m3-autograded

February 13, 2022

0.1 Module 3 - Autograded

0.1.1 Outline:

In this homework assignment, here are learning objectives:

- 1. Motivate the use of two-way ANOVA through real data analysis examples.
- 2. Define a two-way ANOVA model with and without interaction terms.
- 3. Formulate three important research questions that can be answered using two-way ANOVA.
- 4. Interpret the two-way ANOVA model, with and without interaction terms.
- 5. Construct and interpret interaction plots to visually assess the importance of an interaction term.
- 6. Conduct hypothesis tests to decide whether a two-way ANOVA interaction term is statistically significant.
- 7. Use the two-way ANOVA and ANCOVA models to answer research questions using real data.

General tips:

- 1. Read the questions carefully to understand what is being asked.
- 2. When you feel that your work is completed, feel free to hit the Validate button to see your results on the visible unit tests.
- 3. Before submitting, we recommend restarting the kernel and running all the cells in order that they appear to make sure that there are no additional bugs in your code.

```
[1]: # Run this cell to import the required packages for this assignment.
library(testthat)
library(tidyverse)
```

```
      ggplot2
      3.3.0
      purrr
      0.3.4

      tibble
      3.0.1
      dplyr
      0.8.5

      tidyr
      1.0.2
      stringr
      1.4.0

      readr
      1.3.1
      forcats
      0.5.0
```

Conflicts

```
tidyverse_conflicts()
  dplyr::filter()    masks stats::filter()
  purrr::is_null()    masks
testthat::is_null()
  dplyr::lag()    masks stats::lag()
  dplyr::matches() masks
tidyr::matches(), testthat::matches()
```

0.1.2 Problem #1: Does stretching protocol impact vertical jump height? (26 Points)

The experiment used in this problem is a modified version of the one conducted in the 2013 paper "Acute Effects of Warm-Up Stretch Protocols on Balance, Vertical Jump Height and Range of Motion in Dancers"

(Citation: N. Morrin and E. Redding (2013). "Acute Effects of Warm-Up Stretch Protocols on Balnce, Vertical Jump Height and Range of Motion in Dancers," Journal of Dance Medicine & Science, Vol. 17, #1, pp. 34-40)

The research question being asked in this experiment is: Does stretching protocol impact vertical jump height? The variables measured include:

- 1. dancer = dancer (1-10)
- 2. stretch = stretch protocol (1=Static Stretching, 2=Dynamic Stretching, 3=Combination Stretching, 4=No Stretch)
- 3. condition = the physical condition of the dancer (1 = less conditioned, 2 = more conditioned)
- 4. height = vertical jump height (cm)

Dancers were first sorted into a condition group, based on how much dance training that they had recently done. Then, stretching routines were randomly assigned to dancers within each condition group. In this case, condition served as the blocking variable, and stretch as the treatment variable. Vertical jump height is the response.

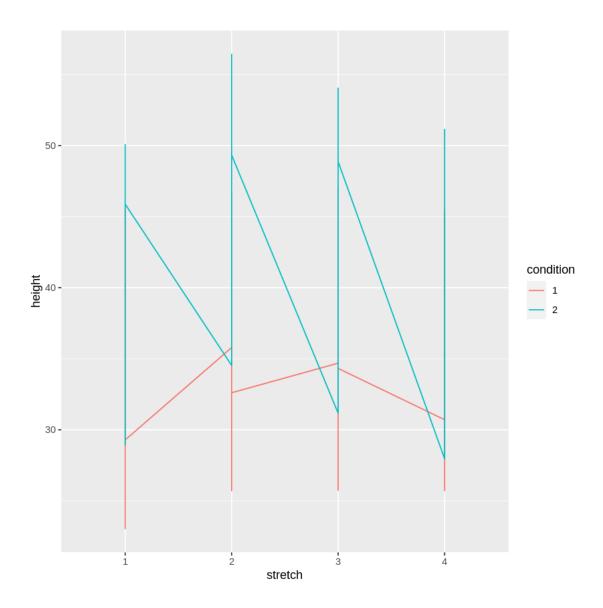
Here's the data...

```
dancer stretch condition
                                                        height
                          <fct>
                                            <fct>
                                                        <dbl>
                                   <fct>
                          1
                                   1
                                            1
                                                        32.76
                          2
                                   1
                                                        32.67
                                            1
A data.frame: 6 \times 4
                          3
                                   1
                                            1
                                                        23.04
                         4
                                   1
                                            1
                                                        45.63
                         5
                                   1
                                            1
                                                        29.29
                      6 \mid 6
                                   1
                                            2
                                                        28.90
```

1. (a) Produce an interaction plot to detect whether there are interactions between stretch and condition. Specifically, store a ggplot object called p1 looking at the relationship between stretch and height grouping on condition.

```
[7]: p1 = NULL

# your code here
p1 = ggplot(data=dance, aes(x=stretch, y=height, group=condition))
p1= p1 + geom_line(aes(color=condition))
p1
```



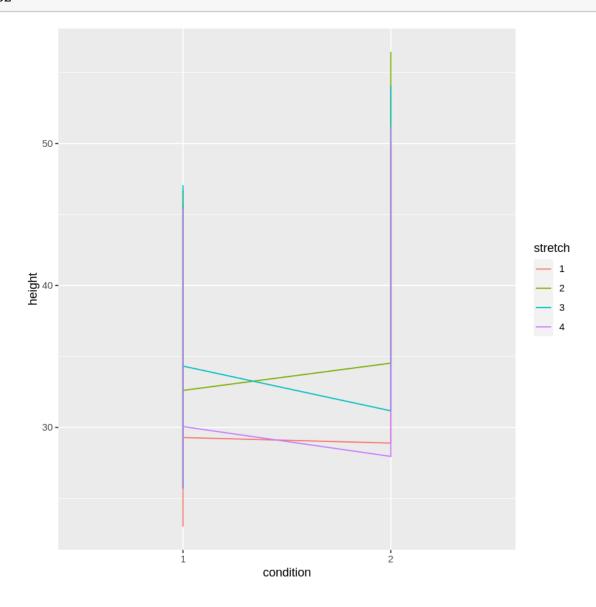
```
[]:  # Test Cell  # This cell has hidden test cases that will run after submission.
```

1. (b) Produce an interaction plot to detect whether there are interactions between stretch and condition. Specifically, store a ggplot object called p2 looking at the relationship between condition and height grouping on stretch.

```
[8]: p2 = NULL

# your code here
p2 = ggplot(data=dance, aes(x=condition, y=height, group=stretch))
p2= p2 + geom_line(aes(color=stretch))
```

p2



[9]: # Test Cell # This cell has hidden test cases that will run after submission.

1. (c) Create two linear models:

- A model, stored as rcbd_int, that uses stretch, condition, and an interaction term to predict jump height.
- A model, stored as rcbd, that uses stretch, condition, and *NO* interaction term to predict jump height.

```
[11]: rcbd_int = NULL
     rcbd = NULL
     # your code here
     rcbd_int = lm(height ~ stretch + condition + stretch:condition, data=dance)
     rcbd = lm(height ~ stretch + condition, data=dance)
     summary(rcbd int)
     print("No Interaction Model Below----")
     summary(rcbd)
     Call:
     lm(formula = height ~ stretch + condition + stretch:condition,
        data = dance)
     Residuals:
        Min
                 1Q Median
                                3Q
                                       Max
     -15.124 -3.092 0.037 6.742 12.952
     Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                         32.678
                                     3.790 8.622 7.48e-10 ***
     (Intercept)
                          2.926
                                    5.360 0.546 0.5889
     stretch2
                                    5.360 0.583 0.5638
     stretch3
                          3.126
     stretch4
                          0.106
                                    5.360 0.020 0.9843
                                   5.360 1.990 0.0552 .
     condition2
                         10.664
     stretch2:condition2 0.988
                                    7.580 0.130 0.8971
     stretch3:condition2 -0.174
                                    7.580 -0.023 0.9818
     stretch4:condition2 -0.714
                                   7.580 -0.094
                                                    0.9255
     Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
     Residual standard error: 8.475 on 32 degrees of freedom
     Multiple R-squared: 0.3541, Adjusted R-squared: 0.2128
     F-statistic: 2.506 on 7 and 32 DF, p-value: 0.03579
     [1] "No Interaction Model Below-----"
     Call:
     lm(formula = height ~ stretch + condition, data = dance)
     Residuals:
                       Median
         Min
                   1Q
                                    3Q
                                           Max
     -15.2235 -3.4005 -0.1455
                                6.4913 12.9655
     Coefficients:
                Estimate Std. Error t value Pr(>|t|)
```

```
(Intercept)
             32.666
                         2.867 11.392 2.52e-13 ***
stretch2
              3.420
                         3.627 0.943 0.352178
                         3.627
stretch3
              3.039
                                 0.838 0.407779
stretch4
             -0.251
                         3.627 -0.069 0.945221
                         2.565
                                 4.168 0.000192 ***
condition2
             10.689
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Residual standard error: 8.11 on 35 degrees of freedom
Multiple R-squared: 0.353, Adjusted R-squared: 0.2791
F-statistic: 4.774 on 4 and 35 DF, p-value: 0.00352
```

```
[]: # Test Cell
   if(test_that('checking 2 models: ',{
      expect_is(rcbd_int,"lm")
      expect_is(rcbd,"lm")})){
       print('Two linear models: PASS')
           print('Reminder: make sure that you have the correct predictors/response!')
   }
   # This cell has hidden test cases that will run after submission.
```

1. (d) Run an F-test between rcbd_int and rcbd to determine if the interaction term is statistically significant. Store the p-value from the F-test in the object rcbd_ftest_pvalue.

```
[17]: rcbd_ftest_pvalue = NULL

# your code here
rcbd_ftest_pvalue = anova(rcbd, rcbd_int)[2, "Pr(>F)"]
rcbd_ftest_pvalue
```

0.996764942169362

```
[]: # Test Cell # This cell has hidden test cases that will run after submission.
```

1. (e) Run a full F-test on the better model (determined by 1.(d)) in order to decide if there is a statistically significant difference in mean vertical jump height across stretching routines. Store the p-value of the stretch factor from the F-test in the object stretch_ftest_pvalue.

```
[28]: stretch_ftest_pvalue = NULL

# your code here
anova(rcbd)
stretch_ftest_pvalue = 0.6348088114
```

		Df	Sum Sq	Mean Sq	F value	Pr(>F)
		<int></int>	<dbl $>$	<dbl $>$	<dbl $>$	<dbl></dbl>
A anova: 3×5	stretch	3	113.6011	37.86702	0.5757083	0.6348088114
	condition	1	1142.5472	1142.54721	17.3706269	0.0001916087
	Residuals	35	2302.1134	65.77467	NA	NA

[22]: # Test Cell # This cell has hidden test cases that will run after submission.