

$$\forall \theta, \forall \text{Dist}, \quad \text{Adv}^{\text{Dist}}(\text{Enc}(\theta), \text{Enc}(\theta^*)) \leq \text{negl}(\lambda)$$

\downarrow

$$\forall \theta, \theta', \forall \text{Dist} \quad \text{Adv}^{\text{Dist}}(\text{Enc}(\theta), \text{Enc}(\theta')) \leq \text{negl}(\lambda)$$

To show this, take the contrapositive:

$$\exists \theta, \theta', \text{Dist.} \quad \text{s.t.} \quad \text{Adv}^{\text{Dist}}(\text{Enc}(\theta), \text{Enc}(\theta')) \geq \eta$$

η is non-negl.

Then, we want to argue that either

$$(I) \quad \text{Adv}^{\text{Dist}}(\text{Enc}(\theta), \text{Enc}(\theta')) \approx_{\text{negl}} \text{Adv}^{\text{Dist}}(\text{Enc}(\theta), \text{Enc}(\theta'))$$

or

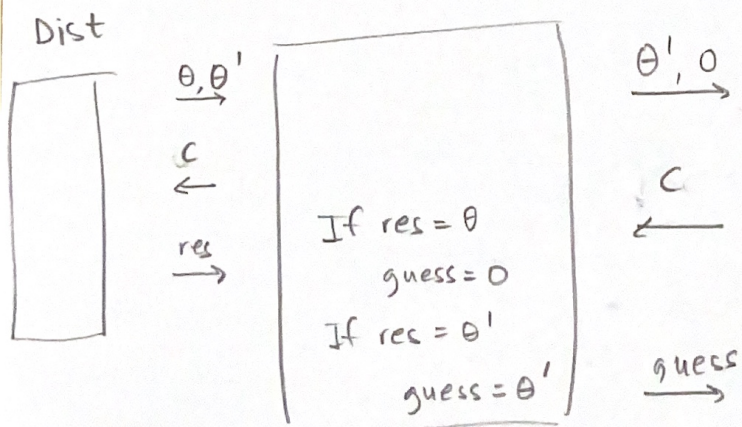
(\Rightarrow Dist also distinguishes $\text{Enc}(\theta)$ & $\text{Enc}(\theta')$)

\exists Dist' that distinguishes $\text{Enc}(\theta), \text{Enc}(\theta')$

OR

(II) same as (I) w/ θ & θ' swapped.

We construct Dist' as follows:



claim: Dist' wins w/ non-negl prob (or its opposite guess does)