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1.

 $A \cdot F(a) \vee V(a)$

 $B . S(a,b) \vee S(b,a)$

 $C \cdot \sim F(c)6V(c)$

D . $(F(a)^{\sim}V(a)) \vee (\sim F(a)^{\sim}V(a))$

2.

A. Cauliflower is not a fruit and it is not a vegetable.

B. Banana is not vegetable or banana is not fruit and cauliflower is not vegetable.

C. Banana is not vegetable or not fruit, and cauliflower is a vegetable.

D. Apple is fruit and apple is sweeter than banana, or banana is fruit and banana is sweeter than apple.

3.

B.
$$\sim V(b) \ v \sim [F(b) \land V(c)]$$

C.
$$[\sim V(b) \ v \sim F(b)] \wedge V(c)$$

B and C are different because they actually have different means.

Because, B is a disjunction, so one of each left and right sides is true then the entire expression would be true.

On the contrary, C is a conjunction and it needs to have both sides true to make the expression true.

One situation (or counter example) that makes only one of the statement true is:

Banana is not a vegetable but fruit. And cauliflower is not vegetable. In this case, B will be true since the left side is true. And C is false since not both sides in B are true.