## Supplementary document of the paper

Enforcement of Time-Constrained GMECs on Time-Colored Petri Nets

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## 1 Nomenclature

N	Colored Petri net, $N = (P, T, C, Pre, Post)$
P	Set of places of a colored Petri net
T	Set of transitions of a colored Petri net
C	Set of colors of a colored Petri net
$\mathbb{N}$	Set of non-negative integers
Pre	Pre-incidence function of a Petri net
Post	Post-incidence function of a Petri net
M	Marking of a colored Petri net
$(N, M_0)$	Colored Petri net system
$\mathcal{C}$	Incidence matrix of a colored Petri net
$M[t\rangle M'$	Transition $t$ fires at $M$ generating $M'$
$\mathcal{EN}(M)$	Set of transitions logically enabled at $M$
$M[\sigma angle$	Transition sequence $\sigma$ is sequentially enabled at $M$
$M[\sigma\rangle M'$	Transition sequence $\sigma$ fires at $M$ generating $M'$
$R(N, M_0)$	Reachable marking set of a colored Petri net system $(N, M_0)$
G	Time-colored Petri net, $G = (N, M_0, I)$
I	Time function
$\mathbb{Q}_0^+$	Set of non-negative rational numbers
c(t)	Time value associated to $t$
(M,c)	State of a time-colored Petri net
$(M,c) \xrightarrow{\delta} (M,c+\delta)$	State of a time-colored Petri net Continuous transition step
$(M,c) \xrightarrow{\delta} (M,c+\delta)$	Continuous transition step
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$	Continuous transition step  Discrete transition step
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ New(M,t)	Continuous transition step Discrete transition step Newly enabled transition set at $M$
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\phi$	Continuous transition step  Discrete transition step  Newly enabled transition set at $M$ Admissible timed trajectory
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\phi$ $\varphi$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$ $RI(G)$ $\mathcal{SC}$ $\Theta$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$ Set of all reachable markings in $G$ State class Inequality set representing the remaining firing time interval
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $T\mathcal{L}(G)$ $RI(G)$ $\mathcal{SC}$ $\Theta$ $\bar{M}$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$ Set of all reachable markings in $G$ State class Inequality set representing the remaining firing time interval $m \times o$ matrix derived from $M$
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$ $RI(G)$ $\mathcal{SC}$ $\Theta$ $\bar{M}$ $vt$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$ Set of all reachable markings in $G$ State class Inequality set representing the remaining firing time interval $m \times o$ matrix derived from $M$ C-GMEC
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$ $RI(G)$ $\mathcal{SC}$ $\Theta$ $\bar{M}$ $vt$ $\mathcal{R}(G,vt)$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$ Set of all reachable markings in $G$ State class Inequality set representing the remaining firing time interval $m \times o$ matrix derived from $M$ C-GMEC Marking set defined by $vt$
$(M,c) \xrightarrow{\delta} (M,c+\delta)$ $(M,c) \xrightarrow{t} (M',c')$ $New(M,t)$ $\varphi$ $\varphi$ $\bar{\varphi}$ $\rho$ $\mathcal{TL}(G)$ $RI(G)$ $\mathcal{SC}$ $\Theta$ $\bar{M}$ $vt$	Continuous transition step Discrete transition step Newly enabled transition set at $M$ Admissible timed trajectory Transition-time sequence logical transition sequence Logical trajectory Set of all admissible timed trajectory in $G$ Set of all reachable markings in $G$ State class Inequality set representing the remaining firing time interval $m \times o$ matrix derived from $M$ C-GMEC

 $egin{array}{lll} V & {
m time-constrained C-GMEC} \\ st & {
m Time constraint function} \\ {\cal V} & {
m time-constrained C-GMEC set} \\ \end{array}$ 

 $\mathcal{V}_{ma}$  Mandatory time-constrained C-GMEC set  $\mathcal{V}_{il}$  Illegal time-constrained C-GMEC set

 $T_{so}$  Soft transition set  $T_{st}$  Strict transition set

 $\mathcal{P}$  Parameterized modified state class graph,  $\mathcal{P} = (Q, E, f, q_0)$ 

 $egin{array}{ll} Q & & ext{Vertex set in } \mathcal{P} \\ E & & ext{Edge set in } \mathcal{P} \\ \chi & & ext{Path in } \mathcal{P} \\ \end{array}$ 

 $\chi$  Path in  $\mathcal{P}$  Set of all terminal vertices in  $\mathcal{P}$ 

 $Q^{te}(vt_{ma,s})$  Set of all mandatory vertices with respect to  $vt_{ma,s}$ 

 $Q^{te}(vt_{il,s})$  Set of all illegal vertices with respect to  $vt_{il,s}$ 

 $\chi_{te}$  Initial-to-terminal path in  $\mathcal{P}$ 

 $X_{te}$  Set of initial-to-terminal paths in  $\mathcal{P}$ 

 $\chi_{te}(vt_{ma,s})$  Initial-mandatory-terminal path with respect to  $vt_{ma,s}$ 

 $\chi_{te}(vt_{il,s})$  Initial-illegal-terminal path with respect to  $vt_{il,s}$ 

 $X_{te}(vt_{ma,s})$  Set of initial-mandatory-terminal paths with respect to  $vt_{ma,s}$ 

 $X_{te}(vt_{il,s})$  Set of initial-illegal-terminal paths with respect to  $vt_{il,s}$ 

 $\kappa(\mathcal{P})$  Edge density of  $\mathcal{P}$ 

## 2 Application of Time-Constrained C-GMEC Enforcement in a Port System

In this section, we present the detailed data of the constructed partial modified state class graph (PAMSCG) used in the case study of the paper "Enforcement of Time-Constrained GMECs on Time-Colored Petri Nets". Particularly, in Section VI of this paper, we discuss the application of the proposed time-constrained C-GMEC enforcement in a port system within the maritime domain, where the layout (shown in Fig. 3), the operational behavior, and the TCPN model (illustrated in Fig. 4) of the port system are presented.

For the enforcement of time-constrained C-GMECs, constructing the PAMSCG of the TCPN is a key step. However, due to the excessive size of the PAMSCG in this case (including 75 state classes and 35 initial-to-terminal paths) and the space limitations of the paper, we present the PAMSCG in tabular form (Tables I–III). In addition, we also record all the initial-to-terminal paths of the PAMSCG in these tables, enabling a clearer understanding of how transition sequences unfold along the paths.

Table 1: Marking information of the PAMSCG of the TCPN G in Fig. 4 of the paper

$M_0 = (1, 2, 0)p_1 + (0, 0, 1)p_6$	$M_{10} = (0, 1, 0)p_1 + (0, 1, 1)p_2 + (1, 0, 0)p_4$	
$M_1 = (0, 2, 0)p_1 + (1, 0, 0)p_2 + (0, 0, 1)p_6$	$M_{11} = (0,1,0)p_1 + (1,0,0)p_3 + (0,1,0)p_5 + (0,0,1)p_6$	
$M_2 = (1, 1, 0)p_1 + (0, 1, 1)p_2$	$M_{12} = (1,1,1)p_2 + (0,1,0)p_5$	
$M_3 = (0, 2, 0)p_1 + (1, 0, 0)p_3 + (0, 0, 1)p_6$	$M_{13} = (1,0,0)p_1 + (0,2,0)p_5 + (0,0,1)p_6$	
$M_4 = (0, 1, 0)p_1 + (1, 1, 1)p_2$	$M_{14} = (0,1,0)p_1 + (1,0,0)p_4 + (0,1,0)p_5 + (0,0,1)p_6$	
$M_5 = (1, 1, 0)p_1 + (0, 1, 0)p_5 + (0, 0, 1)p_6$	$M_{15} = (0,1,1)p_2 + (1,0,0)p_3 + (0,1,0)p_5$	
$M_6 = (0, 2, 0)p_1 + (1, 0, 0)p_4 + (0, 0, 1)p_6$	$M_{16} = (1,0,0)p_2 + (0,2,0)p_5 + (0,0,1)p_6$	
$M_7 = (0, 1, 0)p_1 + (0, 1, 1)p_2 + (1, 0, 0)p_3$	$M_{17} = (0,1,1)p_2 + (1,0,0)p_4 + (0,1,0)p_5$	
$M_8 = (0, 1, 0)p_1 + (1, 0, 0)p_2 + (0, 1, 0)p_5 + (0, 0, 1)p_6$	$M_{18} = (1,0,0)p_3 + (0,2,0)p_5 + (0,0,1)p_6$	
$M_9 = (1,0,0)p_1 + (0,1,1)p_2 + (0,1,0)p_5$	$M_{19} = (1,0,0)p_4 + (0,2,0)p_5 + (0,0,1)p_6$	

Table 2: Vertex components of the PAMSCG of the TCPN G in Fig. 4 of the paper

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(M_{16}, \{max\{0, 35 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10} - \Delta_5^{21}\} \le \theta_2 < 46 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10} - \Delta_5^{21}\})
                    (M_0, \{\hat{l}_1 \le \theta_1 < \hat{u}_1, \hat{l}_4 \le \theta_4 < \hat{u}_4\})
                                                                                                                                                                                                                                                                                                                                                  \begin{array}{l} (M_{10},(\max\{0,\hat{i}_4-\Delta_3^{23}\} \leq \theta_4 < \hat{u}_4 - \Delta_3^{23}\}) \\ (M_{15},\{\max\{0,\hat{i}_3-\Delta_5^{11}-\Delta_4^{23}\} \leq \theta_3 < \hat{u}_3 - \Delta_5^{11} - \Delta_4^{23},40 \leq \theta_5 < 55\}) \\ \end{array} 
                   (M_1, \{35 \le \theta_2 < 46, \max\{0, \hat{l}_4 - \Delta_1^0\} \le \theta_4 < \hat{u}_4 - \Delta_1^0\})
                                                                                                                                                                                                                                                                                                                              q_{39}
                   \begin{array}{l} (M_2, \{\max\{0, \hat{l}_1 - \Delta_4^0\} \leq \theta_1 < \hat{u}_1 - \Delta_4^0, 40 \leq \theta_5 < 55\}) \\ (M_3, \{\hat{l}_3 \leq \theta_3 < \hat{u}_3, \max\{0, \hat{l}_4 - \Delta_1^0 - \Delta_2^1\} \leq \theta_4 < \hat{u}_4 - \Delta_1^0 - \Delta_2^1\}) \end{array} 
                                                                                                                                                                                                                                                                                                                              q_{40}
                                                                                                                                                                                                                                                                                                                                                 (M_{14}, \{ \max\{0, \hat{l}_4 - \Delta_2^{12} - \Delta_3^{24} \} \le \theta_4 < \hat{u}_4 - \Delta_2^{12} - \Delta_3^{24} \})
                    (M_4, \{max\{0, 35 - \Delta_4^1\} \le \theta_2 < 46 - \Delta_4^1, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                              q_{42}
                                                                                                                                                                                                                                                                                                                                                  (M_{15}, \{max\{0, \hat{l}_3 - \Delta_4^{24}\} \le \theta_3 < \hat{u}_3 - \Delta_4^{24}, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                                                 (M_{15}, \{\hat{l}_3 \le \theta_3 < \hat{u}_3, max\{0, 40 - \Delta_2^{25}\} \le \theta_5 < 55 - \Delta_2^{25}\})
                    (M_4, \{35 \le \theta_2 < 46, \max\{0, 40 - \Delta_1^2\} \le \theta_5 < 55 - \Delta_1^2\})
                                                                                                                                                                                                                                                                                                                              q_{43}
                                                                                                                                                                                                                                                                                                                                                 (M_{16}, \{max\{0, 35 - \Delta_5^5 - \Delta_4^{12} - \Delta_2^{55}\} \leq \theta_2 < 46 - \Delta_5^5 - \Delta_4^{12} - \Delta_2^{55}\}) \\ (M_{14}, \{max\{0, \hat{l}_4 - \Delta_1^6 - \Delta_2^{13} - \Delta_3^{26}\} \leq \theta_4 < \hat{u}_4 - \Delta_1^6 - \Delta_2^{13} - \Delta_3^{26}\})
                   (M_5, \{max\{0, \hat{l}_1 - \Delta_4^0 - \Delta_5^2\} \le \theta_1 < \hat{u}_1 - \Delta_4^0 - \Delta_5^2, \hat{l}_4 \le \theta_4 < \hat{u}_4\})
                                                                                                                                                                                                                                                                                                                             q_{44}
                   (M_6, \{\max\{0, \hat{l}_4 - \Delta_1^0 - \Delta_2^1 - \Delta_3^3\} \le \theta_4 < \hat{u}_4 - \Delta_1^0 - \Delta_2^1 - \Delta_3^3\})
                                                                                                                                                                                                                                                                                                                             q_{45}
                   (M_7, \{max\{0, \hat{l}_3 - \Delta_4^3\} \le \theta_3 < \hat{u}_3 - \Delta_4^3, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                                                 (M_{15}, \{max\{0, \hat{l}_3 - \Delta_4^{26}\} \le \theta_3 < \hat{u}_3 - \Delta_4^{26}, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                              q_{46}
                    (M_7, \{\hat{l}_3 \leq \theta_3 < \hat{u}_3, \max\{0, 40 - \Delta_2^4\} \leq \theta_5 < 55 - \Delta_2^4\})
                                                                                                                                                                                                                                                                                                                                                 (M_{15}, \{\hat{l}_3 \le \theta_3 < \hat{u}_3, max\{0, 40 - \Delta_2^{27}\} \le \theta_5 < 55 - \Delta_2^{27}\})
                                                                                                                                                                                                                                                                                                                             q_{47}
                  \begin{array}{l} (M_5, \{m_3, \{0.35, -\Delta_4^1 - \Delta_5^1\}, \{0.35, -\Delta_4
                                                                                                                                                                                                                                                                                                                                                 (M_{15}, (\hat{l}_{35} + \Delta_{1}^{13} - \Delta_{5}^{27}) \leq \theta_{2} < 46 - \Delta_{1}^{13} - \Delta_{5}^{27}) 
(M_{15}, (\hat{l}_{3} \leq \theta_{3} < \hat{u}_{3}, max\{0, 40 - \Delta_{1}^{14} - \Delta_{2}^{28}\} \leq \theta_{5} < 55 - \Delta_{1}^{14} - \Delta_{2}^{28}\})
                                                                                                                                                                                                                                                                                                                              q_{48}
                                                                                                                                                                                                                                                                                                                                                 (M_{16}, \{max\{0, 35 - \Delta_5^{28}\} \le \theta_2 < 46 - \Delta_5^{28}\})
                    (M_8, \{max\{0, 35 - \Delta_5^5\} \le \theta_2 < 46 - \Delta_5^5, \hat{l}_4 \le \theta_4 < \hat{u}_4\})
                                                                                                                                                                                                                                                                                                                              q_{50}
                    (M_8, \{35 \le \theta_2 < 46, \max\{0, \hat{l}_4 - \Delta_1^6\} \le \theta_4 < \hat{u}_4 - \Delta_1^6\})
                                                                                                                                                                                                                                                                                                                                                  (M_{16}, \{35 \le \theta_2 < 46\})
                                                                                                                                                                                                                                                                                                                              q_{51}
q_{13}
                    (M_9, \{max\{0, \hat{l}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6\} \le \theta_1 < \hat{u}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                                                  (M_{17}, \{40 \le \theta_5 < 55\})
q_{14}
                                                                                                                                                                                                                                                                                                                             q_{52}
                                                                                                                                                                                                                                                                                                                                                  (M_{17}, \{max\{0, 40 - \Delta_3^{32}\} \le \theta_5 < 55 - \Delta_3^{32}\})
                    (M_{10}, \{40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                              q_{53}
q_{15}
                    (M_{10}, \{max\{0, 40 - \Delta_3^8\} \le \theta_5 < 55 - \Delta_3^8\})
                                                                                                                                                                                                                                                                                                                                                  (M_{18}, \{max\{0, \hat{l}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17} - \Delta_5^{22}\} \le \theta_3 < \hat{u}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17} - \Delta_5^{22}\})
q_{16}
                                                                                                                                                                                                                                                                                                                             q_{54}
                  (M_{11}, \{\max\{0, \hat{i}_3 - \Delta_4^3 - \Delta_5^8\} \le \theta_3 < \hat{u}_3 - \Delta_4^3 - \Delta_5^8, \hat{i}_4 \le \theta_4 < \hat{u}_4\}) 
(M_{10}, \{\max\{0, 40 - \Delta_2^4 - \Delta_3^9\} \le \theta_5 < 55 - \Delta_2^4 - \Delta_3^9\})
                                                                                                                                                                                                                                                                                                                                                 \begin{array}{ll} (M_{18}, (\max\{0, 40 - \Delta_3^{34}\} \leq \theta_5 < 55 - \Delta_3^{34}\}) \\ (M_{18}, (\max\{0, \hat{l}_3 - \Delta_5^{9} - \Delta_4^{19} - \Delta_5^{54}\} \leq \theta_3 < \hat{u}_3 - \Delta_5^{9} - \Delta_4^{19} - \Delta_5^{34}\}) \end{array}
q_{17}
                                                                                                                                                                                                                                                                                                                              q_{55}
q_{18}
                                                                                                                                                                                                                                                                                                                             q_{56}
                                                                                                                                                                                                                                                                                                                                                (M_{11}, \{max\{0, \hat{l}_3 - \Delta_5^9\} \le \theta_3 < \hat{u}_3 - \Delta_5^9, \hat{l}_4 \le \theta_4 < \hat{u}_4\})
                                                                                                                                                                                                                                                                                                                              q_{57}
                   \begin{aligned} & (M_{11}, \{ max\{0, 3 - \Delta_5 \} \geq \theta_3 < u_3 - \Delta_5, t_4 \geq \theta_4 < u_4 \}) \\ & (M_{11}, \{ \hat{l}_3 \leq \theta_3 < \hat{u}_3, max\{0, \hat{l}_4 - \Delta_2^{10} \} \leq \theta_4 < \hat{u}_4 - \Delta_2^{10} \}) \\ & (M_{12}, \{ max\{0, 35 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10} \} \leq \theta_2 < 46 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10}, 40 \leq \theta_5 < 55 \}) \\ & (M_{10}, \{ max\{0, 40 - \Delta_1^2 - \Delta_2^5 - \Delta_3^{11} \} \leq \theta_5 < 55 - \Delta_1^2 - \Delta_2^5 - \Delta_3^{11} \}) \end{aligned} 
                                                                                                                                                                                                                                                                                                                                                 (M_{18}, \{max\{0, \hat{l}_3 - \Delta_5^{37}\} \le \theta_3 < \hat{u}_3 - \Delta_5^{37}\})
                   \begin{array}{l} (M_{11},\{max\{0,\hat{l}_3-\Delta_5^{11}\} \leq \hat{\theta}_3 < \hat{u}_3-\Delta_5^{11},\hat{l}_4 \leq \theta_4 < \hat{u}_4\}) \\ (M_{11},\{\hat{l}_3 \leq \theta_3 < \hat{u}_3,max\{0,\hat{l}_4-\Delta_2^{12}\} \leq \theta_4 < \hat{u}_4-\Delta_2^{12}\}) \end{array} 
                                                                                                                                                                                                                                                                                                                                                 (M_{18}, \{\hat{l}_3 \le \theta_3 < \hat{u}_3\})
                                                                                                                                                                                                                                                                                                                                                 (M_{17}, \{max\{0, 40 - \Delta_3^{40}\} \le \theta_5 < 55 - \Delta_3^{40}\})
                                                                                                                                                                                                                                                                                                                              q_{62}
q_{24}
                    (M_{12}, \{max\{0, 35 - \Delta_5^5 - \Delta_4^{12}\} \le \theta_2 < 46 - \Delta_5^5 - \Delta_4^{12}, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                                                 (M_{18}, \{max\{0, \hat{l}_3 - \Delta_5^{11} - \Delta_4^{23} - \Delta_5^{40}\} \le \theta_3 < \hat{u}_3 - \Delta_5^{11} - \Delta_4^{23} - \Delta_5^{40}\})
q_{25}
                                                                                                                                                                                                                                                                                                                              q_{63}
                    (M_{11}, \{\hat{l}_3 \leq \theta_3 < \hat{u}_3, max\{0, \hat{l}_4 - \Delta_1^6 - \Delta_2^{13}\} \leq \theta_4 < \hat{u}_4 - \Delta_1^6 - \Delta_2^{13}\})
                                                                                                                                                                                                                                                                                                                                                  (M_{17}, \{max\{0, 40 - \Delta_3^{42}\} \le \theta_5 < 55 - \Delta_3^{42}\})
q_{26}
                                                                                                                                                                                                                                                                                                                              q_{64}
                                                                                                                                                                                                                                                                                                                                                  \begin{array}{l} (M_{18}, \{max\{0, \hat{13} - \Delta_4^{24} - \Delta_5^{42}\} \leq \theta_3 < \hat{u}_3 - \Delta_4^{24} - \Delta_5^{42}\} ) \\ (M_{17}, \{max\{0, 40 - \Delta_2^{25} - \Delta_3^{43}\} \leq \theta_5 < 55 - \Delta_2^{25} - \Delta_3^{43}\} ) \end{array} 
                   (M_{12}, \{max\{0, 35 - \Delta_4^{13}\} \le \theta_2 < 46 - \Delta_4^{13}, 40 \le \theta_5 < 55\})
q_{27}
                                                                                                                                                                                                                                                                                                                             q_{65}
                   (M_{12}, \{35 \le \theta_2 < 46, max\{0, 40 - \Delta_1^{14}\} \le \theta_5 < 55 - \Delta_1^{14}\})
q_{28}
                                                                                                                                                                                                                                                                                                                              q_{66}
                                                                                                                                                                                                                                                                                                                                                 \begin{array}{ll} (M_{11},\{\max\{0,\hat{A}_{0},\Delta^{2}_{1}\} \leq \theta_{3} < \delta \delta - \Delta^{43}_{1}\}) \\ (M_{18},\{\max\{0,\hat{A}_{0}-\Delta^{43}_{0}\} \leq \theta_{3} < \delta \delta - \Delta^{43}_{1}\}) \\ (M_{17},\{\max\{0,40-\Delta^{46}_{3}\} \leq \theta_{5} < 55-\Delta^{46}_{3}\}) \\ (M_{18},\{\max\{0,\hat{A}_{0}-\Delta^{46}_{2}-\Delta^{46}_{5}\} \leq \theta_{3} < \hat{u}_{3} - \Delta^{46}_{4} - \Delta^{46}_{5}\}) \end{array}
                   (M_{13}, \{max\{0, \hat{l}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6 - \Delta_5^{14}\} \le \theta_1 < \hat{u}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6 - \Delta_5^{14}\})
q_{29}
                                                                                                                                                                                                                                                                                                                              q_{67}
                   (M_{14}, \{\hat{l}_4 \le \theta_4 < \hat{u}_4\})
                                                                                                                                                                                                                                                                                                                              q_{68}
                    (M_{14}, \{max\{0, \hat{l}_4 - \Delta_3^{17}\} \le \theta_4 < \hat{u}_4 - \Delta_3^{17}\})
                                                                                                                                                                                                                                                                                                                              q_{69}
                                                                                                                                                                                                                                                                                                                                                  \begin{aligned} & (M_{18}, \{ max\{0, \{3 - \Delta_4^{4^+} - \Delta_5^{-} \} \} \leq \theta_3 < u_3 - \Delta_4^{4^+} - \Delta_5^{-} \} ) \\ & (M_{17}, \{ max\{0, 40 - \Delta_2^{27} - \Delta_3^{47} \} ) \leq \theta_5 < 55 - \Delta_2^{27} - \Delta_3^{47} \} ) \\ & (M_{18}, \{ max\{0, \hat{\mathbf{i}}_3 - \Delta_5^{47} \} \leq \theta_3 < \hat{u}_3 - \Delta_5^{47} \} ) \\ & (M_{17}, \{ max\{0, 40 - \Delta_1^{14} - \Delta_2^{28} - \Delta_3^{49} \} ) \leq \theta_5 < 55 - \Delta_1^{14} - \Delta_2^{28} - \Delta_3^{49} \} ) \\ & (M_{18}, \{ max\{0, \hat{\mathbf{i}}_3 - \Delta_5^{49} \} \leq \theta_3 < \hat{u}_3 - \Delta_5^{49} \} ) \end{aligned} 
                  \begin{array}{l} (M_{15},(\max\{0,\hat{l}_3-\Delta_4^3-\Delta_5^8-\Delta_4^{17}\} \leq \theta_3 < \hat{u}_3 - \Delta_4^3-\Delta_5^8-\Delta_4^{17}, 40 \leq \theta_5 < 55\}) \\ (M_{14},(\max\{0,\hat{l}_4-\Delta_3^{19}\} \leq \theta_4 < \hat{u}_4-\Delta_3^{19}\}) \end{array}
                                                                                                                                                                                                                                                                                                                              q_{71}
q_{33}
                    (M_{15}, \{max\{0, \hat{l}_3 - \Delta_5^9 - \Delta_4^{19}\} \le \theta_3 < \hat{u}_3 - \Delta_5^9 - \Delta_4^{19}, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                              q_{72}
                   (M_{14}, \{max\{0, \hat{l}_4 - \Delta_2^{10} - \Delta_3^{20}\} \le \theta_4 < \hat{u}_4 - \Delta_2^{10} - \Delta_3^{20}\})
                                                                                                                                                                                                                                                                                                                              q_{73}
q_{35}
                   (M_{15}, \{max\{0, \hat{l}_3 - \Delta_4^{20}\} \le \theta_3 < \hat{u}_3 - \Delta_4^{20}, 40 \le \theta_5 < 55\})
                                                                                                                                                                                                                                                                                                                                                 (M_{19}, \emptyset)
q_{36}
                                                                                                                                                                                                                                                                                                                             q_{74}
                   (M_{15}, \{\hat{l}_3 \le \theta_3 < \hat{u}_3, \max\{0, 40 - \Delta_2^{21}\} \le \theta_5 < 55 - \Delta_2^{21}\})
```

## Table 3: Edges of the PAMSCG of the TCPN G in Fig. 4 of the paper

```
f(e_{55}) = (t_4, \Delta_4^{30} \in [\hat{l}_4, \hat{u}_4))

f(e_{56}) = (t_4, \Delta_4^{31} \in [max\{0, \hat{l}_4 - \Delta_3^{17}\}, \hat{u}_4 - \Delta_3^{17}))
                                                                                  f(e_1) = (t_1, \Delta_1^0)
                                                                                                                                                      \in [\hat{l}_1, min\{\hat{u}_1, \hat{u}_4\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{55} = (q_{30}, q_{52})
        e_1 = (q_0, q_1)
                                                                                  \begin{array}{l} f(t) = (t_1, \Delta_4^0 \in [\hat{t}_1, \min\{\hat{u}_1, \hat{u}_4\}]) \\ f(e_2) = (t_2, \Delta_2^1 \in [35, \min\{46, \hat{u}_4 - \Delta_1^0\})) \\ f(e_3) = (t_2, \Delta_2^1 \in [35, \min\{46, \hat{u}_4 - \Delta_1^0\})) \\ f(e_4) = (t_4, \Delta_4^1 \in [\max\{0, \hat{l}_4 - \Delta_1^0\}, \min\{46, \hat{u}_4 - \Delta_1^0\}]) \\ \end{array} 
         e_2 = (q_0, q_2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{56} = (q_{31}, q_{52})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \begin{split} f(e_{56}) &= (t_4, \Delta_4^{34} \in [max\{0, t_4 - \Delta_4^4'\}, \hat{u}_4 - \Delta_4^4'], \min\{\hat{u}_3 - \Delta_4^3 - \Delta_4^8 - \Delta_4^{17}, \min\{\hat{u}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17}, 55\})) \\ f(e_{57}) &= (t_5, \Delta_3^{32} \in [40, \min\{\hat{u}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17}, 55\})) \\ f(e_{59}) &= (t_4, \Delta_4^{33} \in [max\{0, \hat{t}_4 - \Delta_3^{19}, \hat{u}_4 - \Delta_3^{19}), \inf\{\hat{u}_3 - \Delta_5^9 - \Delta_4^{17}, 55\})) \\ f(e_{69}) &= (t_5, \Delta_3^{34} \in [max\{0, \hat{t}_4 - \Delta_3^{19}\}, \hat{u}_4 - \Delta_3^{19}), \min\{\hat{u}_3 - \Delta_5^9 - \Delta_4^{19}, 55\})) \\ f(e_{61}) &= (t_5, \Delta_3^{34} \in [max\{0, \hat{t}_4 - \Delta_2^{19} - \Delta_4^{19}, 55\})) \\ f(e_{62}) &= (t_4, \Delta_3^{36} \in [max\{0, \hat{t}_4 - \Delta_2^{10} - \Delta_3^{20}), \inf\{\hat{u}_3 - \Delta_5^9 - \Delta_4^{19}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_4 - \Delta_2^{10} - \Delta_3^{20}), \min\{\hat{u}_3 - \Delta_4^2, 55\})) \\ f(e_{62}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_4 - \Delta_2^{10} - \Delta_3^{20}), \min\{\hat{u}_3 - \Delta_4^2, 55\})) \\ f(e_{62}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{62}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{62}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{62}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\})) \\ f(e_{63}) &= (t_7, \Delta_3^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\}) \\ f(e_{63}) &= (t_7, \Delta_4^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\}) \\ f(e_{63}) &= (t_7, \Delta_4^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\}) \\ f(e_{63}) &= (t_7, \Delta_4^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\}) \\ f(e_{63}) &= (t_7, \Delta_4^{36} \in [max\{0, \hat{t}_3 - \Delta_4^{20}, 55\}) \\ f(e_{63}) &= (t_7, \Delta_4^{36} \in [max\{0, \hat{t}_
        e_3 = (q_1, q_3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{57} = (q_{32}, q_{53})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{58} = (q_{32}, q_{54})
         e_4 = (q_1, q_4)
        e_5 = (q_2, q_5)
                                                                                 f(e_5) = (t_1, \Delta_1^2 \in [max\{0, \hat{l}_1 - \Delta_4^0\}, min\{\hat{u}_1 + \Delta_4^0, 55\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{59} = (q_{33}, q_{52})
        e_6 = (q_2, q_6)
                                                                                 f(e_6) = (t_5, \Delta_5^2 \in [40, min\{\hat{u}_1 - \Delta_4^0, 55\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{60} = (q_{34}, q_{55})
         e_7 = (q_3, q_7)
                                                                                 e_{61} = (q_{34}, q_{56})
        e_8 = (q_3, q_8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{62} = (q_{35}, q_{52})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{63}) = (t_4, \Delta_4)

f(e_{63}) = (t_3, \Delta_3^{36})

f(e_{64}) = (t_5, \Delta_5^{36})
         e_9 = (q_4, q_9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{63} = (q_{36}, q_{57})
                                                                                 f(e_{10}) = (t_5, \Delta_5^4 \in [40, min\{46 - \Delta_4^1, 55\}))

f(e_{11}) = (t_2, \Delta_5^2 \in [35, min\{46 - \Delta_1^2, 55\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \begin{array}{l} \in \{40, \min\{\hat{u}_3 - \Delta_4^{20}, 55\}\}) \\ \in [\hat{l}_3, \min\{\hat{u}_3, 55 - \Delta_2^{21}\})) \\ \in [\max\{0, 40 - \Delta_2^{21}\}, \min\{\hat{u}_3, 55 - \Delta_2^{21}\})) \\ \in [\max\{0, 40 - \Delta_2^{21}\}, \min\{\hat{u}_3, 55 - \Delta_2^{21}\})) \\ \in [\max\{0, \hat{l}_4 - \Delta_3^{24} - \Delta_4^{10} - \Delta_5^{21}\}, 46 - \Delta_4^{1} - \Delta_5^{4} - \Delta_4^{10} - \Delta_5^{21}\}) \\ \in [\max\{0, \hat{l}_4 - \Delta_3^{23}\}, \hat{u}_4 - \Delta_3^{23}\}) \\ \in [\max\{0, \hat{l}_4 - \Delta_3^{21}\}, \hat{u}_4 - \Delta_3^{23}\}) \\ \in [\max\{0, \hat{l}_4 - \Delta_3^{21} - \Delta_4^{23}\}, \min\{\hat{u}_3 - \Delta_1^{51} - \Delta_4^{23}, 55\}\}) \\ \in [\max\{0, \hat{l}_4 - \Delta_2^{12} - \Delta_3^{24}\}, \hat{u}_4 - \Delta_2^{12} - \Delta_3^{24}\}) \\ \in [\max\{0, \hat{l}_3 - \Delta_4^{21}\}, \min\{\hat{u}_3 - \Delta_4^{24}, 55\}\}) \\ \in [40, \min\{\hat{u}_3 - \Delta_4^{21}\}, \min\{\hat{u}_3 - \Delta_4^{24}, 55\}\}) \\ \in [40, \min\{\hat{u}_3, 55 - \Delta_2^{25}\})) \\ \in [\max\{0, 40 - \Delta_2^{25}\}, \min\{\hat{u}_3, 55 - \Delta_2^{25}\})) \\ \in [\max\{0, 40 - \Delta_2^{25}\}, \min\{\hat{u}_3, 55 - \Delta_2^{25}\})) \end{array}
     e_{10} = (q_4, q_{10})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{64} = \left(q_{36}, q_{58}\right)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \in [40, min{\{\hat{u}_3 - \Delta_4^{20}, 55\}})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{64}) = (t_5, \Delta_5)

f(e_{65}) = (t_3, \Delta_3^{37})

f(e_{66}) = (t_5, \Delta_5^{37})

f(e_{67}) = (t_2, \Delta_2^{38})
     e_{11} = (q_5, q_{11})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{65} = (q_{37}, q_{59})
                                                                                 \begin{array}{ll} f(c_{11}) & = (2,2,\Delta_{2} \in [bos, min(40-\Delta_{1}^{2},bd]), \\ f(e_{12}) & = (f_{5},\Delta_{5}^{2} \in [max\{0,40-\Delta_{1}^{2}\}, min\{46,55-\Delta_{1}^{2}\})) \\ f(e_{13}) & = (t_{1},\Delta_{1}^{6} \in [max\{0,\hat{l}_{1}-\Delta_{4}^{0}-\Delta_{5}^{2}\}, min\{\hat{u}_{1}-\Delta_{4}^{0}-\Delta_{5}^{2},\hat{u}_{4}\})) \\ f(e_{14}) & = (t_{4},\Delta_{4}^{6} \in [\hat{l}_{4}, min\{\hat{u}_{1}-\Delta_{4}^{0}-\Delta_{5}^{2},\hat{u}_{4}\})) \end{array}
      e_{12} = (q_5, q_{12})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{66} = (q_{37}, q_{60})
     e_{13} = (q_6, q_{13})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{67} = (q_{38}, q_{61})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{68} = (q_{39}, q_{52})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{68}) = (t_4, \Delta_4^{39})
        e_{14} = (q_6, q_{14})
                                                                                 f(e_{15}) = (t_4, \Delta_4^7 \in [max\{0, \hat{l}_4 - \Delta_1^0 - \Delta_1^1 - \Delta_3^3\}, \hat{u}_4 - \Delta_1^0 - \Delta_2^1 - \Delta_3^3))
     e_{15} = (q_7, q_{15})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{69} = (q_{40}, q_{62})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{69}) = (t_3, \Delta_3^{40})
                                                                                 f(e_{16}) = (t_3, \Delta_3^8 \in [max\{0, \hat{l}_3 - \Delta_4^3\}, min\{\hat{u}_3 - \Delta_4^3, 55\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{70}) = (t_5, \Delta_5^{40})
     e_{16} = (q_8, q_{16})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{70} = (q_{40}, q_{63})
      e_{17} = (q_8, q_{17})
                                                                                 f(e_{17}) = (t_5, \Delta_5^8 \in [40, min\{\hat{u}_3 - \Delta_4^3, 55\}))

f(e_{18}) = (t_3, \Delta_3^9 \in [\hat{l}_3, min\{\hat{u}_3, 55\} - \Delta_2^4))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{71} = (q_{41}, q_{52})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{71}) = (t_4, \Delta_4^{41})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{72}) = (t_3, \Delta_3^{42})

f(e_{73}) = (t_5, \Delta_5^{42})

f(e_{74}) = (t_3, \Delta_3^{43})
     e_{18} = (q_0, q_{18})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{72} = (q_{42}, q_{64})
                                                                                 \begin{array}{l} f(e_{18}) = (c_{3}, \Delta_{3}^{2} \in [e_{3}, \min\{a_{3}, sob_{4}^{4}\}, \min\{\hat{u}_{3}, 55 - \Delta_{4}^{4}\})) \\ f(e_{19}) = (f_{5}, \Delta_{3}^{2} \in [\max\{0, 40 - \Delta_{2}^{4}\}, \min\{\hat{u}_{3}, 55 - \Delta_{4}^{4}\})) \\ f(e_{20}) = (t_{2}, \Delta_{2}^{2} \in [\max\{0, 35 - \Delta_{4}^{4} - \Delta_{5}^{4}\}, \min\{\hat{u}_{4}, 55 - \Delta_{4}^{4} - \Delta_{5}^{4}\}, \min\{\hat{u}_{4}, \Delta_{4}^{4} - \Delta_{4}^{4}, \hat{u}_{4}\})) \\ f(e_{21}) = (t_{4}, \Delta_{4}^{40} \in [\hat{l}_{4}, \min\{46 - \Delta_{4}^{4} - \Delta_{5}^{4}, \hat{u}_{4}\})) \end{array}
      e_{19} = (q_9, q_{19})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{73} = (q_{42}, q_{65})
     e_{20} = (q_{10}, q_{20})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{74} = (q_{43}, q_{66})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{75} = (q_{43}, q_{67})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{75}) = (t_5, \Delta_5^{43})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       \in [max\{0, 40 - \Delta_2^{25}\}, min\{\hat{u}_3, 55 - \Delta_2^{25}\}))
    e_{21} = (q_{10}, q_{21})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{l} \in [\max(0,35-\Delta_5^2-\Delta_1^{12}-\Delta_5^{23}),46-\Delta_5^{5}-\Delta_1^{12}-\Delta_5^{25}))\\ \in [\max\{0,\hat{l}_4-\Delta_1^6-\Delta_1^{12}-\Delta_3^{26}\},\hat{u}_4-\Delta_1^6-\Delta_2^{13}-\Delta_3^{26}))\\ \in [\max\{0,\hat{l}_3-\Delta_4^{26}\},\min\{\hat{u}_3-\Delta_4^{26},55\})) \end{array} 
                                                                                                                                                             \in [\hat{l}_3, min\{\hat{u}_3, 55 - \Delta_1^2 - \Delta_2^5\}))

\in [max\{0, 40 - \Delta_1^2 - \Delta_2^5\}, min\{\hat{u}_3, 55 - \Delta_1^2 - \Delta_2^5\}))
                                                                                 f(e_{22}) = (t_3, \Delta_3^{11})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{76} = (q_{44}, q_{61})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{76}) = (t_2, \Delta_2^{44})
     e_{22} = (q_{11}, q_{22})
                                                                                 f(e_{23}) = (t_5, \Delta_5^{11})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{77}) = (t_4, \Delta_4^{25})
    e_{23} = (q_{11}, q_{23})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{77} = (q_{45}, q_{52})
                                                                                 f(e_{24}) = (t_2, \Delta_2^{12})
                                                                                                                                                                        [max\{0,35-\Delta_5^5\},min\{46-\Delta_5^5,\hat{u}_4\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{78}) = (t_3, \Delta_3^{46})
    e_{24} = (q_{12}, q_{24})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{78} = (q_{46}, q_{68})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \{ \max\{0, 1_3 - \Delta_4^{1\gamma}\}, \min\{u_3 - \Delta_4^{4\gamma}, 55\} \} \} 
 = \{ [40, \min\{\hat{u}_3 - \Delta_4^{26}, 55\} \} \} 
 = \{ [i_3, \min\{\hat{u}_3, 55 - \Delta_2^{27}\} \} \} 
 = \{ \max\{0, 40 - \Delta_2^{27}\}, \min\{\hat{u}_3, 55 - \Delta_2^{27}\} \} \} 
 = \{ \max\{0, 35 - \Delta_4^{13} - \Delta_2^{27}\}, 46 - \Delta_4^{13} - \Delta_2^{27} \} \} 
 = \{ [i_3, \min\{\hat{u}_3, 55 - \Delta_1^{14} - \Delta_2^{28}\} \} \} \} 
 = \{ \max\{0, 40 - \Delta_1^{14} - \Delta_2^{28}\}, \min\{\hat{u}_3, 55 - \Delta_1^{14} - \Delta_2^{28}\} \} \} 
 = \{ \max\{0, 35 - \Delta_2^{58}\}, 46 - \Delta_2^{58} \} \} \} 
    e_{25} = (q_{12}, q_{25})
                                                                                 f(e_{25}) = (t_4, \Delta_4^{12} \in
                                                                                                                                                                        [\hat{l}_4, \min\{46 - \Delta_5^5, \hat{u}_4\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{79} = (q_{46}, q_{69})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{79}) = (t_5, \Delta_5^{46})
                                                                                                                                                             \begin{array}{l} \in [\ell_4, \min\{46 - \Delta_5^2, u_4\}]) \\ \in [35, \min\{46, \hat{u}_4 - \Delta_1^6\}]) \\ \in [\max\{0, \hat{l}_4 - \Delta_1^6\}, \min\{46, \hat{u}_4 - \Delta_1^6\}]) \\ \in [\max\{0, \hat{l}_1 - \Delta_1^6\} - \Delta_2^6 - \Delta_4^6\}, \min\{\hat{u}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6, 55\}]) \\ \in [40, \min\{\hat{u}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6, 55\}]) \end{array} 
                                                                                 f(e_{26}) = (t_4, \Delta_4^{13})

f(e_{26}) = (t_2, \Delta_2^{13})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{80}) = (t_3, \Delta_3^{47})
    e_{26} = (q_{13}, q_{26})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{80} = (q_{47}, q_{70})
                                                                                 f(e_{27}) = (t_1, \Delta_4^{13})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{81} = (q_{47}, q_{71})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{81}) = (t_5, \Delta_5^{47})
    e_{27} = (q_{13}, q_{27}) \\
    e_{28} = (q_{14}, q_{28})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{82}) = (t_2, \Delta_2^{48})

f(e_{83}) = (t_3, \Delta_3^{49})
                                                                                 f(e_{28}) = (t_1, \Delta_1^{14})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{82} = \left(q_{48}, q_{61}\right)
                                                                                 f(e_{29}) = (t_5, \Delta_5^{14})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{83} = (q_{49}, q_{72})
    e_{29} = (q_{14}, q_{29})
                                                                                 f(e_{30}) = (t_5, \Delta_5^{15})

f(e_{31}) = (t_5, \Delta_5^{16})
                                                                                                                                                                        [40, 55))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{84} = (q_{49}, q_{73})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{84}) = (t_5, \Delta_5^{49})

f(e_{85}) = (t_2, \Delta_2^{50})
                                                                                                                                                                        [max\{0, 40 - \Delta_3^8\}, 55 - \Delta_3^8))
    e_{31} = (q_{16}, q_{30})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{85} = (q_{50}, q_{61})
                                                                                                                                                                       \begin{array}{ll} [max\{0,3-\Delta_3^3) \circ 8 - 3) \\ [max\{0,1_3-\Delta_4^3-\Delta_8^4\}, min\{\hat{u}_3-\Delta_4^3-\Delta_8^5, \hat{u}_4\})) \\ [\hat{l}_4, min\{\hat{u}_3-\Delta_4^3-\Delta_8^5, \hat{u}_4\})) \\ [max\{0,40-\Delta_2^4-\Delta_3^9\}, 55-\Delta_2^4-\Delta_3^9)) \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             [35, 46))
     e_{32} = (q_{17}, q_{31})
                                                                                 f(e_{32}) = (t_3, \Delta_3^{17})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{86} = (q_{51}, q_{61})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f(e_{86}) = (t_2, \Delta_2^{51})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{87}) = (t_5, \Delta_5^{52})

f(e_{88}) = (t_5, \Delta_5^{53})

f(e_{88}) = (t_5, \Delta_5^{53})
                                                                                 f(e_{33}) = (t_4, \Delta_4^{17})
    e_{33} = (q_{17}, q_{32})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{l} e_{87} = (q_{52}, q_{74}) \\ e_{88} = (q_{53}, q_{74}) \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ∈ [40, 55))
                                                                                 f(e_{34}) = (t_5, \Delta_5^{18})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{l} \in [\max(3), 40 - \Delta_3^{32}\}, 55 - \Delta_3^{32})) \\ \in [\max\{0, \hat{l}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17} - \Delta_5^{32}\}, \hat{u}_3 - \Delta_4^3 - \Delta_5^8 - \Delta_4^{17} - \Delta_5^{32})) \end{array} 
     e_{34} = (q_{18}, q_{30})
                                                                                                                                                                        [max\{0, \hat{l}_3 - \Delta_5^9\}, min\{\hat{u}_3 - \Delta_5^9, \hat{u}_4\}))
                                                                                 f(e_{35}) = (t_3, \Delta_2^{19} \in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{89}) = (t_3, \Delta_2^{54})
    e_{35} = (q_{19}, q_{33})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{89} = (q_{54}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{l} (\max\{0,3\} - 4_4 - 5_5 - \Delta_3^4)) \\ \in [\max\{0,40 - \Delta_3^{34}\}, 55 - \Delta_3^{34})) \\ \in [\max\{0,\hat{4}0 - \Delta_5^{34} - \Delta_5^{40} - \Delta_5^{34}\}, \hat{\alpha}_3 - \Delta_5^9 - \Delta_4^{19} - \Delta_5^{34})) \\ \in [\max\{0,40 - \Delta_3^{36}\}, 55 - \Delta_3^{36})) \end{array} 
                                                                                 f(e_{36}) = (t_4, \Delta_4^{19})
                                                                                                                                                                        [\hat{l}_4, min\{\hat{u}_3 - \Delta_5^9, \hat{u}_4\}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{90} = (q_{55}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{90}) = (t_5, \Delta_5^{55})
    e_{36} = (q_{19}, q_{34})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{91}) = (t_3, \Delta_3^{56})

f(e_{92}) = (t_5, \Delta_5^{57})
                                                                                 \begin{array}{l} f(e_{37}) = (t_3, \Delta_3^{20} \in [\hat{l}_3, \min\{\hat{u}_3, \hat{u}_4 - \Delta_2^{10}\})) \\ f(e_{38}) = (t_4, \Delta_4^{20} \in [\max\{0, \hat{l}_4 - \Delta_2^{10}\}, \min\{\hat{u}_3, \hat{u}_4 - \Delta_2^{10}\})) \end{array}
     e_{37} = (q_{20}, q_{35})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{91} = \left(q_{56}, q_{74}\right)
    e_{38} = (q_{20}, q_{36})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{92} = (q_{57}, q_{74})
                                                                                 f(e_{39}) = (t_4, \Delta_4^{21} \in f(e_{39}) = (t_2, \Delta_5^{21} \in f(e_{40}) = (t_5, \Delta_5^{21} \in f(e_{41}) = (t_5, \Delta_5^{22} \in
                                                                                                                                                              \in [\max\{0, 35 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10}\}, \min\{46 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10}, 55\}))   \in [\max\{0, 35 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10}\}, \min\{46 - \Delta_4^1 - \Delta_5^4 - \Delta_4^{10}, 55\})) 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \begin{array}{l} f(e_{33}) = (f_{3},\Delta_{3}^{3}) \in [\max\{0,\hat{1}_{3}-\Delta_{3}^{2}\},\Delta_{3}^{3}\}, (\hat{1}_{3}-\Delta_{3}^{2}),\Delta_{3}^{3}\}, (\hat{1}_{3}-\Delta_{3}^{2}),\Delta_{3}^{3}\}, (\hat{1}_{3}-\Delta_{3}^{2}),\Delta_{3}^{3}\}, (\hat{1}_{3}-\Delta_{3}^{2})) \\ f(e_{94}) = (f_{5},\Delta_{3}^{50}) \in [\max\{0,40-\Delta_{2}^{21}-\Delta_{3}^{37}\},55-\Delta_{2}^{21}-\Delta_{3}^{37})) \\ f(e_{95}) = (t_{3},\Delta_{3}^{60}) \in [\max\{0,\hat{1}_{3}-\Delta_{3}^{57}\},\hat{1}_{3}-\Delta_{3}^{57})) \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        e_{93} = (q_{58}, q_{74})
     e_{39} = (q_{21}, q_{37})
    e_{40} = \left(q_{21}, q_{38}\right)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{94} = \left(q_{59}, q_{74}\right)
                                                                                                                                                                        [max\{0, 40 - \Delta_1^2 - \Delta_2^5 - \Delta_1^{31}\}, 55 - \Delta_1^2 - \Delta_2^5 - \Delta_1^{11}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{95} = (q_{60}, q_{74})
    e_{41} = (q_{22}, q_{30})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \begin{split} f(e_{05}) &= (t_3, \Delta_3^{64} \in [\max\{0, t_3 - \Delta_5^e\}, u_3 - \Delta_5^e\}), u_3 - \Delta_5^e\}) \\ f(e_{96}) &= (t_3, \Delta_5^{61} \in [\hat{\eta}_3, \hat{u}_3]) \\ f(e_{97}) &= (t_5, \Delta_6^{62} \in [\max\{0, 40 - \Delta_3^{40}\}, 55 - \Delta_3^{40}\})) \\ f(e_{98}) &= (t_3, \Delta_5^{63} \in [\max\{0, \hat{t}_3 - \Delta_5^{11} - \Delta_4^{23} - \Delta_5^{40}\}, \hat{u}_3 - \Delta_5^{11} - \Delta_4^{23} - \Delta_5^{40}\})) \\ f(e_{99}) &= (t_5, \Delta_5^{64} \in [\max\{0, 40 - \Delta_3^{22}\}, 55 - \Delta_3^{24}\})) \\ f(e_{100}) &= (t_3, \Delta_5^{65} \in [\max\{0, \hat{t}_3 - \Delta_4^{24} - \Delta_4^{22}\}, \hat{u}_3 - \Delta_4^{24} - \Delta_4^{42}\})) \\ f(e_{101}) &= (t_5, \Delta_5^{66} \in [\max\{0, 40 - \Delta_2^{25} - \Delta_3^{43}\}, 55 - \Delta_2^{25} - \Delta_3^{43}\})) \\ f(e_{102}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{102}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{103}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{104}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_3^{83}\}, \hat{u}_3 - \Delta_4^{36}\})) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{86}\}, \hat{t}_3 - \Delta_4^{86}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{86}\}, \hat{t}_3 - \Delta_4^{86}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{86}\}, \hat{t}_3 - \Delta_4^{86}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{86}\}, \hat{t}_3 - \Delta_4^{86}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, \Delta_3^{87} \in [\max\{0, \hat{t}_3 - \Delta_4^{87}\}, \hat{t}_3 - \Delta_4^{87}]) \\ f(e_{105}) &= (t_3, 
                                                                                f(e_1) = (t_5, \Delta_5^2) \in [max(0, 40 - \Delta_1^2 - \Delta_2 - \Delta_3^2), 50 - \Delta_1^2 - \Delta_2^2 - \Delta_3^2)
f(e_42) = (t_3, \Delta_3^2) \in [max(0, \hat{i}_3 - \Delta_3^1), min\{\hat{u}_3 - \Delta_5^1, \hat{u}_4\}))
f(e_{43}) = (t_4, \Delta_4^{23} \in [\hat{t}_4, min\{\hat{u}_3 - \Delta_5^1, \hat{u}_4\}))
f(e_{44}) = (t_3, \Delta_3^3) \in [\hat{i}_3, min\{\hat{u}_3, \hat{u}_4 - \Delta_2^1\}))
f(e_{45}) = (t_4, \Delta_4^{24} \in [max\{0, \hat{i}_4 - \Delta_3^1, min\{\hat{u}_3\}, \hat{u}_4 - \Delta_2^1\}))
f(e_{46}) = (t_2, \Delta_2^2) \in [max\{0, 35 - \Delta_5^2, -\Delta_4^1\}, min\{46 - \Delta_5^5 - \Delta_4^1, 55\}))
f(e_{47}) = (t_5, \Delta_2^{26} \in [40, min\{46 - \Delta_5^2 - \Delta_4^1\}, 35\}))
    e_{42} = (q_{23}, q_{39})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{96} = (q_{61}, q_{74})
    e_{43} = (q_{23}, q_{40})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{97} = (q_{62}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{98} = (q_{63}, q_{74})
    e_{44} = (q_{24}, q_{41})
    e_{45} = (q_{24}, q_{42})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{99} = \left(q_{64}, q_{74}\right)
    e_{46} = (q_{25}, q_{43})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{100} = (q_{95}, q_{74})
     e_{47} = (q_{25}, q_{44})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{101} = (q_{66}, q_{74})
                                                                                \begin{split} f(e_{47}) &= (t_5, \Delta_5^{48}) \in [40, \min\{46 - \Delta_5^{6} - \Delta_4^{14}, 55\})) \\ f(e_{48}) &= (t_3, \Delta_5^{26} \in [l_3, \min\{48, \hat{u}_4 - \Delta_1^{6} - \Delta_2^{13}\})) \\ f(e_{49}) &= (t_4, \Delta_4^{6} \in [\max\{0, \hat{1}_4 - \Delta_1^{6} - \Delta_2^{13}\}, \min\{\hat{u}_3, \hat{u}_4 - \Delta_1^{6} - \Delta_2^{13}\})) \\ f(e_{50}) &= (t_2, \Delta_2^{27} \in [\max\{0, 35 - \Delta_4^{13}\}, \min\{46 - \Delta_4^{13}, 55\})) \\ f(e_{51}) &= (t_5, \Delta_5^{27} \in [40, \min\{46 - \Delta_4^{13}, 55\})) \\ f(e_{52}) &= (t_5, \Delta_2^{28} \in [35, \min\{46, 55 - \Delta_1^{14}\})) \\ f(e_{53}) &= (t_5, \Delta_5^{28}) \in [\max\{0, 40 - \Delta_4^{14}\}, \min\{46, 55 - \Delta_1^{14}\})) \\ f(e_{53}) &= (t_5, \Delta_5^{28}) \in [\max\{0, 40 - \Delta_4^{14}\}, \min\{46, 55 - \Delta_1^{14}\})) \\ \end{split}
    e_{48} = (q_{26}, q_{45})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{102} = (q_{67}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{49} = (q_{26}, q_{46})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{103} = (q_{68}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{103}) = (t_5, \Delta_5^{68})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{104} = (q_{69}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{104}) = (t_3, \Delta_{\frac{3}{2}}^{69})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{105}) = (t_5, \Delta_5^{70})
    e_{51} = (q_{27}, q_{48})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{105} = (q_{70}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f(e_{106}) = (t_3, \Delta_3^{71})

f(e_{107}) = (t_5, \Delta_5^{72})
     e_{52} = (q_{28}, q_{49})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e_{106} = (q_{71}, q_{74})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e_{107} = (q_{71}, q_{74})

e_{107} = (q_{72}, q_{74})
    e_{53} = (q_{28}, q_{50})
                                                                                 f(e_{54}) = (t_1, \Delta_1^{29} \in [max\{0, \hat{l}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6 - \Delta_5^{14}\}, \hat{u}_1 - \Delta_4^0 - \Delta_5^2 - \Delta_4^6 - \Delta_5^{14}])) \parallel
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f(e_{108}) = (t_3, \Delta_3^{73} \in [max\{0, \hat{l}_3 - \Delta_5^{49}\}, \hat{u}_3 - \Delta_5^{49}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    e_{108} = (q_{73}, q_{74})
e_{54} = (q_{29}, q_{51})
```

List of all initial-to-terminal paths in the PAMSCG of the TCPN G in Fig. 4 of the paper.

• 
$$\chi_{te,1} = q_{0,1} \stackrel{c_{1,1}}{\rightleftharpoons} q_{1,1} \stackrel{c_{3,1}}{\rightleftharpoons} q_{3,1} \stackrel{c_{3,1}}{\rightleftharpoons} q_{7,1} \stackrel{c_{1,5}}{\rightleftharpoons} q_{1,2} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,2} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,2} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{1,5}}{\rightleftharpoons} q_{1,2} \stackrel{c_{1,5}}{\rightleftharpoons} q_{1,2} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,2} \stackrel{c_{3,7}}{\rightleftharpoons} q_{7,4} \stackrel{c_{1,5}}{\rightleftharpoons} q_{1,2} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,3} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,4} \stackrel{c_{3,4}}{\rightleftharpoons} q_{4,5} \stackrel{c_{3,5}}{\rightleftharpoons} q_{5,5} \stackrel{c_{1,5}}{\rightleftharpoons} q_{1,5} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,5} q_{3,5} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,5} q_{3,5} \stackrel{c_{3,5}}{\rightleftharpoons} q_{3,5} \stackrel{c_{$$

• 
$$\chi_{te,27} = q_{0,27} \xrightarrow{e_{2,27}} q_{2,27} \xrightarrow{e_{6,27}} q_{6,27} \xrightarrow{e_{13,27}} q_{13,27} \xrightarrow{e_{26,27}} q_{26,27} \xrightarrow{e_{49,27}} q_{46,27} \xrightarrow{e_{78,27}} q_{68,27} \xrightarrow{e_{103,27}} q_{74,27}$$
•  $\chi_{te,28} = q_{0,28} \xrightarrow{e_{2,28}} q_{2,28} \xrightarrow{e_{6,28}} q_{6,28} \xrightarrow{e_{13,28}} q_{13,28} \xrightarrow{e_{26,28}} q_{26,28} \xrightarrow{e_{49,28}} q_{26,28} \xrightarrow{e_{79,28}} q_{69,28} \xrightarrow{e_{104,28}} q_{74,28}$ 
•  $\chi_{te,29} = q_{0,29} \xrightarrow{e_{2,29}} q_{2,29} \xrightarrow{e_{6,29}} q_{6,29} \xrightarrow{e_{13,29}} q_{13,29} \xrightarrow{e_{27,29}} q_{27,29} \xrightarrow{e_{50,29}} q_{47,29} \xrightarrow{e_{80,29}} q_{70,29} \xrightarrow{e_{105,29}} q_{74,29}$ 
•  $\chi_{te,30} = q_{0,30} \xrightarrow{e_{2,30}} q_{2,30} \xrightarrow{e_{6,30}} q_{6,30} \xrightarrow{e_{13,30}} q_{13,30} \xrightarrow{e_{27,30}} q_{27,30} \xrightarrow{e_{50,30}} q_{47,30} \xrightarrow{e_{81,30}} q_{71,30} \xrightarrow{e_{106,30}} q_{74,30}$ 
•  $\chi_{te,31} = q_{0,31} \xrightarrow{e_{2,31}} q_{2,31} \xrightarrow{e_{6,31}} q_{6,31} \xrightarrow{e_{13,31}} q_{13,31} \xrightarrow{e_{27,31}} q_{27,31} \xrightarrow{e_{51,31}} q_{48,31} \xrightarrow{e_{82,31}} q_{61,31} \xrightarrow{e_{96,31}} q_{74,31}$ 
•  $\chi_{te,32} = q_{0,32} \xrightarrow{e_{2,32}} q_{2,32} \xrightarrow{e_{6,32}} q_{6,32} \xrightarrow{e_{14,32}} q_{14,32} \xrightarrow{e_{28,32}} q_{28,32} \xrightarrow{e_{52,32}} q_{49,32} \xrightarrow{e_{83,32}} q_{72,32} \xrightarrow{e_{107,32}} q_{74,32}$ 
•  $\chi_{te,33} = q_{0,33} \xrightarrow{e_{2,33}} q_{2,33} \xrightarrow{e_{6,33}} q_{6,33} \xrightarrow{e_{14,33}} q_{14,33} \xrightarrow{e_{28,33}} q_{28,33} \xrightarrow{e_{53,34}} q_{49,33} \xrightarrow{e_{84,33}} q_{73,33} \xrightarrow{e_{108,33}} q_{74,33}$ 
•  $\chi_{te,34} = q_{0,34} \xrightarrow{e_{2,34}} q_{2,34} \xrightarrow{e_{6,34}} q_{6,34} \xrightarrow{e_{14,34}} q_{14,34} \xrightarrow{e_{28,34}} q_{28,34} \xrightarrow{e_{53,34}} q_{50,34} \xrightarrow{e_{85,34}} q_{61,34} \xrightarrow{e_{96,34}} q_{74,34}$ 
•  $\chi_{te,35} = q_{0,35} \xrightarrow{e_{2,35}} q_{2,35} \xrightarrow{e_{6,35}} q_{6,35} \xrightarrow{e_{14,35}} q_{14,35} \xrightarrow{e_{29,35}} q_{29,35} \xrightarrow{e_{54,35}} q_{51,35} \xrightarrow{e_{86,35}} q_{61,35} \xrightarrow{e_{96,35}} q_{74,35}$