CORE
Control + Optimization Research Lab

Trust Region Policy Optimization (TRPO) & Proximal Policy Optimization (PPO)

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Outline

- Trust Region Policy Optimization (TRPO)
  - Learning process
  - Hyperparameter
  - Main loop
  - Train model
  - Train & TensorboardX
  - Learning curve & Test
- Proximal Policy Optimization (PPO)
  - Train model
- TRPO vs. PPO - Learning curve

Trust Region Policy Optimization (TRPO)

- TRPO Algorithm

Algorithm 1 Trust Region Policy Optimization

Input: initial policy parameters θ_0, initial value function parameters ϕ_0

Hyperparameters: KL-divergence limit δ, backtracking coefficient α, maximum number of backtracking steps K

for $k = 0, 1, 2, \ldots$ **do**

Collect set of trajectories $\mathcal{D}_k = \{\tau_i\}$ by running policy $\pi_k = \pi(\theta_k)$ in the environment.

Compute rewards-to-go $\hat{R}_t$.

Compute advantage estimates, $\hat{A}_t$ (using any method of advantage estimation) based on the current value function V_{ϕ_k}.

Estimate policy gradient as

$$\hat{g}_k = \frac{1}{|\mathcal{D}_k|} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^{T} \nabla_\theta \log \pi_\theta(a_t|s_t)|_{\theta_k} \hat{A}_t.$$

Use the conjugate gradient algorithm to compute

$$\hat{x}_k \approx \hat{H}_k^{-1} \hat{g}_k,$$

where $\hat{H}_k$ is the Hessian of the sample average KL-divergence.

Update the policy by backtracking line search with

$$\theta_{k+1} = \theta_k + \alpha^j \sqrt{\frac{2\delta}{\hat{x}_k^T \hat{H}_k \hat{x}_k}} \hat{x}_k,$$

where $j \in \{0, 1, 2, \ldots K\}$ is the smallest value which improves the sample loss and satisfies the sample KL-divergence constraint.

Fit value function by regression on mean-squared error:

$$\phi_{k+1} = \arg\min_\phi \frac{1}{|\mathcal{D}_k| T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^{T} \left(V_\phi(s_t) - \hat{R}_t \right)^2,$$

typically via some gradient descent algorithm.

end for

source : https://spinningup.openai.com/en/latest/algorithms/trpo.html

Trust Region Policy Optimization (TRPO)

- Learning process
  1. 상태에 따른 행동 선택
  2. 환경에서 선택한 행동으로 한 time step을 진행한 후, 다음 상태와 보상을 받음
  3. Sample (s, a, r)을 trajectories set에 저장
  4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
     - Step 1 : Return 구하기
     - Step 2 : Critic network 업데이트
     - Step 3 : Surrogate loss를 통해 actor loss의 gradient 구하기
     - Step 4 : Conjugate gradient method를 통해 search direction 구하기
     - Step 5 : Step size와 maximal step 구하기
     - Step 6 : Backtracking line search를 통해 trust region안에서 actor network 업데이트

Trust Region Policy Optimization (TRPO)

- Actor network

```
4   class Actor(nn.Module):
5       def __init__(self, state_size, action_size, args):
6           super(Actor, self).__init__()
7           self.fc1 = nn.Linear(state_size, args.hidden_size)
8           self.fc2 = nn.Linear(args.hidden_size, args.hidden_size)
9           self.fc3 = nn.Linear(args.hidden_size, action_size)
10
11      def forward(self, x):
12          x = torch.tanh(self.fc1(x))
13          x = torch.tanh(self.fc2(x))
14
15          mu = self.fc3(x)
16          log_std = torch.zeros_like(mu)
17          std = torch.exp(log_std)
18
19          return mu, std
```

Trust Region Policy Optimization (TRPO)

- Actor network

```python
class Actor(nn.Module):
    def __init__(self, state_size, action_size, args):
        super(Actor, self).__init__()
        self.fc1 = nn.Linear(state_size, args.hidden_size)
        self.fc2 = nn.Linear(args.hidden_size, args.hidden_size)
        self.fc3 = nn.Linear(args.hidden_size, action_size)

    def forward(self, x):
        x = torch.tanh(self.fc1(x))
        x = torch.tanh(self.fc2(x))

        mu = self.fc3(x)
        log_std = torch.zeros_like(mu)
        std = torch.exp(log_std)

        return mu, std
```

The number of parameters

Layer	Weight	Bias
1	$3 \times 64 = 192$	64
2	$64 \times 64 = 4096$	64
3	$64 \times 1 = 64$	1
Sum	4352	129
Total	4481	

Trust Region Policy Optimization (TRPO)

- Critic network

```
21  class Critic(nn.Module):
22      def __init__(self, state_size, args):
23          super(Critic, self).__init__()
24          self.fc1 = nn.Linear(state_size, args.hidden_size)
25          self.fc2 = nn.Linear(args.hidden_size, args.hidden_size)
26          self.fc3 = nn.Linear(args.hidden_size, 1)
27
28      def forward(self, x):
29          x = torch.tanh(self.fc1(x))
30          x = torch.tanh(self.fc2(x))
31          value = self.fc3(x)
32
33          return value
```

Learning process

1. 상태에 따른 행동 선택

```
156                 mu, std = actor(torch.Tensor(state))
157                 action = get_action(mu, std)
```

train.py

```
5   def get_action(mu, std):
6       normal = Normal(mu, std)
7       action = normal.sample()
8
9       return action.data.numpy()
```

utils.py

- Normal(Gaussian) distribution example

```
mu = torch.Tensor([1,  0, -1])
std = torch.Tensor([1., 1., 1.])

from torch.distributions import Normal
normal = Normal(mu, std)
```

```
x = normal.sample()
print(x)
'''
tensor([-0.2713,  0.3903, -0.1373])
'''
```

Learning process

1. 상태에 따른 행동 선택

```
156                 mu, std = actor(torch.Tensor(state))
157                 action = get_action(mu, std)
```

train.py

```
5   def get_action(mu, std):
6       normal = Normal(mu, std)
7       action = normal.sample()
8
9       return action.data.numpy()
```

utils.py

- Normal(mu, std)
  - Normal(Gaussian) distribution에서 sampling을 할 경우, 분산을 일정하게 유지하면서 지속적인 exploration이 가능
  - std를 1로 고정함으로써 일정한 폭을 가지는 normal distribution에서 sampling

Learning process

2. 환경에서 선택한 행동으로 한 time step을 진행한 후, 다음 상태와 보상을 받음

```
159                 next_state, reward, done, _ = env.step(action)
```

3. Sample (s, a, r)을 trajectories set에 저장

```
139             trajectories = deque()
```

```
161                 mask = 0 if done else 1
162
163                 trajectories.append((state, action, reward, mask))
```

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 1 : Return 구하기
     - time step 6까지 진행하고 episode가 끝났을 경우를 가정

$$G_1 = R_2 + \gamma R_3 + \gamma^2 R_4 + \gamma^3 R_5 + \gamma^4 R_6$$

$$G_2 = R_3 + \gamma R_4 + \gamma^2 R_5 + \gamma^3 R_6$$

$$G_3 = R_4 + \gamma R_5 + \gamma^2 R_6$$

$$G_4 = R_5 + \gamma R_6$$

$$G_5 = R_6$$

     - 거꾸로 계산하며 계산해놓은 return값을 이용

$$G_5 = R_6$$

$$G_4 = R_5 + \gamma G_5$$

$$G_3 = R_4 + \gamma G_4$$

$$G_2 = R_3 + \gamma G_3$$

$$G_1 = R_2 + \gamma G_2$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 1 : Return 구하기
     - 거꾸로 계산하며 계산해놓은 return값을 이용

$$G_5 = R_6$$

$$G_4 = R_5 + \gamma G_5$$

$$G_3 = R_4 + \gamma G_4$$

$$G_2 = R_3 + \gamma G_3$$

$$G_1 = R_2 + \gamma G_2$$

utils.py

```
11  def get_returns(rewards, masks, gamma):
12      returns = torch.zeros_like(rewards)
13      running_returns = 0
14
15      for t in reversed(range(0, len(rewards))):
16          running_returns = rewards[t] + masks[t] * gamma * running_returns
17          returns[t] = running_returns
18
19      returns = (returns - returns.mean()) / returns.std()
20
21      return returns
```

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 2 : Critic network 업데이트
     - Critic Loss

$$J_V(\phi) = (V_\phi(s) - R)^2$$

Prediction Target

train.py

```
47      # ----------------------------
48      # step 2: update ciritic
49      criterion = torch.nn.MSELoss()
50
51      values = critic(torch.Tensor(states))
52      targets = returns.unsqueeze(1)
53
54      critic_loss = criterion(values, targets)
55      critic_optimizer.zero_grad()
56      critic_loss.backward()
57      critic_optimizer.step()
```

Learning process

- Optimization problem of theoretical TRPO → Surrogate objective function

$$maximize_\theta \ \mathcal{L}_{\theta_{old}}(\theta) = \mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)} A_{\pi_{\theta_{old}}}(s,a)\right]$$

$$s.t. \ \bar{D}_{KL}^{\rho_{\theta_{old}}}(\theta_{old},\theta) \le \delta$$

- But how do we solve it? → Approximation!

$$\mathcal{L}_{\theta_{old}}(\theta) \approx g^T(\theta-\theta_{old}) \qquad g \doteq \nabla_\theta \mathcal{L}_{\theta_{old}}(\theta)\,|_{\theta_{old}}$$

$$\bar{D}_{KL}^{\rho_{\theta_{old}}}(\theta_{old},\theta) \approx \frac{1}{2}(\theta-\theta_{old})^T H(\theta-\theta_{old}) \qquad H \doteq \nabla_\theta^2 \bar{D}_{KL}^{\rho_{\theta_{old}}}(\theta_{old},\theta)\,|_{\theta_{old}}$$

Learning process

- Approximate optimization problem of practical TRPO

$$maximize_{\theta} \ \ g^T(\theta - \theta_{old})$$

$$s.t. \ \frac{1}{2}(\theta - \theta_{old})^T H(\theta - \theta_{old}) \leq \delta$$

- Approximate optimization problem of practical TRPO (argmax form)

$$\theta_{k+1} = \underset{\theta}{\operatorname{argmax}}\, g^T(\theta - \theta_k)$$

$$s.t. \ \frac{1}{2}(\theta - \theta_k)^T H(\theta - \theta_k) \leq \delta$$

- Solution to approximate problem

$$\theta_{k+1} = \theta_k + \underbrace{\sqrt{\frac{2\delta}{g^T H^{-1} g}}}_{\text{Step size}} \underbrace{H^{-1} g}_{\text{Search direction}}$$

Learning process

- Solution to approximate problem

$$\theta_{k+1} = \theta_k + \underbrace{\sqrt{\frac{2\delta}{g^T H^{-1} g}} H^{-1} g}_{\text{Maximal step}}$$

- TRPO adds a modification to this update rule → Backtracking line search

$$\theta_{k+1} = \theta_k + \underbrace{\alpha^j}_{\text{Backtracking coefficient}} \sqrt{\frac{2\delta}{g^T H^{-1} g}} H^{-1} g$$

Learning process

❖ 정리

1) Get surrogate objective function

$$\mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}A_{\pi_{\theta_{old}}}(s,a)\right]$$

2) Find search direction, step size and maximal step through CGM and Hessian of KL

- Search direction : $H^{-1}g$
- Step size : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}$
- Maximal step : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$

3) Do line search on that direction inside trust region through Backtracking line search

$$\theta_{k+1}=\theta_k+\alpha^j\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 3 : Surrogate loss를 통해 actor loss의 gradient 구하기

train.py

```
59    # -----------------------------
60    # step 3: get gradient of actor loss through surrogate loss
61    mu, std = actor(torch.Tensor(states))
62    old_policy = get_log_prob(actions, mu, std)
```

utils.py

```
23    def get_log_prob(actions, mu, std):
24        normal = Normal(mu, std)
25        log_prob = normal.log_prob(actions)
26
27        return log_prob
```

- The probability density of the normal distribution

$$\pi_\theta(a|s) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(a-\mu_\theta(s))^2}{2\sigma^2}\right)$$

- Multiply the log on both sides

$$\log \pi_\theta(a|s) = -\log\sqrt{2\pi} - \log\sigma - \frac{\left(a-\mu_\theta(s)\right)^2}{2\sigma^2}$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 3 : Surrogate loss를 통해 actor loss의 gradient 구하기

train.py

```
59      # ----------------------------
60      # step 3: get gradient of actor loss through surrogate loss
61      mu, std = actor(torch.Tensor(states))
62      old_policy = get_log_prob(actions, mu, std)
63      actor_loss = surrogate_loss(actor, values, targets, states, old_policy.detach(), actions)
```

utils.py

```
29  def surrogate_loss(actor, values, targets, states, old_policy, actions):
30      mu, std = actor(torch.Tensor(states))
31      new_policy = get_log_prob(actions, mu, std)
32
33      advantages = targets - values
34
35      surrogate_loss = torch.exp(new_policy - old_policy) * advantages
36      surrogate_loss = surrogate_loss.mean()
37
38      return surrogate_loss
```

   - surrogate_loss

$$\mathcal{L}_{\theta_{old}}(\theta) = \mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)} A_{\pi_{\theta_{old}}}(s,a)\right]$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 3 : Surrogate loss를 통해 actor loss의 gradient 구하기

train.py

```
59      # ----------------------------
60      # step 3: get gradient of actor loss through surrogate loss
61      mu, std = actor(torch.Tensor(states))
62      old_policy = get_log_prob(actions, mu, std)
63      actor_loss = surrogate_loss(actor, values, targets, states, old_policy.detach(), actions)
64
65      actor_loss_grad = torch.autograd.grad(actor_loss, actor.parameters())
66      actor_loss_grad = flat_grad(actor_loss_grad)
```

   - ○ torch.autograd.grad(outputs, inputs) - actor.parameter : 4481(weight : 4352, bias : 129)

> `torch.autograd.grad(`*outputs, inputs, grad_outputs=None, retain_graph=None, create_graph=False, only_inputs=True, allow_unused=False*`)` [SOURCE]
>
> Computes and returns the sum of gradients of outputs w.r.t. the inputs.

   - example

$$y = \sum_{i=1}^{4} 3 \times x_i$$

$$\frac{\partial y}{\partial x_i} = 3$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 3 : Surrogate loss를 통해 actor loss의 gradient 구하기

train.py

```
59      # ----------------------------
60      # step 3: get gradient of actor loss through surrogate loss
61      mu, std = actor(torch.Tensor(states))
62      old_policy = get_log_prob(actions, mu, std)
63      actor_loss = surrogate_loss(actor, values, targets, states, old_policy.detach(), actions)
64
65      actor_loss_grad = torch.autograd.grad(actor_loss, actor.parameters())
66      actor_loss_grad = flat_grad(actor_loss_grad)
```

   - ○ flat_grad(actor_loss_grad)

utils.py

```
94  def flat_grad(grads):
95      grad_flatten = []
96      for grad in grads:
97          grad_flatten.append(grad.view(-1))
98      grad_flatten = torch.cat(grad_flatten)
99      return grad_flatten
```

Weight	Bias
3×64	64
64×64	64
64×1	1

Learning process

❖ 정리

1) Get surrogate objective function Clear!

$$\mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}A_{\pi_{\theta_{old}}}(s,a)\right]$$

2) Find search direction, step size and maximal step through CGM and Hessian of KL

- Search direction : $H^{-1}g$
- Step size : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}$
- Maximal step : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$

3) Do line search on that direction inside trust region through Backtracking line search

$$\theta_{k+1} = \theta_k + \alpha^j\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 4 : Conjugate gradient method를 통해 search direction 구하기

train.py

```
68      # ----------------------------
69      # step 4: get search direction through conjugate gradient method
70      search_dir = conjugate_gradient(actor, states, actor_loss_grad.data, nsteps=10)
```

Learning process

❖ 정리

1) Get surrogate objective function Clear!

$$\mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}A_{\pi_{\theta_{old}}}(s,a)\right]$$

2) Find search direction, step size and maximal step through CGM and Hessian of KL

- Search direction : $H^{-1}g$ Clear!
- Step size : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}$
- Maximal step : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$

3) Do line search on that direction inside trust region through Backtracking line search

$$\theta_{k+1}=\theta_k+\alpha^j\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 5 : Step size와 maximal step 구하기

train.py

```
72      # ----------------------------
73      # step 5: get step size and maximal step
74      gHg = (hessian_vector_product(actor, states, search_dir) * search_dir).sum(0, keepdim=True)
75      step_size = torch.sqrt(2 * args.max_kl / gHg)[0]
76      maximal_step = step_size * search_dir
```

   - Step size : $\sqrt{\frac{2\delta}{g^T H^{-1} g}}$ $(Hx = g)$, (max_kl δ : 0.01)
   - Maximal step : $\sqrt{\frac{2\delta}{g^T H^{-1} g}} H^{-1} g$

Learning process

❖ 정리

1) Get surrogate objective function Clear!

$$\mathbb{E}_{s,a\sim\pi_{\theta_{old}}}\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}A_{\pi_{\theta_{old}}}(s,a)\right]$$

2) Find search direction, step size and maximal step through CGM and Hessian of KL

- Search direction : $H^{-1}g$ Clear!
- Step size : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}$ Clear!
- Maximal step : $\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$ Clear!

3) Do line search on that direction inside trust region through Backtracking line search

$$\theta_{k+1}=\theta_k+\alpha^j\sqrt{\frac{2\delta}{g^TH^{-1}g}}H^{-1}g$$

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 6 : Backtracking line search를 통해 trust region안에서 actor network 업데이트

train.py

```
78      # ----------------------------
79      # step 6: perform backtracking line search and update actor in trust region
80      params = flat_params(actor)
```

utils.py

```
109   def flat_params(model):
110       params = []
111       for param in model.parameters():
112           params.append(param.data.view(-1))
113       params_flatten = torch.cat(params)
114       return params_flatten
```

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 6 : Backtracking line search를 통해 trust region안에서 actor network 업데이트

train.py

```
78      # ----------------------------
79      # step 6: perform backtracking line search and update actor in trust region
80      params = flat_params(actor)
81
82      old_actor = Actor(state_size, action_size, args)
83      update_model(old_actor, params)
```

utils.py

```
def update_model(model, new_params):
    index = 0
    for params in model.parameters():
        params_length = len(params.view(-1))
        new_param = new_params[index: index + params_length]
        new_param = new_param.view(params.size())
        params.data.copy_(new_param)
        index += params_length
```

```
params_length 192
params_length 64
params_length 4096
params_length 64
params_length 64
params_length 1
```

Weight	Bias
$3 \times 64 = 192$	64
$64 \times 64 = 4096$	64
$64 \times 1 = 64$	1
4352	129

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 6 : Backtracking line search를 통해 trust region안에서 actor network 업데이트

train.py

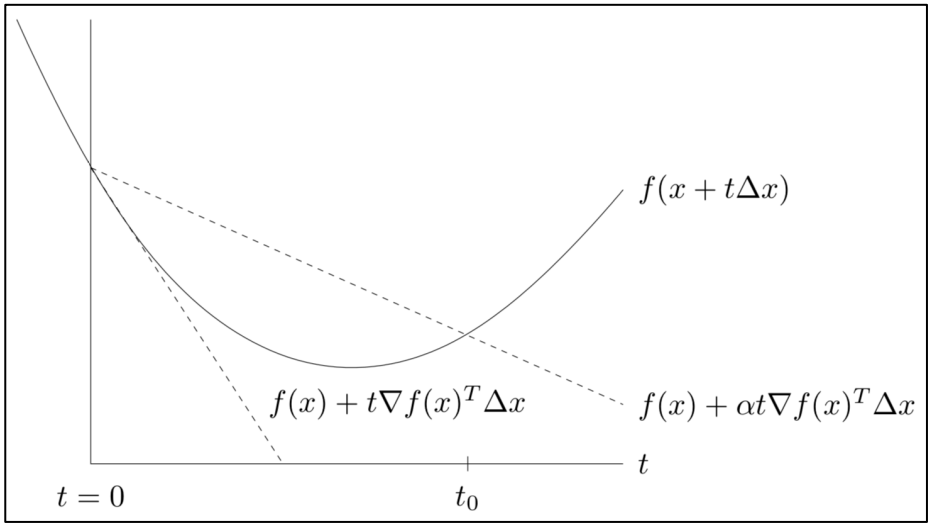
```
78      # ----------------------------
79      # step 6: perform backtracking line search and update actor in trust region
80      params = flat_params(actor)
81
82      old_actor = Actor(state_size, action_size, args)
83      update_model(old_actor, params)
84
85      backtracking_line_search(old_actor, actor, actor_loss, actor_loss_grad,
86                               old_policy, params, maximal_step, args.max_kl,
87                               values, targets, states, actions)
```

Learning process

4. 일정 sample들이 모이면 trajectories set으로 Actor & Critic network 업데이트
   - Step 6 : Actor network를 업데이트하고, backtracking line search를 통해 trust region안에서 업데이트

Algorithm 9.2 *Backtracking line search.*

given a descent direction Δx for f at $x \in \mathbf{dom}\, f$, $\alpha \in (0, 0.5)$, $\beta \in (0, 1)$.
$t := 1$.
while $f(x + t\Delta x) > f(x) + \alpha t \nabla f(x)^T \Delta x$, $\quad t := \beta t$.



source : https://web.stanford.edu/~boyd/cvxbook/bv_cvxbook.pdf

Hyperparameter

```
14    parser = argparse.ArgumentParser()
15    parser.add_argument('--env_name', type=str, default="Pendulum-v0")
16    parser.add_argument('--load_model', type=str, default=None)
17    parser.add_argument('--save_path', default='./save_model/', help='')
18    parser.add_argument('--render', action="store_true", default=False)
19    parser.add_argument('--gamma', type=float, default=0.99)
20    parser.add_argument('--hidden_size', type=int, default=64)
21    parser.add_argument('--critic_lr', type=float, default=1e-3)
22    parser.add_argument('--max_kl', type=float, default=1e-2)
23    parser.add_argument('--max_iter_num', type=int, default=500)
24    parser.add_argument('--total_sample_size', type=int, default=2048)
25    parser.add_argument('--log_interval', type=int, default=5)
26    parser.add_argument('--goal_score', type=int, default=-300)
27    parser.add_argument('--logdir', type=str, default='./logs',
28                        help='tensorboardx logs directory')
29    args = parser.parse_args()
```

Main loop

- Initialization
  - Seed - random number 고정
  - Actor network
  - TensorboardX
  - Recent rewards

```
119  def main():
120      env = gym.make(args.env_name)
121      env.seed(500)
122      torch.manual_seed(500)
123
124      state_size = env.observation_space.shape[0]
125      action_size = env.action_space.shape[0]
126      print('state size:', state_size)
127      print('action size:', action_size)
128
129      actor = Actor(state_size, action_size, args)
130      critic = Critic(state_size, args)
131      critic_optimizer = optim.Adam(critic.parameters(), lr=args.critic_lr)
132
133      writer = SummaryWriter(args.logdir)
134
135      recent_rewards = deque(maxlen=100)
136      episodes = 0
```

Main loop

- Episode 진행
  - Initialize trajectories set
  - 상태에 따른 행동 선택
  - 다음 상태와 보상을 받음
  - Trajectories set에 저장

```
138     for iter in range(args.max_iter_num):
139         trajectories = deque()
140         steps = 0
141 
142         while steps < args.total_sample_size:
143             done = False
144             score = 0
145             episodes += 1
146 
147             state = env.reset()
148             state = np.reshape(state, [1, state_size])
149 
150             while not done:
151                 if args.render:
152                     env.render()
153 
154                 steps += 1
155 
156                 mu, std = actor(torch.Tensor(state))
157                 action = get_action(mu, std)
158 
159                 next_state, reward, done, _ = env.step(action)
160 
161                 mask = 0 if done else 1
162 
163                 trajectories.append((state, action, reward, mask))
164 
165                 next_state = np.reshape(next_state, [1, state_size])
166                 state = next_state
167                 score += reward
168 
169                 if done:
170                     recent_rewards.append(score)
```

Main loop

- Train model
- Print & Visualize log
- Termination : 최근 100개의 episode의 평균 score가 -300보다 크다면
  - Save model
  - 학습 종료

```
172         actor.train(), critic.train()
173         train_model(actor, critic, critic_optimizer,
174                     trajectories, state_size, action_size)
175
176         writer.add_scalar('log/score', float(score), episodes)
177
178         if iter % args.log_interval == 0:
179             print('{} iter | {} episode | score_avg: {:.2f}'.format(iter, episodes, np.mean(recent_rewards)))
180
181         if np.mean(recent_rewards) > args.goal_score:
182             if not os.path.isdir(args.save_path):
183                 os.makedirs(args.save_path)
184
185             ckpt_path = args.save_path + 'model.pth'
186             torch.save(actor.state_dict(), ckpt_path)
187             print('Recent rewards exceed -300. So end')
188             break
```

Train model

- Trajectories → Numpy array
- Trajectories에 있는 2200개의 sample들을 각각 나눔
  - state - (2200, 3)
  - action - (2200, 1)
  - reward - (2200)
  - mask - (2200)

```
31  def train_model(actor, critic, critic_optimizer,
32                  trajectories, state_size, action_size):
33      trajectories = np.array(trajectories)
34      states = np.vstack(trajectories[:, 0])
35      actions = list(trajectories[:, 1])
36      rewards = list(trajectories[:, 2])
37      masks = list(trajectories[:, 3])
38
39      actions = torch.Tensor(actions).squeeze(1)
40      rewards = torch.Tensor(rewards).squeeze(1)
41      masks = torch.Tensor(masks)
```

Train model

- **returns** - (2200)
- **values** - (2200, 1)
- **targets** - (2200, 1)

```
43      # ----------------------------
44      # step 1: get returns
45      returns = get_returns(rewards, masks, args.gamma)
46
47      # ----------------------------
48      # step 2: update ciritic
49      criterion = torch.nn.MSELoss()
50
51      values = critic(torch.Tensor(states))
52      targets = returns.unsqueeze(1)
53
54      critic_loss = criterion(values, targets)
55      critic_optimizer.zero_grad()
56      critic_loss.backward()
57      critic_optimizer.step()
```

Train model

- old_policy - (2200, 1)
- actor_loss_grad - (4481)
- search_dir - (4481)

```
59      # ----------------------------
60      # step 3: get gradient of actor loss through surrogate loss
61      mu, std = actor(torch.Tensor(states))
62      old_policy = get_log_prob(actions, mu, std)
63      actor_loss = surrogate_loss(actor, values, targets, states, old_policy.detach(), actions)
64
65      actor_loss_grad = torch.autograd.grad(actor_loss, actor.parameters())
66      actor_loss_grad = flat_grad(actor_loss_grad)
67
68      # ----------------------------
69      # step 4: get search direction through conjugate gradient method
70      search_dir = conjugate_gradient(actor, states, actor_loss_grad.data, nsteps=10)
```

Train model

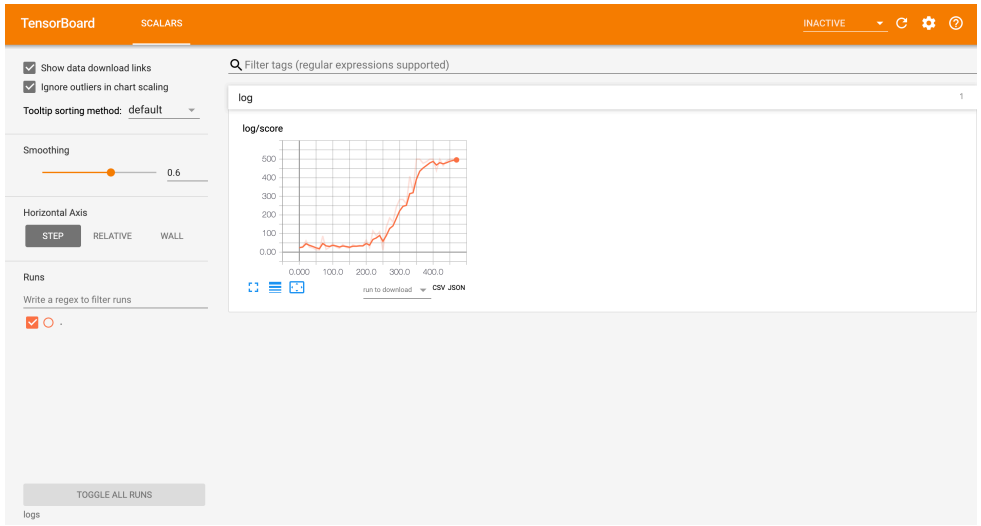
- **params** - (4481)

```
72      # ----------------------------
73      # step 5: get step size and maximal step
74      gHg = (hessian_vector_product(actor, states, search_dir) * search_dir).sum(0, keepdim=True)
75      step_size = torch.sqrt(2 * args.max_kl / gHg)[0]
76      maximal_step = step_size * search_dir
77
78      # ----------------------------
79      # step 6: perform backtracking line search and update actor in trust region
80      params = flat_params(actor)
81
82      old_actor = Actor(state_size, action_size, args)
83      update_model(old_actor, params)
84
85      backtracking_line_search(old_actor, actor, actor_loss, actor_loss_grad,
86                               old_policy, params, maximal_step, args.max_kl,
87                               values, targets, states, actions)
```

Train & TensorboardX

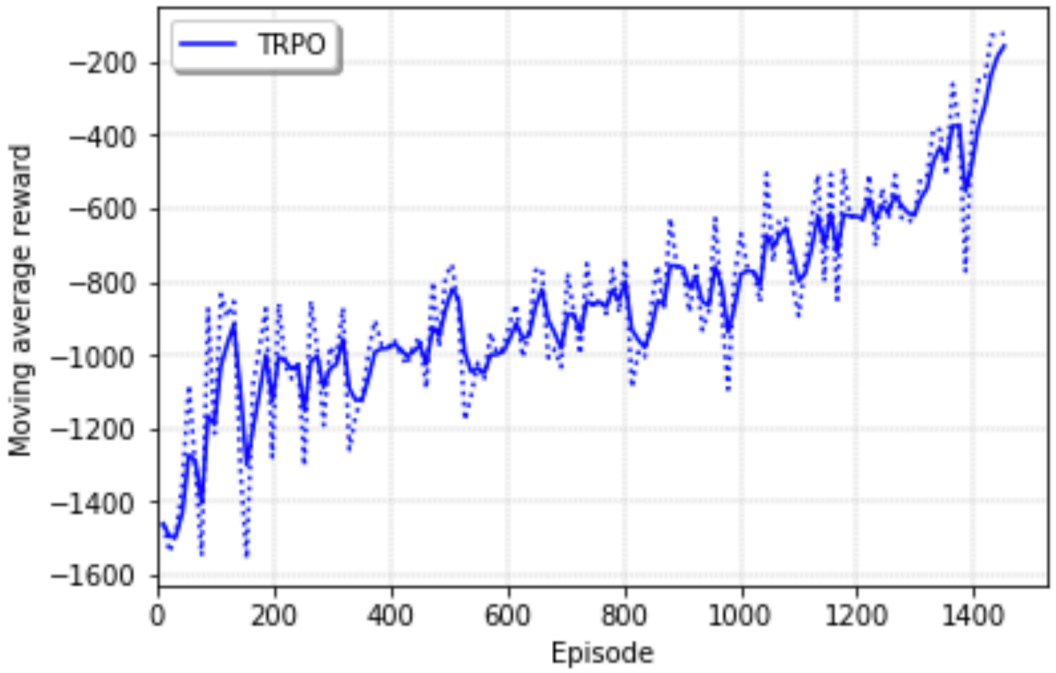
- Terminal A - train 실행
  - conda activate env_name
  - python train.py

- Terminal B - tensorboardX 실행
  - conda activate env_name
  - tensorboard --logdir logs
  - (웹에서) localhost:6006



Learning curve & Test

- Learning curve



- Test
  - ➢ python test.py

PPO - Train model

- Mini batch 형태로 Actor & Critic network 업데이트
  - Mini batch로 나누기

```
52      criterion = torch.nn.MSELoss()
53
54      n = len(states)
55      arr = np.arange(n)
56
57      for _ in range(args.model_update_num):
58          np.random.shuffle(arr)
59
60          for i in range(n // args.batch_size):
61              mini_batch_index = arr[args.batch_size * i : args.batch_size * (i + 1)]
62              mini_batch_index = torch.LongTensor(mini_batch_index)
63
64              states_samples = torch.Tensor(states)[mini_batch_index]
65              actions_samples = torch.Tensor(actions)[mini_batch_index]
```

```
args.batch_size * i 0
args.batch_size * (i + 1) 64

args.batch_size * i 64
args.batch_size * (i + 1) 128

args.batch_size * i 128
args.batch_size * (i + 1) 192

        .
        .
        .

args.batch_size * i 1984
args.batch_size * (i + 1) 2048

args.batch_size * i 2048
args.batch_size * (i + 1) 2112

args.batch_size * i 2112
args.batch_size * (i + 1) 2176
```

- n = 2200
- Batch size = 64

PPO - Train model

- Mini batch 형태로 Actor & Critic network 업데이트
  - Critic Loss

$$J_V(\phi) = (V_\phi(s) - R)^2$$

Prediction Target

```
67            # get critic loss
68            values_samples = critic(states_samples)
69            targets_samples = returns.unsqueeze(1)[mini_batch_index]
70
71            critic_loss = criterion(values_samples, targets_samples)
```

PPO - Train model

- The probability ratio $r_t(\theta)$

$$r_t(\theta) = \frac{\pi_\theta(a_t|s_t)}{\pi_{\theta_{old}}(a_t|s_t)}$$

- Surrogate objective function of TRPO

$$\mathcal{L}(\theta) = \mathbb{E}_t\left[\frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}\hat{A}_t\right] = \left[r_t(\theta)\hat{A}_t\right]$$

- Main objective function of PPO

$$\mathcal{L}^{CLIP}(\theta) = \mathbb{E}_t\left[\min\left(\ r_t(\theta)\hat{A}_t,\ \text{clip}(r_t(\theta), 1-\epsilon, 1+\epsilon)\,\hat{A}_t\ \right)\right]$$

PPO - Train model

- Mini batch 형태로 Actor & Critic network 업데이트
  - Actor Loss (clip param : 0.2)

$$J_\pi(\theta) = \min\left(r_t(\theta)\hat{A}_t,\ \text{clip}(r_t(\theta), 1-\epsilon, 1+\epsilon)\,\hat{A}_t \right)$$

```
73            # get actor loss
74            actor_loss, ratio, advantages_samples = surrogate_loss(actor, values_samples, targets_samples,
75                                                                   states_samples, old_policy.detach(),
76                                                                   actions_samples, mini_batch_index)
77
78            clipped_ratio = torch.clamp(ratio,
79                                        1.0 - args.clip_param,
80                                        1.0 + args.clip_param)
81            clipped_actor_loss = clipped_ratio * advantages_samples
82
83            actor_loss = -torch.min(actor_loss, clipped_actor_loss).mean()
```

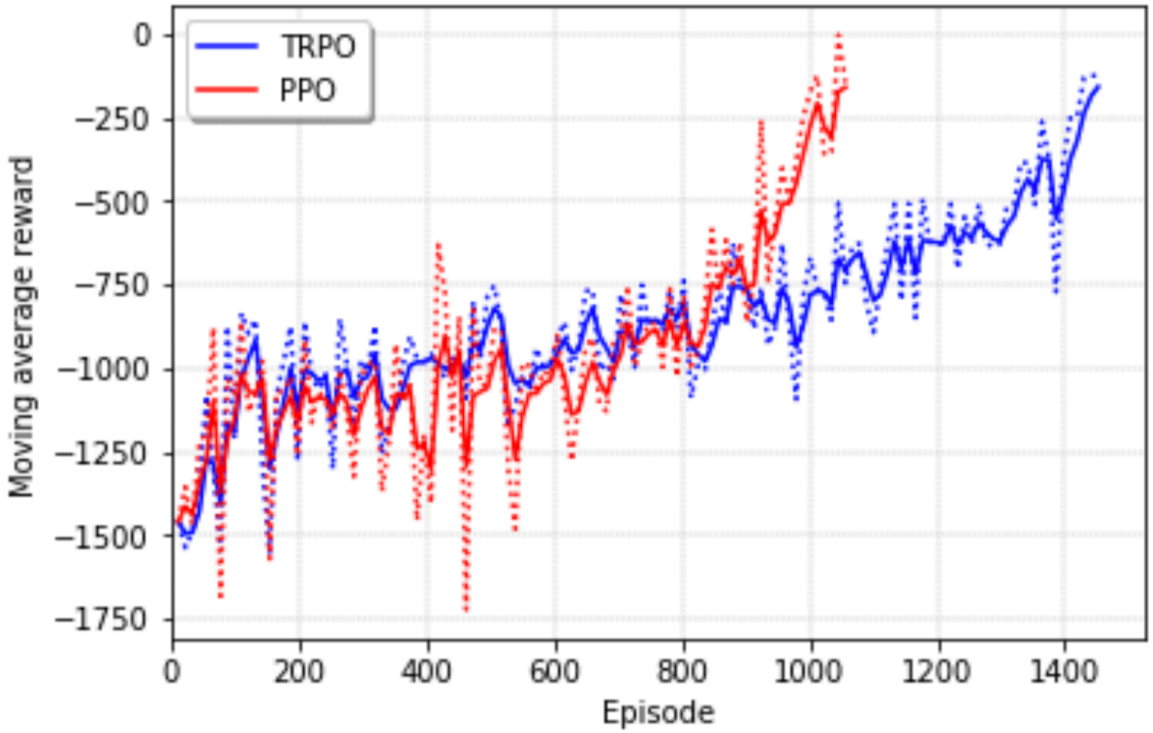
PPO - Train model

- Mini batch 형태로 Actor & Critic network 업데이트
  - Update actor & critic

```
85          # update actor & critic
86          loss = actor_loss + 0.5 * critic_loss
87
88          critic_optimizer.zero_grad()
89          loss.backward(retain_graph=True)
90          critic_optimizer.step()
91
92          actor_optimizer.zero_grad()
93          loss.backward()
94          actor_optimizer.step()
```

TRPO vs. PPO

- Learning curve



Thank you