18-447 Lecture 15: Principles of Caching

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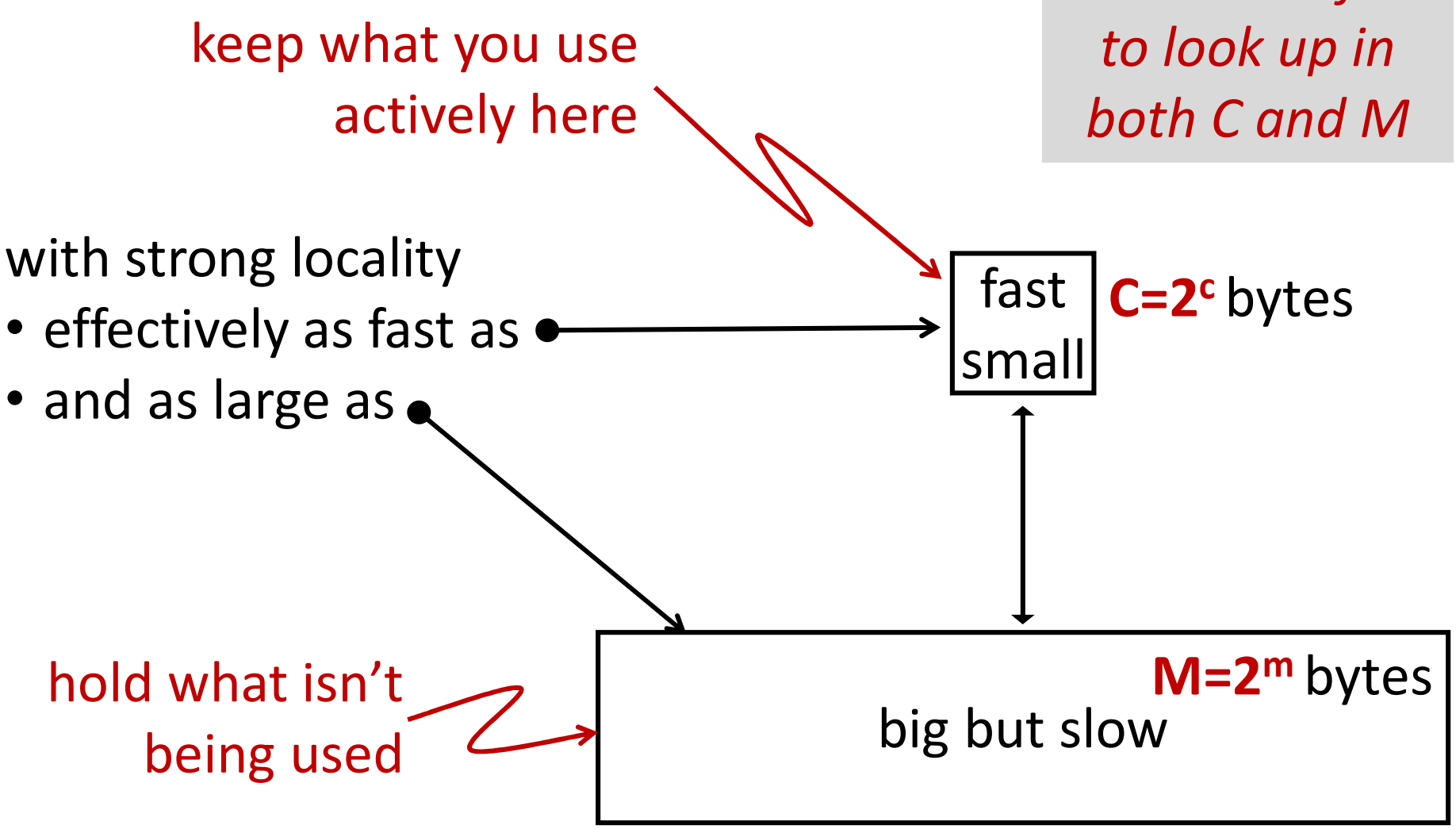
Housekeeping

- Your goal today
  - understand caching ("aBC" and "3 C's") in the abstract and in isolation
- Notices
  - HW 4, past due
  - HW 5, due 4/4 (Handout #13)
  - Lab 3, due week 10
  - Midterm 1 regrade due Monday 3/28 noon
- Readings
  - P&H Ch 5

Cache Hierarchy

use index of M to look up in both C and M



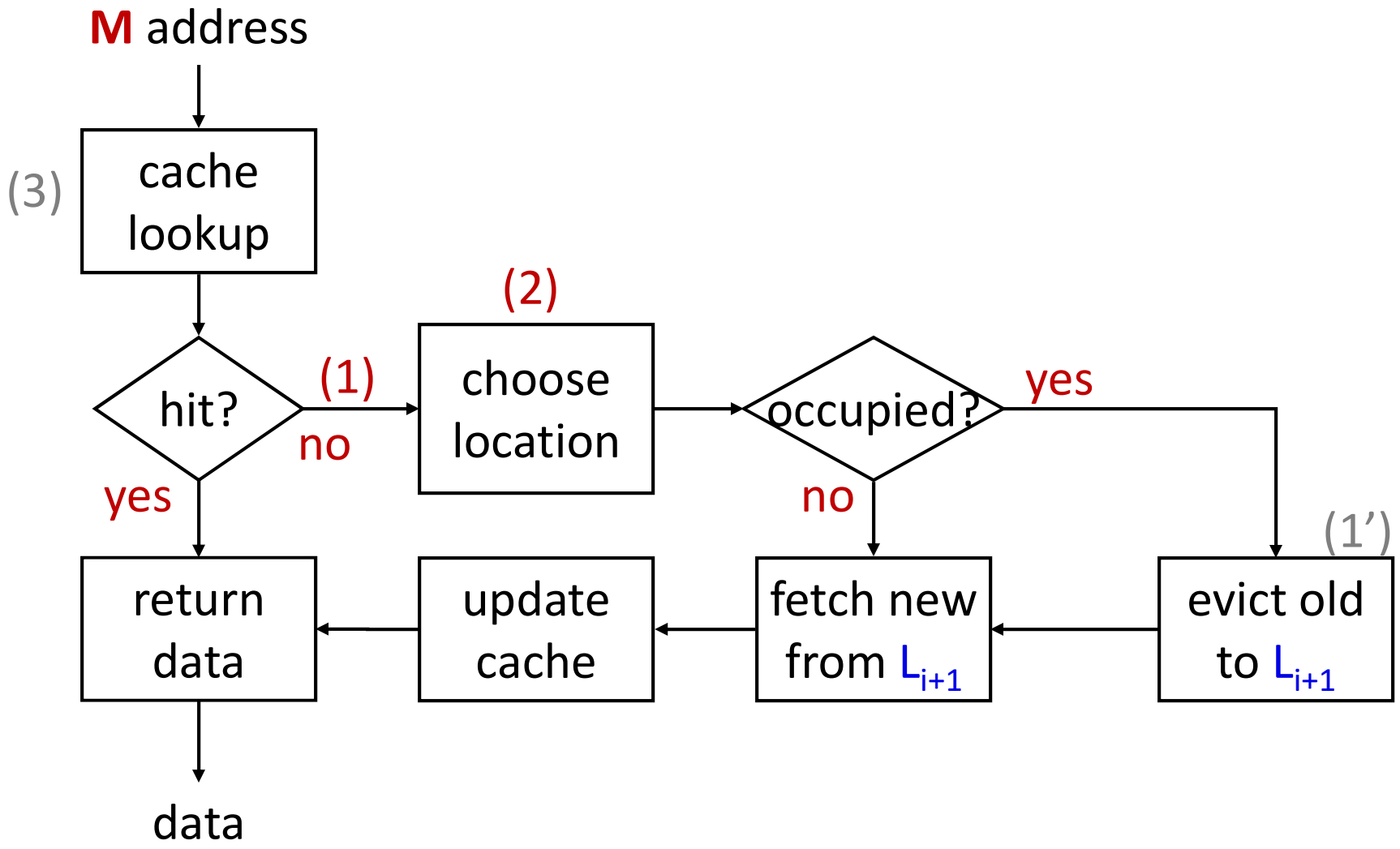
The Basic Problem

- Potentially **M=2^m** bytes of memory, how to keep "copies" of most frequently used locations in **C** bytes of fast storage where **C << M**

- Basic issues (intertwined)
  (1) when to cache a "copy" of a memory location
  (2) where in fast storage to keep the "copy"
  (3) how to find the "copy" later on *(LW and SW only give indices into* **M***)*

Capacity

Basic Operation (demand-driven version)



Basic Cache Parameters

- **M = 2^m** : size of address space in bytes

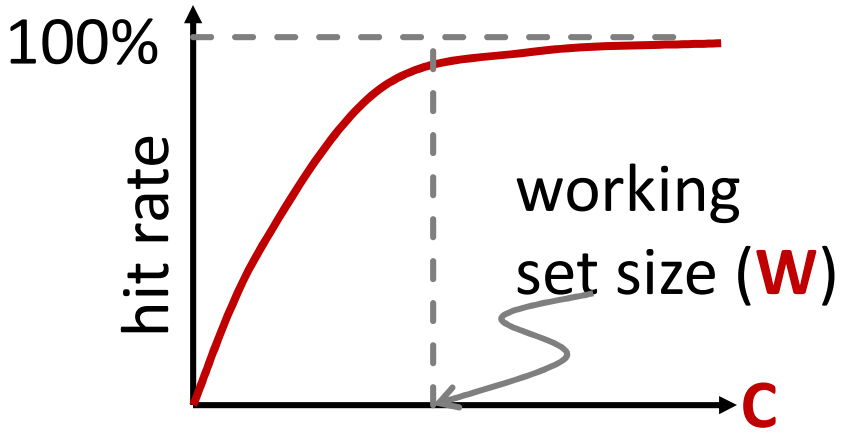
  sample values: 2^{32}, 2^{64}

- **G=2^g** : cache access granularity in bytes

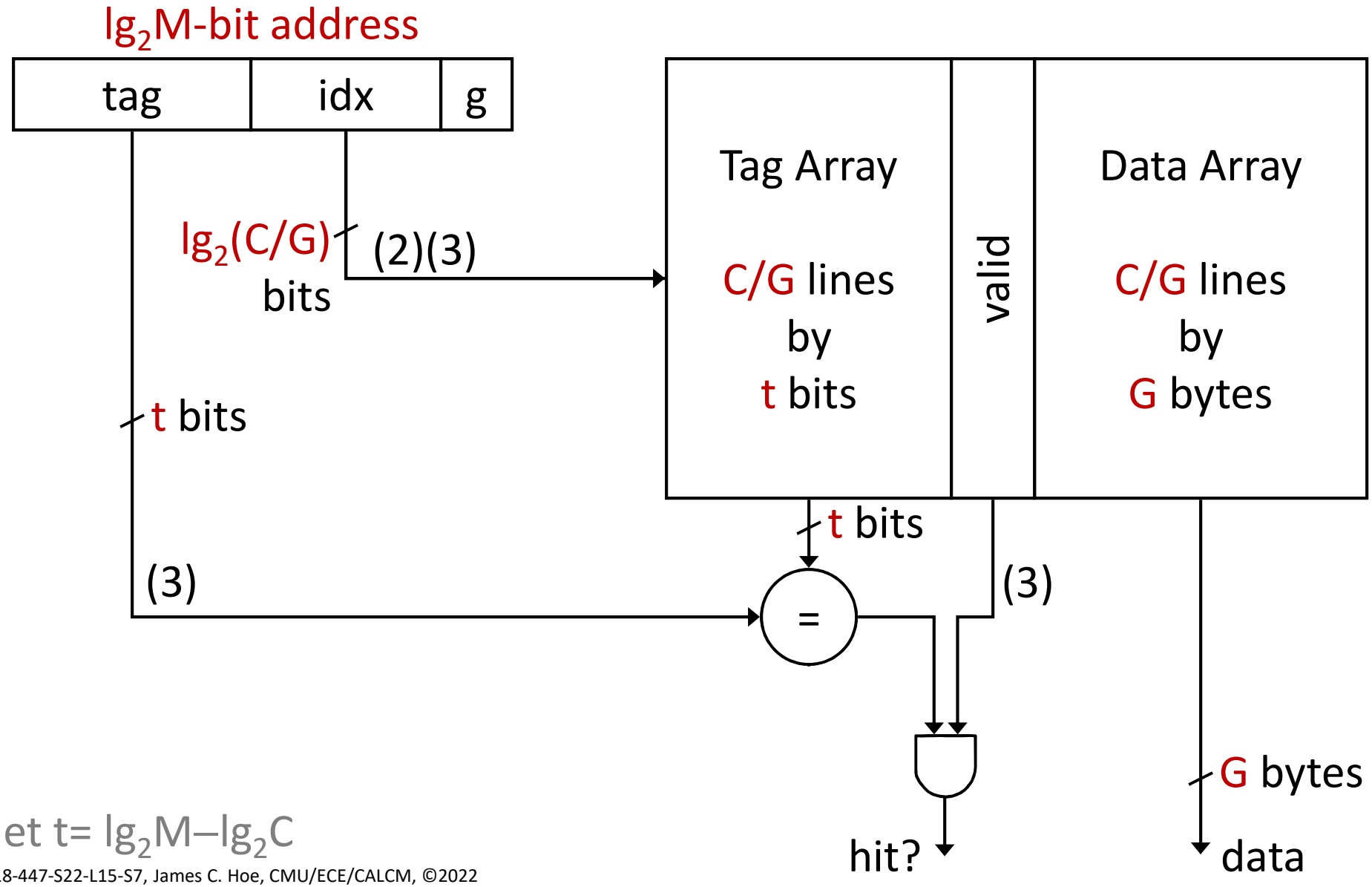
  sample values: 4, 8

- **C** : "capacity" of cache in bytes

  sample values: 16 KByte (L1), 1 MByte (L2)



Direct-Mapped Placement (first try)



let t= $lg_2M - lg_2C$

Storage Overhead and Block Size

- For each cache block of **G** bytes, also storing "**t+1**" bits of tag (where $t=\lg_2 M - \lg_2 C$)
  - if $M=2^{32}$, $G=4$, $C=16K=2^{14}$

  $\Rightarrow$ **t**=18 bits for each 4-byte block

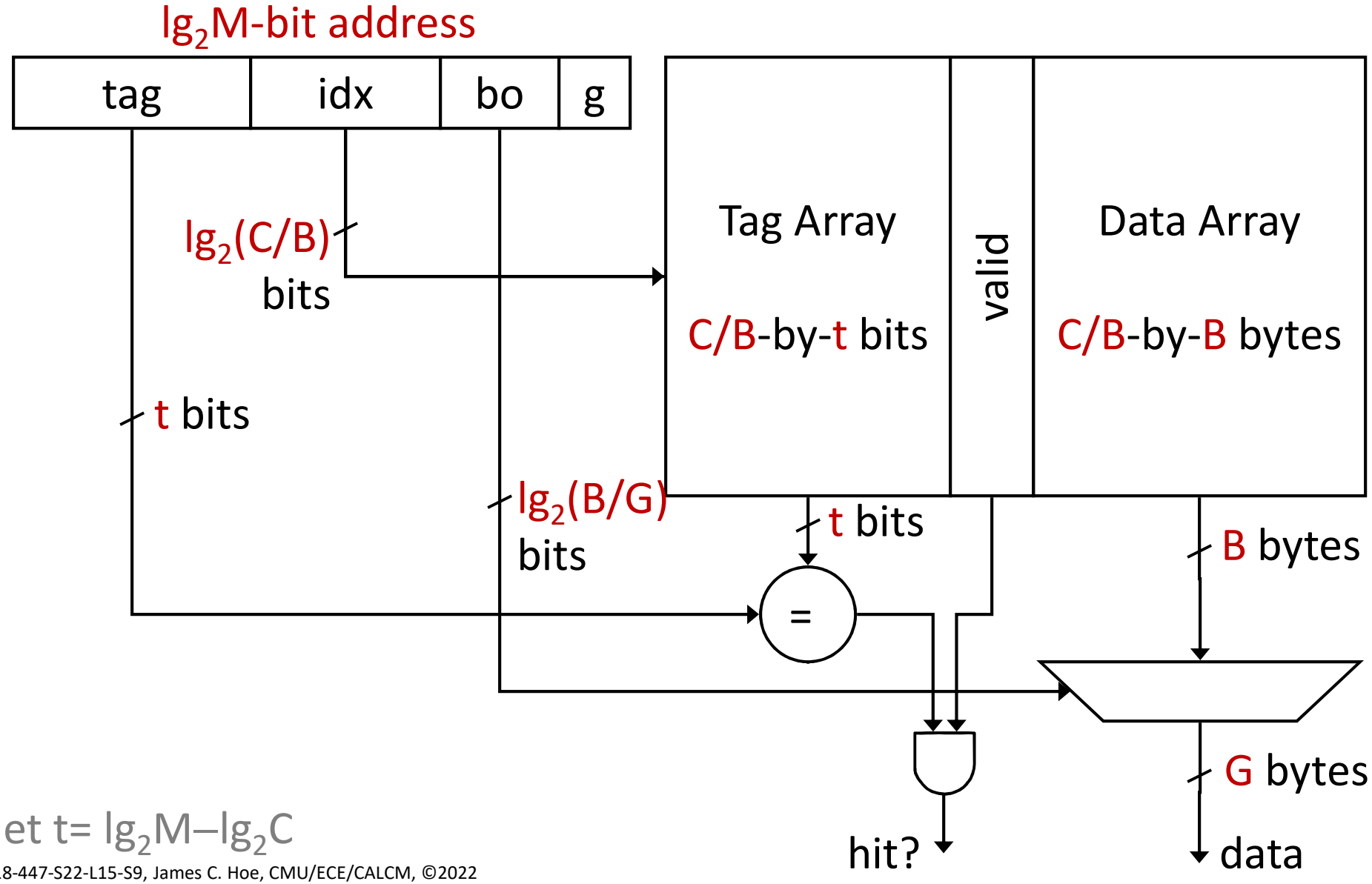
  60% overhead; 16KB cache actually 25.5KB SRAM
- Solution: "amortize" tag over larger **B**-byte block
  - manage **B/G** consecutive words as indivisible unit
  - if $M=2^{32}$, **B**=16, **G**=4, **C**=16K

  $\Rightarrow$ **t**=18 bits for each 16-byte block

  15% overhead; 16KB cache actually 18.4KB SRAM
  - spatial locality also says this is good *(Q1: when)*
- Larger caches wants even bigger blocks

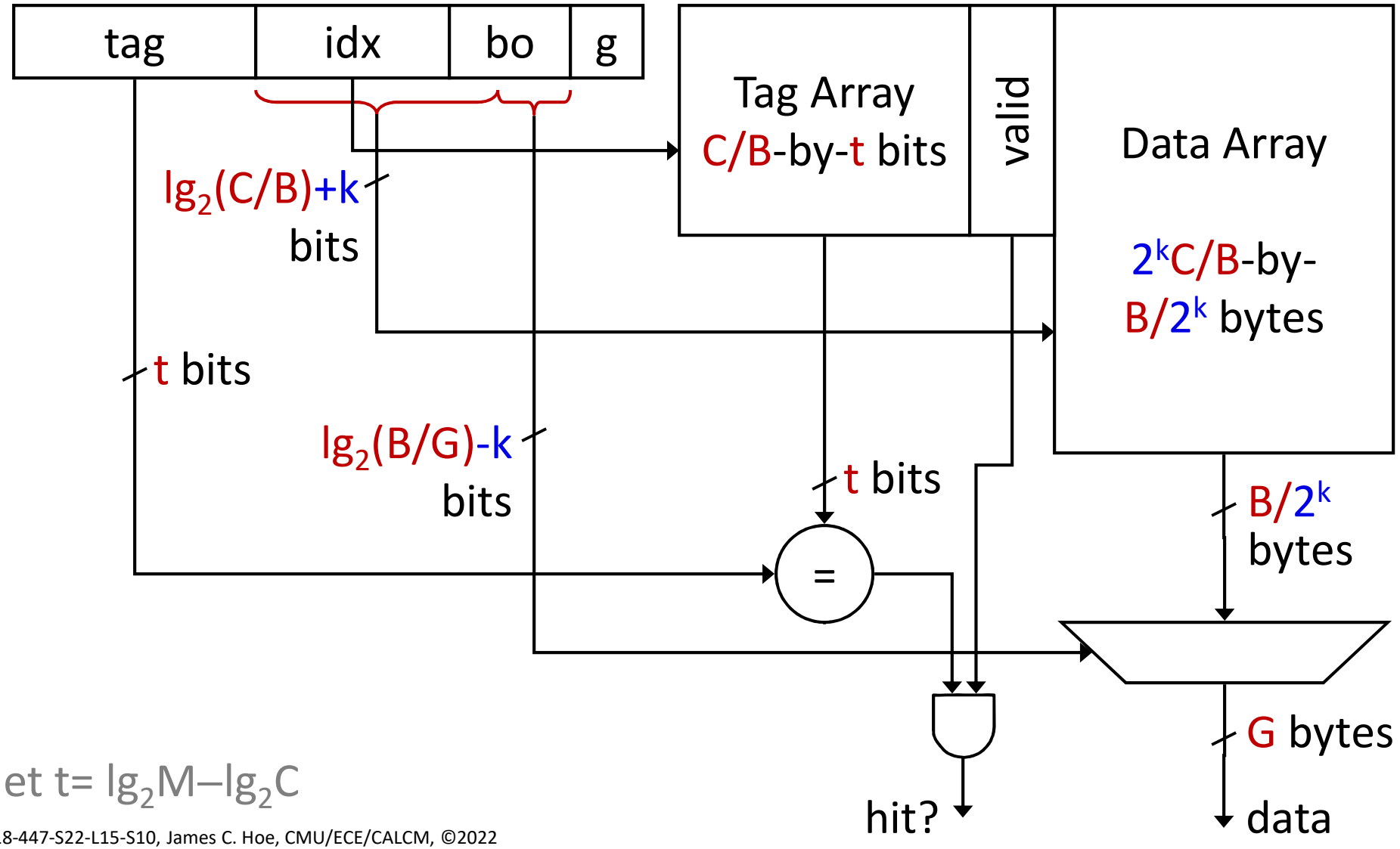
B

Direct-Mapped Placement (final)



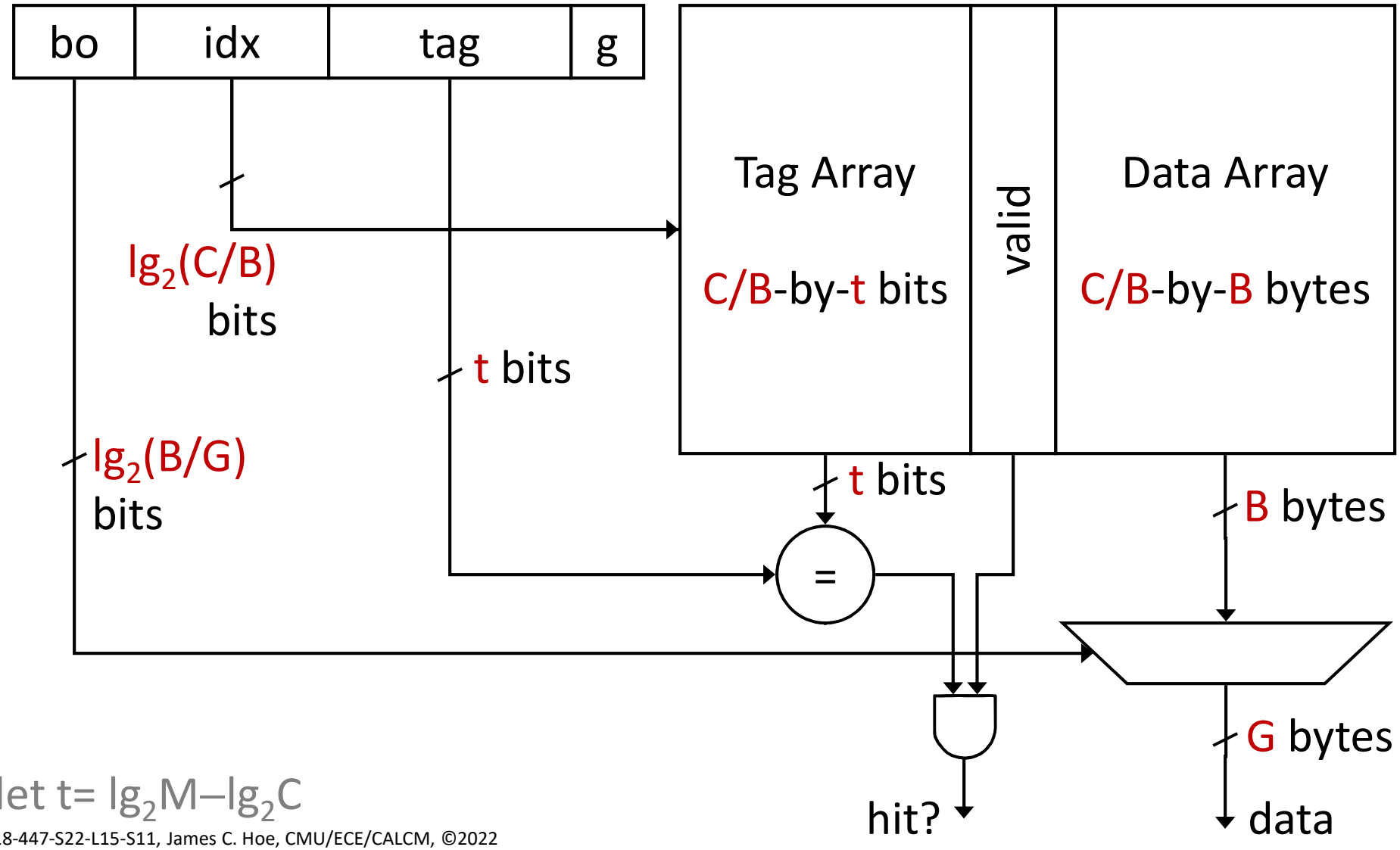
let t= $lg_2M - lg_2C$

Is this different?



let t= $lg_2M - lg_2C$

Is this okay?

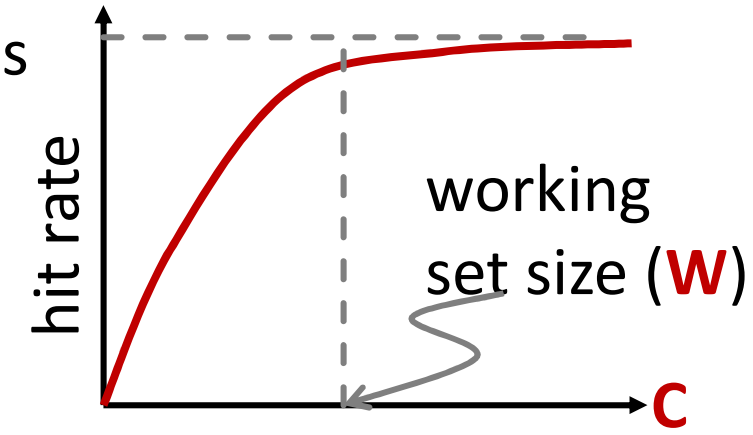


let t= $lg_2M – lg_2C$

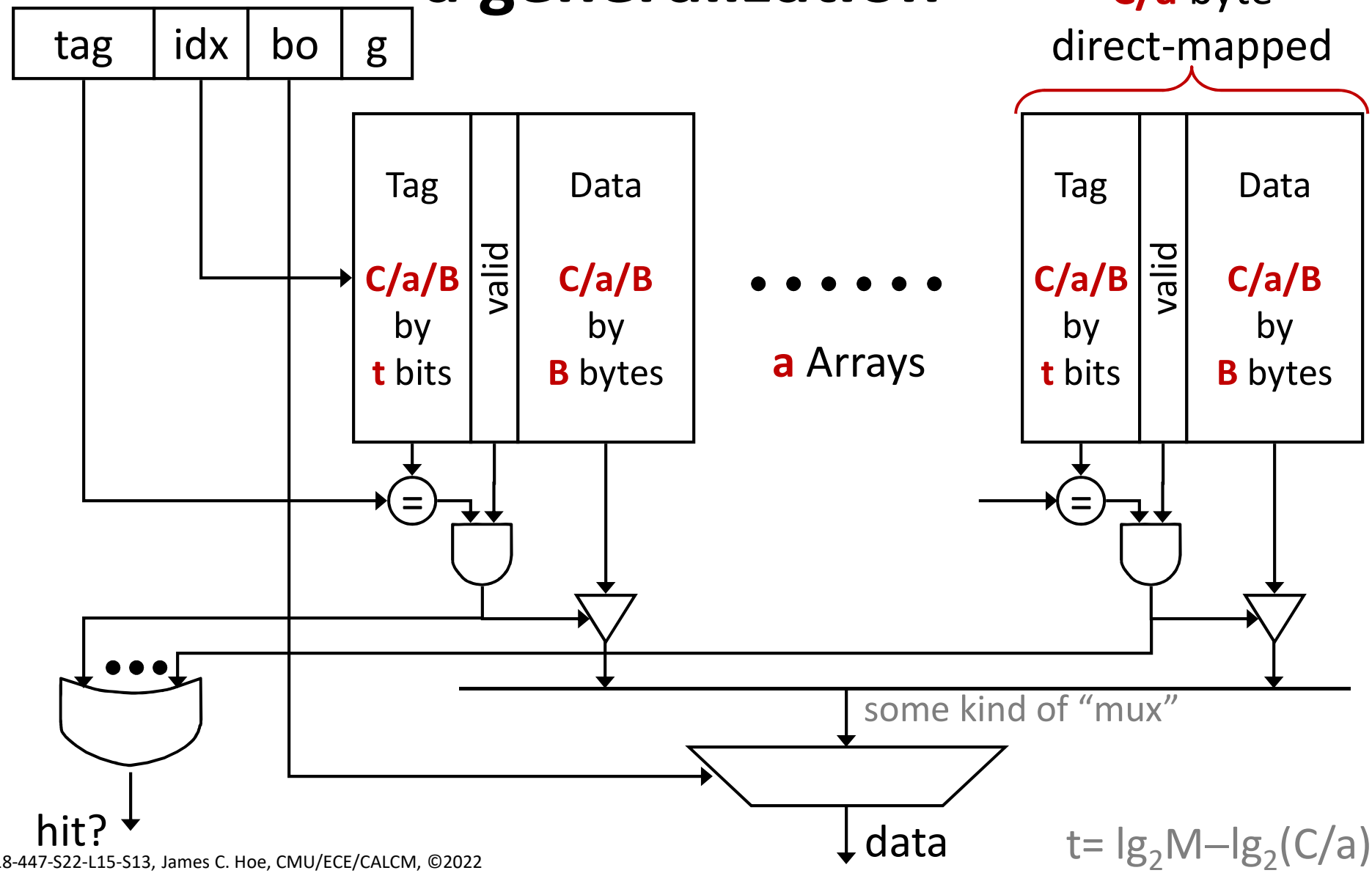
Direct-Mapped Policy in Essence

- **C**-byte storage array managed as **C**/**B** cache blocks
- A given block address directly maps to exactly one choice of cache block (by block index field)
- Block addresses with same block index field map to same cache block
  - of 2^{t} such addresses, hold only one at a time
  - even if **C** > working set size, conflict is possible

    ("working set" is not one continuous region)
  - probability 2 random addresses conflict is 1/(**C**/**B**); likelihood for conflict increases with decreasing number of blocks



Set Associative Placement Policy: a generalization



$t = \lg_2 M - \lg_2 (C/a)$

a-way Set-Associative Placement

- **C** bytes of storage divided into **a** direct-mapped arrays (aka "ways" and sometimes "banks")
  - each "way" has (**C**/**a**)/**B** cache blocks
  - a given block address maps to exactly one choice per "way"; **a** choices constitute the "set"

    direct-mapped is special case **a**=1
  - overhead: **a** comparators and **a**-to-1 multiplexer
- Block addresses with same index map to same set
  - 2^t such addresses; hold **a** different ones at a time
  - if **C** > working set size

    higher-degree of associativity ⇒ fewer conflicts

    What if **C** < working set size?

associativity

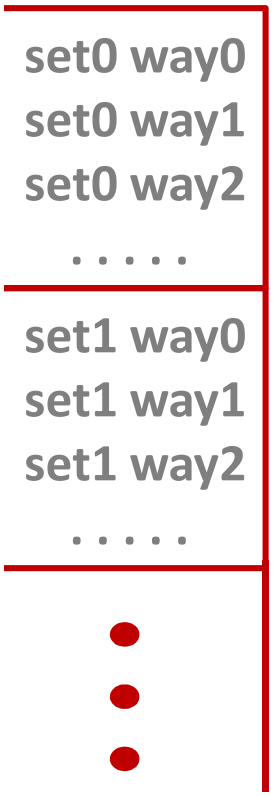
Replacement Policy to Choose from a

- New block displaces an existing block from "set"
  - pick the one that is least recently used (LRU)

    exactly LRU expensive for **a**>2
  - pick any one except the most recently used
  - ~~pick the most recently used one~~
  - ~~pick one based on some part of the address bits~~
  - pick the one used again furthest in the future Belady
  - pick a (pseudo) random one
- No real best choice; second-order impact only
  - if actively using less than **a** blocks in a set, any sensible replacement policy will quickly converge
  - if actively using more than **a** blocks in a set, no replacement policy can help you

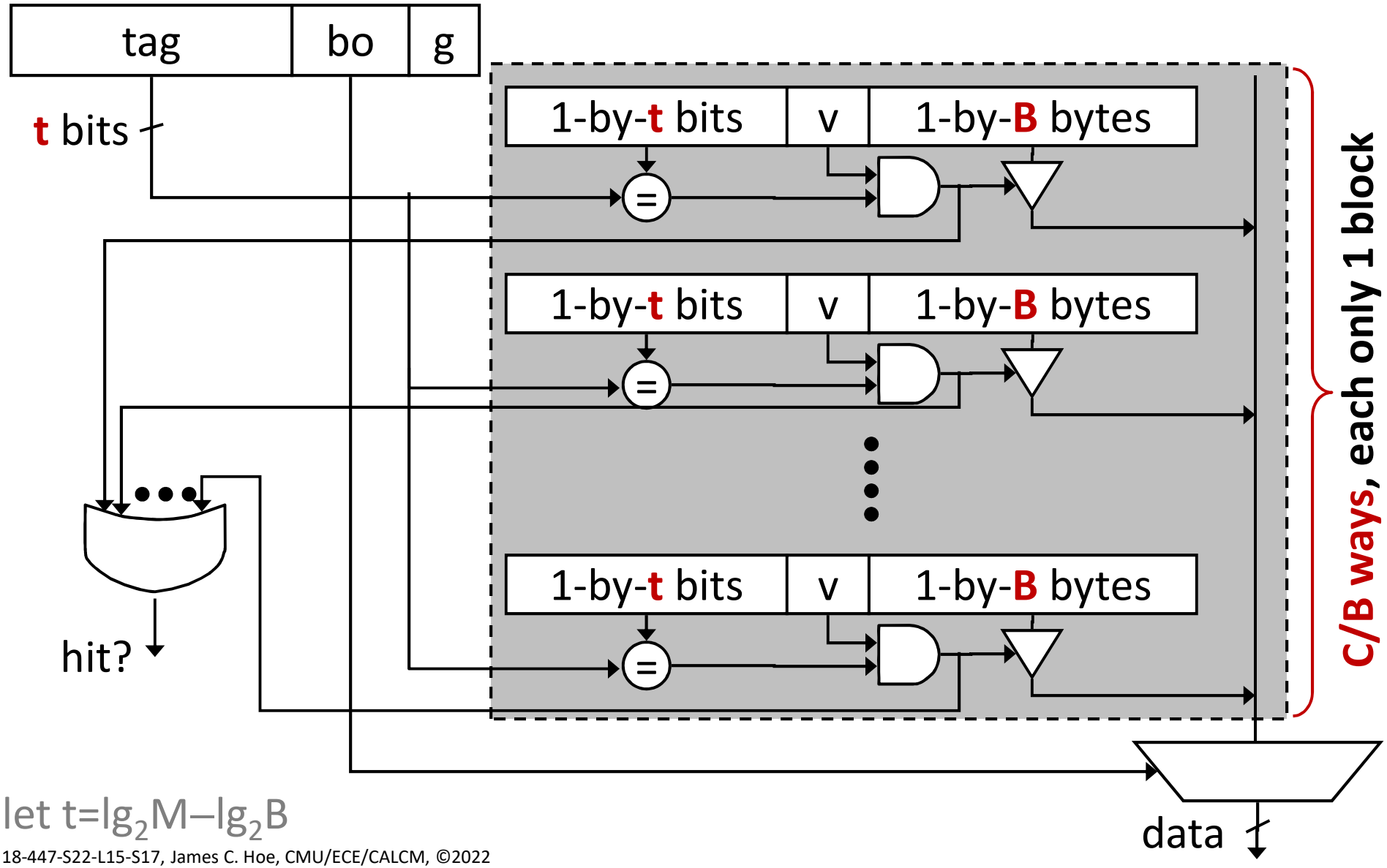
Policy vs Realization

- Associativity is a placement policy
  - it says a block address could be placed in one of **a** different blocks
  - it doesn't say "ways" are parallel look-up banks
- "Pseudo" **a**-way associative cache
  - given a direct-mapped array with **C**/**B** blocks
  - logically partition into **C**/**B**/**a** sets
  - given an address **A**, index into set and sequentially search its ways:
- Optimization: record the most recently used way (MRU) to check first



e.g., used by MIPS R10K L2

Fully Associative Cache: a≡C/B

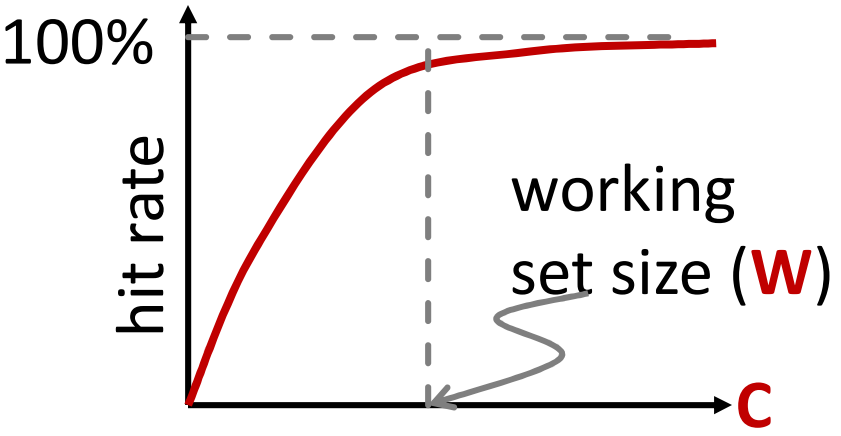


let $t=\lg_2 M - \lg_2 B$

3C's of Cache Misses

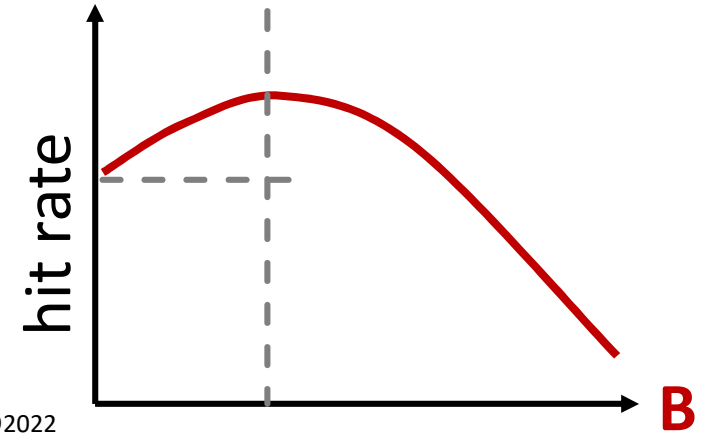
Capacity Miss

- Cache is too small to hold everything needed
- Defined as the misses that would occur in a fully-associative cache of the same capacity using optimum (Belady) replacement
- Dominates when **C** < **W**
  - for example, the L1 cache usually not big enough due to cycle-time tradeoff
- Main design factor: **C**



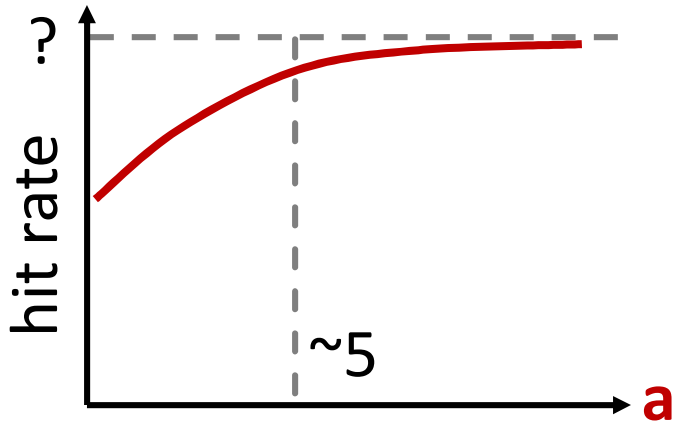
Compulsory Miss

- First reference to a block address always misses (if no prefetching)
- Dominates when locality is poor
  - for example, in a "streaming" data access pattern where many addresses are visited, but each is used only once
- Main design factor: **B** and "prefetching"



Conflict Miss

- Miss to a previously visited block address displaced due to conflict under direct-mapped or set-associative allocation
- Defined as "a miss that is neither compulsory nor capacity"
- Dominates when **C≈W** or when **C/B** is small
- Main design factor: **a**



3'C worksheet: a=1, B=1, C=2

addr	set#	which C?	set[2]	F.A. + Belady
0x0	0	compulsory	[-,-] → [0,-]	{ } → {0}
0x2	0			
0x0	0			
0x2	0			
0x1	1			
0x0	0			
0x2	0			
0x0	0			

3'C worksheet: a=1, B=1, C=2

addr	set#	which C?	set[2]	F.A. + Belady
0x0	0	compulsory	[-,-] → [0,-]	{ } → {0}
0x2	0	compulsory	[0,-] → [2,-]	{0} → {0,2}
0x0	0	conflict	[2,-] → [0,-]	$\{0,2\}_{hit}$
0x2	0	conflict	[0,-] → [2,-]	$\{0,2\}_{hit}$
0x1	1	compulsory	[2,-] → [2,1]	{0,2} → {0,1}
0x0	0	conflict	[2,1] → [0,1]	$\{0,1\}_{hit}$
0x2	0	capacity	[0,1] → [2,1]	{0,1} → {0,2}
0x0	0	conflict	[2,1] → [0,1]	$\{0,2\}_{hit}$

Recap: Basic Cache Parameters

ISA

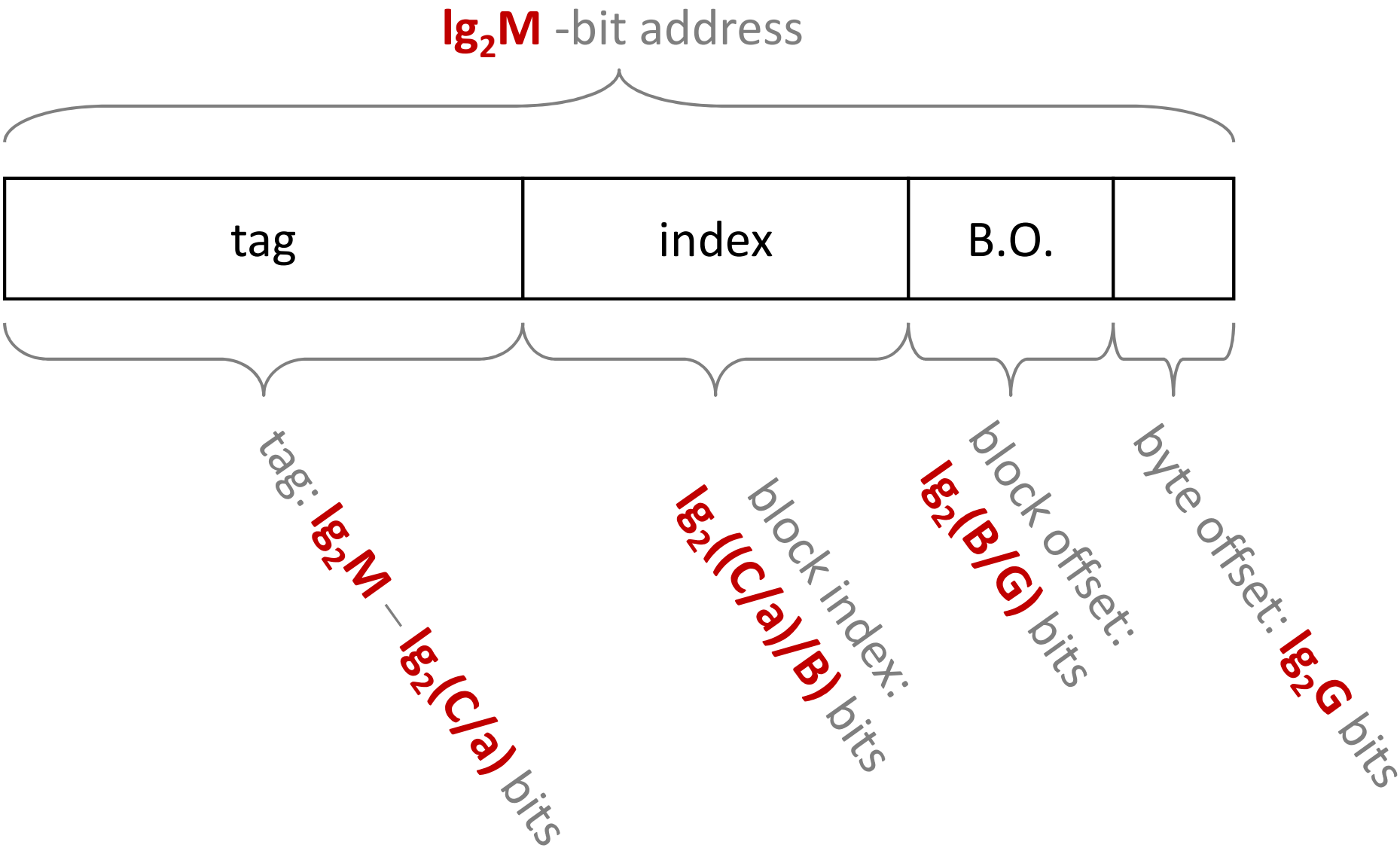
- **M = 2^m** : size of address space in bytes
  sample values: 2^{32}, 2^{64}
- **G=2^g** : cache access granularity in bytes
  sample values: 4, 8

Implementation

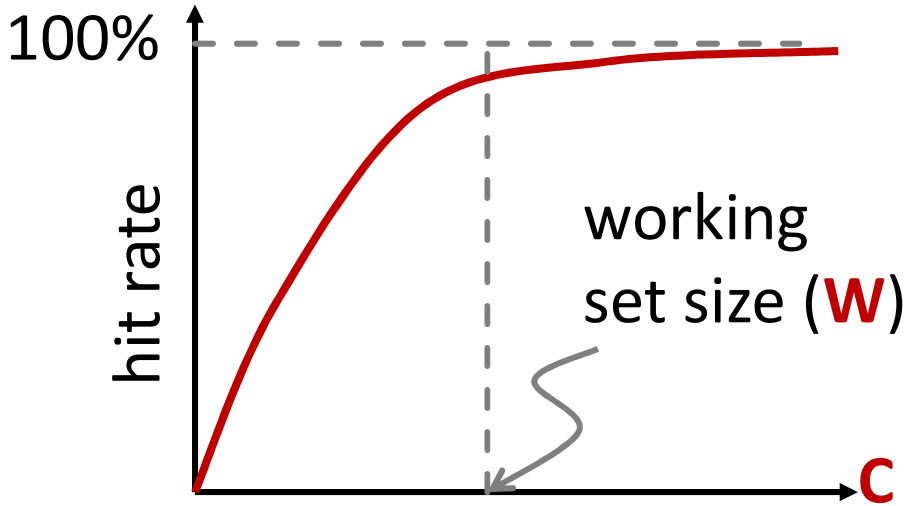
- **C** : "capacity" of cache in bytes
  sample values: 16 KByte (L1), 1 MByte (L2)
- **B = 2^b**: "block size" in bytes
  sample values: 16 (L1), >64 (L2)
- **a**: "associativity" of the cache
  sample values: 1, 2, 4, 5(?),... "C/B"

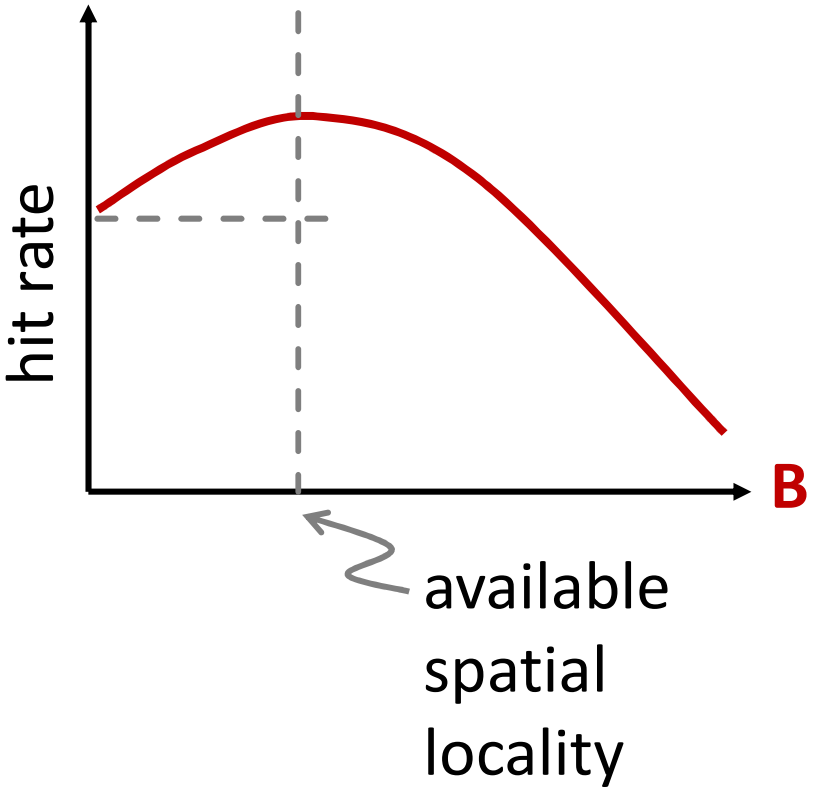
C/a should be a 2-power

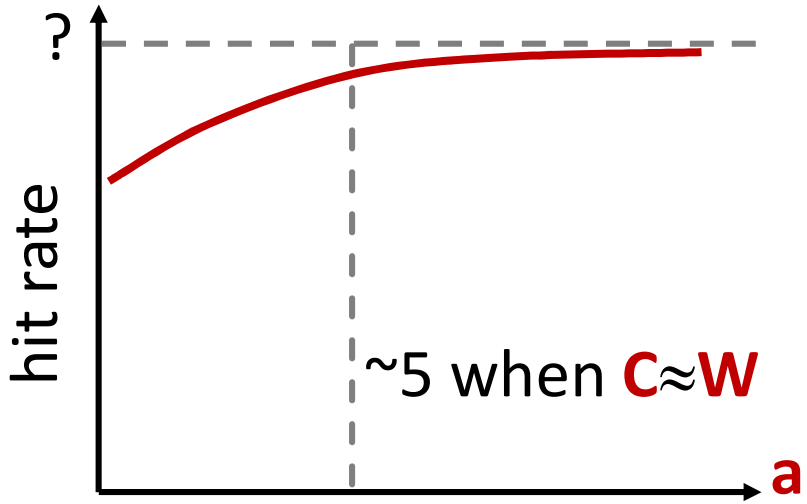
Recap: Address Fields



aBC Rule of Thumb Cribsheet



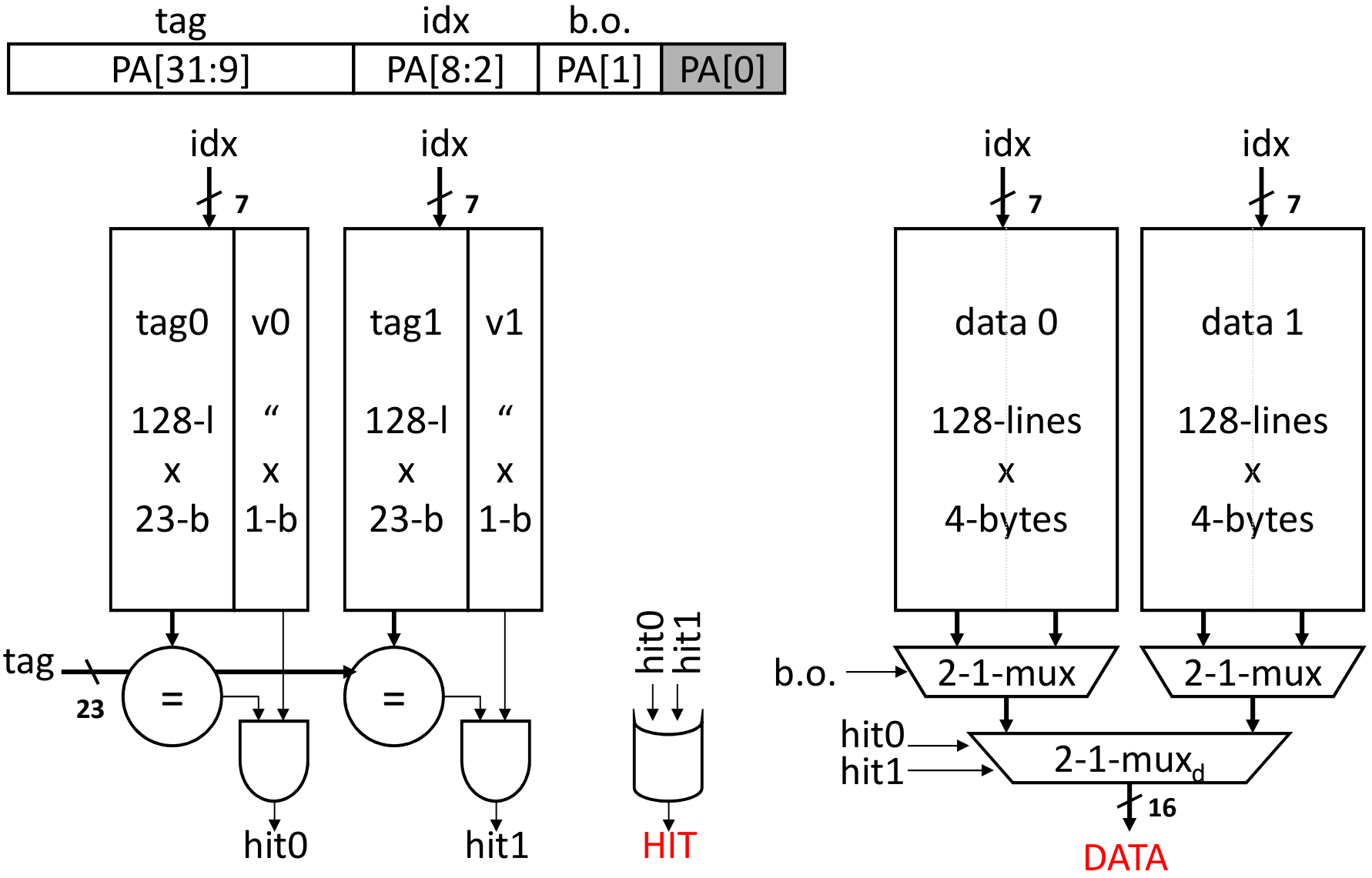




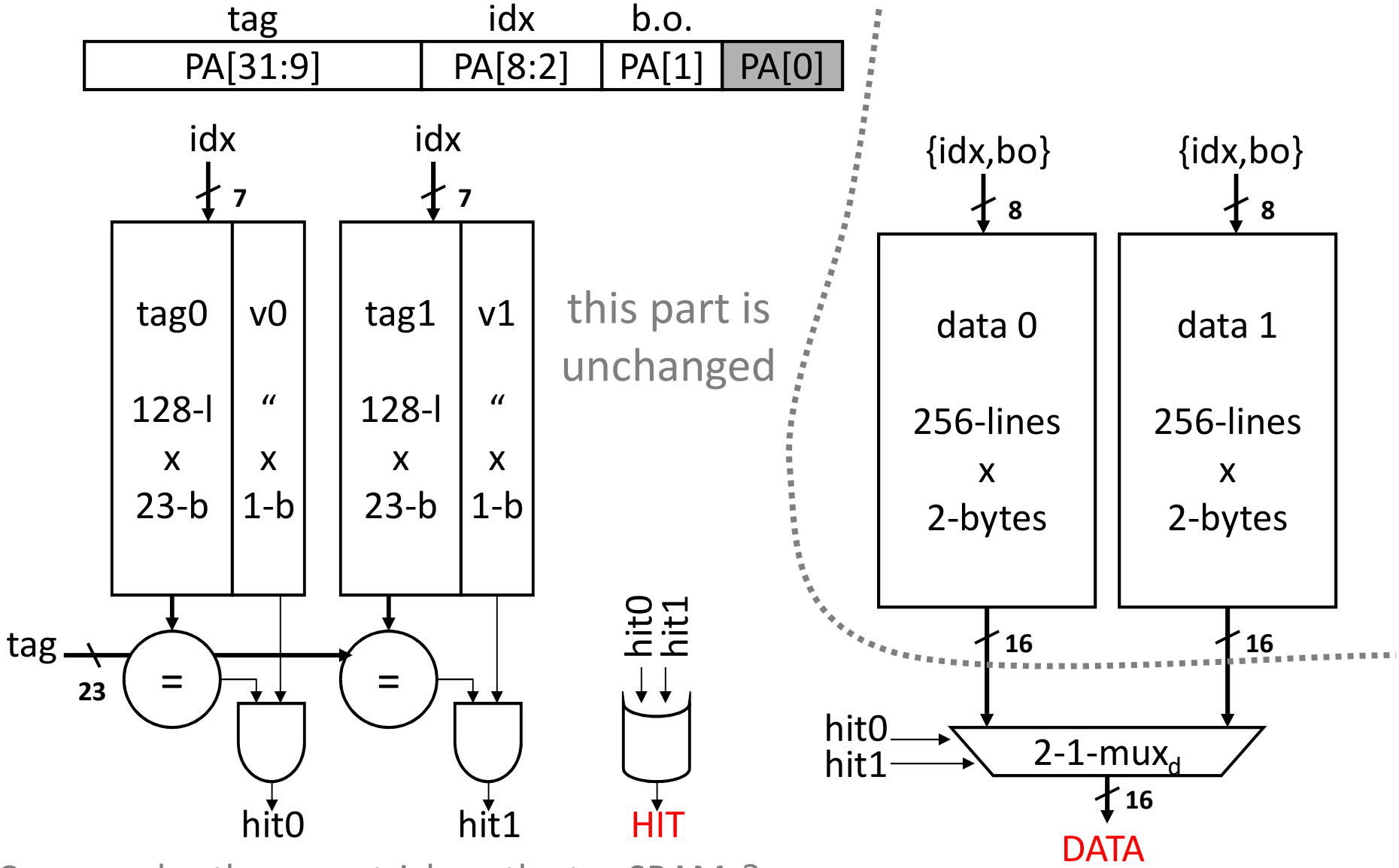
For "typical" programs

$M=2^{32}$, $a=2$, $C=1K$, $B=4$, $G=2$

M=2^{32}, a=2, C=1K, B=4, G=2: "textbook" solution

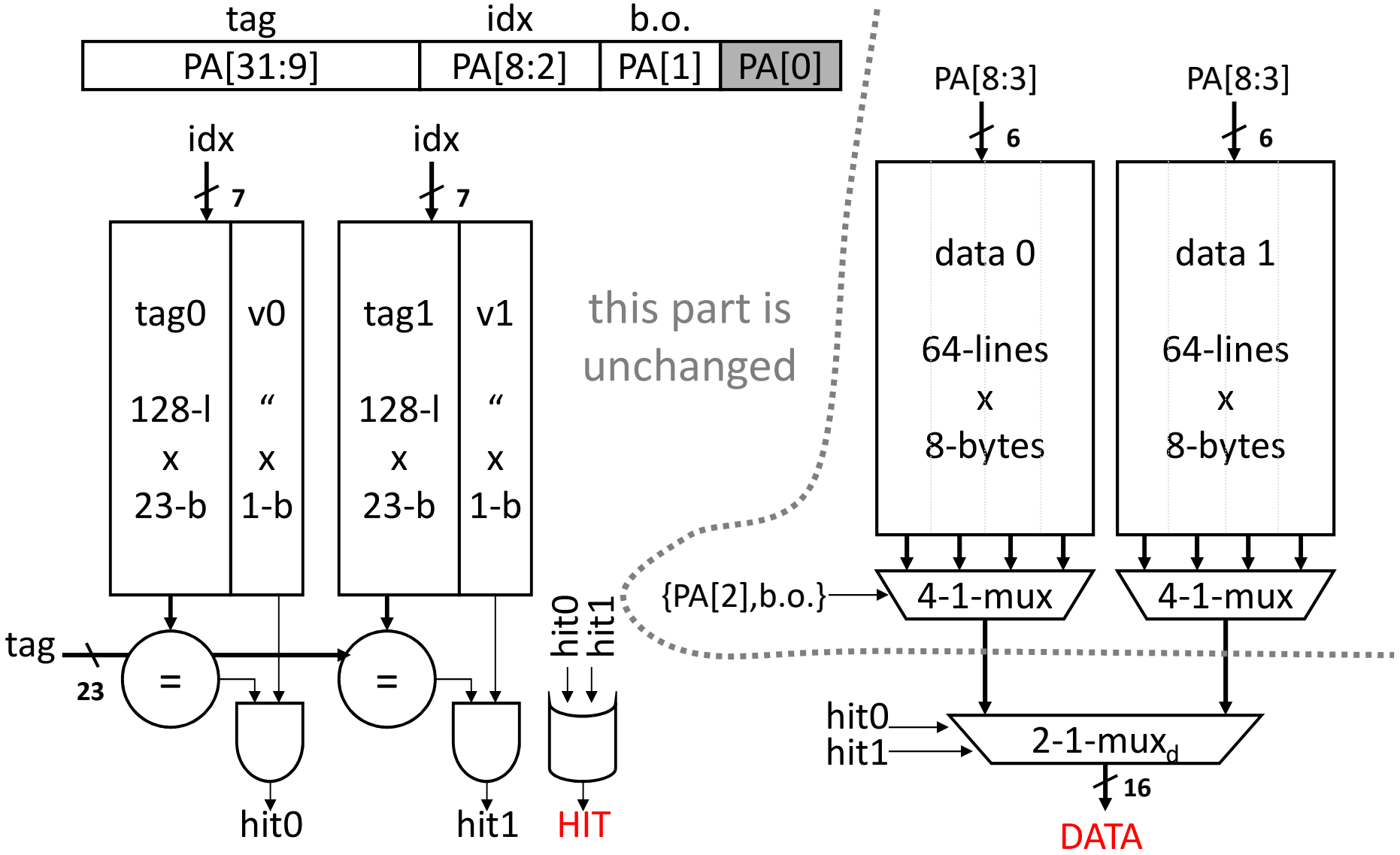


Same cache parameters
but tune for "narrower" data SRAM banks



Can you play the same trick on the tag SRAMs?

Same cache parameters but tune for "fatter" data SRAM banks



Can you play the same trick on the tag SRAMs?

Same cache parameters but each block frame is interleaved over 2 SRAM banks