

- 6.1 Given an array a_1, \dots, a_n , to compute the longest contiguous subsequence sum, we first consider the best sum, s_b and the current sum at that variable, s_c , and set them respectively to $s_b = -\infty, s_c = 0$, additionally we define the start and end indices of the ideal sum to be and the current sum as i_s, i_e, c_s, c_e . Then we iterate through the array, where for each $i \in [n]$, we first check if $a_i > a_i + s_c$, if this statement is true we set $c_s = i$ and $s_c = a_i$. If $a_i = a_i + s_c$ we set $c_s = i$. If $a_i < a_i + s_c$ we set $s_c = s_c + a_i$ and $c_e = i$. Next, if $s_c \geq s_b$ is true then we set $s_b = s_c$ and $i_e = i, i_s = c_s$. Note the algorithm mentioned before trivially runs in $O(n)$ time, and it will arrive at the best solution because in every moment it trades up to the maximum current sum/element, which will identify when we need to look at a new contiguous array, then after it will swap up to the best sum.
- 6.2 To figure out the best journey, predicated on for x miles driven in a day $(200 - x)^2$ to be the penalty. For the array of a_1, \dots, a_n hotel distances, we will define $a_0 = 0$, and the arrays $dp, prev$, where $dp[i]$ is the optimal penalty up to hotel i , and $prev[i]$ is the optimal last hotel. We start by setting $prev[0] = 0$ and $dp[0] = 0$. Then for each $i \in [n]$, we compute $dp[i] = \min(dp[1] + (200 - (a_i - a_1))^2, dp[2] + (200 - (a_i - a_2))^2, \dots, dp[i-1] + (200 - (a_i - a_{i-1}))^2)$, then store $prev[i]$ based on which hotel was picked previously. This will find the least penalty to get to hotel i . By returning the $prev$ array and dp we can do $dp[n]$ to get the best penalty to hotel n and then all the path took via looking up indices of the last hotel in $prev$ recursively.
- 6.3 Similarly as before, one has the dp array which is maximum profit including the i -th location. This is done via first setting $dp[1] = \max_{i \in \mathbb{N}} p_i$, then iterating through for each $i \in [n] \setminus \{1\}$ computing $dp[i] = \max(p_i, \{p_j + dp[j] : m_j - m_i > k, j \in [n] \setminus [i]\})$, where the previous most profitable location is stored in a separate $prev$ array. Finally one returns the $prev$ and dp arrays, where one can extract the most profitable wackdonalds locations for n potential locations and their positions via $dp[n]$ and working backwards through the $prev$ array.