

6.6

$$\frac{(A \wedge B) \vee (A \wedge C)}{A \wedge (B \vee C)}$$

$$1. (A \wedge B) \vee (A \wedge C)$$

$$2. A \wedge B$$

$$3. A \quad \wedge \text{Elim} : 2$$

$$4. B \quad \wedge \text{Elim} : 2$$

$$5. B \vee C \quad \vee \text{Intro} : 4$$

$$6. A \wedge (B \vee C) \quad \wedge \text{Intro} : 3, 5$$

$$7. A \wedge C$$

$$8. A \quad \wedge \text{Elim} : 7$$

$$9. C \quad \wedge \text{Elim} : 7$$

$$10. B \vee C \quad \vee \text{Intro} : 9$$

$$11. A \wedge (B \vee C) \quad \wedge \text{Intro} : 8, 10$$

$$12. A \wedge (B \vee C) \quad \vee \text{Elim} : 1, 2 \sim 6, 7 \sim 11$$

$$(a=b) \vee (a=c)$$

$$(Cube(b) \wedge Cube(c))$$

$$Cube(a)$$

$$1. (a=b) \vee (a=c)$$

$$2. Cube(b) \wedge Cube(c)$$

$$3. Cube(b) \quad \wedge E \text{lim: } 2$$

$$4. a=b \quad \vee E \text{lim: } 1$$

$$5. Cube(a) \quad = E \text{lim: } 3, 4$$

$$6. a=c \quad \vee E \text{lim: } 1$$

$$7. Cube(c) \quad \wedge E \text{lim: } 2$$

$$8. Cube(a) \quad = E \text{lim: } 6, 7$$

$$9. Cube(a) \quad \vee E \text{lim: } 1, 2, 3-5, 6-8$$