Rökfræði (e. Propositional Logic)

KHR 1.3 Table 6: Logical Equivalences

Equivalence	Name
$p \wedge \mathbf{T} \equiv p$ $p \vee \mathbf{F} \equiv p$	Identity laws
$p \lor \mathbf{T} \equiv \mathbf{T}$ $p \land \mathbf{F} \equiv \mathbf{F}$	Domination laws
$p \lor p \equiv p$ $p \land p \equiv p$	Idempotent laws
$\neg(\neg p) \equiv p$	Double negation law
$p \lor q \equiv q \lor p$ $p \land q \equiv q \land p$	Commutative laws
$\begin{aligned} (p \lor q) \lor r &\equiv p \lor (q \lor r) \\ (p \land q) \land r &\equiv p \land (q \land r) \end{aligned}$	Associative laws
$\begin{split} p \lor (q \land r) &\equiv (p \lor q) \land (p \lor r) \\ p \land (q \lor r) &\equiv (p \land q) \lor (p \land r) \end{split}$	Distributive laws
$\neg (p \land q) \equiv \neg p \lor \neg q$ $\neg (p \lor q) \equiv \neg p \land \neg q$	De Morgan's laws
$p \lor (p \land q) \equiv p$ $p \land (p \lor q) \equiv p$	Absorption laws
$p \lor \neg p \equiv \mathbf{T}$ $p \land \neg p \equiv \mathbf{F}$	Negation laws

 ${\rm KHR}$ 1.3 Table 7: Logical Equivalences Involving Conditional Statements

$$p \rightarrow q \equiv \neg p \lor q$$

$$p \rightarrow q \equiv \neg q \rightarrow \neg p$$

$$p \lor q \equiv \neg p \rightarrow q$$

$$p \land q \equiv \neg (p \rightarrow \neg q)$$

$$\neg (p \rightarrow q) \equiv p \land \neg q$$

$$(p \rightarrow q) \land (p \rightarrow r) \equiv p \rightarrow (q \land r)$$

$$(p \rightarrow r) \land (q \rightarrow r) \equiv (p \lor q) \rightarrow r$$

$$(p \rightarrow q) \lor (p \rightarrow r) \equiv p \rightarrow (q \lor r)$$

$$(p \rightarrow r) \lor (q \rightarrow r) \equiv (p \land q) \rightarrow r$$

KHR 1.3 Table 8: Logical Equivalences Involving Biconditional Statements

$$\begin{aligned} p &\leftrightarrow q \equiv (p \to q) \land (q \to p) \\ \\ p &\leftrightarrow q \equiv \neg p \leftrightarrow \neg q \\ \\ p &\leftrightarrow q \equiv (p \land q) \lor (\neg p \land \neg q) \\ \\ \neg (p \leftrightarrow q) \equiv p \leftrightarrow \neg q \end{aligned}$$

Mengi (e. Sets)

KHR 2.2 Table 1: Set Identities

Identity	Name
$A \cap U = A$ $A \cup \emptyset = A$	Identity laws
$A \cup U = U$ $A \cap \emptyset = \emptyset$	Domination laws
$A \cup A = A$ $A \cap A = A$	Idempotent laws
$\overline{(A)} = A$	Complementation law
$A \cup B = B \cup A$ $A \cap B = B \cap A$	Commutative laws
$A \cup (B \cup C) = (A \cup B) \cup C$ $A \cap (B \cap C) = (A \cap B) \cap C$	Associative laws
$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$	Distributive laws
$\overline{A \cap B} = \overline{A} \cup \overline{B}$ $\overline{A \cup B} = \overline{A} \cap \overline{B}$	De Morgan's laws
$A \cup (A \cap B) = A$ $A \cap (A \cup B) = A$	Absorption laws
$A \cup \overline{A} = U$ $A \cap \overline{A} = \emptyset$	Complement laws

$$|A \cup B| = |A| + |B| - |A \cap B|$$

$$|A \cup B \cup C| = |A| + |B| + |C| - |A \cap B| - |A \cap C| - |B \cap C| + |A \cap B \cap C|$$

Summur (e. Summations)

KHR 2.4 Theorem 1

THEOREM 1

If a and r are real numbers and $r \neq 0$, then

$$\sum_{j=0}^{n} ar^{j} = \begin{cases} \frac{ar^{n+1} - a}{r-1} & \text{if } r \neq 1\\ (n+1)a & \text{if } r = 1. \end{cases}$$

KHR 2.4 Table 2: Some Useful Summation Formulae

Sum	Closed Form
$\sum_{k=0}^{n} ar^k \ (r \neq 0)$	$\frac{ar^{n+1}-a}{r-1}, r \neq 1$
$\sum_{k=1}^{n} k$	$\frac{n(n+1)}{2}$
$\sum_{k=1}^{n} k^2$	$\frac{n(n+1)(2n+1)}{6}$
$\sum_{k=1}^{n} k^3$	$\frac{n^2(n+1)^2}{4}$
$\sum_{k=0}^{\infty} x^k, x < 1$	$\frac{1}{1-x}$
$\sum_{k=1}^{\infty} k x^{k-1}, x < 1$	$\frac{1}{(1-x)^2}$