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CS157A HW2
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Q1

# R(A,B,C,D) with FDs: AB-> C, C -> D, D-> A

a.

Step 1: we need to project the set of functional dependencies, which can be inferred from R

Consider:

$$\{A\}+=A$$

$$\{B\}+=B$$

$$\{C\}+=\{C,D,A\}=>C->A$$

$${A,B}+ = {C,D,A,B} => AB->D$$

$${A,C}+ ={D,A} => AC->D$$

$${A,D}+ ={A,D}$$

$$\{B,C\}+=\{B,C,D,A\}=>BC->A,BC->D$$

$$\{B,D\}+=\{A,B,C,D\}=>BD->A,BD->C$$

$$\{C,D\}+=\{A,C,D\}=>CD->A$$

$${A,B,C}+ = {A,B,C,D} => ABC->D$$

$$\{B,C,D\}+=\{A,B,C,D\}=>BCD->A$$

$$\{C,D,A\}+=\{A,C,D\}$$

$${A,B,D}+ ={A,B,C,D}=> ABD->C$$

Step 2, from the set of FDs, we determine the keys are AB BC and BD

Step 3, BCNF violations are

C->A

C->D

D->A

AC->D

CD->A

b. Now, we decompose the relation into BCNF compliances. Pick C->A

We decompose the table into

$$R1=R(C, D, A)$$

$$R2=R(B,C)$$

As what we can see, BC is BCNF compliant. For CDA, we will evaluate the relation for BCNF.

We go through the same process of FD projection as above. We conclude that C is the key for

R(A, C, D). So, the FD: D-> A violates BCNF. So R(A, C, D) violates BCNF

Thus, we continue to break down R1 into AD and CD

In conclusion, we break R(A,B,C,D) into BC, AD, CD.

## R(A, B, C, D) with B-> C and B-> D

a. We process through the same process as what we did above First, try to project the set of FDs:

The resulting FDs:

B->D

B->C

AB->C

AB->D

BD->C

BC->D

BCA->D

BDA->C

Next, we determine the key: AB

**BCNF** violations:

B->D

B->C

BC->D

BD->C

b. Decompose the table

We choose B->C to begin the decomposition.

 $\{B\}+=\{B, C, D\}.$ 

We break down the table R(A, B, C, D) into R(B, C, D) and R(A, B)

R(A, B) satisfies BCNF. For the table R(B, C, D), we see that B is the only key. The projected FDs all contain B on the left hand side  $\rightarrow$  no BCNF violations.

The final decompositions: R(A, B) and R(B, C, D)

# R(A, B, C, D) with AB->C, CB-> D, CD-> A, DA-> B

a.

Step 1: we need to project the set of functional dependencies, which can be inferred from R

## Consider:

- $\{A\}+=A$
- $\{B\}+=B$
- $\{C\}+=C$
- $\{D\}+=D$

$${A,B}+ = {C,D,A,B} => AB->D$$

$${A,C}+={A,C}$$

$${A,D}+ ={A, D, B, C}=> AD->C$$

$$\{B,C\}+=\{B,C,D,A\}=> BC->A$$

$$\{B,D\}+=\{B,D\}$$

$$\{C,D\}+=\{A,C,D,B\}=>CD->B$$

$${A,B,C}+ = {A,B,C,D} => ABC->D$$

$$\{B,C,D\}+=\{A,B,C,D\}=> BCD->A$$

$${A,B,D}+ ={A,B,C,D}=> ABD->C$$

Infer the key: AB, AD, BC, CD

h.

It is obvious that all FDs identified above contains the key on LHS→ no BCNF violations No need to decompose

## R(A, B, C, D) with A->B, B-> C, C-> D, D-> A

a.

We need to project the set of functional dependencies, which can be inferred from R The set of new FDs inferred from the above:

A->B

B->C

C->D

D->A

A->D, A->C

B->A, B->D

C->A, C->B

D->C, D->B

AB->C, AB->D

CA->B, CA->D

DA->B, DA->C

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BC->A, BC-> D
DB-> A, DB->C
DC->A, DC->B
ABC->D
ABD->C
BCD->A
ADC->B
We can infer that A, B, C, D are the keys.
It is clear that all of the above FDs contain keys on the left hand side. Thus, there is no
BCNF violations.
b.
So, we do not need to decompose this.
R(A, B, C, D, E) with AB->C, DE->C, B->D.
a.
We go through the same process as above
We obtain the list of FDs:
AB->C
DE->C
B->D
BA->D
BC->D
EB->C, EB->D
ABC->D
ABD->C
AEB->C, AEB->D
AED->C
BEC->D
DBE->C
ABCE->D, ABDE->C
From the list of FDs above, we infer the key as: ABE
BCNF violations are:
AB->C
DE->C
B->D
BA->D
BC->D
EB->C, EB->D
ABC->D
ABD->C
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AED->C BEC->D

#### DBE->C

b.

We choose AB-> C to decompose the table.

{AB}+=ABCD

So, we initially decompose ABCDE into ABCD and ABE.

ABE is already in BCNF

We evaluate ABCD. The key is AB. We see that B->C violates BCNF (not contain the key). So we decompose ABCD into ABC and BD.

BD is in BCBF. ABC is also in BCNF (AB is the only key and all FDs satisfies BCNF).

Thus, we conclude that the decompositions are: ABE, ABC and BD.

# R(A, B, C, D, E) with AB-> C, C->D, D->B, D->E

a.

## Project the FDs:

C->B, C->D, C->E

D->B, D->E

BA->C, BA->D, BA->E

CA->B, CA->D, CA->E

AD->B, AD->C, AD->E

CB->D, CB->E

BD->E

CD->B, CD->E

CE->B, CE->D

DE->B

ACB->E

ABD->C, ABD->E

ABE->C, ABE->D

ACD->B, ACD->E

ACE->B, ACE->D

ADE->C, ADE->B

BCD->E, BCD->D

CED->B

ABCD->E

ACBE->D

We infer the keys as: AB, AC and DA

BCNF violations as the below:

C->B, C->D

D->E, D->B

BC->D, BC->E

DB->E

DC->B, DC->E

CE->B, CE->D

DE->B

BCD->E

BCE->D

CDE->B

b.

We choose D->B to decompose

 $\{D\}+=\{D, B, E\}$ 

Thus, the newly decomposed tables: BDE and ABC

BDE is in BCNF (D, ED and DB are the keys; all FDs contain the key on the left hand side) ABC is not in BCNF (AB & AC are the keys; however C->B does not contain the key on the left hand side)

# Decompose ABC into BC and AC

Both are BCNF compliant

So, we have: BDE, AC and BC

Q2

a.

Α	В	С	D	E
a	b	С	d1	e1
a1	b	С	d	e1
a	b1	С	d1	е

Applying the functional dependencies (B->E, CE->A), we now have the new table (green is what has changed)

Α	В	С	D	E
а	b	С	d1	e1
а	b	С	d	e1
а	b1	С	d1	е

It is clear that this is a lossy join. It is not a lossless decomposition.

# Example:

A	В	C
a	b	С
a	$b_1$	С

В	C	D
b	c	$d_1$
b	С	d
b <sub>1</sub>	С	$d_1$

A	C	E
a	c	$e_1$
a	С	e

After we join them, this is the result.

A	В	C	D	E
a	b	c	$d_1$	$e_1$
a	b	c	d	$e_1$
a	$b_1$	С	$d_1$	$e_1$
a	b	c	$d_1$	e
a	b	С	d	e
a	$b_1$	С	$d_1$	e

There are 3 more tuples than the original table  $\rightarrow$  It is a lossy join!

b. AC ->E and BC ->D

Α	В	С	D	E
а	b	С	d1	e1
a1	b	С	d	e1
а	b1	С	d1	е

Applying the functional dependencies, we now have the new table (green is what has changed)

Α	В	С	D	Е
a	b	С	d	е
a1	b	С	D	e1
а	b1	С	d1	е

It is clear that this is a lossless join.

c.

Α	В	С	D	Е
а	b	С	d1	e1
a1	b	С	d	e1
а	b1	С	d1	е

Applying the functional dependencies, we now have the new table (green is what has changed)

Α	В	С	D	Е
a	b	С	d	е
a1	b	С	d	е
а	b1	С	d	е

The decomposition is lossless.

d.

Α	В	С	D	Е
а	b	С	d1	e1
a1	b	С	d	e1
а	b1	С	d1	е

Applying the functional dependencies, we now have the new table (green is what has changed)

Α	В	С	D	E
а	b	С	d	е
a1	b	С	d	E
а	b1	С	d	е

This is lossless join.

Q3.

a.

**SELECT address** 

FROM Studio

WHERE name = 'MGM';

b.

SELECT birthdate

FROM MovieStar

WHERE name = 'Sandra Bullock';

c.

SELECT starName

FROM StarsIn

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WHERE movieYear = 1980
  OR movieTitle LIKE '%Love%';
Q4
a.
SELECT MovieStar.name
FROM MovieStar, StarsIn
WHERE MovieStar.name = StarsIn.starName
 AND StarsIn.movieTitle = 'Titanic'
 AND MovieStar.gender = 'M';
b.
SELECT StarsIn.starName
FROM Movies ,StarsIn, Studios
WHERE Studios.name = 'MGM'
 AND Movies.year = 1995
 AND Movies.title = StarsIn.movieTitle
 AND Movies.studioName = Studios.name;
c.
SELECT MovieExec.name
FROM MovieExec, Studios
WHERE MovieExec.cert# = Studios.presC#
 AND Studios.name = 'MGM';
d.
SELECT M1.title
FROM Movies M1,
   Movies M2
WHERE M1.length > M2.length
 AND M2.title ='Gone With the Wind';
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