

Assignment # 3

Due 12noon Wednesday 7th December

Assignment #3: Integration

We use $\ln(x)$ for the Natural Logarithm function.

① Find

- ① the area under the curve of $y = \sqrt{x-4}$ between 4 and 8.
- ② the curve $y = f(x)$ that passes through the point (9, 4) where the derivative of $f(x)$ is $3 * \sqrt{x}$ i.e. $f'(x) = 3 * \sqrt{x}$.

② Determine

- ① $\int (\sin \theta) * (\cos^5 \theta) d\theta$.
- ② $\int \frac{1}{x * \ln(x)} dx$.

③ Show that

- ① $\int_2^4 \frac{1}{x * (\ln(x))^2} dx = \frac{1}{\ln(4)}$.
- ② $\int_0^1 9^x dx = \frac{4}{\ln(3)}$.

④ Approximate a value for $\ln(5)$ using the series:

$$\ln\left(\frac{1+x}{1-x}\right) = 2 * \left(x + \frac{x^3}{3} + \frac{x^5}{5} + \frac{x^7}{7} \dots\right), \text{ for } |x| < 1$$

Note: for $t > 1$, $\ln(t) = \ln\left(\frac{1+x}{1-x}\right)$, where $x = \frac{t-1}{t+1}$.

(Use the first 3 terms of the series).