

## DIFERÉAIL (DIFFERENTIATION)

$$f'(x) \equiv \frac{d}{dx} [f(x)]$$

$$x^n \quad nx^{n-1}$$

$$\ln x \quad \frac{1}{x}$$

$$\cos x \quad -\sin x$$

$$\sin x \quad \cos x$$

$$\tan x \quad \sec^2 x$$

$$\sec x \tan x \quad \sec^2 x$$

$$\csc x \cot x \quad -\csc^2 x$$

$$\cot x \quad -\csc^2 x$$

$$e^x \quad e^x$$

$$a^{ex} \quad a^{ex} \ln a$$

$$a^x \ln a$$

$$\cos^{-1} \frac{x}{a} \quad -\frac{1}{\sqrt{a^2 - x^2}}$$

$$\sin^{-1} \frac{x}{a} \quad \frac{1}{\sqrt{a^2 - x^2}}$$

$$\tan^{-1} \frac{x}{a} \quad \frac{a}{a^2 + x^2}$$

$$\sec^{-1} \frac{x}{a} \quad \frac{a}{x\sqrt{x^2 - a^2}}$$

$$\csc^{-1} \frac{x}{a} \quad -\frac{a}{x\sqrt{x^2 - a^2}}$$

$$\cot^{-1} \frac{x}{a} \quad -\frac{a}{a^2 + x^2}$$

$$\sinh x \quad \cosh x$$

$$\cosh x \quad \sinh x$$

$$\tanh x \quad \text{sech}^2 x$$

$$\coth x \quad -\text{cosech}^2 x$$

$$\text{sech } x \tanh x \quad -\text{sech } x \coth x$$

$$\csc \text{ch } x \coth x \quad -\csc \text{ch } x \text{sech } x$$

$$\sinh^{-1} x \quad \frac{1}{\sqrt{x^2 + 1}}$$

$$\cosh^{-1} x \quad \frac{1}{\sqrt{x^2 - 1}}$$

$$\tanh^{-1} x \quad \frac{1}{1 - x^2}$$

## SUIMEÁIL (INTEGRATION)

Glactar  $a > 0$  agus fágtar tairisigh na suimeála ar lár.

We take  $a > 0$  and omit constants of integration.

$$f(x) \quad \int f(x) dx$$

$$x^n \quad (n \neq -1) \quad \frac{x^{n+1}}{n+1}$$

$$\ln |x| \quad \ln |x|$$

$$\frac{\sin x}{\cos x} \quad -\ln |\sec x|$$

$$\ln |\sec x + \tan x|$$

$$\csc x \quad \ln \left| \tan \frac{x}{2} \right|$$

$$\cot x \quad \ln |\sin x|$$

$$e^x \quad e^x$$

$$e^{ax} \quad \frac{1}{a} e^{ax}$$

$$a^x \quad \frac{a^x}{\ln a}$$

$$\frac{1}{\sqrt{a^2 + x^2}} \quad \ln \left| \frac{x + \sqrt{a^2 + x^2}}{a} \right|$$

$$\frac{1}{\sqrt{a^2 - x^2}} \quad \sin^{-1} \frac{x}{a}$$

$$\frac{1}{x^2 + a^2} \quad \frac{1}{a} \tan^{-1} \frac{x}{a}$$

$$\frac{1}{x\sqrt{x^2 - a^2}} \quad \frac{1}{a} \sec^{-1} \frac{x}{a}$$

$$\frac{1}{\sqrt{x^2 - a^2}} \quad \ln \left| \frac{x + \sqrt{x^2 - a^2}}{a} \right|$$

$$\frac{1}{a^2 - x^2} \quad \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right|$$

## Differentiation

$$\coth^{-1} x \quad -\frac{1}{x^2 - 1}$$

$$\text{sech}^{-1} x \quad -\frac{1}{x\sqrt{1-x^2}}$$

$$\text{cosech}^{-1} x \quad -\frac{1}{x\sqrt{x^2+1}}$$

Torthaí agus Líonta:

Products and Quotients:

$$y = uv; \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$y = \frac{u}{v}; \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

Foirmilí áisiúla:

Useful formulae:

$$\sinh^{-1} x = \ln(x + \sqrt{x^2 + 1})$$

$$\cosh^{-1} x = \ln(x + \sqrt{x^2 - 1})$$

$$\tanh^{-1} x = \frac{1}{2} \ln \frac{1+x}{1-x}$$

$$(-1 < x < 1)$$

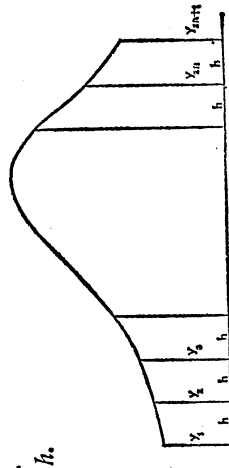
Teoragán Taylor (Taylor's Theorem):

$$f(x+h) = f(x) + hf'(x) + \frac{h^2}{2!} f''(x) + \dots + \frac{h^r}{r!} f^{(r)}(x) + \dots$$

Rial Shimpson (Simpson's Rule):

Corr-uimhir ordanáidí iad  $y_1, y_2, \dots, y_{2n-1}$  fad  $h$  óna chéile.

$y_1, y_2, \dots, y_{2n+1}$  is an odd number of ordinates at intervals of length  $h$ .



$$\text{Achar (Area)} \approx \frac{1}{3} h \{y_1 + y_{2n-1} + 2(y_2 + y_3 + \dots + y_{2n-2}) + 4(y_2 + y_4 + \dots + y_{2n})\}$$

## Integration

$$\sinh x \quad \cosh x$$

$$\cosh x \quad \sinh x$$

$$\tanh x \quad \ln \cosh x$$

$$\coth x \quad \ln |\sinh x|$$

$$\text{sech } x \quad \tan^{-1}(\sinh x)$$

$$\csc \text{ch } x \quad \ln \left| \tanh \frac{x}{2} \right|$$

$$\cos^2 x \quad \frac{1}{2} [x + \frac{1}{2} \sin 2x]$$

$$\sin^2 x \quad \frac{1}{2} [x - \frac{1}{2} \sin 2x]$$

$$\cosh^2 x \quad \frac{1}{2} [x + \frac{1}{2} \sinh 2x]$$

$$\sinh^2 x \quad \frac{1}{2} [-x + \frac{1}{2} \sinh 2x]$$

$$\frac{1}{x\sqrt{a^2 - x^2}} \quad -\frac{1}{a} \text{sech}^{-1} \frac{x}{a}$$

$$\frac{1}{x\sqrt{x^2 + a^2}} \quad -\frac{1}{a} \text{cosech}^{-1} \frac{x}{a}$$

Suimeáil trí mhíreanna:

Integration by parts:

$$\int u dv = uv - \int v du$$

$$e = 2.718281828$$