

The code:

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#include <math.h>
#include <stdio.h>

double Euler( double (*v)(double,double), double x0, double h,
    double T, int flagDataWrite, int flagErrorWrite, FILE *f, FILE *
    fERR){

    double t = 0;
    double x = x0;

    while(t < T){

        if(flagDataWrite)
            fprintf(f, "%f\t%f\n", t, x);
        if(flagErrorWrite)
            fprintf(fERR, "%f\t%f\n",t, fabs(x-1/(1+expf(-t)))
                );
        x = x + h*(*v)(x,t);
        t += h;
    }

    return x;
}

double revEuler(double x0, double h, double T, int flagDataWrite,
    int flagErrorWrite, FILE *f, FILE *fERR){

    double t = 0;
    double x = x0;

    while(t < T){
        if(flagDataWrite) fprintf(f, "%f\t%f\n", t, x);
        x = x/(1+201*h);
        t += h;
    }
    return x;
}

double midpoint( double (*v)(double,double), double x0, double h,
    double T, int flagDataWrite, int flagErrorWrite, FILE *f, FILE *
    fERR){

    double t = 0;
    double x = x0;
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    while(t < T){

        if(flagDataWrite) fprintf(f, "%f\t%f\n", t, x);
        if(flagErrorWrite) fprintf(fERR, "%f\t%f\n",t,
            fabs(x-1/(1+expf(-t))));

        x = x + h*(v)(x + (h/2)*(v)(x,t),t + (h/2));
        t += h;
    }

    return x;
}

double v2(double x, double t){

    return x*(1-x);

}

double v3(double x, double t){
    return cos(pow(x,3)) -cos(pow(x,2) -t);
}

double v4(double x, double t){
    return -201*x;
}

int main(int argc, char* argv[]){

    FILE *s2, *s2E, *s3, *s4, *s5, *s6, *s6E;

    s2 = fopen("s2.dat", "w+");
    s2E = fopen("s2E.dat","w+");
    s3 = fopen("s3.dat", "w+");
    s4 = fopen("s4.dat", "w+");
    s5 = fopen("s5.dat", "w+");
    s6 = fopen("s6.dat", "w+");
    s6E = fopen("s6E.dat", "w+");

    printf("Solution to 2: %f\n", Euler( &v2, 0.5, 0.01, 5, 1,
        1, s2, s2E));

    Euler( &v3, 1, 0.01, 5, 1, 0, s3, NULL);

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    Euler(&v4, 1, 0.01, 0.5, 1, 0, s4, NULL);

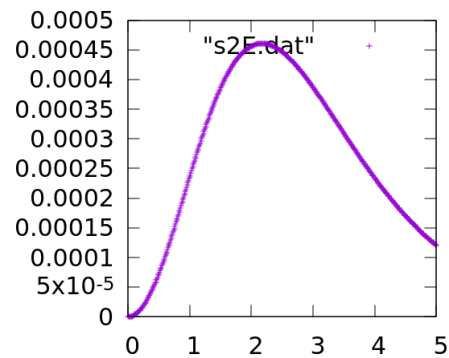
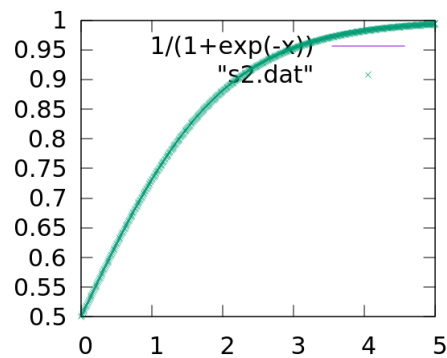
    revEuler(1,0.01,0.5,1,0,s5,NULL);

    midpoint(&v2, 0.5, 0.01, 5, 1, 1, s6, s6E);

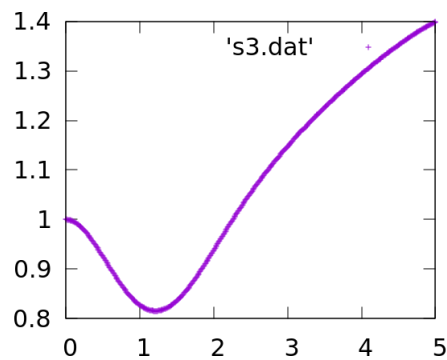
    fclose(s2E);
    fclose(s2);
    fclose(s3);
    fclose(s4);
    fclose(s5);
}

```

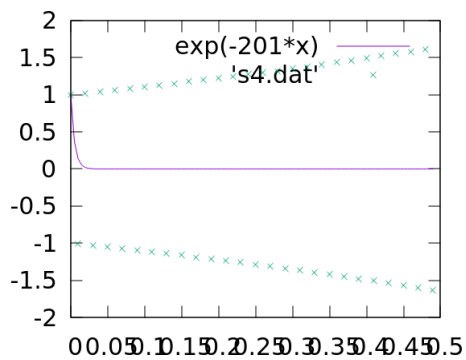
1. First function in the program
2. The solution at $t = 5$ is 0.993493. The order of the greatest error is 10^{-3} .



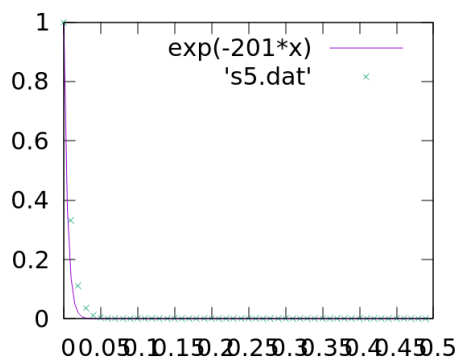
3. Approximation of $x'(t) = \cos(x^3(t)) - \cos(x^2(t) - 3t)$, $x(0) = 1$.



- 4.



5.



6. The order of the greatest error is 10^{-6} . Compared to the standard Euler method, the error is 3 orders of magnitude less.

