

# Formation Eco-Driving for Heterogeneous Electric Vehicles

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**Abstract**—Multiple-vehicle formation driving, which accelerates and cruises the vehicles with the same acceleration and speed, gains a higher transportation throughput. This paper introduces a *formation eco-driving* for battery electric vehicles (BEV or all-electric vehicles powered solely by the battery.) We first calculate the least-energy cruising speed for each BEV in the same formation and derive the most energy-efficient formation speed. We assume V2V (vehicle to vehicle) communications that allows sharing the vehicle power models among the BEVs in the same formation. We address the formation eco-driving with a perspective of low-power embedded systems design in this paper. We formulate the formation eco-driving focusing more on energy efficiency such that the formation is not strictly necessarily maintained as long as each BEV does not interfere other vehicles in the formation, which is more realistic. We present accurate polynomial form of BEV power models that considers characteristics of electric powertrain as well as the optimization framework. Our experimental results show 12.81% total energy saving of the whole formation of BEVs compared with the baseline.

**Index Terms**—Battery Electric vehicles, heterogeneous driving, formation eco-driving

## I. INTRODUCTION

It is well known that eco-driving gains a significant fuel efficiency without upgrading the vehicles. Eco-driving methods have been widely mentioned for internal combustion engine vehicles, but such methods can hardly be used for battery electric vehicles (BEVs) due to the fundamental discrepancies between the internal combustion engine powertrain and electric powertrain. Recent previous research on BEV-specific eco-driving begins to reflect electric powertrain characteristics [1], [2], [3]. However, such work focuses on single BEV even though some work is aware of the traffic condition [4], [2]. Currently, up to one hundred electronic control units (ECUs) are used for autonomous vehicle driving such as adaptive cruise control (ACC). In addition, computing techniques for processing a large amount of data with limited resources are proposed for V2V (vehicle to vehicle) communication.

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As a result, formation driving, which accelerate and cruise the vehicles in the same group, is real. Formation driving efficiently enhances the transportation throughput and can also gain fuel economy due to the reduced air dragging as a byproduct.

This paper introduces a *formation eco-driving of heterogeneous BEVs* on a single lane. The BEVs accelerate and cruise without disturbing other BEVs in the same formation calculating the most efficient acceleration, cruising speed and deceleration for the formation. Unlike the previous work, this paper primarily saves energy consumption of BEVs through the proposed formation eco-driving. We formulate the formation eco-driving problem more realistic such that the formation is not necessarily maintained as long as a BEV does not interfere the other BEVs. For example, the first BEV in the formation may be driven faster than the formation speed if the most-efficient speed for the first BEV is higher than the optimal formation speed.

## II. ELECTRIC VEHICLE MATHEMATICAL POWER MODELS

### A. Vehicle Power Consumption Model

A vehicle dynamics equation is commonly used vehicle power consumption model (1). There is an assumption that efficiency of the powertrain (electric motor and drivetrain) is 100%.

$$P_{trac} = F \frac{ds}{dt} = Fv = (F_R + F_G + F_I + F_A)v$$

$$F_R \propto C_{rr}W, F_G \propto W \sin \theta, F_I \propto ma, \text{ and } F_A \propto \frac{1}{2} \rho C_d A v^2 \quad (1)$$

$$P_{trac} \approx (\alpha + \beta \sin \theta + \gamma a + \delta v^2)mv$$

where  $F_R$ ,  $F_G$ ,  $F_I$ ,  $F_A$ , and  $F_B$  denote the rolling resistance, gradient resistance, inertia resistance, aerodynamic resistance, and brake force provided by hydraulic brakes, respectively [5]. The coefficients  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$  correspond to the rolling resistance, gradient resistance, inertia resistance, and aerodynamic resistance, respectively. Adding a traction motor efficiency in (1) makes more realistic EV power consumption characteristics.  $\eta_{EV*}$  is determined by motor loss and drivetrain. We borrow an EV-specific power ( $P_{EV*}$ ) modeling method considering the loss in EV drivetrain using a multivariable regression method from the measured power data and achieve a polynomial fitting [6].

$$P_{EV*} = \frac{P_{trac}}{\eta_{EV*}} \quad (2)$$

$$\eta_{EV^*} = \frac{P_{trac}}{P_{trac} + C_0 + C_1 v + C_2 v^2 + C_3 T^2}$$

where  $C_0$ ,  $C_1$ ,  $C_2$ , and  $C_3$  mean coefficients for constant loss, iron and friction losses, drivetrain loss, and copper loss, respectively. The power consumption model (2) is commonly used in various analytical EV power managements [3], [4]. EVs mostly use regenerative braking during deceleration, which converts kinetic energy to electric energy. The harvested energy from regenerative braking is closely related to the electromagnetic flux inside of the motor, and the flux is proportional to the motor RPM. The regenerative braking model of an EV is simplified as (3).

$$P_{regen} = \epsilon T v + \zeta \quad (3)$$

where  $\epsilon$  and  $\zeta$  are regenerative braking coefficients.

### B. Electric Vehicle Power Model Library

ADVISOR is a vehicle simulator that takes into account various factors of vehicles including engines, electric traction motors, types of drivetrains, shape of chassis, etc. [7]. However, it is not practical to use ADVISOR for estimation of power consumption of multiple vehicles at the same time and exploration of design space due to the significant time overhead. So, instead of using ADVISOR for the speed optimization, we use ADVISOR for the model coefficient extraction. In other words, we use the same form of polynomial as (2) but derive the coefficients by running ADVISOR. We implement several types of BEV power model based on the vehicle specifications and reports for the driving performance and range at various constant road slopes [8], [9], [10], [11], [12]. Table I summarizes the model coefficients of (2) and (3) of each BEV.

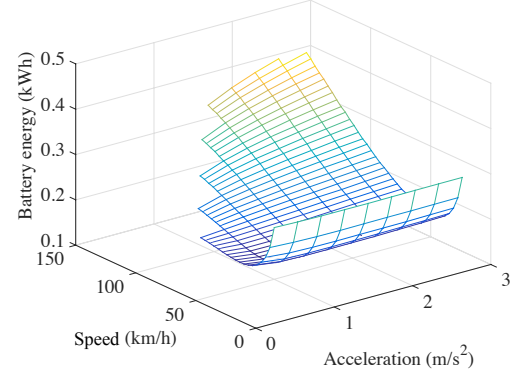
## III. FORMATION ECO-DRIVING

### A. Motivational Example

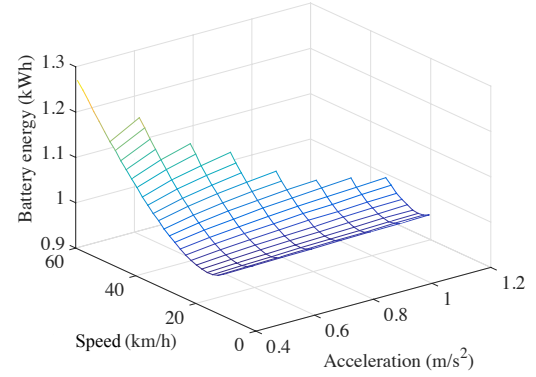
We first demonstrate how the cruising speed, acceleration and deceleration affect BEV energy consumption. We perform a design space exploration (DSE) for all feasible BEV speeds and the acceleration pairs. The results of DSE on an BEV sedan (Model S) and bus (K9) are shown in Fig. 1. We obtain the minimum-energy speed and the initial and final acceleration for a given driving distance. The point at the minimum-energy consumption per distance (Wh/km) represents the least-energy-constant-speed driving. The energy consumption by the cruising speed and acceleration pairs also completely changes by the BEV type. Each BEV type has different curb weight, motor specification, body shape, and tire, which affect energy consumption by acceleration and cruising speed, and, therefore, each BEV type has different least-energy-constant-speed driving.

### B. Problem formulation

A set of formation BEVs on the same lane.  $N$  BEVs, and a BEV  $EV_i$  has a power models defined by (1), (2), (3), and related coefficients in Table I. No interference is assumed for the formation, i.e., no other vehicles, no pedestrians, etc.,



(a)



(b)

Fig. 1. Design space exploration of (a) Tesla Model S and (b) BYD K9.



Fig. 2. An example of a formation driving of heterogeneous BEVs on a single lane.

nearby the formation. The formation driving consists of three stages: a constant acceleration, a constant-speed cruising and a constant deceleration. A segment of the formation driving is between two traffic signals, between two stop signs, and so forth. Use of a V2V communication, BEVs in the same formation can share their vehicle information, i.e., power model coefficients. Each BEV weight is defined by the curb weight and the payload: passengers and cargos. The curb weight is known a priori, and the payload is measured by the sensor.

We define the baseline as follows:

- 1) Independent eco-driving: each BEV has its own minimum-energy acceleration, cruising speed and deceleration. It is permitted to pass a preceding vehicle. This is possible when each BEV occupies its own lane.
- 2) Following the preceding vehicle: each BEV has its own minimum-energy acceleration, cruising speed and deceleration guideline. However, the acceleration or cruising speed of the following BEV is bounded by those of the preceding BEV.

TABLE I  
POWER MODEL COEFFICIENTS OF BEVS.

| BEV              | $\alpha$ | $\beta$ | $\gamma$ | $\delta$    | $C_0$ | $C_1$  | $C_2$  | $C_3$       | $\epsilon$ | $\zeta$ |
|------------------|----------|---------|----------|-------------|-------|--------|--------|-------------|------------|---------|
| Chevrolet Bolt   | 0.06     | 9.5549  | 1.0013   | 0.00012352  | 1000  | 10.588 | 8.11   | 0.00031678  | 0.6633     | 5813.6  |
| Tesla Model S 85 | 0.098    | 9.8794  | 0.9911   | 0.00016564  | 2300  | 11.927 | 4.4359 | 0.00032082  | 0.7642     | 2832.9  |
| Tesla Roadster   | 0.0735   | 8.723   | 0.8461   | 0.000065721 | 2000  | 15.743 | 11.221 | 0.0033      | 0.7464     | 2857.1  |
| Spark EV         | 0.098    | 10.7077 | 1.0567   | 0.00025082  | 700   | 24     | 8      | 0.00075648  | 0.6671     | 2412.9  |
| BYD K9           | 0.098    | 9.8946  | 1.2324   | 0.00044     | 1000  | 492.56 | 90     | 0.000018696 | 0.4095     | 2178.5  |

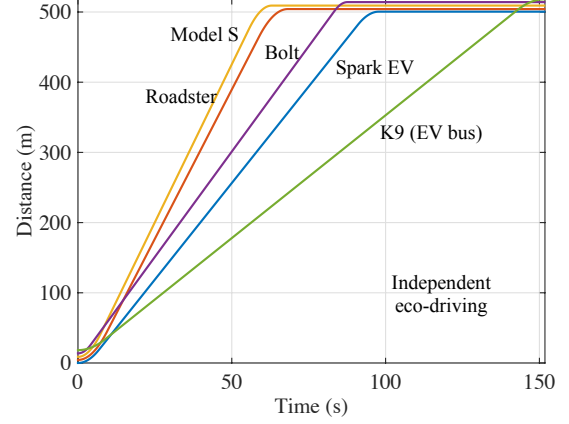
The formation eco-driving problem can be rewritten such that for a given set of formation with the BEV models and lineup order, we minimize the total formation driving energy consumption. The problem formulation accommodates a more realistic situation. The formation acceleration, cruising speed and deceleration are regarded as a reference. Each BEV may not follow the formation driving reference as long as it does not interfere other BEV formation driving. For example, the first BEV may be driven faster than the formation cruising speed as long as it exhibits a smaller energy consumption.

#### IV. EXPERIMENTAL RESULTS

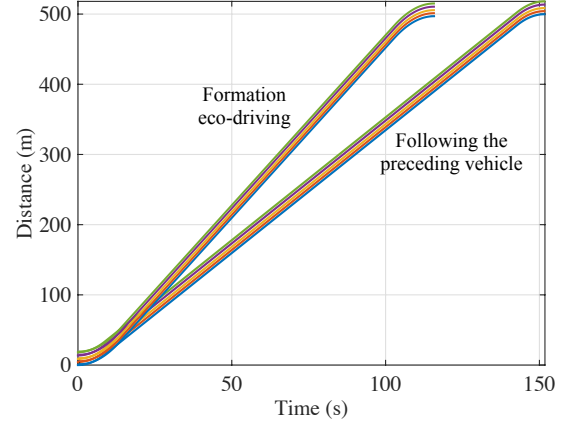
For more comprehensive comparison, we assume several driving cases of five BEVs summarized in Table II. A formation is Chevrolet Spark (tail) – Tesla Roadster – Tesla Model S – Chevrolet Bolt – Kia K9 (head.) The driving segment distance of this example is 500 m, and each BEV has its own minimum-energy acceleration and cruising speed. Fig. 3(a) shows the independent eco-driving of the five BEVs over time. Independent eco-driving is not a formation driving, and thus each BEV arrives at the endpoint at different times. K9 starts at the forefront on the starting point. But, this BEV arrives at the endpoint the latest because the minimum-energy cruising speed of K9 is the slowest among the BEVs in this example. Fig. 3(b) shows the drivings of the five BEVs on a single lane, and no passing is allowed.

One of the baseline, following the preceding BEV, enforces the acceleration and cruising speed are bounded by those of the preceding vehicle while the preceding vehicle accelerates and/or cruises by its own eco-driving policy or by its preceding BEV. Therefore, this particular example enforces all the BEVs in the formation to have the acceleration and cruising speed bounded by those of K9. Total energy consumption of the five BEVs is as 109.7% compared with the independent eco-driving. On the other hands, the formation driving consumes only 104.0% of energy consumption of the independent eco-driving with the proposed formation eco-driving III-B.

We assume a case study of heterogeneous BEV driving with 10 BEVs. Table III summarizes the formations of 10 BEVs. Fig. 4 shows the comparisons of the energy consumption of 10 BEVs for the driving. Blue bars indicate the energy consumption of the following-the-preceding-vehicle baseline. Blue bars show 100% energy consumption in Fig. 4. Green bars indicate the energy consumption by the proposed formation eco-driving, and orange bars indicate the independent eco-driving. The energy gain by the proposed formation eco-driving compared with following the preceding vehicle is from 1.41% to 12.81%.



(a)



(b)

Fig. 3. Heterogeneous BEV driving by (a) passing a preceding vehicle is permitted, and (b) passing is not permitted.

TABLE II  
LIST OF BEVS AND THEIR VEHICLE TYPE.

| Index | Vehicle | Type      | Index | Vehicle  | Type        |
|-------|---------|-----------|-------|----------|-------------|
| 1     | Bolt    | hatchback | 4     | K9       | bus         |
| 2     | Spark   | hatchback | 5     | Roadster | convertible |
| 3     | Model S | sedan     |       |          |             |

TABLE III  
LIST OF HETEROGENEOUS DRIVING FORMATIONS.

| Formations | BEV formation from the tail to head   |
|------------|---------------------------------------|
| A          | 3 – 2 – 3 – 5 – 3 – 5 – 1 – 5 – 3 – 4 |
| B          | 3 – 2 – 3 – 5 – 3 – 5 – 3 – 4 – 5 – 1 |
| C          | 3 – 5 – 3 – 4 – 5 – 3 – 5 – 3 – 2 – 1 |
| D          | 4 – 3 – 2 – 3 – 5 – 3 – 5 – 1 – 5 – 3 |

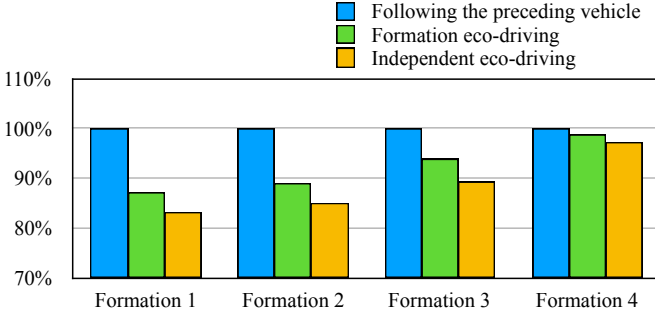


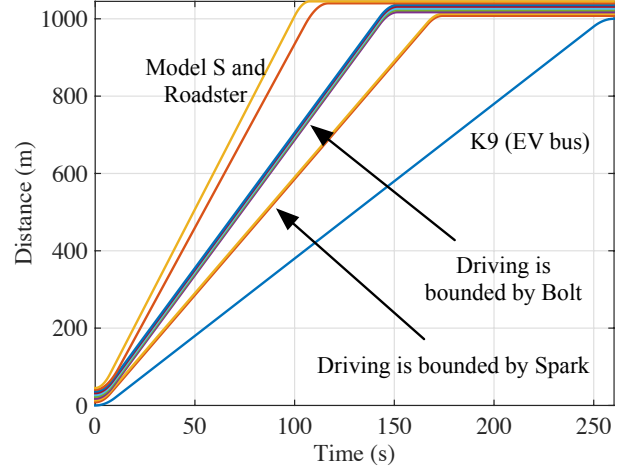
Fig. 4. Heterogeneous driving results by BEV formations.

Formation A has the electric bus at the head of the formation, which it is quite common in a city driving. Drivings of all BEVs are bounded by the least-energy cruising speed of the electric bus. The gain by the proposed formation eco-driving is 12.81% compared with the-following-the-preceding-vehicle baseline. By contrast, the least-energy cruising speeds of two leading BEVs (hatchback and convertible) are faster than a recommended reference, and that of the last BEV (bus) is slower than the reference in Formation D. Therefore, these three BEVs drive their own optimal, and only seven BEVs follow the reference as shown in Fig. 5.

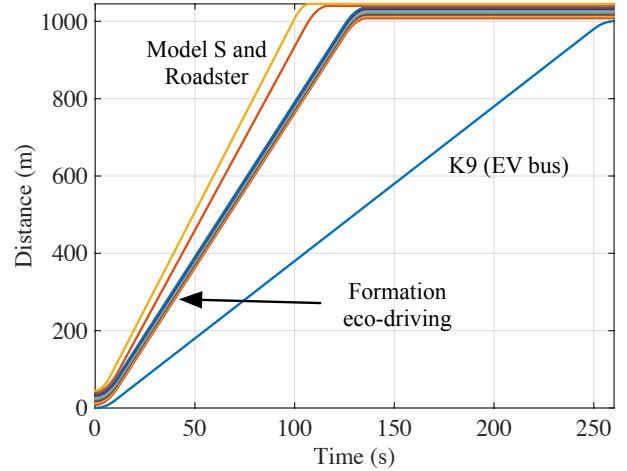
## V. CONCLUSIONS

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(a)



(b)

Fig. 5. Heterogeneous BEV driving result of (a) following the preceding vehicle and (b) formulation eco-driving in case of formation 4.