House Case Study Report

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Loading the data and any packages

```
options("max.print"=10)
suppressMessages(library(tidyverse))
suppressMessages(library(magrittr))
suppressMessages(library(leaps))
suppressMessages(library(VIM))
suppressMessages(library(car))
suppressMessages(library(Hmisc))
suppressMessages(library(glmnet))
suppressMessages(library(grid))
suppressMessages(library(gridExtra))
suppressMessages(library(gridExtra))
suppressMessages(library(olsrr))
house <- read_csv("housing.txt", col_types = cols())
names(house) <- tolower(names(house))
house0 <- house</pre>
```

Convert mssubclass to factor and check for NAs

```
house$mssubclass <- factor(house$mssubclass)
house %>% sapply(function(x) sum(is.na(x))) %>% sort(decreasing = T)
```

```
##
         poolqc miscfeature
                                                 fence fireplacequ
                                    alley
                        1406
                                     1369
                                                  1179
##
          1453
                                                                690
##
  lotfrontage
                 garagetype garageyrblt garagefinish
                                                         garagequal
##
            259
                                       81
   [ reached getOption("max.print") -- omitted 71 entries ]
```

Convert numeric variables that have NA to 0. Change garageyrblt to indicate whether or not the garage was built AFTER the house was built.

```
house$masvnrarea[which(is.na(house$masvnrarea))] <- 0
house$bsmtfintype1[which(is.na(house$bsmtfintype1))] <- 0
house$bsmtfintype2[which(is.na(house$bsmtfintype2))] <- 0
house$garageyrblt <- (house$garageyrblt > house$yearbuilt) * 1
house$garageyrblt[is.na(house$garageyrblt)] <- 0
```

Impute the NA in lotfrontage, electrical with K-Nearest Neighbors

```
Convert all other NAs to "None"
```

```
house[is.na(house)] <- "None"
```

Make a new variable, remodel that indicates whether or not remodeling took place. Remove the yearremodadd variable because it is no longer needed. Make a new variable soldminusbuilt that indicates the number of

years that it took for the house to get sold after getting built.

```
house$remodel <- T
house[house$yearbuilt == house$yearremodadd,]$remodel <- F
house$remodel <- as.numeric(house$remodel)
house %<>% select(-yearremodadd)

house$soldminusbuilt <- (house$yrsold - house$yearbuilt)
house %<>% select(-yrsold,-yearbuilt)
```

Combine all of the porch variables into one. Remove id because it is obviously not important.

```
house$porcharea <- with(house, openporchsf + enclosedporch +
    `3ssnporch` + screenporch)
house %<>% select(-id)
```

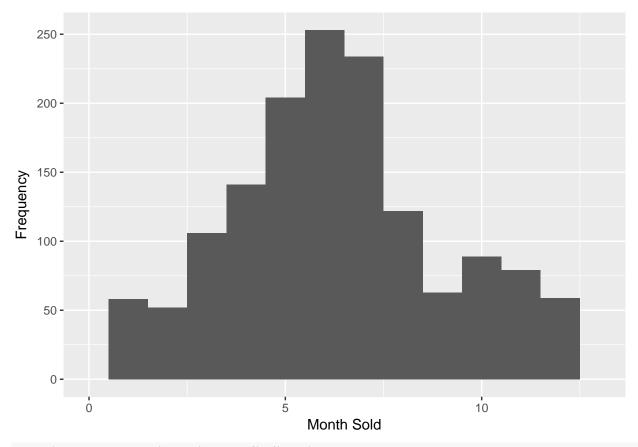
Change lotshape to a boolean whether or not it is Regular.

```
table(house$lotshape)
```

```
##
## IR1 IR2 IR3 Reg
## 484 41 10 925
house$lotshape <- (house$lotshape == 'Reg') *1</pre>
```

Looking at the histogram of mosold we see many more houses being sold near summer time (and part of spring too) so we create a boolean. Most of the time, when we are creating a boolean, it is because it is insignificant otherwise.

```
house %>% ggplot(aes(x=mosold)) + geom_histogram(binwidth = 1) + xlim(0,13)+
    xlab("Month Sold") +
    ylab("Frequency")
```



house\$summertime <- (house\$mosold %in% 5:7) * 1

The next part of the code was very time-consuming but here's the general outline: It is similar to backwards selection but by hand and possibly more thorough because of the refactoring involved rather than simply removing it.

- 1. Check the p-value and signifiance for a particlar variable.
- 2. If the variable is numeric and significant, keep it. If the variable is categorical and all levels are significant, keep it. If only some levels are significant then try to bin the factors into smaller number of levels to try and make them statistically significant. If nothing can be done, then remove the variable.
- 3. Repeat the above steps for the rest of the variables. Each time we remove a variable, we re-run the lm model to check if the Adjusted R Squared changed significantly or not.
- 4. When we finish going through all the variables, there will be about 30 ones left to consider.

```
house %<>% select(-mosold, -landcontour, -alley, -lotshape)
house$lotconfig <- (house$lotconfig == "Inside") * 1
house %<>% select(-lotconfig)
```

Here, we noticed lotfrontage became significant when we take the square root. We remove 1stflrsf, 2ndflrsf, lowqualfinsf because they make up the variable grlivarea. At first, we tried having all three of them and deleting grlivarea however we found that having just grlivarea performed better. We are deleting the porch variables because we have already aggregated them into porcharea.

```
fullmodel <- lm(saleprice~sqrt(lotfrontage)+porcharea+.,data = house)
summary(fullmodel)$r.squared</pre>
```

[1] 0.9328122

```
house$condition1 <- relevel(factor(house$condition1), ref = "Norm")</pre>
house$condition2 <- relevel(factor(house$condition2), ref = "Norm")</pre>
house %<>% select(-roofstyle)
house %<>% select(-exterior2nd)
table(house$bldgtype)
##
##
     1Fam 2fmCon Duplex Twnhs TwnhsE
##
     1220
              31
                      52
                             43
                                   114
house <- house %>% select(-`1stflrsf`, -`2ndflrsf`, -lowqualfinsf,
    -totalbsmtsf, -openporchsf, -enclosedporch, - `3ssnporch`,
    - screenporch, -garagearea)
table(house$salecondition)
##
## Abnorml AdjLand Alloca Family Normal Partial
                         12
                                 20
                                       1198
house$salecondition <- (house$salecondition == "Normal") * 1
table(house$saletype)
##
##
     COD
           Con ConLD ConLI ConLw
                                    CWD
                                           New
                                                 Oth
                                                        WD
                          5
                                           122
                                                   3 1267
##
                                5
house$saletype <- (house$saletype == 'New') * 1
house <- house %>% select(-saletype)
house$miscfeature <- (house$miscfeature != 'None') * 1
house %<>% select(-miscval, -miscfeature)
house$paveddrive <- (house$paveddrive == 'Y') * 1
house %<>% select(-paveddrive)
house$poolqc <- (house$poolqc !="None")*1
house$fence <- (house$fence !="None")*1
Here, I am changing the ordered factor into numeric. I want to make a correlation plot with every significant
variable so I am converting all variables (as long as it makes sense) to numeric.
house$garagecond <- as.numeric(factor(house$garagecond,
    levels = c("None", "Po", "Fa", "TA", "Gd", "Ex"), labels = 0:5))
house$garagequal <- as.numeric(factor(house$garagequal,
    levels = c("None", "Po", "Fa", "TA", "Gd", "Ex"), labels = 0:5))
house %<>% select(-fence,-poolqc,-garagecond)
house %>% group_by(garagefinish) %>%
summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc)) %>% head(2)
## # A tibble: 2 x 2
   garagefinish avgprc
```

```
##
            <chr> <dbl>
## 1
              Fin 215000
## 2
              RFn 190000
house$garagefinish <-(house$garagefinish == "Fin") *1
house %<>% select(-garagefinish)
Here, fireplacequ and fireplaces are obviously correlated so I choose the one that seems to explain
saleprice better. However, they both end up being insignificant.
house$fireplacequ <- as.numeric(factor(house$fireplacequ,
    levels = c("None", "Po", "Fa", "TA", "Gd", "Ex"), labels = 0:5))
cor(house$saleprice,house$fireplacequ); cor(house$saleprice,house$fireplaces)
## [1] 0.5204376
## [1] 0.4669288
house %<>% select(-fireplacequ, -fireplaces)
house %<>% select(-garageyrblt)
house$garagetype <- relevel(factor(house$garagetype), ref = "None")
house$functional <- (house$functional == "Typ") * 1
house$kitchengual <- as.numeric(factor(house$kitchengual,
    levels = c("Po", "Fa", "TA", "Gd", "Ex"), labels = 1:5))
Similarly, totrmsabvgrd is highly correlated with grlivarea so I keep the better of the two.
cor(house$totrmsabvgrd ,house$saleprice);cor(house$grlivarea ,house$saleprice)
## [1] 0.5337232
## [1] 0.7086245
house %<>% select(-totrmsabvgrd)
I try to combine all of the bath variables but they end up not being significant so I just remove them.
table(house$fullbath)
##
                 3
##
     0
         1
             2
     9 650 768 33
house$bath <- house$fullbath + house$balfbath + house$bsmtfullbath + house$bsmthalfbath
house %<>% select(-fullbath,-halfbath, -bsmthalfbath, -bsmtfullbath)
house %<>% select(-bath)
house %>% group_by(electrical) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 5 x 2
     electrical avgprc
##
##
          <chr> <dbl>
          SBrkr 170000
## 1
## 2
          FuseA 121250
## 3
          FuseF 115000
## 4
          FuseP 82000
## 5
            Mix 67000
```

```
house$electrical <- (house$electrical == "SBrkr") * 1
house %<>% select(-electrical, -centralair)
house$heatingqc <- as.numeric(factor(house$heatingqc,</pre>
  levels = c("Po", "Fa", "TA", "Gd", "Ex"), labels = 1:5))
table(house$heatingqc)
##
##
     1 2 3 4 5
##
     1 49 428 241 741
house$heatingqc <- (house$heatingqc == 5) * 1
house %<>% select(-heating)
table(house$bsmtfintype1)
##
##
    O ALQ BLQ GLQ LwQ Rec Unf
## 37 220 148 418 74 133 430
house$bsmtfintype1 <- as.numeric(factor(house$bsmtfintype1,
      levels = c("0","Unf","LwQ","Rec","BLQ","ALQ","GLQ"),
      labels = 0:6))
house$bsmtfintype2 <- as.numeric(factor(house$bsmtfintype2,</pre>
      levels = c("0","Unf","LwQ","Rec","BLQ","ALQ","GLQ"),
      labels = 0:6)
house$bsmtfintype1 <- house$bsmtfintype1 + house$bsmtfintype2
house %<>% select(-bsmtfintype1, -bsmtfintype2)
house$bsmtexposure <- relevel(factor(house$bsmtexposure), ref = "None")
table(house$bsmtexposure)
##
## None
              Gd
                  Mn
                         No
        Αv
     38 221 134 114 953
house %>% group_by(bsmtexposure) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 5 x 2
##
   bsmtexposure avgprc
          <fctr> <dbl>
##
## 1
              Gd 226975
## 2
              Av 185850
## 3
              Mn 182450
## 4
              No 154000
            None 104025
house$bsmtexposure <- (house$bsmtexposure == "Gd") * 1
house %>% group_by(bsmtcond) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 5 x 2
##
   bsmtcond avgprc
##
       <chr> <dbl>
```

```
Gd 193879
## 1
## 2
           TA 165000
           Fa 118500
## 3
## 4
         None 101800
## 5
           Po 64000
table(house$bsmtcond)
##
##
          Gd None
                    Ро
                          TA
     Fa
##
               37
                      2 1311
house$bsmtcond <- as.numeric(factor(house$bsmtcond,</pre>
      levels = c("None", "Po", "Fa", "TA", "Gd", "Ex"),
      labels = 0:5))
house$bsmtqual <- as.numeric(factor(house$bsmtqual,</pre>
      levels = c("None", "Po", "Fa", "TA", "Gd", "Ex"),
      labels = 0:5))
cor(house$bsmtcond,house$bsmtqual)
## [1] 0.6337134
cor(house$bsmtcond,house$saleprice);cor(house$bsmtqual,house$saleprice)
## [1] 0.2126072
## [1] 0.5852072
house %<>% select(-bsmtcond)
house %<>% select(-bsmtqual)
table(house$foundation)
## BrkTil CBlock PConc
                           Slab Stone
                                          Wood
      146
             634
                     647
                             24
house %>% group_by(foundation) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 6 x 2
##
    foundation avgprc
##
          <chr> <dbl>
          PConc 205000
## 1
## 2
           Wood 164000
         CBlock 141500
## 3
## 4
          Stone 126500
## 5
         BrkTil 125250
           Slab 104150
house$foundation <- (house$foundation == "PConc")*1
house$extercond <- as.numeric(factor(house$extercond,</pre>
      levels = c("Po", "Fa", "TA", "Gd", "Ex"),
      labels = 1:5))
house$exterqual <- as.numeric(factor(house$exterqual,</pre>
      levels = c("Po", "Fa", "TA", "Gd", "Ex"),
      labels = 1:5))
cor(house$extercond,house$exterqual)
```

```
## [1] 0.00918398
house$masvnrtype <- relevel(factor(house$masvnrtype), ref = "None")
table(house$masvnrtype)
##
##
      None BrkCmn BrkFace
                             Stone
##
       872
                       445
                                128
                15
house$masvnrtype <- (house$masvnrtype != "None") * 1
Boolean whether or not housestyle is either 2Story or 2.5Fin.
table(house$housestyle)
##
## 1.5Fin 1.5Unf 1Story 2.5Fin 2.5Unf 2Story SFoyer
                                                       SLvl
      154
              14
                    726
                             8
                                   11
                                         445
                                                  37
                                                         65
house %>% group_by(housestyle) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 8 x 2
## housestyle avgprc
         <chr> <dbl>
##
## 1
         2.5Fin 194000
## 2
       2Story 190000
## 3
         SLvl 164500
## 4
        1Story 154750
         SFoyer 135960
## 5
## 6
         2.5Unf 133900
## 7
        1.5Fin 132000
## 8
         1.5Unf 111250
house$housestyle <- (house$housestyle == "2Story" |
                    house$housestyle == "2.5Fin")*1
table(house$bldgtype)
##
##
     1Fam 2fmCon Duplex Twnhs TwnhsE
##
                     52
                            43
                                  114
house$bldgtype <- (house$bldgtype == "1Fam" | house$bldgtype == "2FmCon") * 1
house %<>% select(-bldgtype)
table(house$landslope)
##
## Gtl Mod Sev
## 1382
         65
               13
house$landslope <- (house$landslope == "Gtl") * 1
house %<>% select(-landslope)
table(house$utilities)
```

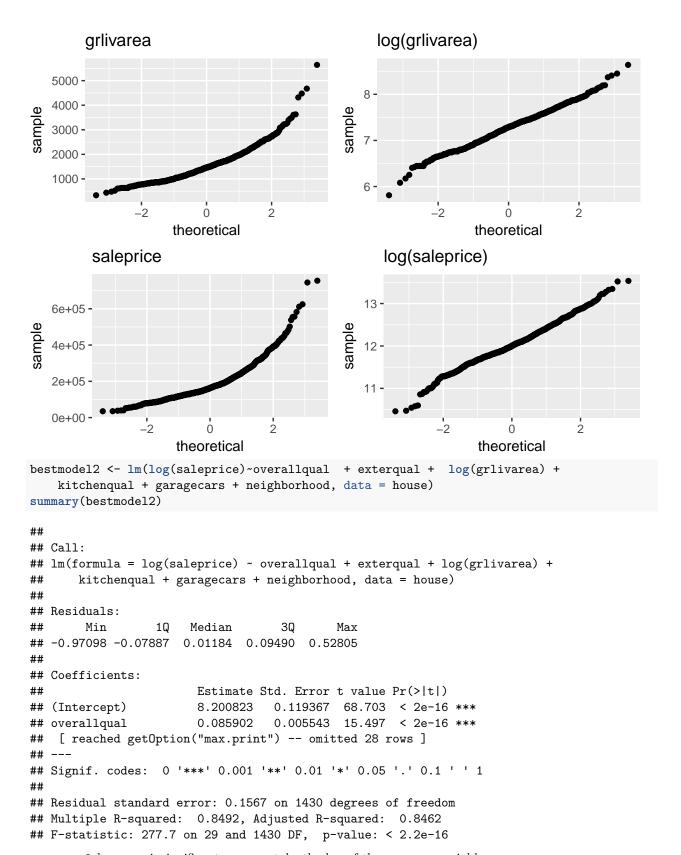
AllPub NoSeWa

```
1459
##
house %<>% select(-utilities, -street)
house %>% group_by(mszoning) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 5 x 2
##
    mszoning avgprc
##
        <chr> <dbl>
## 1
           FV 205950
## 2
           RL 174000
## 3
           RH 136500
           RM 120500
## 5 C (all) 74700
table(house$mszoning)
##
## C (all)
                F۷
                                RL
                                         RM
                        RH
##
        10
                65
                        16
                              1151
                                        218
house$mszoning <- relevel(factor(house$mszoning), ref = "RL")
house %<>% select(-mszoning)
house %>% group_by(mssubclass) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 15 x 2
##
      mssubclass avgprc
##
          <fctr> <dbl>
##
   1
              60 215200
##
   2
             120 192000
              80 166500
##
  3
##
  4
              75 163500
##
   5
              20 159250
##
   6
              70 156000
##
   7
             160 146000
##
              40 142500
  8
##
   9
              85 140750
## 10
              90 135980
## 11
              50 132000
## 12
             190 128250
## 13
              45 107500
              30 99900
## 14
             180 88500
## 15
house %<>% select(-mssubclass, -lotfrontage, -porcharea, -extercond,-foundation,
                  -exterior1st)
house %>% group_by(condition1) %>% summarise(avgprc = median(saleprice)) %>% arrange(desc(avgprc))
## # A tibble: 9 x 2
##
     condition1 avgprc
         <fctr> <dbl>
           RRNn 214000
## 1
## 2
           PosA 212500
```

```
## 3
           PosN 200000
## 4
           RRNe 190750
## 5
           RRAn 171495
## 6
           Norm 166500
## 7
           RRAe 142500
## 8
          Feedr 140000
## 9
         Artery 119550
house$condition1 <- (house$condition1 == "Artery" | house$condition1 == "Feedr" |
  house$condition1 == "RRAe")*1
house$condition2 <- (house$condition2 == "PosN") * 1
cor(house$garagequal, house$garagecars)
## [1] 0.5766224
house %<>% select(-garagequal)
fullmodel <- lm(saleprice~.,data = house)</pre>
summary(fullmodel)
##
## Call:
## lm(formula = saleprice ~ ., data = house)
## Residuals:
##
       Min
                1Q Median
                                 30
                                        Max
## -187252 -12044
                        669
                              11896 187252
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        -7.012e+05 3.467e+04 -20.226 < 2e-16 ***
## lotarea
                         4.753e-01 8.365e-02
                                                 5.682 1.62e-08 ***
## [ reached getOption("max.print") -- omitted 62 rows ]
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26650 on 1396 degrees of freedom
## Multiple R-squared: 0.8923, Adjusted R-squared: 0.8875
## F-statistic: 183.6 on 63 and 1396 DF, p-value: < 2.2e-16
Checking multicollinearity. Looks good. For the generalized variance inflation factor (normalized by the
degree of freedom), everything except one is less than 2.
vif(fullmodel)
##
                        GVIF Df GVIF^(1/(2*Df))
## lotarea
                    1.431941 1
                                       1.196637
                                       1.095492
## neighborhood
                  79.659389 24
## condition1
                    1.184234 1
                                       1.088225
   [ reached getOption("max.print") -- omitted 26 rows ]
Interestingly, soldminusbuilt which is yrsold - yearbuilt becomes insignificant in this smaller model with
only the best predictors
house_numeric <- house[,sapply(house,function(x) is.numeric(x))]</pre>
house_numeric %<>% select(saleprice, everything())
bestpredictors <- names(house_numeric)[sapply(house_numeric,</pre>
```

```
function(x) abs(cor(house_numeric$saleprice, x))) >= 0.5][-1]
bestpredictors <- bestpredictors[-6]</pre>
bestmodel <- lm(saleprice~overallqual + exterqual + grlivarea +
   kitchenqual + garagecars + neighborhood, data = house)
summary(bestmodel)$r.squared
## [1] 0.808378
Subset with only best predictors
housesubset <- house %>% select(bestpredictors)
So, 6 variables capture 0.808378 of the variation in sale price for our model.
Checking assumptions.
cor(housesubset)
               overallqual exterqual grlivarea kitchenqual garagecars
##
                 1.0000000 0.7262785 0.5930074 0.6733308 0.6006707
## overallqual
## exterqual
                 0.7262785 1.0000000 0.4359861 0.7161222 0.5263902
## [ reached getOption("max.print") -- omitted 3 rows ]
vif(bestmodel)
                    GVIF Df GVIF^(1/(2*Df))
##
## overallqual 3.464742 1 1.861382
## exterqual
               3.112695 1
                                   1.764283
                                   1.394005
## grlivarea
                1.943250 1
## [ reached getOption("max.print") -- omitted 3 rows ]
g1 <- ggplot(housesubset, aes(sample = grlivarea)) + stat_qq() + ggtitle("grlivarea")</pre>
g2 <- ggplot(housesubset, aes(sample = log(grlivarea))) + stat_qq() + ggtitle("log(grlivarea)")</pre>
g3 <- ggplot(house, aes(sample = saleprice)) + stat_qq() + ggtitle("saleprice")
g4 <- ggplot(house, aes(sample = log(saleprice))) + stat_qq() + ggtitle("log(saleprice)")
```

grid.arrange(g1,g2,g3,g4)



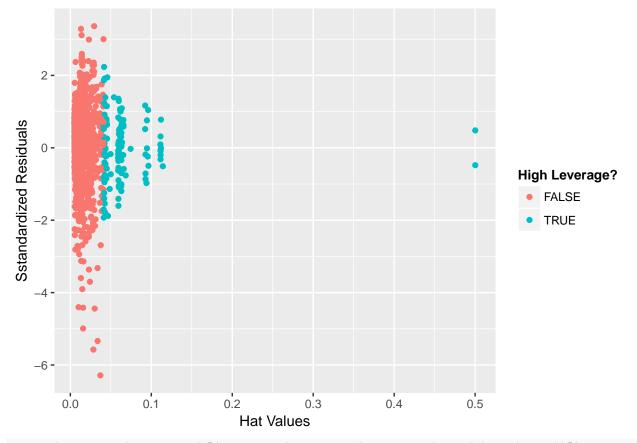
```
bestmodel3 <- lm(log(saleprice)~overallqual + log(grlivarea) +
   kitchenqual + garagecars + neighborhood, data = house)
summary(bestmodel3)$r.squared</pre>
```

[1] 0.8488445

Check for high leverage points. There are 98 high leverage points.

(high_leverage <- as.numeric(names(hatvalues(bestmodel3)[(hatvalues(bestmodel3) > 2*ncol(house)/nrow(h

```
## [1] 2 24 54 59 76 121 127 161 173 179
## [reached getOption("max.print") -- omitted 109 entries]
```



length(hatvalues(bestmodel3)[(hatvalues(bestmodel3) > 2*ncol(house)/nrow(house))])

```
## [1] 119
```

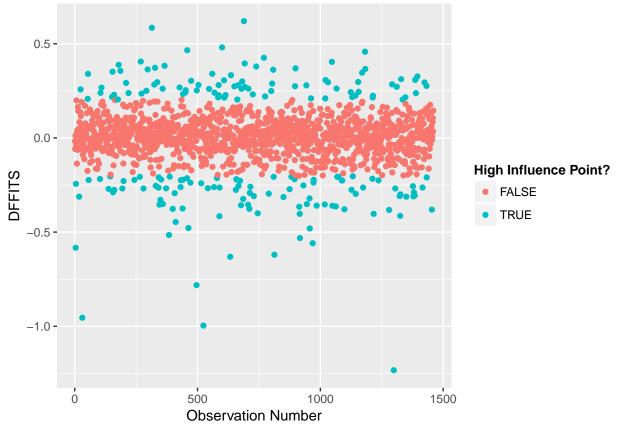
hatvalues(bestmodel) [hatvalues(bestmodel3) > 0.5]

600 957

```
## 0.5001289 0.5001289
```

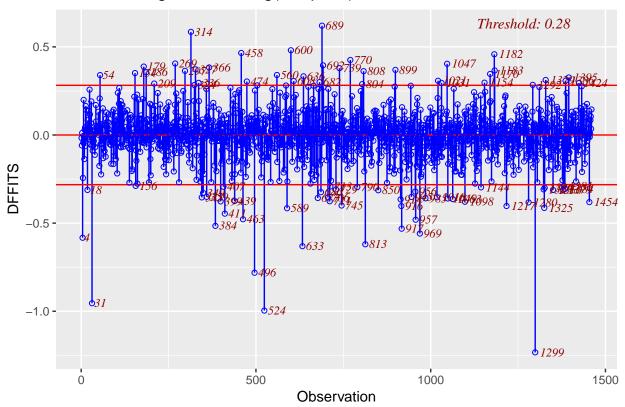
```
infm <- influence.measures(bestmodel3)
threshhold <- sqrt(2*ncol(house)/nrow(house))</pre>
```

Check for influence points. There are 184 high influence points with a threshold of $\sqrt{\frac{p}{n}} = 0.2027212$ (high_influence <- which(abs(infm\$infmat[,30])>threshold))



```
#install.packages("olsrr")
influence <- ols_dffits_plot(bestmodel3)</pre>
```

Influence Diagnostics for log(saleprice)



Let's examine Observation # 1299, and 524

```
house[1299,] %>% View()
house[542,] %>% View()

bestmodel4 <- lm(log(saleprice)~overallqual + log(grlivarea) +
        kitchenqual + garagecars + neighborhood, data = house[c(-1299,-542),])
summary(bestmodel4)$r.squared</pre>
```

[1] 0.8530995

By just removing two points, our Adjusted R-squared went from 0.8458869 to 0.8502211

There are 89 outliers. Let's see what happens if we simply remove the outliers.

```
influenceindex <- unlist(influence$outliers[1])
bestmodelnoinfluence <- lm(log(saleprice)~overallqual + log(grlivarea) +
   kitchenqual + garagecars + neighborhood, data = house[-influenceindex,])
summary(bestmodelnoinfluence)$r.squared</pre>
```

[1] 0.8889236

We see that our Adjusted R-squared went from 0.8502211 to 0.8866905 after removing ALL the influence points.

```
t1 <- names(house)[1:11]
t2 <- names(house)[12:21]
t2[11] <- ""
t3 <- names(house)[22:31]
```

```
t3[11] <- ""

data_frame(t1,t2,t3) %>%
  knitr::kable(col.names = c("","",""))
```

```
lotarea
               bsmtexposure
                                garagetype
neighborhood
               bsmtfinsf1
                                garagecars
               bsmtfinsf2
condition1
                                wooddecksf
               bsmtunfsf
condition2
                                poolarea
housestyle
               heatingqc
                                salecondition
overallqual
               grlivarea
                                saleprice
overallcond
               bedroomabvgr
                                remodel
roofmatl
               kitchenabvgr
                                soldminusbuilt
               kitchenqual
                                summertime
masvnrtype
masvnrarea
               functional
                                NA
extergual
```

```
house2 <- house
house2[influenceindex, ]$saleprice <- NA
house2$saleprice <- kNN(house2, variable = "saleprice", k = k)$saleprice

## Warning in gowerD(don_dist_var, imp_dist_var, weights = weightsx,

## numericalX, : NAs introduced by coercion

## Warning in gowerD(don_dist_var, imp_dist_var, weights = weightsx,

## numericalX, : NAs introduced by coercion

## Warning in gowerD(don_dist_var, imp_dist_var, weights = weightsx,

## numericalX, : NAs introduced by coercion

## Warning in gowerD(don_dist_var, imp_dist_var, weights = weightsx,

## numericalX, : NAs introduced by coercion

bestmodelimputeinfluence <- lm(log(saleprice)~overallqual + log(grlivarea) + kitchenqual + garagecars + neighborhood, data = house2)

summary(bestmodelimputeinfluence)$r.squared
```

[1] 0.8682235

Let's try our model with all of the relevant variables. First, we notice that the R squared improves by taking the log of saleprice, lotarea, grlivarea and the square root of bsmtfinsf1. We also notice that housestyle and masvnrtype is no longer significant so we remove them.

[1] 0.9219723

Accounting for outliers in the full model through imputation

```
## [1] 0.9221831
```

We can try removing the outliers, which improved the R squared by a lot. Now, we can test some interaction terms.

FINAL MODEL

I test the multicollinearity, significance of variables in the model, normality for our final model.

log(lotarea)	1.423439
sqrt(bsmtfinsf1)	2.784409
log(grlivarea)	4.185430
condition1	1.101517
housestyle	2.174226
overallqual	3.506602
overallcond	1.416362
masvnrtype	2.193668
masvnrarea	2.112225
bsmtexposure	1.144744
bsmtfinsf2	1.168368
bsmtunfsf	3.089900
heatingqc	1.493985
bedroomabvgr	1.786380
kitchenabvgr	1.197025
kitchenqual	2.223861
functional	1.164823
garagecars	2.008150
wooddecksf	1.141724
salecondition	1.097912
soldminusbuilt	2.820583
summertime	1.032483

```
options (max.print=999)
summary(endmodel)
##
## Call:
## lm(formula = log(saleprice) ~ log(lotarea) + sqrt(bsmtfinsf1) +
##
       log(grlivarea) + . - lotarea - bsmtfinsf1 - grlivarea, data = house4[-influenceindex,
##
       ])
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    30
                                             Max
  -0.40313 -0.05065
                      0.00314 0.05280
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        6.976e+00
                                   1.115e-01
                                               62.577
                                                       < 2e-16 ***
## log(lotarea)
                        1.021e-01
                                   7.897e-03
                                               12.924
                                                       < 2e-16 ***
## sqrt(bsmtfinsf1)
                        4.928e-03
                                   3.311e-04
                                               14.882
                                                       < 2e-16 ***
## log(grlivarea)
                                               28.317
                        4.579e-01
                                   1.617e-02
                                                       < 2e-16 ***
## neighborhoodBrDale -8.506e-02
                                   3.662e-02
                                               -2.323 0.020352 *
## neighborhoodBrkSide -1.007e-02
                                   3.063e-02
                                               -0.329 0.742387
## neighborhoodClearCr 1.281e-02
                                   3.433e-02
                                                0.373 0.709209
## neighborhoodCollgCr -1.882e-02
                                   2.680e-02
                                               -0.702 0.482531
## neighborhoodCrawfor 1.032e-01
                                   3.113e-02
                                                3.314 0.000945 ***
## neighborhoodEdwards -8.397e-02
                                   2.894e-02
                                               -2.901 0.003777
## neighborhoodGilbert -2.291e-02
                                               -0.805 0.421000
                                   2.847e-02
## neighborhoodIDOTRR -1.002e-01
                                   3.410e-02
                                               -2.939 0.003345 **
## neighborhoodMeadowV -8.290e-02
                                   3.565e-02
                                               -2.325 0.020196 *
## neighborhoodMitchel -5.173e-02
                                   2.986e-02
                                               -1.732 0.083456 .
## neighborhoodNAmes
                       -4.400e-02
                                   2.791e-02
                                               -1.576 0.115179
                                                1.410 0.158703
## neighborhoodNoRidge 4.379e-02
                                   3.105e-02
## neighborhoodNPkVill -9.336e-03
                                   4.009e-02
                                               -0.233 0.815882
## neighborhoodNridgHt 8.753e-02
                                   2.794e-02
                                                3.133 0.001765 **
## neighborhoodNWAmes -5.122e-02
                                   2.899e-02
                                               -1.767 0.077492
## neighborhoodOldTown -8.453e-02
                                   2.996e-02
                                               -2.821 0.004854 **
## neighborhoodSawyer -1.532e-02
                                   2.955e-02
                                               -0.518 0.604321
## neighborhoodSawyerW -4.333e-02
                                   2.878e-02
                                               -1.506 0.132351
## neighborhoodSomerst 6.059e-02
                                   2.710e-02
                                                2.236 0.025513 *
## neighborhoodStoneBr
                       1.182e-01
                                   3.412e-02
                                                3.465 0.000547 ***
## neighborhoodSWISU
                       -4.889e-02
                                   3.507e-02
                                               -1.394 0.163488
## neighborhoodTimber -7.961e-03
                                   3.038e-02
                                               -0.262 0.793334
## neighborhoodVeenker 7.861e-04
                                   4.237e-02
                                                0.019 0.985203
## condition1
                       -6.247e-02
                                   8.898e-03
                                               -7.021 3.52e-12 ***
## housestyle
                       -2.056e-02
                                   8.193e-03
                                               -2.509 0.012225
                        5.533e-02
## overallqual
                                   3.589e-03
                                               15.416
                                                       < 2e-16 ***
## overallcond
                        3.846e-02
                                   2.785e-03
                                               13.807
                                                       < 2e-16 ***
## masvnrtype
                       -1.728e-02
                                   7.764e-03
                                               -2.225 0.026240 *
## masvnrarea
                        5.635e-05
                                   2.168e-05
                                                2.600 0.009427 **
                        4.829e-02
                                               4.886 1.16e-06 ***
## bsmtexposure
                                   9.884e-03
## bsmtfinsf2
                        7.537e-05
                                   1.699e-05
                                                4.436 9.92e-06 ***
## bsmtunfsf
                        7.087e-05
                                   9.969e-06
                                                7.109 1.90e-12 ***
## heatingqc
                        2.446e-02
                                   6.350e-03
                                                3.852 0.000123 ***
```

-3.242 0.001216 **

-4.341 1.53e-05 ***

-1.402e-02 4.323e-03

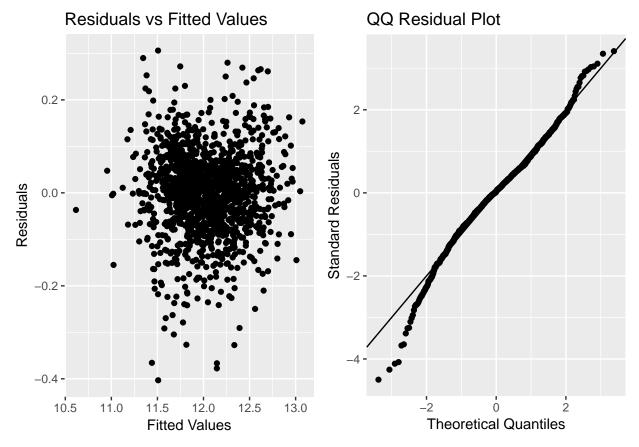
1.311e-02

-5.691e-02

bedroomabvgr

kitchenabvgr

```
## kitchengual
                       4.200e-02 5.777e-03 7.271 6.06e-13 ***
## functional
                       7.553e-02 1.106e-02 6.829 1.30e-11 ***
## garagecars
                       4.874e-02 4.886e-03 9.976 < 2e-16 ***
                      7.433e-05 2.190e-05 3.394 0.000710 ***
## wooddecksf
## salecondition
                       6.082e-04 6.992e-03
                                             0.087 0.930696
## soldminusbuilt
                      -2.300e-03 2.135e-04 -10.771 < 2e-16 ***
## summertime
                       1.908e-02 5.014e-03
                                            3.806 0.000148 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09077 on 1325 degrees of freedom
## Multiple R-squared: 0.9412, Adjusted R-squared: 0.9392
## F-statistic: 471.6 on 45 and 1325 DF, p-value: < 2.2e-16
ks.test(endmodel$residuals, pnorm, mean(endmodel$residuals),
       sd(endmodel$residuals))
##
##
   One-sample Kolmogorov-Smirnov test
##
## data: endmodel$residuals
## D = 0.04419, p-value = 0.009455
## alternative hypothesis: two-sided
ncvTest(endmodel)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 3.09348 Df = 1
                                    p = 0.07860654
resid_df <- data_frame(res = endmodel$residuals)</pre>
r1 <- ggplot(endmodel, aes(.fitted, .resid)) + geom_point() + xlab("Fitted Values") + ylab("Residuals")
 ggtitle("Residuals vs Fitted Values")
r2 <- ggplot(endmodel, aes(qqnorm(.stdresid)[[1]], .stdresid)) + geom_point(na.rm = T) +geom_abline(int
 ylab("Standard Residuals") + ggtitle("QQ Residual Plot")
grid.arrange(r1,r2,ncol=2)
```



Checking with LASSO if any variables to remove. Although LASSO recommends to delete bsmtunsf and bedroomabvgr, removing them lowers the R squared so I will keep them. Many of the neighborhoods are in fact significant so I will leave the non-significant levels in the model anyway.

```
lassorefactor <- function(){</pre>
x <- model.matrix(saleprice ~ ., data = house4)[,-1]</pre>
y <- house$saleprice
train <- sample(1:nrow(x), nrow(x) / 2)</pre>
test <- (-train)
y.train <- y[train]</pre>
y.test <- y[test]</pre>
grid.lambda <- 10^seq(10, -2, length = 100)
lasso.model <- glmnet(x, y, alpha = 1, lambda = grid.lambda)</pre>
 cv.out <- cv.glmnet(x[train,], y.train, alpha = 1)</pre>
best.lambda <- cv.out$lambda.min</pre>
lasso.pred <- predict(lasso.model, s = best.lambda, newx = x[test,])</pre>
mspe.lasso <- mean((lasso.pred - y.test)^2)</pre>
final.model <- glmnet(x, y, alpha = 1, lambda = best.lambda)</pre>
 c <- coef(final.model)</pre>
 ind <- which(c==0)</pre>
variables <- row.names(c)[ind]</pre>
return(variables)
lassorefactor()
```

```
## [1] "neighborhoodClearCr" "neighborhoodGilbert" "neighborhoodSawyerW"
## [4] "bedroomabvgr"
Thus, our final model includes the following variables:
names (house4)
   [1] "lotarea"
##
                         "neighborhood"
                                          "condition1"
                                                            "housestyle"
    [5] "overallqual"
                         "overallcond"
                                          "masvnrtype"
                                                            "masvnrarea"
                         "bsmtfinsf1"
                                                            "bsmtunfsf"
##
  [9] "bsmtexposure"
                                          "bsmtfinsf2"
                                                            "kitchenabvgr"
## [13] "heatingqc"
                         "grlivarea"
                                          "bedroomabvgr"
## [17] "kitchengual"
                         "functional"
                                          "garagecars"
                                                            "wooddecksf"
## [21] "salecondition"
                         "saleprice"
                                          "soldminusbuilt" "summertime"
signif_var <- house4 %>% select(-neighborhood) %>%
  sapply(function(x) abs(cor(x,house4$saleprice)))
signif_var[signif_var >= 0.5]
##
                                                                     saleprice
      overallqual
                       grlivarea
                                    kitchenqual
                                                     garagecars
##
        0.8139162
                       0.7040733
                                      0.6839348
                                                      0.6644831
                                                                     1.0000000
## soldminusbuilt
        0.5643897
summary(lm(log(saleprice)~log(grlivarea) +kitchenqual +garagecars + soldminusbuilt + overallqual, data
##
## Call:
  lm(formula = log(saleprice) ~ log(grlivarea) + kitchenqual +
       garagecars + soldminusbuilt + overallqual, data = house4)
##
##
## Residuals:
                       Median
        Min
                  1Q
                                    3Q
## -0.72057 -0.08846 0.00827 0.09281 0.50344
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
                   8.3028926 0.0978166 84.882
## (Intercept)
                                                  <2e-16 ***
## log(grlivarea) 0.3981633 0.0154317 25.802
                                                   <2e-16 ***
## kitchenqual
                                         9.825
                   0.0798272 0.0081253
                                                   <2e-16 ***
## garagecars
                   0.0745408 0.0070373 10.592
                                                   <2e-16 ***
## soldminusbuilt -0.0022689
                              0.0001713 -13.243
                                                   <2e-16 ***
## overallqual
                   0.0823967 0.0047311 17.416
                                                  <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1469 on 1454 degrees of freedom
## Multiple R-squared: 0.8404, Adjusted R-squared: 0.8399
## F-statistic: 1532 on 5 and 1454 DF, p-value: < 2.2e-16
```

Part I: Explanatory Modeling

TASK 1

The five most relevant features that are most relevant in determining a house's sale price are overallqual, grlivarea, kitchenqual, garagecars, and soldminusbuilt. The fifth variable, soldminusbuilt is equal to yearsold - yearbuilt.

TASK 2

```
morty<- read_csv("Morty.txt", col_types = cols())
## Warning: Missing column names filled in: 'X1' [1]</pre>
```

Function to transform TEST DATA accordingly. Please run the function transform() and provide the data frame to the argument

```
transform <- function(df){</pre>
  names(df) <- tolower(names(df))</pre>
  df[is.na(df)] <- "None"</pre>
  df$soldminusbuilt <- (df$yrsold - df$yearbuilt)</pre>
  df$summertime <- (df$mosold %in% 5:7) * 1
  df$saletype <- (df$saletype == 'New') * 1</pre>
  df %<>% select(intersect(names(df), names(house4)))
  df$condition1 <- (df$condition1 == "Artery" |</pre>
      df$condition1 =="Feedr" | df$condition1 == "RRAe")*1
  df$housestyle <- (df$housestyle == "2Story" |</pre>
                      df$housestyle == "2.5Fin")*1
  df$masvnrtype <- (df$masvnrtype != "None") * 1</pre>
  df$bsmtexposure <- (df$bsmtexposure == "Gd") * 1</pre>
  df$heatingqc <- as.numeric(factor(df$heatingqc,</pre>
  levels = c("Po", "Fa", "TA", "Gd", "Ex"), labels = 1:5))
  df$kitchenqual <- as.numeric(factor(df$kitchenqual,</pre>
    levels = c("Po", "Fa", "TA", "Gd", "Ex"), labels = 1:5))
  df$functional <- (df$functional == "Typ") * 1</pre>
  df$salecondition <- (df$salecondition == "Normal") * 1</pre>
  return(df)
morty2 <- transform(morty)</pre>
```

morty2 is our transformed data. Note that it only has 25 variables

```
confmorty <- exp(predict(endmodel, morty2, interval = "confidence", level = 0.95))
confmorty %>% knitr::kable()
```

fit	lwr	upr
184979.6	173363.4	197374.1

```
morty_stat <- as.numeric(unlist(morty2))</pre>
## Warning: NAs introduced by coercion
names(morty stat) <- names(morty2)</pre>
mean_stat <- sapply(house4, function(x) round(mean(x)))</pre>
## Warning in mean.default(x): argument is not numeric or logical: returning
## NA
morty_stat
##
          lotarea
                     neighborhood
                                       condition1
                                                       housestyle
                                                                       overallqual
##
            14115
                                NA
      overallcond
                                                     bsmtexposure
##
                       masvnrtype
                                       masvnrarea
                                                                        bsmtfinsf1
##
                                                                               732
                 5
                                 0
                                                 0
                                                                 0
##
       bsmtfinsf2
                        bsmtunfsf
                                                                      bedroomabvgr
                                        heatingqc
                                                         grlivarea
##
                                64
                                                 5
                                                              1362
                                                                                 1
     kitchenabvgr
##
                      kitchenqual
                                       functional
                                                        garagecars
                                                                        wooddecksf
##
                                 3
                                                                 2
                                                                                40
                                                 1
##
    salecondition
                        saleprice soldminusbuilt
                                                        summertime
                            143000
##
                                                16
                                                                 0
mean_stat
##
          lotarea
                     neighborhood
                                        condition1
                                                       housestyle
                                                                       overallqual
##
            10517
                                NA
                                                                 Ω
##
      overallcond
                                                                        bsmtfinsf1
                       masvnrtype
                                       masvnrarea
                                                      bsmtexposure
##
                 6
                                 Λ
                                               103
                                                                 0
                                                                               444
##
       bsmtfinsf2
                        bsmtunfsf
                                        heatingqc
                                                         grlivarea
                                                                      bedroomabvgr
                               567
                                                                                 3
##
                47
                                                              1515
                                                 1
                                                        garagecars
##
                      kitchenqual
                                                                        wooddecksf
     kitchenabvgr
                                       functional
##
                                                                 2
                                                                                94
                                                 1
##
    salecondition
                        saleprice soldminusbuilt
                                                        summertime
##
                            179429
                                                37
                 1
(improve <- house4 %>% select(-neighborhood,-saleprice, -soldminusbuilt) %>% sapply(function(x) abs(co
##
     overallqual
                                   kitchenqual
                      grlivarea
                                                   garagecars
                                                                  masvnrarea
##
      0.81391623
                     0.70407328
                                    0.68393477
                                                   0.66448314
                                                                  0.48291550
##
       heatingqc
                     masvnrtype
                                    bsmtfinsf1
                                                   wooddecksf
                                                                bsmtexposure
##
      0.45005133
                     0.40263049
                                    0.38773336
                                                   0.31860765
                                                                  0.28115148
##
      housestyle
                      bsmtunfsf
                                                               bedroomabvgr
                                       lotarea
                                                   condition1
##
      0.26211349
                     0.23892820
                                    0.21090804
                                                   0.18636758
                                                                  0.16497266
##
  salecondition
                 kitchenabvgr
                                    functional
                                                  overallcond
                                                                  summertime
      0.15906379
                     0.14059313
                                    0.12559098
                                                   0.10965141
                                                                  0.03892390
##
##
      bsmtfinsf2
```

##

0.02147044

improve	%>%	knitr:	:kable()
---------	-----	--------	----------

overallqual	0.8139162
grlivarea	0.7040733
kitchenqual	0.6839348
garagecars	0.6644831
masvnrarea	0.4829155
heatingqc	0.4500513
masvnrtype	0.4026305
bsmtfinsf1	0.3877334
wooddecksf	0.3186077
bsmtexposure	0.2811515
housestyle	0.2621135
bsmtunfsf	0.2389282
lotarea	0.2109080
condition1	0.1863676
bedroomabvgr	0.1649727
salecondition	0.1590638
kitchenabvgr	0.1405931
functional	0.1255910
overallcond	0.1096514
summertime	0.0389239
bsmtfinsf2	0.0214704

overallqual and kitchenqual are in the top 3 for correlation with saleprice. grlivarea is difficult/nearly impossible to improve so we will move on to the next variable. masvnrarea and heatingqc are fairly close. We see that Morty already has the highest heatingqc possible so masvnrarea should be considered.

Conclusion: Morty should try to improve the overallqual, which is the overall material and finish of the house. This may mean repainting some areas on the house to make it look nicer. Morty currently has a rating of 5 out 10 (average rating is 6 out of 10) so there is definitely room for improvement. Next, Morty should improve kitchenqual, which is kitchen quality. Maybe, there can be some remodeling done or fixing anything that is either old, or possibly broken. Morty has a rating of 3 out of 5 compared to the average rating of 4 out of 5. Finally, he can increase masvnrarea. He currently does not have a masonary veneer so he can consider building one because he might be able to make a profit from it.

We believe that Morty can sell his house for a maximum of 197,374.1. The 95 % confidence interval goes from 184,979.6 to 197,374.1 with an average of 173,363.4.

Part II Predictive Modeling

Ordinary Least Squares

Define the function to generate models for ridge, lasso and elastic net

```
model_func <- function(input_data, input_alpha){</pre>
set.seed(1)
x <- model.matrix(saleprice ~ ., data = input_data)[,-1]</pre>
y <- house$saleprice
train <- sample(nrow(house)*.8)</pre>
test <- (-train)</pre>
y.train <- y[train]</pre>
y.test <- y[test]</pre>
grid.lambda \leftarrow 10^{\circ}seq(10, -2, length = 100)
model.train <- glmnet(x[train, ], y.train, alpha = input_alpha, lambda = grid.lambda)</pre>
set.seed(1)
cv.out <- cv.glmnet(x[train,], y.train, alpha = input_alpha)</pre>
best.lambda <- cv.out$lambda.min</pre>
pred <- predict(model.train, s = best.lambda, newx = x[test,])</pre>
mspe <- mean((pred - y.test)^2)</pre>
final.model <- glmnet(x, y, alpha = input_alpha, lambda = best.lambda)</pre>
c <- coef(final.model)</pre>
return(c(mspe, final.model))
}
```

Ridge regression model, λ set at 0

prettyNum(lasso_mspe, big.mark = ",")

```
ridge_result <- model_func(house4,0)
ridge_mspe <- ridge_result[1]
prettyNum(ridge_mspe, big.mark = ",")

##
## "1,703,267,895"

lasso regression model, lambda set at 1
lasso_result <- model_func(house4,1)
lasso_mspe <- lasso_result[1]</pre>
```

```
##
## "1,811,789,005"
```

elastic net regression, lambda set at 0.5

```
elastic_result <- model_func(house4,0.5)
elastic_mspe <- elastic_result[1]
prettyNum(elastic_mspe, big.mark = ",")</pre>
```

```
## "1,807,381,275"
```

 λ is chosen to determine whether we are performing Ridge ($\lambda = 0$), Lasso ($\lambda = 1$), Elastic Net ($\lambda = 0.5$). The tuning parameters in the respective models is chosen via cross validation after trying 100 different ones.

```
help(cv.glmnet)
```

Justification

Our ridge model performed the best and has the lowest MSPE. This makes sense, given that our data is very sparse, containing many zeros.

```
countzero <- function(x){
  sum(x==0)
}
sapply(house4, function(x) countzero(x))</pre>
```

##	lotarea	neighborhood	condition1	housestyle	overallqual
##	0	0	1320	1007	0
##	overallcond	${\tt masvnrtype}$	masvnrarea	bsmtexposure	bsmtfinsf1
##	0	872	869	1326	467
##	bsmtfinsf2	bsmtunfsf	heatingqc	grlivarea	bedroomabvgr
##	1293	118	719	0	6
##	kitchenabvgr	kitchenqual	functional	garagecars	wooddecksf
##	1	0	100	81	761
##	salecondition	saleprice	soldminusbuilt	summertime	
##	262	0	64	769	

Many of these are boolean variables, but we can see that masvnrarea, bsmtfinsf, bsmtfinsf2, and bsmtunsf all have zeros. We chose all of these variables because we found them to be statistically significant in our model.

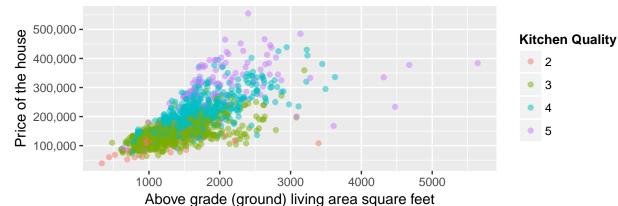
house4 %>% select(-neighborhood) %>% sapply(function(x) abs(cor(x, house4\$saleprice))) %>% sort(decreas

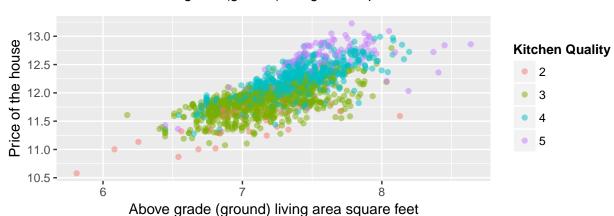
##	saleprice	overallqual	grlivarea	kitchenqual	garagecars
##	1.00000000	0.81391623	0.70407328	0.68393477	0.66448314
##	soldminusbuilt	masvnrarea	heatingqc	${\tt masvnrtype}$	bsmtfinsf1
##	0.56438969	0.48291550	0.45005133	0.40263049	0.38773336
##	wooddecksf	bsmtexposure	housestyle	bsmtunfsf	lotarea
##	0.31860765	0.28115148	0.26211349	0.23892820	0.21090804
##	condition1	bedroomabvgr	salecondition	kitchenabvgr	functional
##	0.18636758	0.16497266	0.15906379	0.14059313	0.12559098
##	overallcond	summertime	bsmtfinsf2		
##	0.10965141	0.03892390	0.02147044		

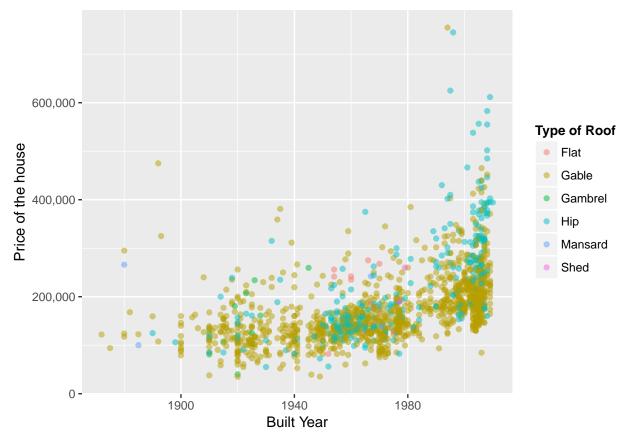
Some variables have more impact than others but nevertheless they are statistically significant in our model so we keep them. Three of these variables are generated from other variables. We created summertime partly because of common sense and after plotting the distribution of houses being sold by month, we saw a peak

in the summer months. This makes sense practically because people tend to have more time during the summer and thus are more likely to buy a house. Secondly, we created soldminusbuilt because we felt that the difference between yearsold and yearbuilt is more useful together rather than seperately. The third variable we created is a boolean for saletype to indicate a house that was "just constructed and sold", which from a common sense perspective, can make the house go much higher. Many of the variables are condensed into smaller levels. Many levels have very few observations so we feel they are not significant enough to have their own level. This helps to prevent overfitting when predicting new values. We chose to not have too many variables in our model to also prevent overfitting. We confirmed the validity of our variables through LASSO regression. Lasso didn't really eliminate any variables, which supports the statistical signifiance of our predictors.

Exploratory Data Analysis







ggsave("plot2.png")

Saving 6.5×4.5 in image

Getting all of the numeric variables.

```
house_numeric <- house4[,sapply(house4,function(x) is.numeric(x))]
house_numeric %<>% select(saleprice, everything())
#install.packages("ggcorrplot")

cor_matrix <- cor(house_numeric)

ggcorrplot(cor_matrix, type = "lower", outline.col = "white", insig = "blank")</pre>
```

