

Self-awareness survey

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1 Topics

1.1 Self-modeling

Bellman et al. (2017) Kwiatkowski and Lipson (2019b) Kwiatkowski and Lipson (2019a)

1.2 Knowledge representation and modeling structures and Trade-offs

Minku et al. (2016)

1.3 Self-awareness and inner speech

Chella et al. (2020)

2 Related terms and notices

- self-modeling robot (Kwiatkowski and Lipson, 2019a)
- Artificial consciousness: Self-awareness is a subtopic of artificial consciousness https://en.wikipedia.org/wiki/Artificial_consciousness. Consciousness alone means: Consciousness at its simplest is "awareness or sentience of internal or external existence" <https://en.wikipedia.org/wiki/Consciousness>.
- Self-expression (Lewis et al., 2011)
- Natural science computing
- evolutionary robotics

3 Assessment

Herbst et al. (2017) Esterle et al. (2017)

4 Definitions

Self-awareness Literal definitions

- implies that Self-awareness must first rely on perception of self as different from the environment and from other agents Chatila et al. (2018).
- Self-awareness models make it possible for an agent to evaluate whether faced situations at a given time correspond to previous experiences Ravanbakhsh et al. (2018).

General definition The capacity to become the object of one's **own attention**, which arises when an agent focuses **not only** on the **external environment** but also on the **internal milieu**. The agent becomes a **reflective observer, processing self-information**. It becomes **aware** that it is **awake** and actually experiencing **specific mental events, emitting behaviors**, and **possessing unique characteristics** Morin (2006).

Ego-thing go-Things are defined as intelligent systems that perceive their internal parameters and adapt them- selves when facing non-stationary situations. Kanapram et al. (2019a)[5]

Private/Public(shared) self-awareness - Subjective/Objective Regazzoni et al. (2020)[2]

- **Private** Private self-aspects relate to externally **unobservable** events and characteristics such as emotions, physiological sensations, perceptions, values, goals, and motives
- **Public** self-aspects are visible attributes such as behavior and physical appearance

Also check more detailed in Lewis et al. (2011) II-A and Baydoun et al. (2018b) Introduction.

5 Levels of self-awareness

As stated in Lewis et al. (2011) II-B As Neisser (1997) these levels of self awareness could be introduced: (See a more modern list in Lewis et al. (2017))

- **Ecological self** The ecological self is the most minimal form of self-awareness. It provides only for basic stimulus response interaction, as the organism has a basic awareness of stimuli. The ecological self can be thought of as the minimum requirement for the organism to not be unconscious.
- **Interpersonal self** The interpersonal self enables the organism to possess a simple awareness of its external interactions, permitting limited adaptation to others in the performance of tasks.
- **Extended self** The extended self extends the interpersonal self to permit reflection of interactions over time. The organism is aware of the existence of past and future
- **Private self** The private self includes that the individual can process more advanced information concerning itself,
- **Conceptual self**: The conceptual self (or self-concept) is the most advanced form of self-awareness, representing that the organism is capable of constructing and reasoning about an abstract symbolic representation of itself

There is a newer list in Lewis et al. (2017)

6 Reflective and Meta-reflective Self-awareness

All taken from Lewis et al. (2017)

6.1 Aspects of Reflective and Meta-reflective Self-awareness

6.1.1 Identity Awareness

6.1.2 State Awareness

6.1.3 Time Awareness

6.1.4 Interaction Awareness

In interaction awareness, run-time models are used to take into account patterns of interactions between entities. There are various sub-aspects here, which build on each other. Most obviously, the system must be able to recognize that some actions form part of interactions, such that they are in some way causally connected. An example of this includes message passing, such as is used in a communications protocol, where one message may be a response to another, rather than an isolated action. There may be, in simple interaction awareness, simply a model of the flow of actions over time (e.g., action b typically occurs after action a), or there may be additional semantics associated with the actions or the combination of them (e.g., actions b is a response and action a is a query).

As a prerequisite to the above form of interaction awareness, there must be some form of identity awareness, at least insofar that the system can identify messages, as apart from the general noise in the environment. It may also be important to be able to identify individuals as those engaged in an interaction, if not in terms of their unique identity, then perhaps in terms of role.

Interaction awareness can also build upon state awareness, since models may encapsulate knowledge of causality such as “when action a is taken in state s , this leads to state t .” Markovian approaches may be effective choices for modeling state- based interaction awareness.

Finally, the interactions need not be external. Causality of internal processes may also be modeled in meta-reflective processes. For example, a system might model the behavior of one of its own decision-making processes, when other parts of the system are either operational or not. In the former case, the system may learn a model of how decision-making degrades (due to more stringent resource constraints), when load elsewhere is high. Such models of internal causality may then be used to provide adaptive internal re-architecting, or perhaps more effective scheduling of tasks.

6.1.5 Behavior Awareness

6.1.6 Appearance Awareness

6.1.7 Goal Awareness

6.1.8 Belief Awareness

6.1.9 Expectation Awareness

7 Domain of self-awareness

Lewis et al. (2017)

8 Meta-Cognition

The higher levels of self-awareness, such as meta-self-awareness introduced in section Lewis et al. (2011)II-B, can also be viewed as meta-cognition, defined Van Overschelde (2008) as knowing about knowing.

9 Uncat

Approaches to tackle SA Common aspects of the proposed approaches lie on the conception of SA as

- A cognitive embodied process composed of representational and inferential operations of an agent situated in an environment,

- An agent’s property which emerges in various forms, including the extent of the SA capabilities (“levels”) Regazzoni et al. (2020)[1], Regazzoni et al. (2020)[6] and the scope of the processed information (“private and public”) Regazzoni et al. (2020)[2], Regazzoni et al. (2020)[7]

10 Application of SA

More recently, SA concepts have been transferred to artificial systems aiming at either

- Designing intelligent agents
- Analyzing their behavior

Why SA in AI? The driving motivation for the transfer of biological SA concepts to artificial systems is to improve:

- autonomy
- robustness
- scalability

and have been investigated in different fields, including software engineering, machine learning, and robotics Regazzoni et al. (2020)[8], Regazzoni et al. (2020)[9], Regazzoni et al. (2020)[10], Regazzoni et al. (2020)[11], Regazzoni et al. (2020)[12], Regazzoni et al. (2020)[13], Regazzoni et al. (2020)[14], Regazzoni et al. (2020)[15].

Challenge : A fundamental challenge in most of these approaches is how to systematically integrate SA capabilities into artificial agents.

Prospective vs exteroceptive : Proprioceptive sensors measure the internal agent’s parameters, whereas exteroceptive sensors observe the agent’s environment (cp. Regazzoni et al. (2020) Fig 1).

SA introspection The SA representation obtained by jointly and dynamically analyzing the sensory data endows the agent with introspection at different hierarchical levels.

Introspection associates with the agent’s capability of estimating and representing *dynamical causal relationships* from the observed sensory data. Such representation allows the agent to model interactions between itself, as observed through proprioceptive sensors; and the environment, as observed through exteroceptive sensors.

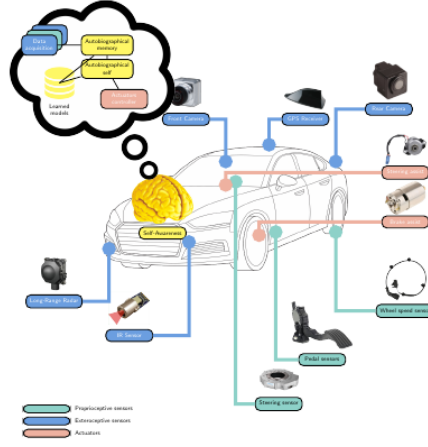


Fig. 1: Concept of a physical architecture for a self-aware autonomous system. The self-aware agent (here conceptually embedded in a vehicle) observes its surrounding environment with exteroceptive sensors (blue) and its internal state with proprioceptive sensors (green) and translates its autonomous decisions into actions through the actuators (in red). The SA core (yellow) is established based on internal representations from the autobiographical memory and the autobiographical self, together with a set of already learned models. The SA core is able to forecast the next state of the environment and the system itself, detects anomalies and executes the derived actions.

Figure 1: Regazzoni et al. (2020)

importance of embodying SA capabilities The extent of the embodied SA capabilities influences the agent's performance when solving tasks and are assumed as reasons for the significant capability differences of the various biological species.

11 Requirements to consider an agent self-aware

The following capabilities as the minimum requirements in to consider an agent self-aware: Regazzoni et al. (2020) Table I describes the proposed SA capabilities and provides a relationship between each of them and biological agents, demonstrating how humans address these capabilities.

11.1 Initialization

11.2 Reference task

Regazzoni et al. (2020); Kanapram et al. (2019a,b, 2020); Baydoun et al. (2018a) have used this method. That is, they had a vehicle and they had a rectangular path along which an automatic vehicle was driven by a human driver. This builds the normal task.

11.2.1 Random Walk

Regazzoni et al. (2020) claimed it was used in (Kanapram et al., 2019a)

11.2.2 Human/IA helped initialization

Such as human-agent driving of an Autonomous Car in an (AV)

11.3 Memorization

11.4 Inference

DBN Dynamic systems are systems whose states evolve over the course of time. In other words their future state can be described by first order differential equation of their current state on time.

11.5 Anomaly detection

Abnormality is defined by the difference between prediction and observation. So for anomaly detection these two factors usually are needed:

- Predicting model Filtering is the matter of estimating an unknown Probability Mass Function (PMF). A popular use case of filtering methods is in robotics where a robot tries to estimate its location after a set of actions it has performed.
 - **Kalman Filtering (KF)** Simon (2010) An example for Bayesian filter using a dynamic model is the Kalman Filter (KF), an optimal state estimator for linear dynamic systems with Gaussian noise iteratively predicting and estimating states from incremental observations. The posterior probability density function (PDF) of the continuous state in the KF is Gaussian.
 - **Particle Filtering (PF)** Gustafsson (2010) A Particle Filter (PF) allows one to manage a numerical approximation of the posterior in a nonlinear, non-Gaussian Bayesian filtering problem. PF approximates PDFs with a set of weighted samples (particles), which are propagated with an iterative random process. Particles are re-weighted based on dynamics and a likelihood score that depends on new observations.
 - **Markov Jump Linear System (MJLS)** Doucet et al. (2001)
 - **Markov Jump Particle Filter (MJPF)** is formed of KP+PF and follows the same direction as MJLS Baydoun et al. (2018a) a method to jointly learn coupled KF and PF models from a training sequence of state-dependent actions. Such filters are jointly used to perform Bayesian inference on a learned plan model. They are used to predict and estimate the states of a moving agent.
- A metric to measure
 - **Hellinger distance** Introduced in Lourenzutti and Krohling (2014) and used in Regazzoni et al. (2020); Kanapram et al. (2019b, 2020)
 - **Bhattacharya distance** used in Baydoun et al. (2018a)

Baydoun et al. (2018a)

- The example is is their customary example. The iCab
- The continuous space of status is formed of $X = [x, y, x', y']$ where $[x, y]$ is the position in the rectangular courtyard of Genoa university and $(x' = dx/dt, y' = dy/dt)$ is the velocity vector.
- It uses Self organising maps (SOM) to to make the above space discrete (shown by S/the vocabulary) (In their forthcoming papers they used Growing Neural Gas)
- For the first time it introduced Markov Jump Particle Filter (MJPF) in this paper and they used it in their recent papers including yours. That's why it clarify gradually everything back. MJPF predicts (filters) states in two levels. Kolman F. is responsible for predicting from previous X to next X and Particle filter is responsible for Predicting from previous S to nex S (previous=time stamp $k-1$, nex= time stamp k)
- Now that there is method to predict, it introduces three metrics for abnormality prediction db1 (eq 18), db2 (eq 19, just assumes that Z happens close to X), y (eq 21 based on weighted distance described in Eq5)
- They tested like this: a human rode the vehicle along the rectangular courtyard. Please notice that they say that location data had 10 cm position accuracy (this is what forms the difference between Z (observation/what is measured by sensors) and X (true status))
- In the next phase they performed three different maneuvers when the normal rectangular path (reference task in your paper) is interrupted. 1. turning around the pedestrian (called avoidance abnormality Fig 7) 2. U-turn (returning back Fig 4c , abnormality Fig 8) 3. And stopping until the pedestrian goes away from the cam view. (abnormality Fig 9)
- Why this paper is important? Abnormality indexes use the generated discrete states in their calculation but the results in Fig 7,8,9 show how well extracted abnormalities from reference task matches the times in the three cases that the pedestrian interrupted the path in all three maneuvers. So their abnormality indexes are maneuver independent, can work on discreet data etc. This discreet state space can form a vocabulary.

Kanapram et al. (2019a) This paper has used MJPF (Markov Jump Particle Filter) and Hellinger distance for feature selection. It wants to pick a feature which is more accurate in predicting and abnormality detection. Normal task is turning around the rectangular of university courtyard without any obstacle and abnormal is the time that the AV has to perform a U-turn when an obstacle interrupts the perimeter. While performing the normal task it gathers 3 sensory data Steering, Velocity and power. Then it uses GNG to make space state and

generate the alphabet of state space and then it puts together the centroid of each cluster and its time derivatives in one set as a word. (Although position is not measured here but you can consider the state space like $[x, y, v_x, v_y]$ and then have one GNG for positions and another for speeds. then each word is made of the centroid of a position class and the centroid of a speed class). Now that we have words, we can use MJPF to observe continuous data and predict the next time-step discrete data (the next word). By this prediction and hellinger distance (eq 5) we can measure the abnormality arises from taught DBN for normal task against the U-turn. On page 5 it tested eq 5 (using the learned MJPF from the normal task) for several features and table 1 on page 7 shows the best feature which eq 5 can get its abnormality and provide better prediction is SP (S=steering, P=Power). (I personally expected SV is the best feature, but MJPF proves that it is better to consider power instead of velocity).

Baydoun et al. (2018b) In this paper, anomaly detection was tackled from two layers of self-awareness. The Shared-level (SL) and Private Level (PL). SL is what is visible by an external observer but PL is only available to the agent. SL is considered the position and velocity of an Autonomous Vehicle (AV) which is observable by an external observer and PL is the video frames captured by the AV. Anomaly detection is performed by training two different models on a reference experience (in this paper, it is called Environment Center (EC) Model, in SA models such as Regazzoni et al. (2020) these reference tasks form initial models) and comparing their predication with the observations from a new task/experience. The reference task is perimeter monitoring (PM) of the rectangular courtyard of Genoa university and the new experience is when this rectangular path is interrupted by a pedestrian twice (Fig 3, a and b). For SL abnormality detection, they have used Gaussian Process (GP) to divide the perimeter into quasi-constant velocity zones (speed is constant in these zones) and over these zones they have trained a bank of Kalman Filters (KFs) for regional position estimation. A sample of such perimeter partitioning can be seen in Fig 7. During the new experience, the distance between KFs bank prediction (trained during the reference task) and the observations come from online, new experience, forms the abnormality measurements which is presented in Equation (3) and graphed in Figure (5). It has captured four times the presence of a pedestrian in two times circling around the perimeter and even 8 times (but lower than the abnormality threshold) the corners of the perimeter. To tackle PL abnormality detection, they have used a GAN with two discriminator and two generators. Each G-D pair is responsible to predict-score once from frame to optical flow and once from optical-flow to frame. GP zones (from the previous experience), will be used here to train a bank of discriminators (similar to banks of KFs) for scoring predicted data from generators. This whole process is performed for two sets in two GANs (GAN 1 and GAN 2). Set1 is for learning straight paths and Set2 for training curves. The abnormality resulted from Eq(4) is used to create Fig 6. The new abnormality which is the result of minimum of GAN 1 and GAN 2, resulted in a better description of the new

TABLE I: Definition of self-awareness capabilities and biological relationships.

Self-awareness capability	Definition	Biological relationship
Initialization	It refers to the initial knowledge from which an agent starts building its own memories. Such initial knowledge provides the agent with the essential tools to interact with its surroundings.	The basic structure of the brain is laid down primarily during the prenatal period, where its <i>initialization</i> depends largely on genetics [16].
Memorization	It refers to the agent's capacity of storing and retaining information such that it can be recovered and exploited in the future.	Long-term memories are stored throughout the brain as groups of neurons that fire together in the same pattern that created the original experience. Such operation is done by the process of memory allocation [17].
Inference	It consists of the agent's ability to make predictions about its own future states and its surroundings depending on its current state.	The brain is responsible for anticipating future events. The <i>predictive coding</i> theory [18] states that at each level of a cognitive process, the brain generates beliefs of the information it should be receiving from the level below it. These beliefs are translated into predictions about what should be experienced in a given situation.
Anomaly detection	It consists of the agent's ability to recognize observations that cannot be explained by its memories. These observations represent new events that the agent has not detected so far.	Brain predictions are sent as feedback to low-level sensory regions of the brain. The brain then compares its predictions [19] with the actual received sensory input and "explains" high differences (prediction errors) between them.
Model creation	It refers to the agent's capability of generating models that encode previous experiences, facilitating the prediction of the agent's future states and the posterior comparison with evidence.	The prediction errors that can't be explained away get passed up through connections to high levels of feedforward signals, where they are considered newsworthy. The internal models get adjusted so that the predicting error gets suppressed [20].
Decision-making influence	It refers to the ability to generate signals that can be employed by the agent's control system such that its actions are self-monitored dynamically	Muscles move based on commands from the brain [21]. Nerve cells in the spinal cord, called motor neurons, enable to convey and evaluate the brain's commands to the muscles.

Figure 2: Table I

experience because not only it can detect the presence of a pedestrian 4 times in two laps, but also it can predict abnormality (pedestrian presence) a few moments before and capture camera's noise on straight paths because of AV's higher speed.

11.6 Model creation

11.7 Inference with control (Decision making)

12 Computing architectures

Sanz et al. (2009)

13 bio-inspired self-awareness theories

13.1 Damasio's Model

https://en.wikipedia.org/wiki/Damasio's_theory_of_consciousness and Damasio (1999)

autobiographical memories (AMs) Neuroscientists such as Damasio Regazzoni et al. (2020)[28] have provided evidence that neural patterns in the oldest parts of the human brain are organized to process and combine proprioceptive and exteroceptive sensorial information according to hierarchical neural layouts culminating into so-called *autobiographical memories (AMs)*.

AMs can constitute a sort of database for memorizing models of **episodes** that the agent has learned from previous experiences Regazzoni et al. (2020)[5].

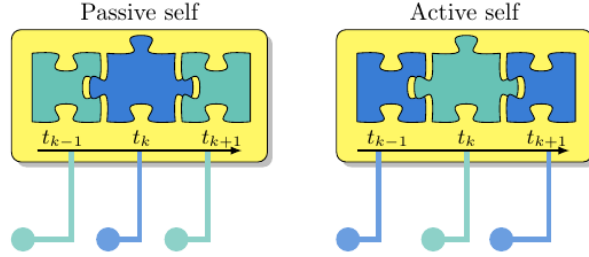


Fig. 2: Two elementary information units depicted in the yellow box correspond to the passive (left) and active (right) self [29]. The passive self unit stores triplets formed by data alternatively acquired from proprioceptive and exteroceptive sensors at different time instants. Proprioceptive data are acquired at time instant t_{k-1} and are followed by data from the environment at time t_k captured by exteroceptive sensors. They cause a change of the internal state of the system at time t_{k+1} that is monitored by proprioceptive sensors. Vice-versa, the active self elementary unit models the cause-effect relation between the data acquired by exteroceptive and proprioceptive sensors.

Figure 3: regazzoni-2020-multi-sensorial-generative-and-descriptive-self-awareness-models-for-autonomous-systems-fig-2.png

Bio-inspired AMs have already been investigated towards implementing self-awareness in artificial agents, for example, in Regazzoni et al. (2020)[29]. Based on anatomical observations, Damasio suggests that episodes in AMs are **represented by a language coding proprioceptive and exteroceptive information according to a temporally ordered causal representation**. Fig. 2 depicts the combination of estimations of the agent's own the external world's state obtained by an early neural layout (named "proto" and "core", respectively) in the form of temporal-causal AM patterns.

According to Damasio, AM patterns are based on *first-person situational descriptors* that enable human agents to represent experienced episodes on the basis of a **neural vocabulary** (i.e., information units). These descriptors always represent exteroceptive data as contextualized to information coming from the agent's body, and vice versa. Thus, patterns encoding episodic experiences are represented by coupling the agent and its dynamic interaction with the surrounding environment.

Elementary information units used in AMs define a temporal representation where an agent and the environment reciprocally take on the role of a *context*. Temporal changes of the internal representation of the state of one of them (that Damasio calls "dispositions") are observed as occurring in the context of the other one assuming a given state (see Fig. 2). Sequences of such patterns

are stored in the AM representing episodes. Therefore, at least in humans and biological agents, SA is based on a **contextual** representation, which is essential for the emergence of the expected SA capabilities as listed in Regazzoni et al. (2020) Table I.

Key element in SA knowledge A dynamic description of agent and environment changes based on their reciprocal states is a key element for the representation of SA knowledge. This is different from many traditional AI systems, where exteroceptive sensory data sequences are often represented at a primary level *without explicit contextual* information.

Traditional AI systems do not consider contextual data: This is different from many traditional AI systems, where exteroceptive sensory data sequences are often represented at a primary level *without explicit contextual information*. As a **consequence**, high-level processing techniques, for example, classifiers based on supervised labeled learning [30], [31], [32], use implicit contextual information to cluster such data into homogeneous groups.

A problem: Despite the impressive classification performance that can be achieved when testing data and training experiences belong to the same class, the observing artificial agent cannot reliably connect such classification results to its internal dynamical state when performing similar actions to the ones performed during training, simply because its state was not observed and memorized together with the observed exteroceptive data. It is therefore not trivial to use such classifiers as building blocks for an artificial agent due to the limited adaptability.

Damasio [28] proposed dispositional units, i.e., information units representing contextualized state changes of the agent or the environment, for modeling “**cognitive cycles**”, i.e., episodes that can be found as the *basis of human self-awareness*. Moreover, he suggests that dispositional units can be hierarchically organized at different levels in the brain, for example for describing *temporal-causal* representations in the activation and processing results of neuron maps dedicated to different goals. Consequentially, an AMs should be hierarchical structured for providing SA models, and thus dispositional units’ representations should be defined such that they can be organized in multi-level hierarchies (see Fig. 3).

Autobiographical self Neuroscience observations show that the parts of the human brain storing AMs are linked and can exchange neural signals with other parts of the brain known to be activated within conscious inference processes [33]. The role of such neural maps is to analyze—at different hierarchical levels—proprioceptive and exteroceptive sensorial data originating from the current agent’s experiences. The process of *recalling* and *comparing multi-level AMs with respect to current experiences* is an *integral capability* of self-awareness related to inference and anomaly detection, which is defined by Damasio as **autobiographical self** (AS).

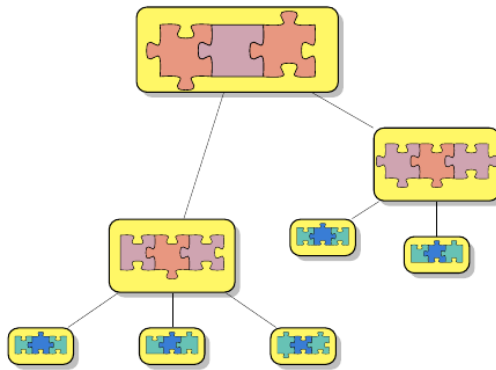


Fig. 3: Hierarchical organization of dispositional units in the autobiographical memory. According to Damasio [28], these elementary information units can be found at different levels in the brain and constitute temporal-causal representations of cognitive processes. This hierarchy expresses experiences at different time scales: directly connecting exteroceptive and proprioceptive data at the leaves and more complex and structured information corresponding to long terms goals at higher-level nodes.

Figure 4: regazzoni-2020-multi-sensorial-generative-and-descriptive-self-awareness-models-for-autonomous-systems-fig-3

Application of AS The AS allows an agent to evaluate whether the current experience matches any episode stored in the AM. Moreover, the AS must provide inference processes to interface with other parts of the agent’s brain (e.g., blocks dedicated to agent’s resource planning and control of actuators) to maintain a dynamic stability condition, i.e., homeostasis Regazzoni et al. (2020)[34].

In a SA model, the inference capability implies that activated AMs’ dispositional units and currently experienced data elaborated by early neural maps can be managed by the AS inference process to perform, for example, predictions on the agent’s future states. Based on the temporal-causal organization of the available episodes stored in the AM, the AS is able to predict future states at multiple abstraction levels by using generative models that represent possible alternative realizations of episodes already experienced adapted to currently observed data. As multiple episodes are stored in the AM, the AS inference processes need to identify models that better match the current experience, which requires the dispositional units’ representation in a SA model to inherently provide a discriminative property to assess current data characteristics.

in AI An artificial AS is also required to determine the difference between episodes contained in its own AMs and the current experiences based on an appropriate metric, which can be interpreted as the basis for the abnormality detection capability (see Fig. 4).

In order to assess the matching degree between predictions derived from the dispositional units of the set of potentially applicable episodes and the current observations, the SA agent must apply a computable metric invariant to the sensor modality. In this case, the agent should be aware that an abnormality, i.e., a non-stationary condition never experienced before, is currently present. Damasio does not address which specific computational neural characteristic included in the neural implementation is able to realize such computational behavior. He only suggests that such matching and prediction inference capabilities can be performed by the AS at different abstraction and temporal levels and so enabling an efficient selection of the hierarchical and dispositional representation of AMs episodes).

Rise of emotions It is worth mentioning that for natural agents, Damasio suggests that the integrated SA system composed by AM and AS can also be used as a possible explanation of higher-level human regulatory psychological phenomena such as emotions and feelings [35]. Emotions and feelings can be considered as emergent results of evaluating current experiences based on multi-level hierarchical AMs by means of the AS [25]. For example, fear can emerge from the capability of detecting abnormalities, recognizing that the current experience does not match with past AMs, or it matches with AMs that describe dangerous episodes. Damasio’s model implicitly implies that AS outcomes enable an agent to incrementally update internal AM models by coding abnormal experiences into new models as well as to define a SA system that derives infer-

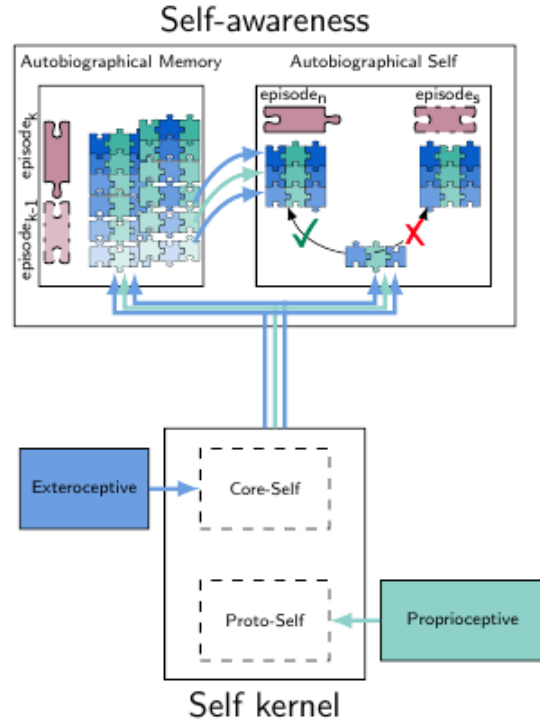


Fig. 4: Autobiographical memory (AM) and autobiographical self (AS) as core components of a self-aware agent founded on Damasio's model. The core-self and the proto-self process exteroceptive and proprioceptive information and store them as dispositional units in the AM. The AS is able to perform inference and anomaly detection based on the stored episodes.

Figure 5: Fig. 4: Autobiographical memory (AM) and autobiographical self (AS) as core components of a self-aware agent founded on Damasio's model. The core-self and the proto-self process exteroceptive and proprioceptive information and store them as dispositional units in the AM. The AS is able to perform inference and anomaly detection based on the stored episodes.

ences invariant to the involved sensor modalities.

13.2 Haykin's model

In comparison with Damasio's work, Haykin proposes a computational framework of neuroscience observations from an engineering perspective referred to as **Cognitive Dynamic Systems (CDS)** [36]. The proposed CDS model is based on the interactions that a *Cognitive Controller (CC)* part of a CDS has to maintain at multiple levels of abstractions with a *Cognitive Perceptor (CP)*. The CP processes exteroceptive information coming from the environment at different hierarchical levels and can be seen as a hierarchical probabilistic filter, generating environment descriptions at different abstraction levels.

Beyond providing information to higher levels, such a filter generates hierarchical feedback information to the CC, which in turn computes commands to actuators that are characterized by uncertainty. The CC block of Haykin's model is described as a top-down structure generating outputs towards lower levels. *At the bottom layer*, it directly generates outputs for the *actuators*.

The *Probabilistic Reasoning Machine (PRM)*, introduced in a joint paper with J. Fuster [37], organizes probabilistic information coming from the CP, i.e., percepts and errors (prediction and update processes), together with information coming from the CC, i.e., planned actions with its related uncertainty. Such an organization is performed over time. As can be seen in Fig. 5, Haykin's model does *not directly employ proprioceptive* sensory data but uses internal strategies to generate commands towards actuators. The **main goal** of the PRM is to maintain a meta-level representation of the *perception-action* cycle based on switching and adapting the behavior of CP and CC.

The relation between Haykin and Damasio As the control strategies embedded in the CP are hypothesized to maintain homeostasis, i.e., a dynamic equilibrium between the agent's state and the changes in the environment, the PRM is contributing to the continuous regulation of agents' processes by providing switching suggestions to CP and CC. Those suggestions are implicitly based on the knowledge that an agent must have been learned from experiences, and it is represented within the PRM. **In this sense, the PRM block is strictly related to Damasio's SA model**, as it has to process representations of actions and percepts organized in a **temporal-causal** order, and the *PRM block can be related to AM and AS as SA model capabilities*.

The PRM elementary representation requires organizing perception and actions into data structures capturing causal and temporal interactions between the agent's actions and percepts originated from the environment. Dispositional information units, as described by Damasio, also represent such interactions but are different because the state of the agent is directly observed by itself. This can be considered either as feedback for the SA agent to evaluate the outcome of commands it has sent to actuators and lower-level blocks or as a multi-sensor

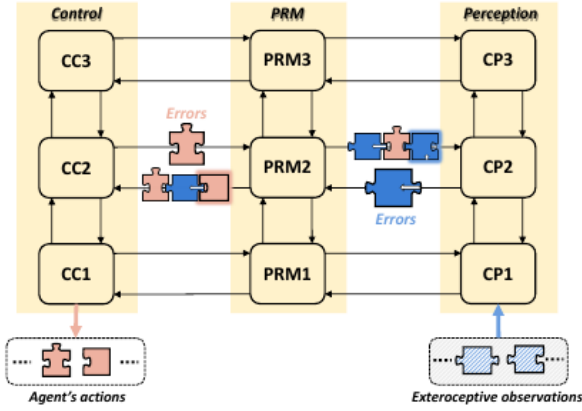


Fig. 5: Hierarchically structured probabilistic reasoning machine (PRM) adopted from [37]. The cognitive perceptor (CP) processes exteroceptive information (“percepts”) at different hierarchical levels, and the cognitive controller (CC) generates outputs towards the actuators in a top-down structure. The PRM organizes probabilistic information from perception and control by data structures capturing causal-temporal interactions that are similar to “dispositional units”.

Figure 6: Fig. 5: Hierarchically structured probabilistic reasoning machine (PRM) adopted from [37]. The cognitive perceptor (CP) processes exteroceptive information (“percepts”) at different hierarchical levels, and the cognitive controller (CC) generates outputs towards the actuators in a top-down structure. The PRM organizes probabilistic information from perception and control by data structures capturing causal-temporal interactions that are similar to “dispositional units”.

source of proprioceptive signals representing the agent state to itself. This concept is exploited in Regazzoni et al. (2020) SA model (depicted in Fig. 10). If this second view is taken, a modified PRM can be considered as a structure where appropriately modified dispositional units are processed based on hierarchical filters that work on proprioceptive feedback and in a bottom-up way also in the CC.

In Haykin’s approach, the *focus is on control* instead of SA. Therefore, the PRM is designed to make a CDS capable of using interactive behavioral rules to switch among different perceptions and action modalities adaptively. Such inferences can drive actions that the agent’s sensors and actuators should accomplish anticipatorily by activating available models in the PRM memory when it performs a given experience. This allows the CDS of an attention capability towards preferred control or sensing actions in a given homeostatic cycle. In the case of the SA model discussed here, the agent has no direct knowledge of the control strategy actions that are generated by its own decision-making subsystem, but it can observe and fuse their outcomes through parallel proprioceptive feedback from sensors coupled with exteroceptive environmental observations. Haykin’s model, however, suggests how a SA model can provide useful data to adapt decision making processes behaviors at homogeneous hierarchical levels to the PRM. For example, SA can share with decision-making estimates of present and predicted contextualized states as well as errors and deviations of models describing previous agent experiences.

Furthermore, Haykin’s model facilitates identifying temporal variations of uncertainty associated with actions and percepts, which is a key aspect for addressing a proper computational framework for the CDS design, i.e., a PRM in Regazzoni et al. (2020) SA model. Moreover, the organization of a PRM at multiple abstraction levels is coherent with the hierarchical characteristics of Damasio’s dispositional units. In this case, actions and percepts as temporal aggregations (equivalent to dispositional units) at different hierarchical levels can describe the joint state of lower-level parts of the agent body down to the directly observed proprioceptive and exteroceptive characteristics of the agent and the environment. Although Haykin’s approach does not provide a specific probabilistic model for uncertainties and dependencies, it proposes a Bayesian framework to model uncertainty and causality and make inferences computationally, e.g., parametric conditional probability models.

Although the goal of Haykin is not to specify a univocal PRM model but to provide a generic framework for CDSs, his model is essential for addressing the main techniques for SA in artificial agents. His work then suggests that SA models originating from a computational domain should be associated with an appropriate calculus of uncertainty propagation. In [38], a CDS inspired by such a probabilistic approach uses a simple PRM unit that allows a vision system on a mobile platform to make inferences about future states. Moreover, Haykin’s

work does not directly provide a unitary view of the techniques that could be used to store a coherent multi-level generative and discriminative PRM’s knowledge. Nonetheless, Regazzoni et al. (2020) work integrates Haykin’s viewpoint on uncertainty and makes a relation between the perception-control blocks and Damasio’s theory, which includes AM and AS and dispositional units. Regazzoni et al. (2020) Fig. 10 displays a revisited block scheme of Haykin’s model.

13.3 Friston’s model

Another relevant cognitive framework for SA that aims at establishing links between neuroscientific observations and computational models is the one proposed by Friston [39], [27]. Here, Bayesian dynamical systems are the computational tool that facilitates an uncertain and hierarchical self-coherent representation to describe and generate simulations of inferences performed by the human brain utilizing neuron firings. Friston’s approach is innovative in the context of developing self-aware models for artificial agents due to the following characteristics: i) It formally relates a statistical mechanics’ optimization framework, that can be summarized as free energy and variational based reasoning, with Bayesian inference. It founds a theoretical domain for describing SA knowledge and models (in the AM) as well as inference (in the AS). ii) It proposes the concept of generalized states (GS) to develop a class of computational and hierarchical Bayesian filters that we use to embed representation and inference over dispositional temporal knowledge.

The good regulator theorem [35] states that “every good regulator of a system must be a model of that system”. In this sense, SA models can be considered as joint discriminative and generative models that contribute to the regulation of an artificial agent representing an adaptive code of the system itself and its incremental experiences at the same time. The free energy principle represents an optimization criterion that can be related with a variational computational framework to both define and discover optimal SA models from a given set of dynamic experiences, i.e., available data sequences originating from exteroceptive and proprioceptive sensors.

In [27], Friston suggests that establishing an equivalence between a probabilistic and a mechanical statistics’ representation of the dynamic equilibrium in the sensed internal state and the contextual environment allows one to explain the observed neuron firing in the human brain through the free energy concept. He further shows that Bayesian inference is an equivalent way to do so. As SA in humans is based on brain inference processes, probabilistic dynamic representation and inference models are good candidates to form the **language** for expressing a SA model in an artificial agent as well. Such models must be capable of including temporally ordered descriptions of contextual dependencies between proprioceptive and exteroceptive variables.

The variational computational representation and inference techniques he proposes clarify how different models can describe statistically different sensorial experiences that can be seen as trajectories in generalized spaces. The models can also provide explicit measurements to evaluate or to discriminate best-fitting models of new observed sequences. At the same time, the same models, that can include multiple conditionally connected random variables at different hierarchical and temporal levels, are capable of predicting multi-level, temporal data series characterized by the same statistical properties of the training experiences from which they can be learned (thanks to their generative nature). Such a model, if used within the SA model of an artificial agent, together with appropriate learning techniques, can facilitate incremental model creation. An AS can so actively memorize incrementally generative and discriminative new models in the AM by processing sensorial experiences. Such models have to capture different causality interactions between the agent and the environment and serve as the basis for *symbolic* descriptors in an artificial SA agent.

The SA capability of abnormality detection can also be explained with Friston’s model, i.e., the free energy that models generate when the AS compares them to a new experience. A metric can be defined to evaluate the amount of abnormality which is related to a particular component of free energy, describing the orthogonal perturbations to the dynamic equilibrium condition described by the model. Such a metric enables the AS to rank the abnormalities measured from a set of AM models, so relating the discriminative SA property of the model to the abnormality detection and inference capabilities.

Contribution ii) to the SA model definition is a specific class of Bayesian filters, namely GS filters. Friston et al. [40] explain that thanks to such filters, active and variational Bayesian inference techniques can be obtained with better performances. GSs describe a class of trajectories in terms of generalized coordinates of motion. The resulting model can be shown to better describe the dynamical nature of the pattern in terms of temporal and causal explainability of dependencies among states as well as computational benefits. In a SA model, hierarchical Bayesian models derived from GS filters can provide the description language for the AM, depicted as individual “pages” in Fig. 6. Regazzoni et al. (2020) shows how these models can be learned by observing proprioceptive and exteroceptive data series both independently and in a coupled way that is oriented to represent their dispositional nature. Such filters can be used both as generative and discriminative models, and they can be good candidates to be related to the “good regulator” code [35], as they can represent the rules that describe the agent, as well as such rules, can be used by the agent to predict the dynamic contextualized behavior where it is acting.

Coupled proprioceptive and exteroceptive signals of GS filters can efficiently represent Damasio’s dispositional units in a SA model. For example, a Switching Dynamic Bayesian Network (DBN) [41], [42] uses multi-level discrete and

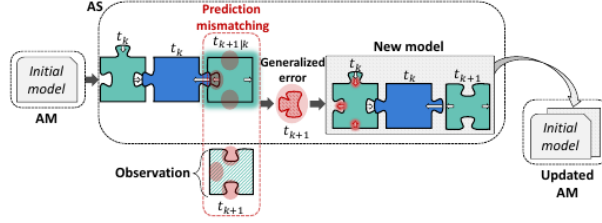


Fig. 6: An **initial** model is employed to predict passive self states, i.e., glowing green puzzle pieces at instant $t_{k+1|k}$. Errors from such a model are utilized to **create** new models, depicted as new *pages* in the **AM** structure. Such new models minimize the free energy between the agent’s **inferences** and the observed data. Note that the same logic can be applied to an active self (blue-green-blue puzzle pieces).

Figure 7: Regazzoni et al. (2020) Fig. 6

continuous generalized states as variables that will be further discussed in the following sections.

Dynamic Expectation Maximization (DEM) filters [40] are hierarchical parametric GS filters that are here used to derive coupled GS-DBNs. These filters have been shown to jointly perform parameter, hyperparameters, and GS estimations within a continuous variable Bayesian network that is by itself a fully continuous DBN. However, discrete variables are needed in a SA model too. Such variables are used to represent different models (i.e., different pages in the AM structure) and to provide finer level discriminative descriptions of learned models to determine a different class of probabilistic dependencies within an episode, useful both for generative and discriminative purposes. Coupled GS-DBNs are, therefore, better-suited filters than DEM, in particular when all model properties are necessary to reach the SA capabilities (see Fig. 7).

14 SIGNAL REPRESENTATION AND MODEL LEARNING

14.1 Bio-inspired SA Model

The main difference between Haykin’s and Damasio’s models is that the objective of the latter lies in the bottom-up explanation of neuroscientific observations, while the first one focuses on the definition of control within a CDS. Similar to Haykin’s model, Friston’s approach is based on a Bayesian and computationally efficient approach for SA representations. Friston’s approach is more focused on a bottom-up joint analysis of proprioceptive and exteroceptive

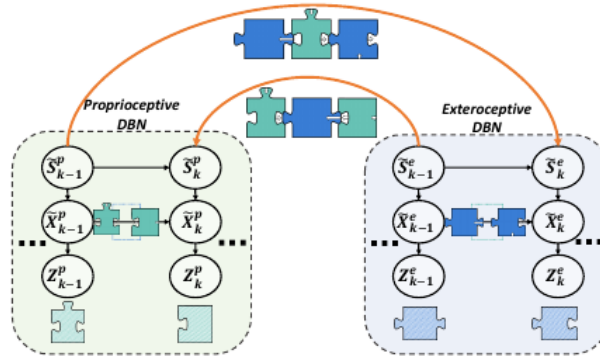


Fig. 7: Proprioceptive DBN (P-DBN) represented in a green block and exteroceptive DBN (E-DBN) represented in a blue block are connected by orange links that encode the agent's **contextual information**. Each DBN (P-DBN and E-DBN) performs continuous \tilde{X} and discrete \tilde{S} inferences. This coupling facilitates to model **interactions** between multi-sensory data and perform inferences within a contextual SA framework. Observations are represented as Z , and k encodes time instances. Proprioceptive and exteroceptive information is indexed as p and e , respectively.

Figure 8: Regazzoni et al. (2020)Fig. 7

TABLE II: Comparison of inherent self-awareness properties of the presented bio-inspired self-awareness theories.

Self-awareness properties	Damasio's model	Haykin's model	Friston's model
Generative modeling	Dispositional units are facilitated to make non-probabilistic predictions of future agent's states based on a top-down approach	Predictions of next actions and exteroceptive states performed by the PRM	Predictive GS probabilistic models
Discriminative modeling	Not considered	Not considered	Focused more on filtering than on semantic labeling of experiences
Interactive	It includes dispositional units but interactions are not explicitly explained	PRM relates information between exteroceptive data and agent's actions	Self-organization in agents explained as system of GS filters related to agent actions and sensory perceived environment
Hierarchical modeling	It considers several abstraction levels ranging from raw observations to feelings/emotions	Multilevel representation of control, PRM and perception, see Fig. 5	Continuous variables in upper inference levels parameterize predictive models in lower ones
Temporal reasoning	Dispositional units relate present states with future ones	Temporal dependencies between control and environment perception during time	In Bayesian DEM filters different temporal reasoning at abstraction levels of parameters and GSs
Uncertain reasoning	Not considered	Bayesian reasoning	Equivalence of active Bayesian inference and attractors in statistical mechanics

Figure 9: Regazzoni et al. (2020) Table II

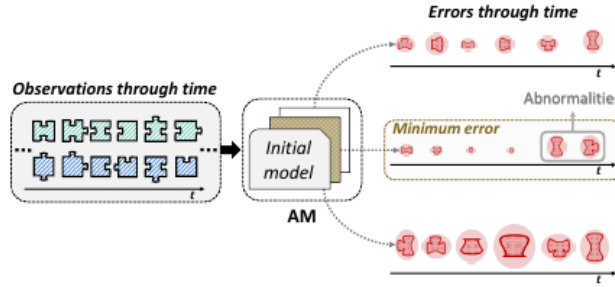


Figure 10: Regazzoni et al. (2020) Fig 8 Models in the agent's memory produce error measurements as observations arrive. The fittest model is identified/discriminated and abnormalities (high errors w.r.t a threshold) are extracted from it. Such high errors are then used to create new models incrementally as shown in Fig. 6.

signals, while Haykin's model aims at providing a framework for defining computational aspects of perception-action cycle decision making outcomes towards actuators in a CDS. A computational SA model for an artificial agent can be obtained by merging different aspects of the three frameworks. Such SA model should include SA properties as discussed in Section I and enlisted in Regazzoni et al. (2020) Table II.

How to build new models from big errors Regazzoni et al. (2020) Fig. 6 and Fig. Regazzoni et al. (2020) 8 depict how the AM can be represented as a book containing **multiple pages**. Each page corresponds to a probabilistic model learned based on observed sequences of dispositional units during different experiences. Such a model should be both generative and discriminative.

Basis for initialization Regazzoni et al. (2020) Fig. 6 shows that an initial reference model serves as a **basis for initialization**. This initial model should represent quite general behavioral rules obtained in correspondence to a reference experience. For example, as Regazzoni et al. (2020) will show, it can contain knowledge useful to predict the agent's state, even if the environment does not interact with it, and therefore exteroceptive signals do not provide significant contextual temporal and causal information. In that case, the expected agent's state changes are null, except for random perturbations, and state and its derivatives estimated from proprioceptive signals can be stationary.

The initial model and all generated models in the AM must be generative, i.e., they should be capable, under the effect of a latent null variable, to generate a sequence of predictions in the form of expected probabilistic properties of the dispositional unit that could be observed as evidence. This has to happen as part of the inference process in the AS module. The AS module must be capable of comparing the current set of dispositional units from the current experience with the predictions of the **currently activated AM page**. This comparison has to produce both an evaluation of the **mismatch degree** between predicted and observed dispositional units but also to describe such errors and memorizing them for further steps. When mismatches are relevant, i.e., abnormalities with respect to the initial model are too high, the sequences of dispositional units and related errors (generalized errors) are processed for describing the **new experience**. The model creation phase organizes such data series that can be considered as sparse acquisitions of generalized errors with respect to selected AM available models, e.g., by using unsupervised machine learning tools into new models. The results of the analysis of the sparse generalized errors are described again in terms of behavioral rules expressed using generative models with the same language of the initial models. **Such new models can be seen as new pages to be added to the AM book.** Memorization includes the capability to organize the learned models within the AM model as incremental pages in a book. Regazzoni et al. (2020) Section II-B describes how this can be obtained starting from free energy and generalizes state concepts in a way inspired to Friston's approach.

Regazzoni et al. (2020) Fig. 8 highlights the inference capability of the AS when the AM is composed of multiple pages, i.e., to **discriminatively select a page that better fits to the current experience**. Again, this can be obtained by comparing the generalized errors obtained by processing in multiple parallel models and evaluating when the minimum detected error is sufficiently small. The page which produced such a set of generalized error also contains the causal and temporal knowledge to predict the dynamic evolution of the contextual state of the agent and the environment, so providing to the agent a symbolic and continuous SA description of what is happening compared to past experiences. The minimum abnormality criterion to discriminate the most fitting model can be considered as the selection of the model characterized by the

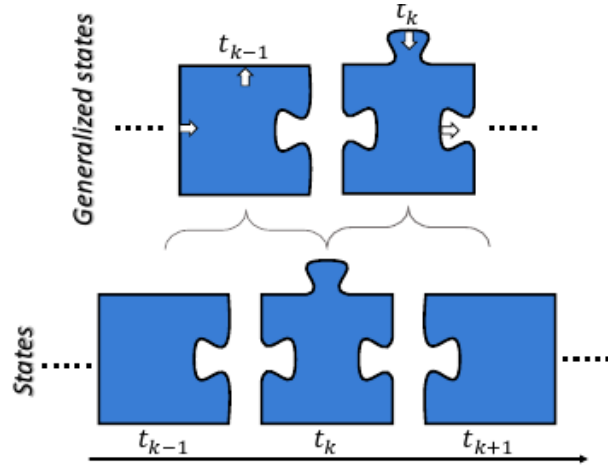


Figure 11: Regazzoni et al. (2020) Fig 9 Relationships between exteroceptive states (bottom) and generalized states (top). Two consecutive states are abstracted into a generalized state that has information about i) the current state (depicted by the shape of the puzzle piece) and ii) its derivative (depicted by the arrows pointing at the expected state's change in the succeeding time instant). Note that the same logic can be applied to proprioceptive data (green puzzle pieces).

lowest generalized error, evaluated by using an appropriate metric. Therefore, the SA discriminative capability results by comparing the current experience to the generated predictions of a set of models of experiences available at a given moment in an agent. Regazzoni et al. (2020) Fig. 8 shows how the inference process in the AS can also generate useful information for decision making. In particular, the set of predictions and related errors derived from comparing activated models with the current dispositional units can be used by a decision making block to plan resources usage as well as to decide among alternative actuator signals to perform planned actions.

Regazzoni et al. (2020) Fig. 9 shows that, in contrast to Haykin's theory, the SA model does not explain the perception-action cycle, so it does not include a hierarchical control block. Instead, proprioceptive signals provided by observing agent actuators are processed in parallel in a bottom-up way with exteroceptive signals processed in the block defined as Perception in Regazzoni et al. (2020)[43]. As can be seen in Regazzoni et al. (2020) Fig. 10, the PRM is replaced by the SA model as it aims to organize extero and proprio percepts, with the latter being considered as the feedback generated by actuators controls by the agent itself.

For the proposed model to be effective, it must fulfill the properties listed in Table II. In particular, Regazzoni et al. (2020) note that the content of AM pages represents models organized into random variables that should come from observations of dispositional units (i.e., interactive variables embedding causal and temporal aspects). They are random variables at multiple hierarchical levels. Moreover, the SA process has to be autopoietic in the sense that it should be able to learn new pages of the AM book from computed generalized errors by generating predictions from pages already available in the AM book. As a function of generalized errors over the generalized state-space describes the differences between the current experience and the existing AM page, this means that a new page generated during model creation should provide a generalized null error, i.e., that learning process should be capable of representing a function of generalized error over the generalized state space as a book page model.

15

16 SA in computational context

In a computational context, self-awareness (SA) is a capability of an autonomous system to describe the acquired experience about itself and its surrounding environment with appropriate models and correlate them incrementally with the currently perceived situation to expand its knowledge continuously.

17 Definition from sensor data and signal processing perspective

: An artificial agent is considered self-aware if it can **dynamically observe itself** and **its surrounding environment** through different **proprioceptive** and **exteroceptive** sensors and **learn** and **maintain a contextual representation** by processing the observed multi-sensorial data.

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