Data Structures Chapter 5 Tree

- 1. introduction
- 2. Binary tree
 - Definition and Properties
 - Traversal
 - Coding Quizzes
- 3. Binary search tree
- 4. Tree balancing

Operations: size()

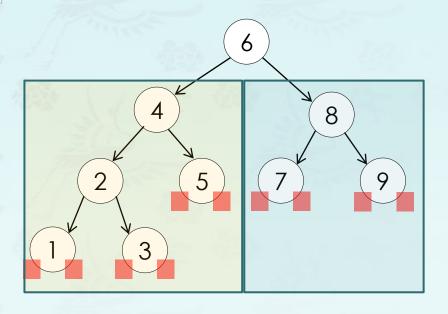
```
// returns the number of nodes in the binary tree
int size(tree node) {
  if (empty(node)) return 0;
  return size(node->left) + size(node->right) + 1;
}
```

 Q1. What is the total number of the function calls to complete with the tree and how many returns each?

```
17 (return 0 * 8 + return size * 9)
```

- Q2. Which node invokes the last function call?
 Node 9
- Q3. Which node finishes its size function call and returns size = 1 for the first time?

Node 1



Operations: height()

```
// returns the max depth of a tree.
// height = -1 for empty tree, 0 for root only tree
int height(tree node) {
  if (empty(node)) return -1;
  int left = height(node->left);
  int right = height(node->right);
  return max(left, right) + 1;
}
```

Q1. What is the total number of the function call to complete with the tree below?

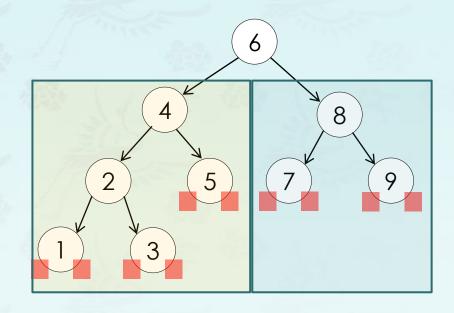
```
17 (return -1 * 8 + return height * 9)
```

Q2. What is the return value of the 10th and 12th function call?

-1, 1 (node 5's left empty node, node 8)

Q3. What is the return value of the node 2?





Operations: containsBT(), findBT()

```
// returns true if key is in a given binary tree, false otherwise.
bool containsBT(tree root, int key) {
  if (empty(root)) return false;
  if (key == root->key) return true;

return containsBT(root->left, key) || containsBT(root->right, key);
}
```

Q1: Which node invokes containsBT(root->right, key) for the first time?

Node 1

- Q2: Which node will invoke return false for the first time?
 Node 1
- Q3: How many function calls are made to reach the node key=5?

10

- Q4: How many function calls still remains in the system stack to finish after key=5 is found and what are they?
 - **0**, containsBT(node 6, 5) returns true and exit, because constainsBT(root->left, 5) returns true

