

$$\bar{z} = \pm \sqrt{1 - \left(\frac{\tilde{x}}{|\vec{y}|} \right)^2}$$