

# Finite-State Machines

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# Overview

- ▶ Debugging with waveforms
- ▶ Fun with counters
- ▶ Finite-state machines
- ▶ Collection with Vec

# Organization and Lab Work

- ▶ Look into files at DTU Learn
- ▶ Looks like it the 7-segment decoder was fine last week
- ▶ This week it will be counters to test the 7-segment display
- ▶ I am aware of that not everyone has an FPGA board
- ▶ A lot can be done with simulation and testing
- ▶ I do provide some FPGA board simulation
- ▶ But, at the end of the day I want to see a vending machine in an FPGA

# Testing with Chisel

- ▶ Set input values with `poke`
- ▶ Advance the simulation with `step`
- ▶ Read the output values with `peek`
- ▶ Compare the values with `expect`
- ▶ Import following packages:

```
import chisel3._  
import chisel3.iotesters._
```

## Using peek, poke, and expect

```
// Set input values
poke(dut.io.a, 3)
poke(dut.io.b, 4)
// Execute one iteration
step(1)
// Print the result
val res = peek(dut.io.result)
println(res)

// Or compare against expected value
expect(dut.io.result, 7)
```

# A Chisel Tester

- ▶ Extends class PeekPokeTester
- ▶ Has the device-under test (DUT) as parameter
- ▶ Testing code can use all features of Scala

```
class CounterTester(dut: Counter) extends  
    PeekPokeTester(dut) {  
  
    // Here comes the Chisel/Scala code  
    // for the testing  
}
```

# Using ScalaTest for our Tester

- ▶ Little verbose syntax
- ▶ Copy example code to start with

```
class SimpleSpec extends FlatSpec with Matchers {  
  
  "Tester" should "pass" in {  
    chisel3.iotesters.Driver(() => new  
      DeviceUnderTest()) { c =>  
      new Tester(c)  
    } should be (true)  
  }  
}
```

# Generating Waveforms

- ▶ Waveforms are timing diagrams
- ▶ Good to see many parallel signals and registers
- ▶ Additional parameters: "--generate-vcd-output", "on"
- ▶ IO signals and registers are dumped
- ▶ Generates a .vcd file
- ▶ Viewing with GTKWave or ModelSim



# A Self-Running Circuit

- ▶ SevenSegTest is a self-running circuit
- ▶ Needs no stimuli (poke)
- ▶ Just run for a few cycles
- ▶ Tester for today's lab
- ▶ This tester does NOT test the circuit
  - ▶ You are not finished when this test does not show an error

```
class SevenSegTest(dut: CountSevenSeg) extends  
    PeekPokeTester(dut) {  
    step(100)  
}
```

# Display Waveform with GTKWave

- ▶ Run the tester: `sbt test`
- ▶ Locate the `.vcd` file in `test_run_dir/SevenSegCountSpecnnn`
- ▶ Start GTKWave
- ▶ Open the `.vcd` file with
  - ▶ File – Open New Tab
- ▶ Select the circuit
- ▶ Drag and drop the interesting signals

# Call the Tester for Waveform Generation

- ▶ Using here ScalaTest
- ▶ Note `Driver.execute`
- ▶ Note `Array("--generate-vcd-output", "on")`

```
class SevenSegCountSpec extends
  FlatSpec with Matchers {
  "SevenSegTest " should "pass" in {
    chisel3.iotesters.Driver
      .execute(Array("--generate-vcd-output", "on"),
        () => new CountSevenSeg)
    { c => new SevenSegTest(c)} should be (true) }
  }
```

# Counters as Building Blocks

- ▶ Counters are versatile tools
- ▶ Count events
- ▶ Generate timing ticks
- ▶ Generate a one-shot timer

# Counting Up and Down

## ► Up:

```
val cntReg = RegInit(0.U(8.W))
```

```
cntReg := cntReg + 1.U  
when(cntReg === N) {  
  cntReg := 0.U  
}
```

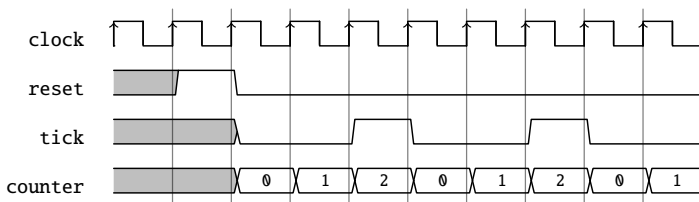
## ► Down:

```
val cntReg = RegInit(N)
```

```
cntReg := cntReg - 1.U  
when(cntReg === 0.U) {  
  cntReg := N  
}
```

# Generating Timing with Counters

- ▶ Generate a tick at a lower frequency
- ▶ We used it in Lab 1 for the blinking LED
- ▶ Use it for today's lab
- ▶ Use it for driving the display multiplexing at 1 kHz



# The Tick Generation

```
val tickCounterReg = RegInit(0.U(4.W))
val tick = tickCounterReg === (N-1).U

tickCounterReg := tickCounterReg + 1.U
when (tick) {
    tickCounterReg := 0.U
}
```

# Using the Tick

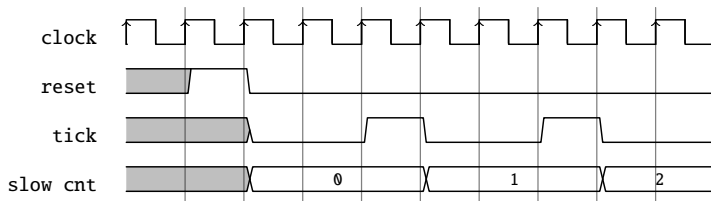
- ▶ A counter running at a *slower frequency*
- ▶ By using the tick as an enable signal

```
val lowFrequCntReg = RegInit(0.U(4.W))  
when (tick) {  
    lowFrequCntReg := lowFrequCntReg + 1.U  
}
```



# The *Slow* Counter

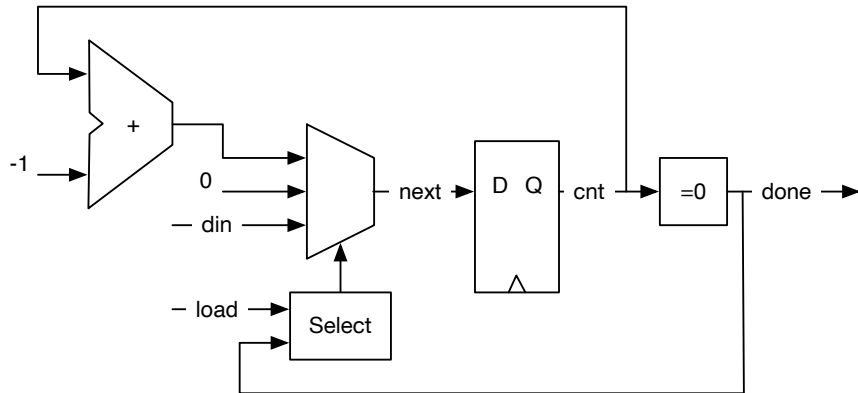
- Incremented every tick



# A Timer

- ▶ Like a kitchen timer
- ▶ Start by loading a timeout value
- ▶ Count down till 0
- ▶ Assert done when finished

# One-Shot Timer

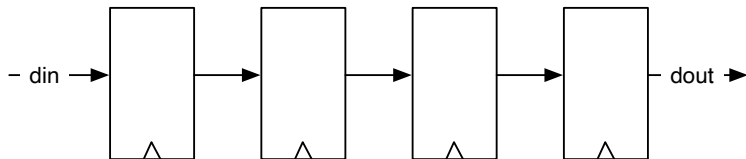


# One-Shot Timer

```
val cntReg = RegInit(0.U(8.W))
val done = cntReg === 0.U

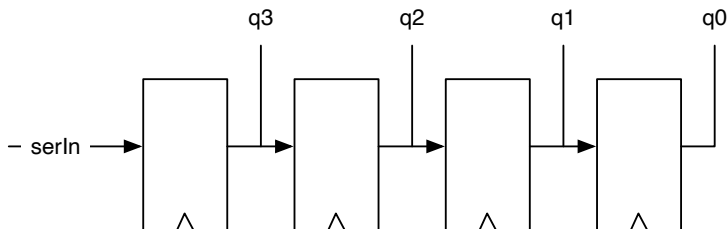
val next = WireDefault(0.U)
when (load) {
    next := din
} .elsewhen (!done) {
    next := cntReg - 1.U
}
cntReg := next
```

## A 4 Stage Shift Register



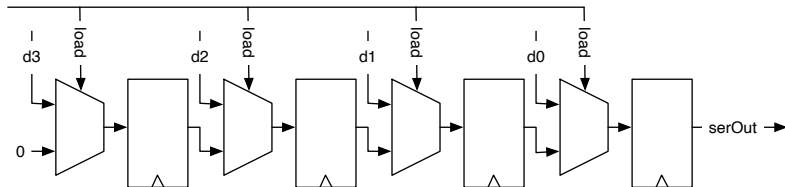
```
val shiftReg = Reg(UInt(4.W))  
shiftReg := Cat(shiftReg(2, 0), din)  
val dout = shiftReg(3)
```

## A Shift Register with Parallel Output



```
val outReg = RegInit(0.U(4.W))  
outReg := Cat(serIn, outReg(3, 1))  
val q = outReg
```

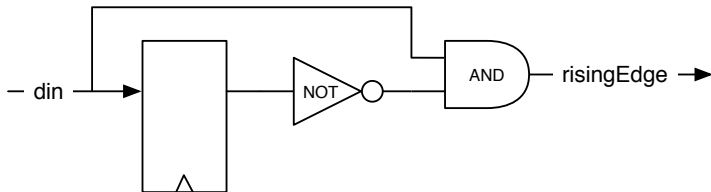
# A Shift Register with Parallel Load



```
val loadReg = RegInit(0.U(4.W))
when (load) {
  loadReg := d
} otherwise {
  loadReg := Cat(0.U, loadReg(3, 1))
}
val serOut = loadReg(0)
```

# A Simple Circuit

- ▶ What does the following circuit?
- ▶ Is this related to a finite-state machine?



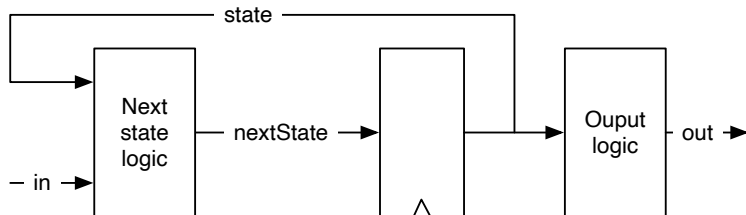


# Finite-State Machine (FSM)

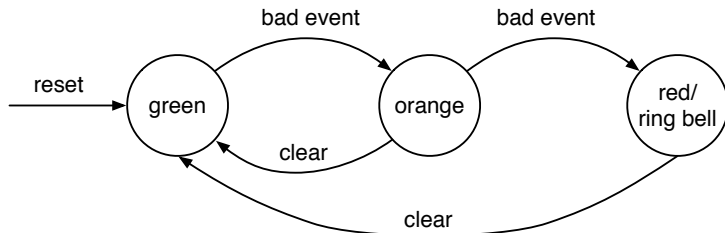
- ▶ Has a register that contains the state
- ▶ Has a function to computer the next state
  - ▶ Depending on current state and input
- ▶ Has an output depending on the state
  - ▶ And maybe on the input as well
- ▶ Every synchronous circuit can be considered a finite state machine
- ▶ However, sometimes the state space is a little bit too large

# Basic Finite-State Machine

- ▶ A state register
- ▶ Two combinational blocks



# State Diagram



- ▶ States and transitions depending on input values
- ▶ Example is a simple alarm FSM
- ▶ Nice visualization
- ▶ Will not work for large FSMs
- ▶ Complete code in the Chisel book

## State Table for the Alarm FSM

State	Input		Next state	Ring bell
	Bad event	Clear		
green	0	0	green	0
green	1	-	orange	0
orange	0	0	orange	0
orange	1	-	red	0
orange	0	1	green	0
red	0	0	red	1
red	0	1	green	1

# The Input and Output of the Alarm FSM

- ▶ Two inputs and one output

```
val io = IO(new Bundle{  
    val badEvent = Input(Bool())  
    val clear = Input(Bool())  
    val ringBell = Output(Bool())  
})
```

# Encoding the State

- ▶ We can optimize state encoding
- ▶ Two common encodings are: binary and one-hot
- ▶ We leave it to the synthesize tool
- ▶ Use symbolic names with an Enum
- ▶ Note the number of states in the Enum construct
- ▶ We use a Scala list with the `::` operator

```
val green :: orange :: red :: Nil = Enum(3)
```

# Start the FSM

- ▶ We have a starting state on reset

```
val stateReg = RegInit(green)
```

## The Next State Logic

```
switch (stateReg) {  
  is (green) {  
    when(io.badEvent) {  
      stateReg := orange  
    }  
  }  
  is (orange) {  
    when(io.badEvent) {  
      stateReg := red  
    } .elsewhen(io.clear) {  
      stateReg := green  
    }  
  }  
  is (red) {  
    when (io.clear) {  
      stateReg := green  
    }  
  }  
}
```



# The Output Logic

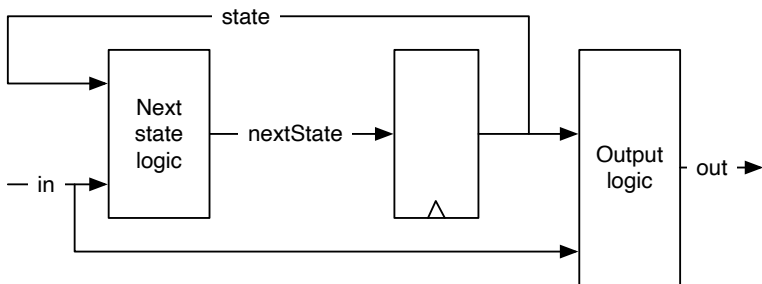
```
io.ringBell := stateReg === red
```

# Summary on the Alarm Example

- ▶ Three elements:
  1. State register
  2. Next state logic
  3. Output logic
- ▶ This was a so-called Moore FSM
- ▶ There is also a FSM type called Mealy machine

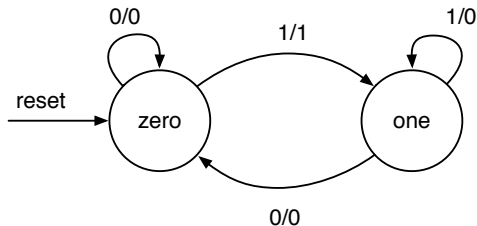
# A so-called Mealy FSM

- ▶ Similar to the former FSM
- ▶ Output also depends in the input
- ▶ It is *faster*
- ▶ Less composable (draw it)



# The Mealy FSM for the Rising Edge

- ▶ That was our starting example
- ▶ Output is also part of the transition arrows

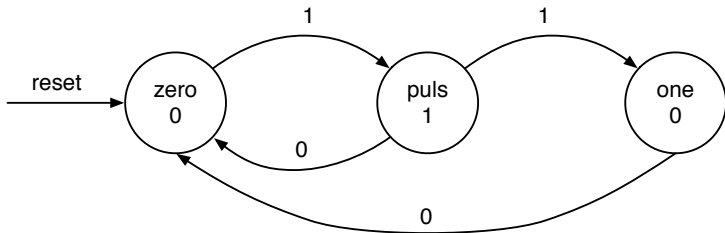


# The Mealy Solution

- ▶ Show code from the book as it is too long for slides

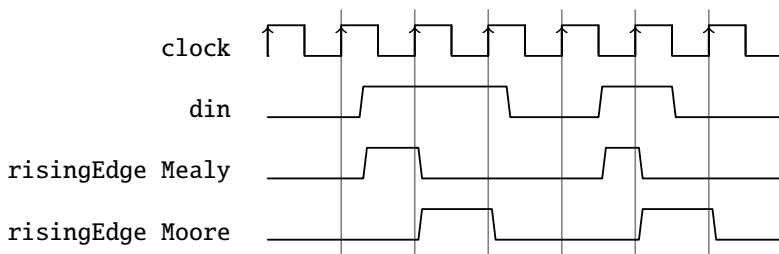
# State Diagram for the Moore Rising Edge Detection

- We need three states



# Comparing with a Timing Diagram

- Moore is delayed one clock cycle compared to Mealy



# What is Better?

- ▶ It depends ;-)
- ▶ Moore is on the save side
- ▶ More is composable
- ▶ Mealy has *faster* reaction
- ▶ Both are tools in you toolbox
- ▶ Keep it simple with your vending machine and use a Moore FSM



## Another Simple FSM

- ▶ a FSM for a single word buffer
- ▶ Just two symbols for the state machine

```
val empty :: full :: Nil = Enum(2)
```

# Finite State Machine for a Buffer

```
val empty :: full :: Nil = Enum(2)
val stateReg = RegInit(empty)
val dataReg = RegInit(0.U(size.W))

when(stateReg === empty) {
  when(io.enq.write) {
    stateReg := full
    dataReg := io.enq.din
  }
}.elsewhen(stateReg === full) {
  when(io.deq.read) {
    stateReg := empty
  }
}
```

- A simple buffer for a bubble FIFO

# A Collection of Signals with Vec

- ▶ Chisel Vec is a collection of signals of the same type
- ▶ The collection can be accessed by an index
- ▶ Similar to an array in other languages
- ▶ Wrap into a Wire() for combinational logic
- ▶ Wrap into a Reg() for a collection of registers

```
val v = Wire(Vec(3, UInt(4.W)))
```

## Using a Vec

```
v(0) := 1.U
```

```
v(1) := 3.U
```

```
v(2) := 5.U
```

```
val idx = 1.U(2.W)
```

```
val a = v(idx)
```

- ▶ Reading from an Vec is a multiplexer
- ▶ We can put a Vec into a Reg

```
val registerFile = Reg(Vec(32, UInt(32.W)))
```

An element of that register file is accessed with an index and used as a normal register.

```
registerFile(idx) := dIn
```

```
val dOut = registerFile(idx)
```

## Mixing Vecs and Bundles

- ▶ We can freely mix bundles and vectors
- ▶ When creating a vector with a bundle type, we need to pass a prototype for the vector fields. Using our `Channel`, which we defined above, we can create a vector of channels with:

```
val vecBundle = Wire(Vec(8, new Channel()))
```

- ▶ A bundle may as well contain a vector

```
class BundleVec extends Bundle {  
    val field = UInt(8.W)  
    val vector = Vec(4, UInt(8.W))  
}
```

# Today's Lab

- ▶ Driving your 7-segment decoder
- ▶ Use a counter to count from 0 to 15, driving your display
- ▶ Use another counter to generate your timing
  - ▶ We talked about this today
- ▶ You clock on the board is 100 MHz
- ▶ The given tester does only generate a waveform, no testing
- ▶ Use a different maximum count value for waveform debugging
- ▶ Then synthesize it for the FPGA
- ▶ Show a TA your working design
- ▶ Lab 6

# Summary

- ▶ Waveform testing is the way to develop/debug
- ▶ Counters are important tools, e.g., to generate timing
- ▶ Finite-state machines are another tool of the trade
- ▶ Two types: Moore and Mealy
- ▶ A Chisel Vec is the hardware version of an array