

Stack: Quiz

- The time complexity $T(N)$ of inserting first N items by using `resize(capacity * 2)` may be expressed in an open form:

$$T(N) = N + (1 + 2 + 4 + 8 + \dots + N)$$

- Rewrite $T(N)$ shown above in a closed form.

- $T(N) = 3N - 1$ (closed form)

$$1 + a + a^2 + a^3 + \dots + a^n = \frac{a^{n+1} - 1}{a - 1}$$

$$1 + 2 + 4 + \dots + 2^n = \frac{2^{n+1} - 1}{2 - 1} = 2^{n+1} - 1$$

Let, $N = 2^k$,

$$\begin{aligned} T(N) &= N + (1 + 2 + 4 + \dots + 2^k) \\ &= N + (2^{k+1} - 1) \\ &= N + 2 * 2^{\log_2 k} - 1 \\ &= 3N - 1 \end{aligned}$$

Therefore, $T(N) = N + (1 + 2 + 4 + \dots + N)$
 $= ?$

The time complexity of the algorithm is $O(n)$.

