



**Trinity College Dublin**

Coláiste na Tríonóide, Baile Átha Cliath

The University of Dublin

# Bit Manipulation

CS1021 – Introduction to Computing I

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# Bitwise Logical Operations

2

Bitwise logical operations perform operations on the individual bits of a (word) value, rather than the value as a whole

AND, OR, EXCLUSIVE-OR (binary operators)

A	B	A AND B
0	0	0
0	1	0
1	0	0
1	1	1

A	B	A OR B
0	0	0
0	1	1
1	0	1
1	1	1

A	B	A EOR B
0	0	0
0	1	1
1	0	1
1	1	0

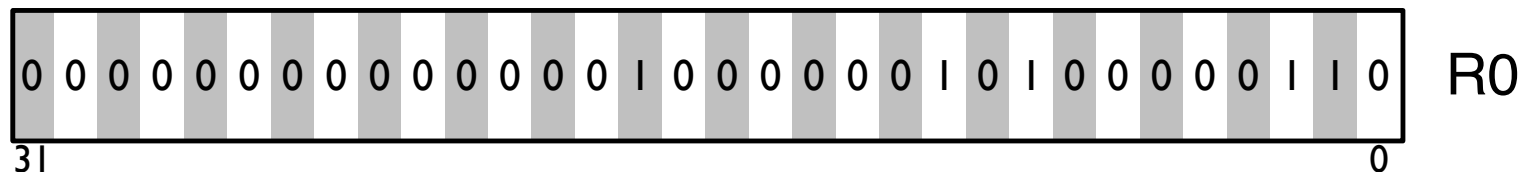
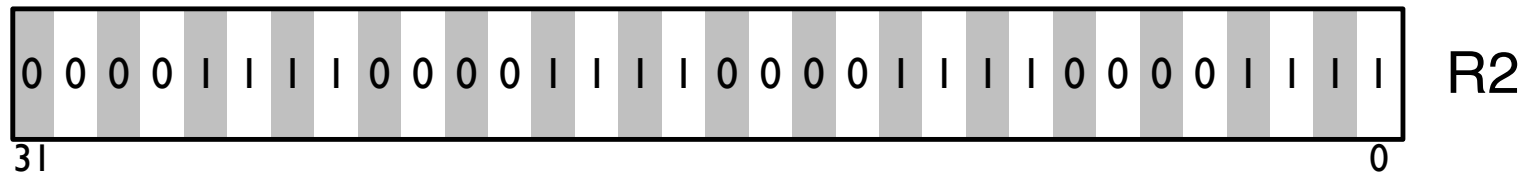
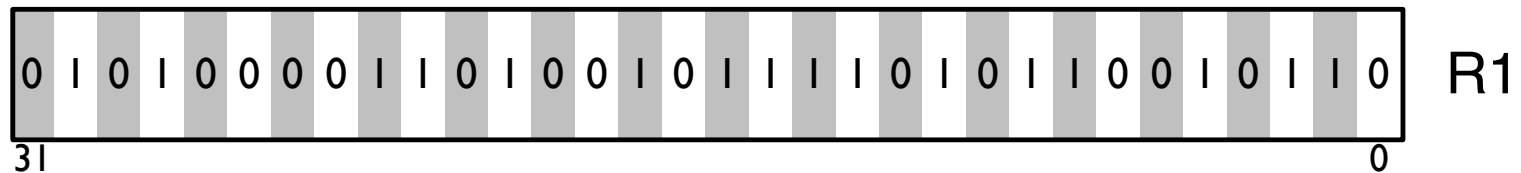
NOT (inversion, complement, a unary operator)

A	NOT A
0	1
1	0

# Bitwise Operation Instructions – AND

3

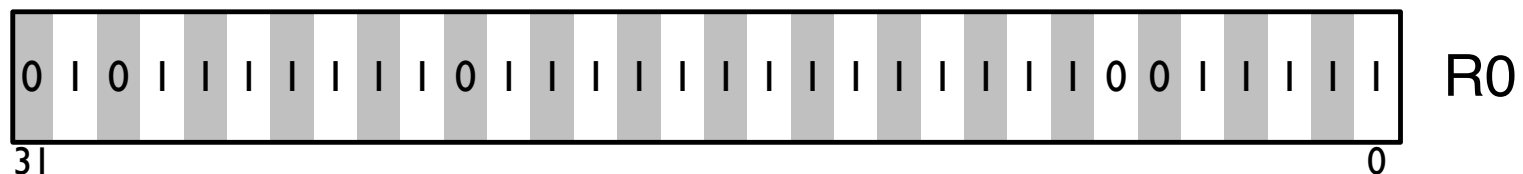
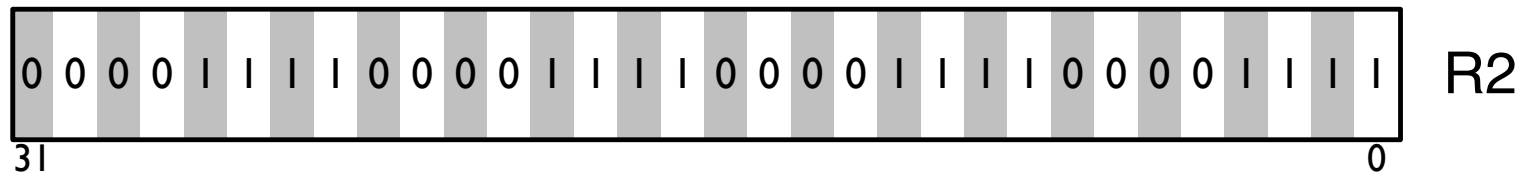
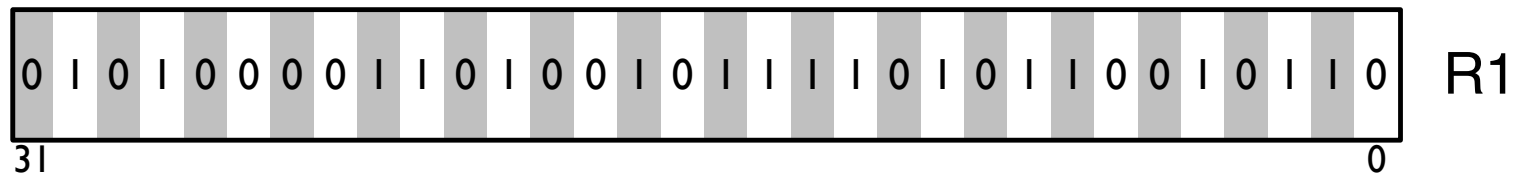
```
AND r0, r1, r2      ; r0 = r1 . r2 (r1 AND r2)
```



# Bitwise Operation Instructions – OR

4

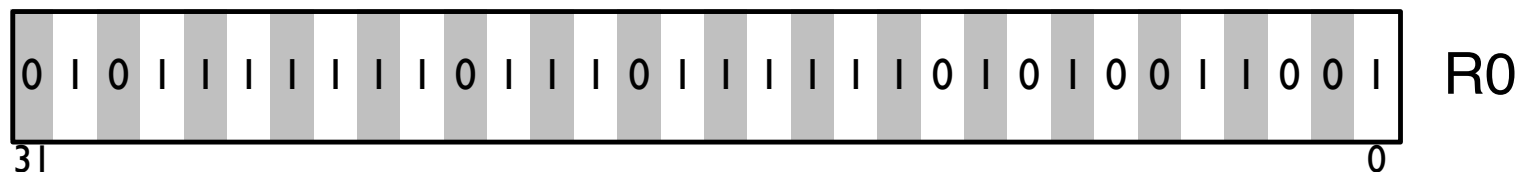
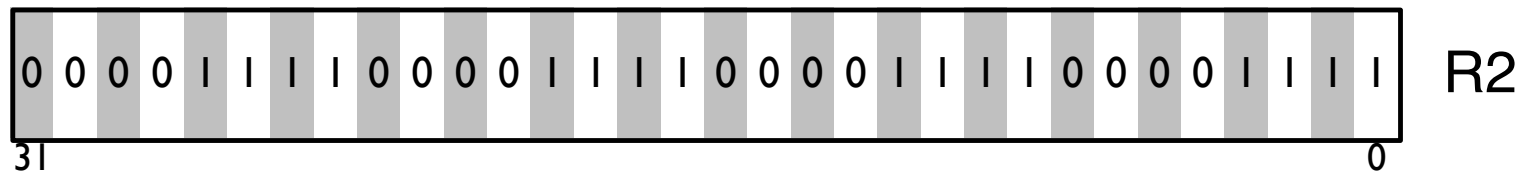
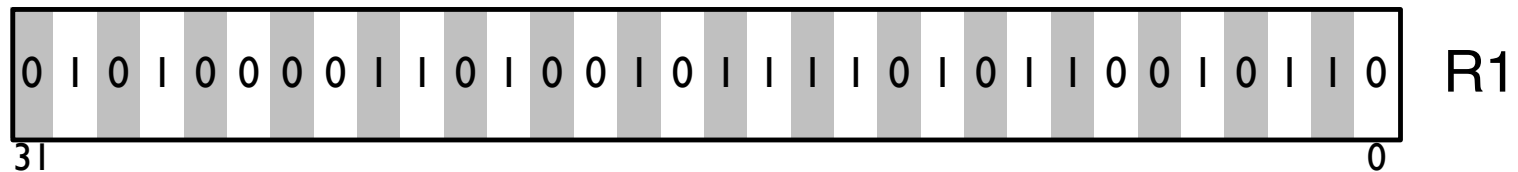
```
ORR r0, r1, r2      ; r0 = r1 + r2 (r1 OR r2)
```



# Bitwise Operation Instructions – EOR

5

```
EOR r0, r1, r2      ; r0 = r1  $\oplus$  r2 (r1 EOR r2)
```

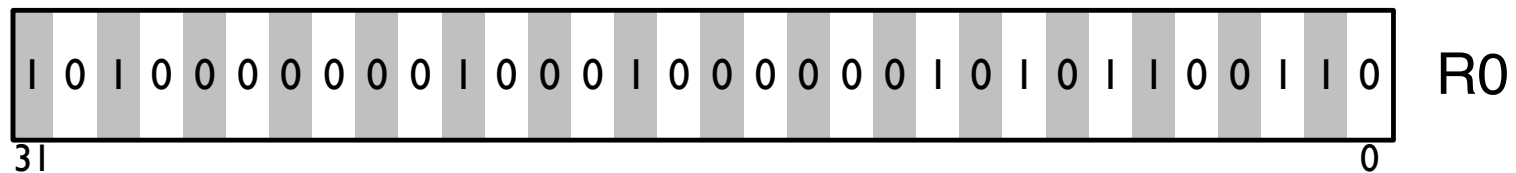
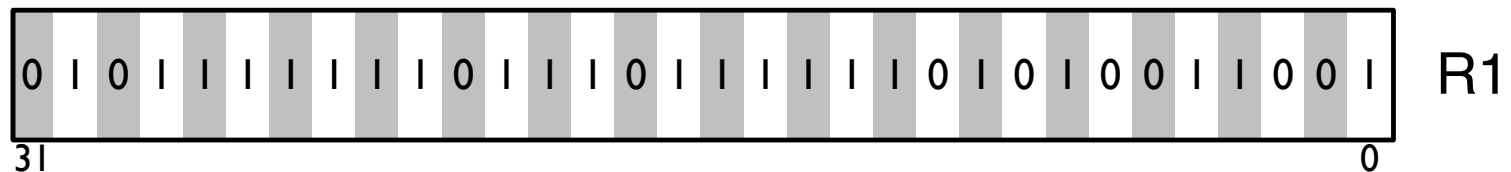


# Bitwise Operation Instructions – NOT

6

```
MVN r0, r0          ; r0 = ¬r0 (NOT r0)
```

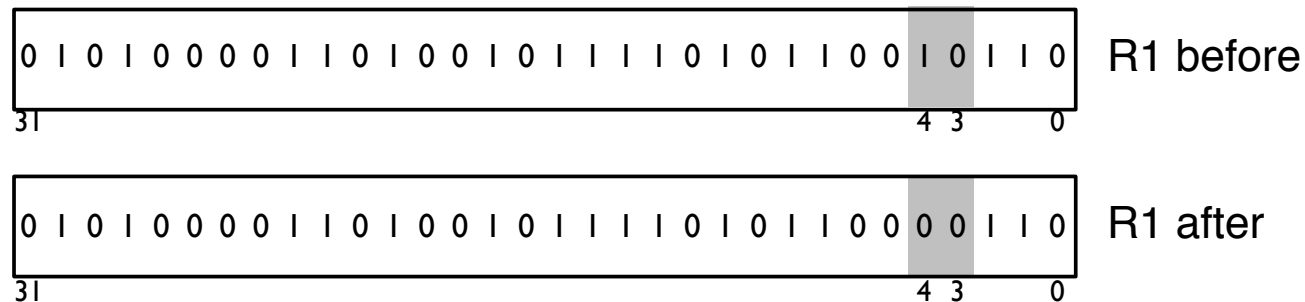
```
MVN r0, r1          ; r0 = ¬r1 (NOT r1)
```



# Bit Manipulation – Clear Bits

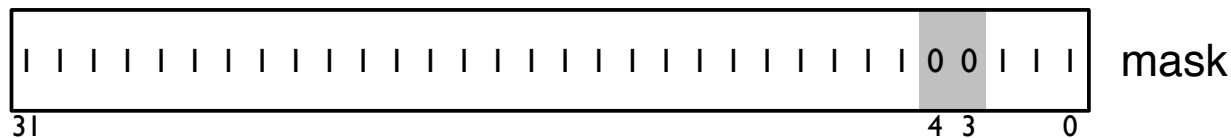
7

e.g. Clear bits 3 and 4 (i.e. the 4th and 5th bits) of the value in r1



Observe  $0 \cdot x = 0$  and  $1 \cdot x = x$

Construct a mask with 0 in the bit positions we want to clear and 1 in the bit positions we want to leave unchanged

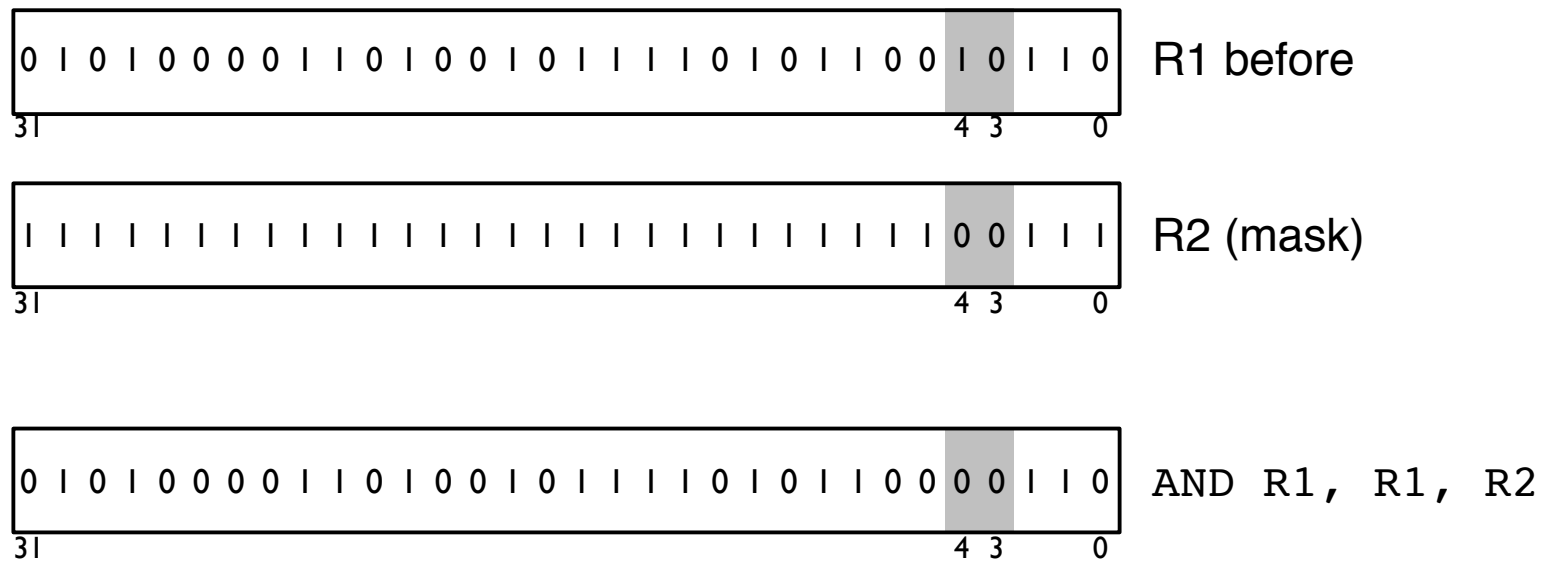


Perform a bitwise logical AND of the value with the mask

# Bit Manipulation – Clear Bits

8

e.g. Clear bits 3 and 4 of the value in r1 (continued)





## Example: Clear Bits

9

Write an assembly language program to clear bits 3 and 4 (i.e. the 4th and 5th bits) of the value in R1

```
LDR r1, =0x61E87F4C ; load test value
LDR r2, =0xFFFFFE7  ; mask to clear bits 3 and 4
AND r1, r1, r2       ; clear bits 3 and 4
                      ; result should be 0x61E87F44
```

Alternatively, the BIC (BIt Clear) instruction allows us to define a mask with 1's in the positions we want to clear

```
LDR r2, =0x00000018 ; mask to clear bits 3 and 4
BIC r1, r1, r2       ; r1 = r1 AND NOT(r2)
```

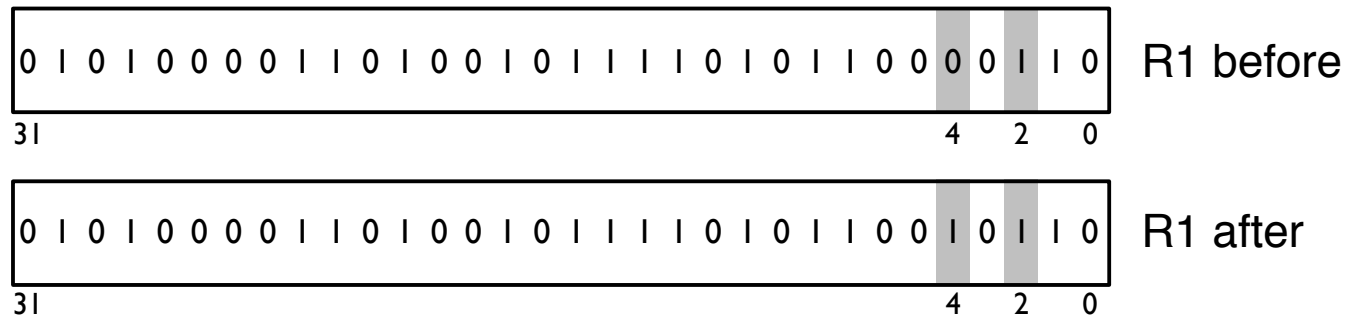
Or use an immediate value, saving one instruction

```
BIC r1, r1, #0x00000018 ; r1 = r1 AND NOT(0x00000018)
```

# Bit Manipulation – Set Bits

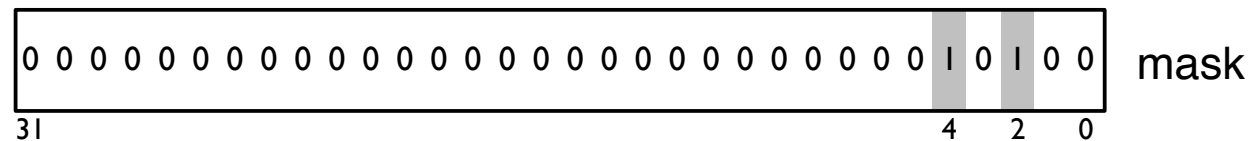
10

e.g. Set bits 2 and 4 (i.e. the 3rd and 5th bits) of the value in r1



Observe  $1 + x = 1$  and  $0 + x = x$

Construct a mask with 1 in the bit positions we want to set and 0 in the bit positions we want to leave unchanged

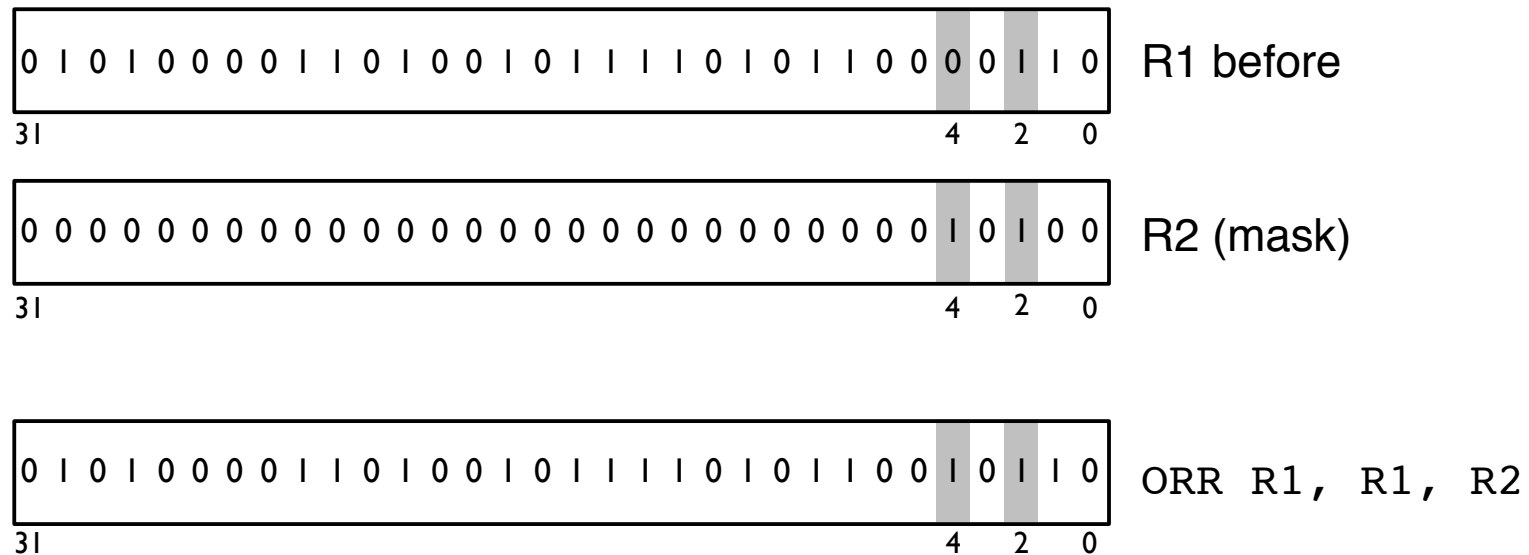


Perform a bitwise logical OR of the value with the mask

# Bit Manipulation – Set Bits

11

e.g. Set bits 2 and 4 of the value in r1 (continued)



## Example: Set Bits

12

Write an assembly language program to set bits 2 and 4 (i.e. the 3rd and 5th bits) of the value in R1

```
LDR  r1, =0x61E87F4C ; load test value
LDR  r2, =0x00000014 ; mask to set bits 2 and 4
ORR  r1, r1, r2      ; set bits 2 and 4
                        ; result should be 0x61E87F5C
```

Save one instruction by specifying the mask as an immediate operand in the ORR instruction

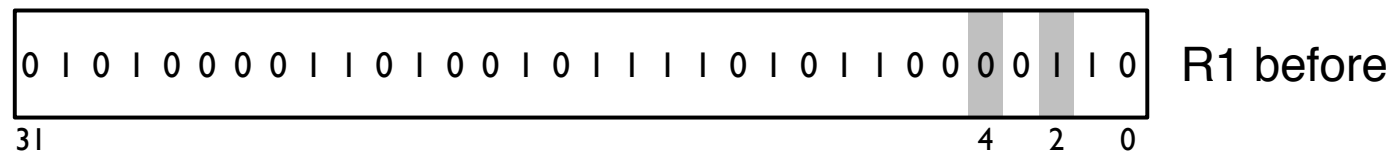
```
ORR  r1, r1, #0x00000014; set bits 2 and 4
```

REMEMBER: since the ORR instruction must fit in 32 bits, only some 32-bit immediate operands can be encoded. Assembler will warn you if the immediate operand you specify is invalid.

# Bit Manipulation – Invert Bits

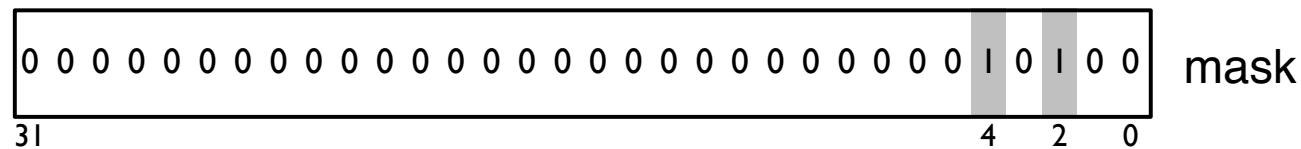
13

e.g. Invert bits 2 and 4 (i.e. the 3rd and 5th bits) of the value in r1



Observe  $1 \oplus x = \neg x$  and  $0 \oplus x = x$

Construct a mask with 1 in the bit positions we want to invert and 0 in the bit positions we want to leave unchanged

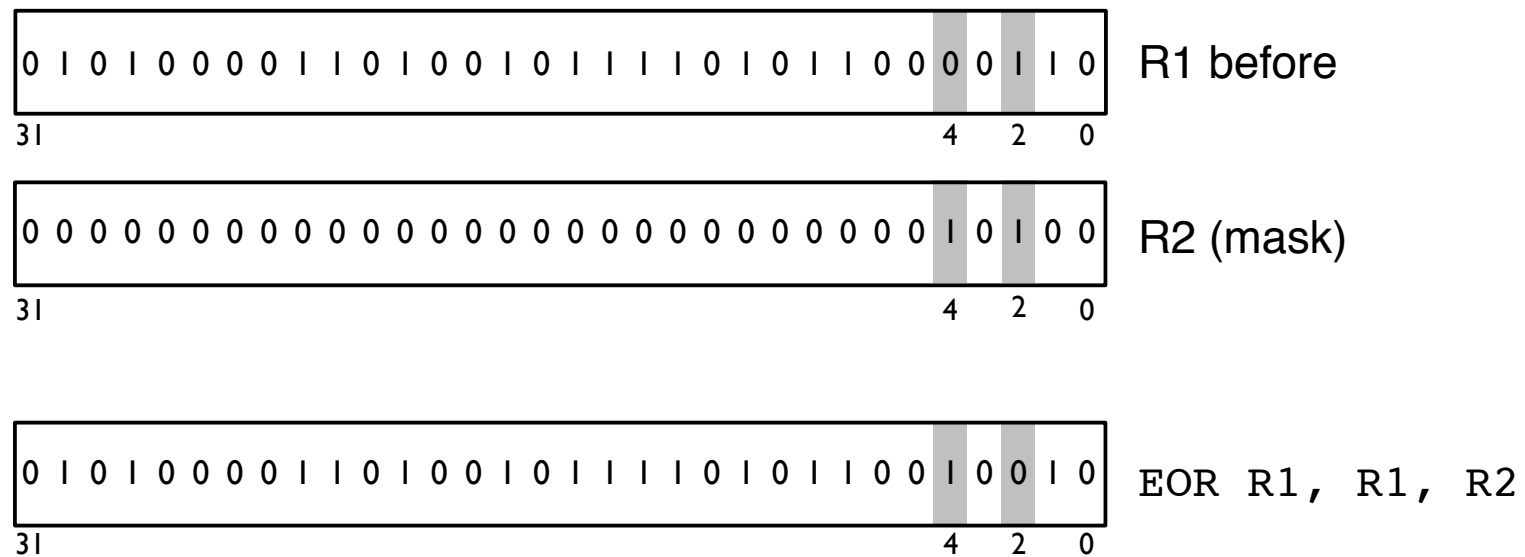


Perform a bitwise logical exclusive-OR of the value with the mask

# Bit Manipulation – Invert Bits

14

e.g. Invert bits 2 and 4 of the value in r1 (continued)



## Example: Invert Bits

15

Write an assembly language program to invert bits 2 and 4 of the value in r1

```
LDR r1, =0x61E87F4C ; load test value
LDR r2, =0x00000014 ; mask to invert bits 2 and 4
EOR r1, r1, r2      ; invert bits 2 and 4
                    ; result should be 0x61E87F46
```

Again, can save an instruction by specifying the mask as an immediate operand in the EOR instruction

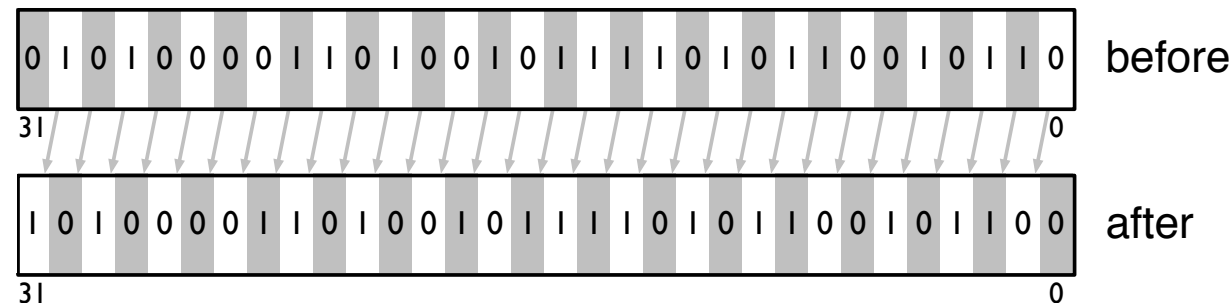
```
EOR r1, r1, #0x00000014 ; invert bits 2 and 4
```

Again, only some 32-bit immediate operands can be encoded

# Logical Shift Left

16

Logical Shift Left by 1 bit position



ARM MOV instruction allows a source operand, Rm, to be shifted left by  $n = 0 \dots 31$  bit positions before being stored in the destination operand, Rd

**MOV Rd, Rm, LSL #n**

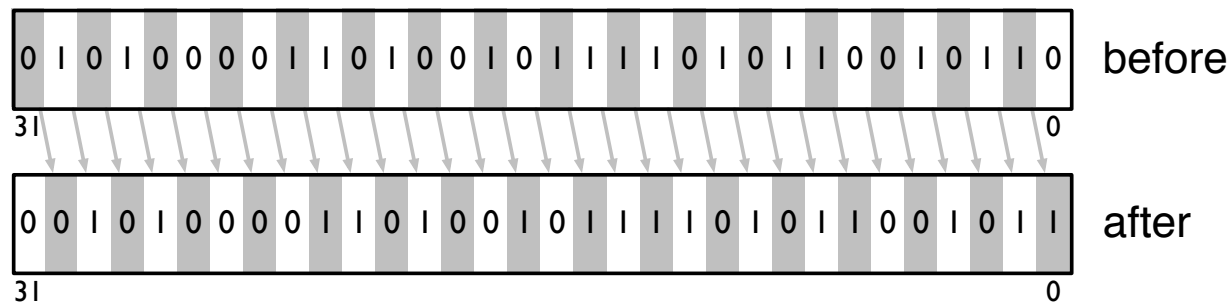
LSB of Rd is set to zero, MSB of Rm is discarded



# Logical Shift Right

17

Logical Shift Right by 1 bit position



ARM MOV instruction allows a source operand, Rm, to be shifted right by  $n = 0 \dots 31$  bit positions before being stored in the destination operand, Rd

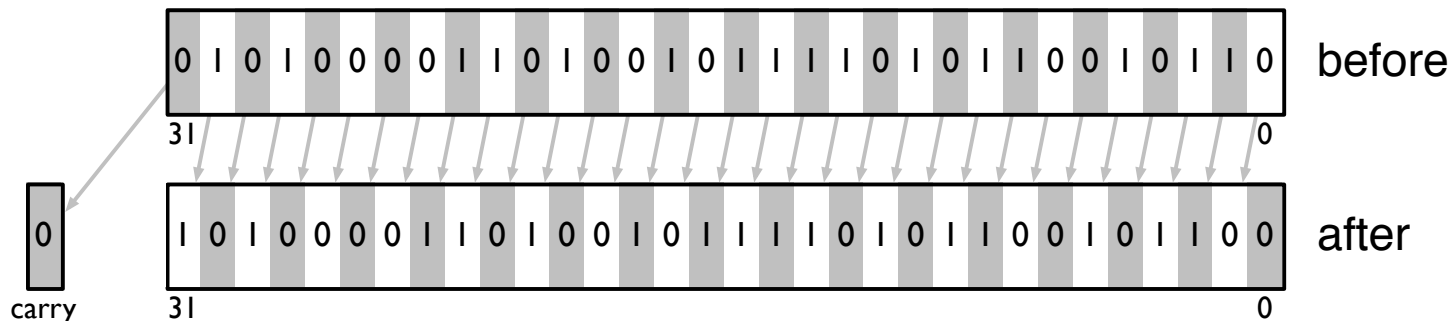
**MOV Rd, Rm, LSR #n**

MSB of Rd is set to zero, LSB of Rm is discarded

Instead of discarding the MSB when shifting left (or LSB when shifting right), we can cause the last bit shifted out to be stored in the Carry Condition Code Flag

By using MOVS instead of MOV

(i.e. by setting the S-bit in the MOV machine code instruction)



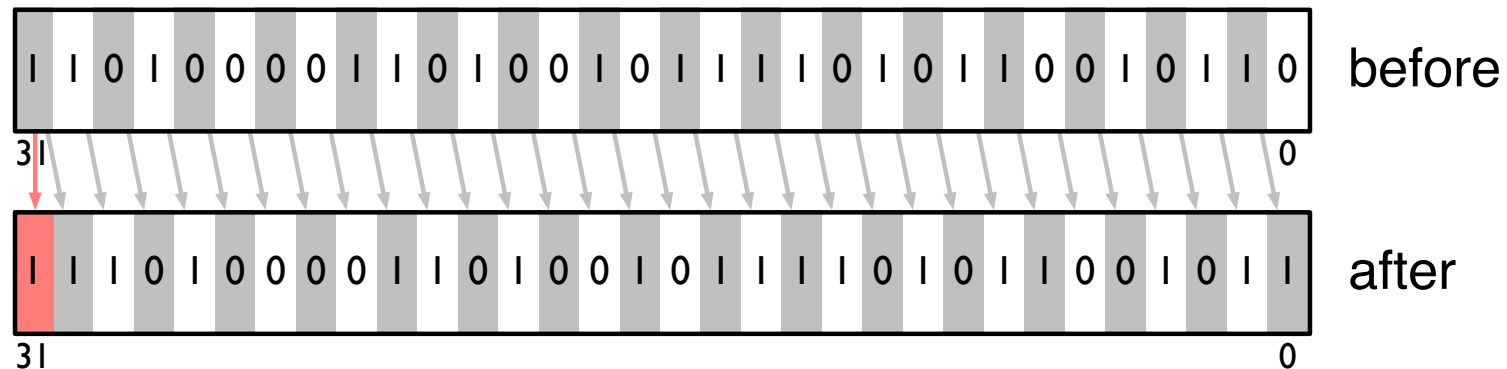
**MOVS Rd, Rm, LSL #n**

**MOVS Rd, Rm, LSR #n**

# Arithmetic Shift Right

19

e.g. Arithmetic Shift Right by 1 bit position



ASR shifts source operand, Rm, right by  $n = 0 \dots 31$  bit positions, copying the sign (MSB) from the source to the sign (MSB) of the destination operand, Rd

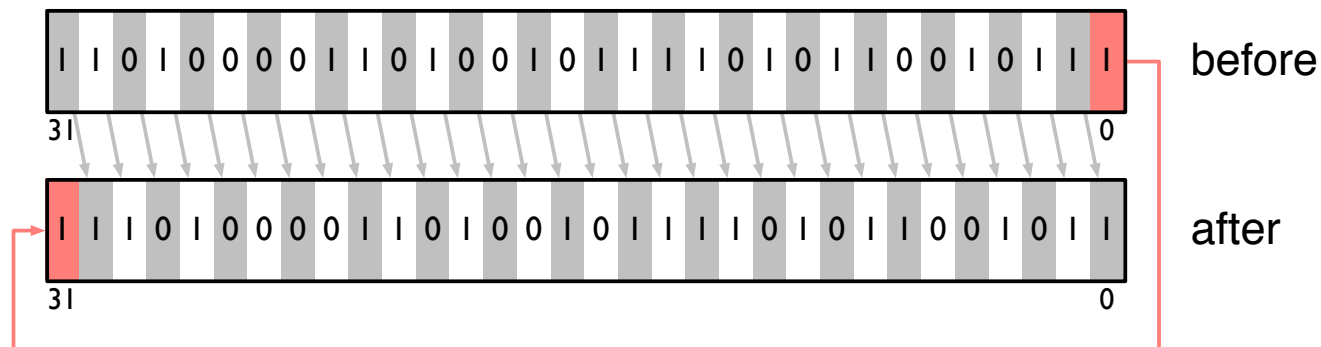
**MOV Rd, Rm, ASR #n**

If right-shift is used for division, ASR maintains correct sign

# Rotate Right

20

Rotate Right by 1 bit position



ROR rotates source operand,  $R_m$ , to the right by  $n = 0 \dots 31$  bit positions before being stored in the destination operand,  $R_d$

**MOV  $R_d$ ,  $R_m$ , ROR # $n$**

MSB of  $R_d$  is set to LSB of  $R_m$

*No ROL?*