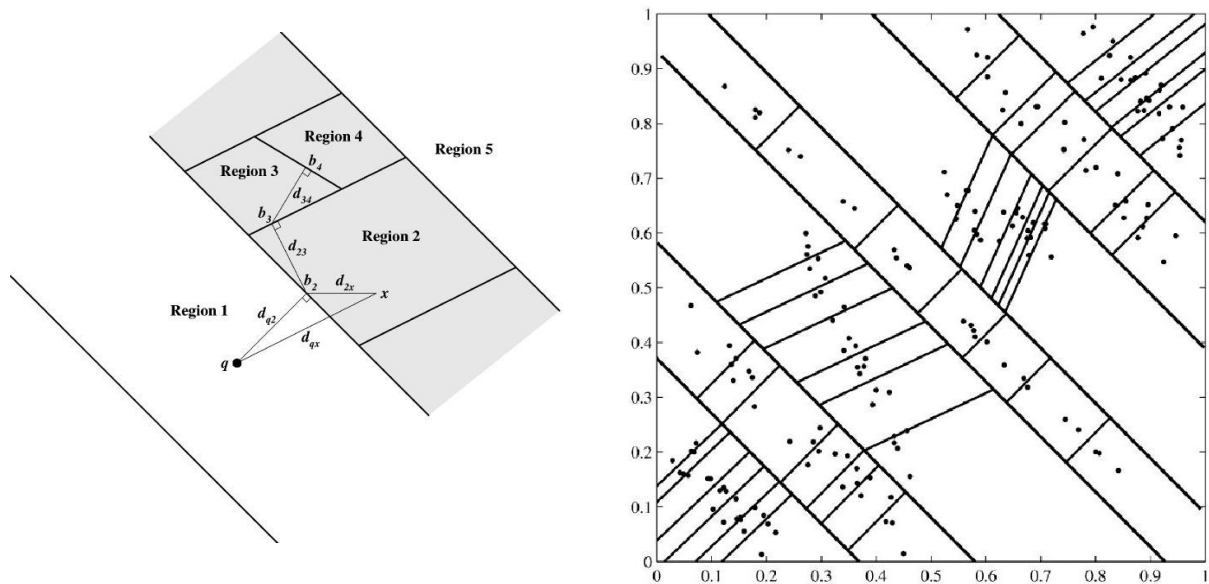


Fig 3(a). Partition of a 2D Data Set using a Principal Axis Tree[51], (b)Pruning Data Set using a Principal Axis Tree [51]

One of the techniques to find kNN is Principal Axis-kNN. As the method implies, the dataset is divided into several subsets. The dividing is continued until every subset is smaller than a specific threshold (e.g. 'nc'). Along with dividing, a principle axis tree (PAT) is developed so that the leaf's nodes have 'nc' data points at most (Figure 3a). Each node in PAT has a principle axis which is used for mapping data and calculating distance as well as pruning. For search operation, first the node where the q is located is searched through a binary query. Then, the node and/or sibling nodes are searched to find kNN of query point q (Figure 3b). To have faster process, some regions are pruned using the principle axis [51, 52].

4. Assessment and Comparison of Techniques

Each of the presented techniques in this paper is suitable for using in spaces with special data but it can't be used generally. So in this section, these techniques are compared and evaluated. These comparison and evaluation are presented. In table 3 presented each technique's idea and applications.

Table 3. Nearest Neighbor Techniques

S.No.	Technique	Method	Application
1	Simple	Comparing query with all data points.	All
2	kNN	Searching based on almost votes.	Massive Data Classification
3	Weighted-kNN	1. Making weight to the neighbors based on distance 2. Making weight to the classes based on the number of members.	Massive Data Unbalanced Data Classification
4	Modified-kNN	Making weight to the points based on the neighbors.	Classification
5	Pseudo-kNN	Making weight to the points based on their effect of dispersal.	Classification
6	Condensed-kNN	Omitting the repetitive and redundant data.	Environment with Limited Memory Duplicate Data & Pattern
7	Reduced-kNN	Omitting the data which are ineffective on results.	Large & Null Data set
8	ModelBased-kNN	Creating model from data and replacing it instead of data.	Dynamic Web Mining for Large Repository
9	Clustered-kNN	Clustering data in classes and omitting far data.	Text Classification
10	NFL	Mapping points to lines for increasing data and accuracy.	Pattern Recognition Face Recognition Classification
11	Local-kNN	Mapping points of each group to lines distinct	Pattern Recognition Classification
12	CenterBased-kNN	Creating lines from data points and data center.	Pattern Recognition Classification
13	Tunable-kNN	Adjusting distance and level that are in the same level based on data condition.	Bias Problem Classification
14	Reverse-kNN	Discussing data that are the closest to query pints.	Spatial Data Set Business Location Planning Profile Based Marketing Maintaining Document Repositories
15	Mutual-kNN	Discussing data that are the closest to query pints and on the vice versa.	Dynamic Databases
16	Continues-kNN	Consuming query point in a straight line continuesly.	Nearest Data on Route Mobile Data
17	Range-kNN	Consuming query point in a d-dimensional zone continusely	Nearest Hotel to the City Park Nearest Printer Unit to College
18	PrincipalAxis-kNN	Using the main axis to prune data.	Pattern Recognition Spatial Data Set
19	Orthogonal-kNN	Mapping data on the main axis and prune them.	Pattern Recognition Spatial Data Set
20	Constrained-kNN	1) The nearest neighbor in a specific zone. 2) The number of result is more than m threshold.	Nearest South Data Nearest Restaurant in Next City Client & Server Link in Busy Network
21	Rank-kNN	Ranking data and query and sorting them based on its calculated rank.	Multidimensional Data Points Data Points with General Information
22	Group-kNN	The nearest neighbor to a group of query points.	Spatial Data Set Meeting Point Problem

5. Conclusion

In this paper, the metric and non-metric spaces are defined. The first one is used in NNS problem. Diverse distance formulas which are used in this problem to find the nearest data point are described and then different structures are introduced. These structures are used for indexing points and making the searching operation faster. Some of these structures such as: Ball-Tree, LSH and KD-Tree are considered as technique for NNS problem. Finally, a new categorization based on the functionality of different techniques for NNS problem is introduced. Techniques with similar functionality are grouped together in this categorization. This categorization consists of six groups; Weighted, Reductional, Additive, Reverse, Continuous, Principal Axis techniques. In each group, the main features of the group are described and each technique is introduced briefly. Finally, a complete comparison of these techniques is done.

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