Assignment 6: GLMs (Linear Regressios, ANOVA, & t-tests)

Student Name

OVERVIEW

This exercise accompanies the lessons in Environmental Data Analytics on generalized linear models.

Directions

##

- 1. Rename this file <FirstLast>_A06_GLMs.Rmd (replacing <FirstLast> with your first and last name).
- 2. Change "Student Name" on line 3 (above) with your name.
- 3. Work through the steps, creating code and output that fulfill each instruction.
- 4. Be sure to **answer the questions** in this assignment document.
- 5. When you have completed the assignment, **Knit** the text and code into a single PDF file.

Set up your session

- 1. Set up your session. Check your working directory. Load the tidyverse, agricolae and other needed packages. Import the *raw* NTL-LTER raw data file for chemistry/physics (NTL-LTER_Lake_ChemistryPhysics_Raw.csv). Set date columns to date objects.
- 2. Build a ggplot theme and set it as your default theme.

date, intersect, setdiff, union

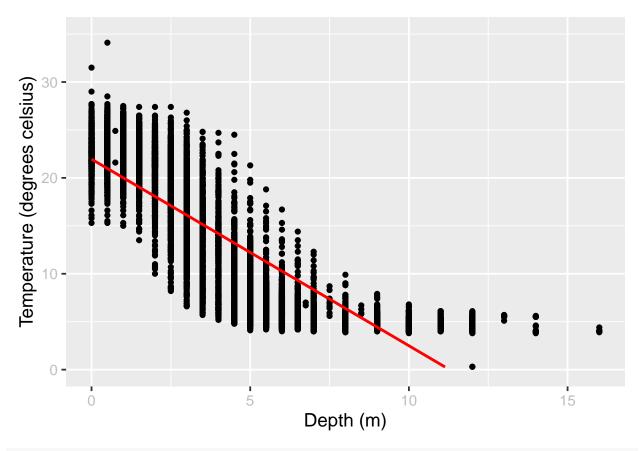
```
# 1
getwd()
## [1] "/home/guest/R/EDA Fall"
library(tidyverse)
## -- Attaching packages -
## v ggplot2 3.3.6
                              0.3.4
                     v purrr
## v tibble 3.1.8
                     v dplyr
                              1.0.10
## v tidyr
           1.2.0
                     v stringr 1.4.1
## v readr
           2.1.2
                     v forcats 0.5.2
## -- Conflicts -----
                            ## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(agricolae)
library(ggplot2)
library(lubridate)
##
## Attaching package: 'lubridate'
##
## The following objects are masked from 'package:base':
##
```

Simple regression

Our first research question is: Does mean lake temperature recorded during July change with depth across all lakes?

- 3. State the null and alternative hypotheses for this question: > Answer: H0: Temperature across the lakes will vary regardless of depth. There will not be a significant relationship between the variables and slope should be 0 Ha: Temperature across the lakes will decrease as depth lowers and will increase at shallower depths.
- 4. Wrangle your NTL-LTER dataset with a pipe function so that the records meet the following criteria:
- Only dates in July.
- Only the columns: lakename, year4, daynum, depth, temperature_C
- Only complete cases (i.e., remove NAs)
- 5. Visualize the relationship among the two continuous variables with a scatter plot of temperature by depth. Add a smoothed line showing the linear model, and limit temperature values from 0 to 35 °C. Make this plot look pretty and easy to read.

```
# 4
NTL_LTR_wrangled <- NTL_LTR %>%
    mutate(Month = month(sampledate)) %>%
    filter(Month == "7") %>%
    select("lakename", "year4", "daynum", "depth", "temperature_C") %>%
    drop_na("temperature_C")
# wrangling data to only have the selected columns and filtering out the data
# in those columns so it only has values from July, and dropping the NAs 5
NTL_LTR_Plot1 <- ggplot(NTL_LTR_wrangled, aes(x = depth, y = temperature_C)) + geom_point(aes(Color = "geom_smooth(method = lm, se = FALSE, color = "red") + ylim(0, 35) + GLM_plot_theme + xlab("Depth (m)") + ylab("Temperature (degrees celsius)")
## Warning: Ignoring unknown aesthetics: Color
print(NTL_LTR_Plot1)
## 'geom_smooth()' using formula 'y ~ x'
## Warning: Removed 24 rows containing missing values (geom_smooth).</pre>
```



making the first scatter plot with a single line of best fit

6. Interpret the figure. What does it suggest with regards to the response of temperature to depth? Do the distribution of points suggest about anything about the linearity of this trend?

Answer: The figure indicates that in general, as the depth of the lake increases, the temperature at that depth decreases in conjunction. Yes, there is a linear relationship but it is not a strong correlation at higher depths the points seem to be more varied indicating a wider range in temperatures, as the depth lowers the range of temperature decreases.

7. Perform a linear regression to test the relationship and display the results

```
# 7

NTL_LTR_regression <- lm(NTL_LTR_wrangled$temperature_C ~ NTL_LTR_wrangled$depth)
summary(NTL_LTR_regression)</pre>
```

```
##
## Call:
## lm(formula = NTL_LTR_wrangled$temperature_C ~ NTL_LTR_wrangled$depth)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -9.5173 -3.0192
                    0.0633
                           2.9365 13.5834
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          21.95597
                                       0.06792
                                                  323.3
                                                          <2e-16 ***
```

8. Interpret your model results in words. Include how much of the variability in temperature is explained by changes in depth, the degrees of freedom on which this finding is based, and the statistical significance of the result. Also mention how much temperature is predicted to change for every 1m change in depth.

Answer: The model indicates about 74% of the variability in temperature is related to changes in depth and that there are 9726 degrees of freedom, that results are statistically significant since the P value is $< 2.2e^-16$. The slope is -1.946 meaning that the temperature will decrease by about 2 degrees for every one meter.

Multiple regression

Let's tackle a similar question from a different approach. Here, we want to explore what might the best set of predictors for lake temperature in July across the monitoring period at the North Temperate Lakes LTER.

- 9. Run an AIC to determine what set of explanatory variables (year4, daynum, depth) is best suited to predict temperature.
- 10. Run a multiple regression on the recommended set of variables.

```
# 9
NTL_LTR_AIC <- lm(data = NTL_LTR_wrangled, temperature_C ~ depth + daynum + year4)
summary(NTL_LTR_AIC)
##
## Call:
## lm(formula = temperature_C ~ depth + daynum + year4, data = NTL_LTR_wrangled)
##
## Residuals:
                1Q Median
##
       Min
                                3Q
                                       Max
## -9.6536 -3.0000 0.0902 2.9658 13.6123
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.575564
                                      -0.994 0.32044
                           8.630715
## depth
               -1.946437
                           0.011683 -166.611
                                              < 2e-16 ***
## daynum
                                              < 2e-16 ***
                0.039780
                           0.004317
                                       9.215
## year4
                0.011345
                           0.004299
                                       2.639 0.00833 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.817 on 9724 degrees of freedom
## Multiple R-squared: 0.7412, Adjusted R-squared: 0.7411
## F-statistic: 9283 on 3 and 9724 DF, p-value: < 2.2e-16
# creating an AIC model
step(NTL_LTR_AIC)
```

```
## Start: AIC=26065.53
## temperature_C ~ depth + daynum + year4
##
##
            Df Sum of Sq
                            RSS
                                  AIC
## <none>
                         141687 26066
## - year4
                     101 141788 26070
             1
## - daynum 1
                    1237 142924 26148
## - depth
             1
                  404475 546161 39189
##
## Call:
## lm(formula = temperature_C ~ depth + daynum + year4, data = NTL_LTR_wrangled)
## Coefficients:
## (Intercept)
                      depth
                                  daynum
                                                 year4
      -8.57556
                   -1.94644
                                  0.03978
                                               0.01134
##
# using step function to see which variables should be included
# 10
NTL_Regression_multi <- lm(data = subset(NTL_LTR_wrangled), depth ~ daynum + year4)
summary(NTL Regression multi)
##
## Call:
## lm(formula = depth ~ daynum + year4, data = subset(NTL_LTR_wrangled))
##
## Residuals:
##
      Min
              10 Median
                            3Q
                                  Max
##
  -4.816 -2.734 -0.295 2.208 11.318
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.9530162 7.4913761
                                      -0.394
                                                 0.693
                                      -0.096
                                                 0.923
## daynum
               -0.0003614 0.0037471
## year4
                0.0038870 0.0037313
                                        1.042
                                                 0.298
##
## Residual standard error: 3.313 on 9725 degrees of freedom
## Multiple R-squared: 0.0001124, Adjusted R-squared:
## F-statistic: 0.5468 on 2 and 9725 DF, p-value: 0.5788
# runnign a multiple regression model
```

11. What is the final set of explanatory variables that the AIC method suggests we use to predict temperature in our multiple regression? How much of the observed variance does this model explain? Is this an improvement over the model using only depth as the explanatory variable?

Answer: The final set of explanatory variables is depth, daynum, and year 4 The model explains 74.12% of the observed variance, this is an improvement of the previous model.

Analysis of Variance

12. Now we want to see whether the different lakes have, on average, different temperatures in the month of July. Run an ANOVA test to complete this analysis. (No need to test assumptions of normality

or similar variances.) Create two sets of models: one expressed as an ANOVA models and another expressed as a linear model (as done in our lessons).

```
NTL_anova <- aov(data = NTL_LTR_wrangled, temperature_C ~ lakename)</pre>
summary(NTL anova)
##
                Df Sum Sq Mean Sq F value Pr(>F)
## lakename
                  8 21642 2705.2
                                       50 <2e-16 ***
## Residuals
               9719 525813
                              54.1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# running an anova model
NTL_LM <- lm(data = NTL_LTR_wrangled, temperature_C ~ lakename)
summary(NTL_LM)
##
## lm(formula = temperature_C ~ lakename, data = NTL_LTR_wrangled)
##
## Residuals:
##
      Min
               10 Median
                                30
                                       Max
## -10.769 -6.614 -2.679
                                    23.832
                            7.684
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            17.6664
                                         0.6501 27.174 < 2e-16 ***
## lakenameCrampton Lake
                            -2.3145
                                         0.7699 -3.006 0.002653 **
## lakenameEast Long Lake
                             -7.3987
                                         0.6918 -10.695 < 2e-16 ***
## lakenameHummingbird Lake -6.8931
                                         0.9429
                                                -7.311 2.87e-13 ***
## lakenamePaul Lake
                            -3.8522
                                         0.6656
                                                -5.788 7.36e-09 ***
## lakenamePeter Lake
                            -4.3501
                                         0.6645
                                                -6.547 6.17e-11 ***
## lakenameTuesday Lake
                            -6.5972
                                         0.6769
                                                -9.746 < 2e-16 ***
## lakenameWard Lake
                             -3.2078
                                         0.9429
                                                -3.402 0.000672 ***
## lakenameWest Long Lake
                            -6.0878
                                         0.6895
                                                -8.829 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.355 on 9719 degrees of freedom
## Multiple R-squared: 0.03953,
                                    Adjusted R-squared: 0.03874
                  50 on 8 and 9719 DF, p-value: < 2.2e-16
## F-statistic:
# running an lm model
```

13. Is there a significant difference in mean temperature among the lakes? Report your findings.

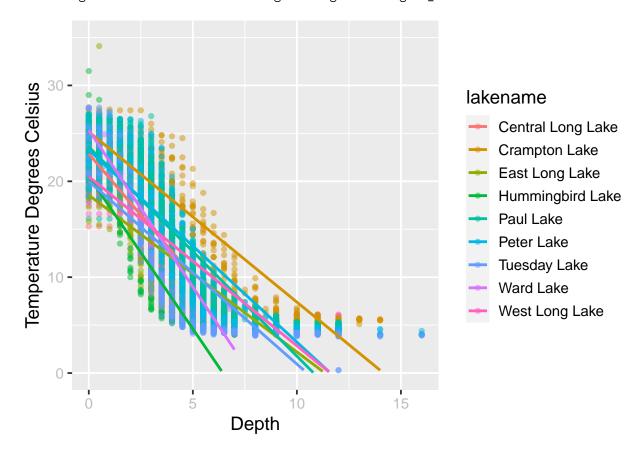
Answer: Yes there is a significant difference, since the P value is less than $2e^-16$. The observed variance explained by the model is about 4%

14. Create a graph that depicts temperature by depth, with a separate color for each lake. Add a geom_smooth (method = "lm", se = FALSE) for each lake. Make your points 50 % transparent. Adjust your y axis limits to go from 0 to 35 degrees. Clean up your graph to make it pretty.

```
aes(color = lakename)) + xlab("Depth") + ylab("Temperature Degrees Celsius")
print(NTL_LTR_plot2)
```

`geom_smooth()` using formula 'y ~ x'

Warning: Removed 73 rows containing missing values (geom_smooth).



creating the second plot with variables differentiated by lakename and with
multiple lines of regression

15. Use the Tukey's HSD test to determine which lakes have different means.

15 TukeyHSD(NTL_anova)

```
Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
##
## Fit: aov(formula = temperature_C ~ lakename, data = NTL_LTR_wrangled)
##
## $lakename
##
                                            diff
                                                        lwr
                                                                    upr
                                      -2.3145195 -4.7031913 0.0741524 0.0661566
## Crampton Lake-Central Long Lake
## East Long Lake-Central Long Lake
                                      -7.3987410 -9.5449411 -5.2525408 0.0000000
## Hummingbird Lake-Central Long Lake -6.8931304 -9.8184178 -3.9678430 0.0000000
## Paul Lake-Central Long Lake
                                      -3.8521506 -5.9170942 -1.7872070 0.0000003
                                      -4.3501458 -6.4115874 -2.2887042 0.0000000
## Peter Lake-Central Long Lake
```

```
## Tuesday Lake-Central Long Lake
                                      -6.5971805 -8.6971605 -4.4972005 0.0000000
## Ward Lake-Central Long Lake
                                      -3.2077856 -6.1330730 -0.2824982 0.0193405
## West Long Lake-Central Long Lake
                                      -6.0877513 -8.2268550 -3.9486475 0.0000000
## East Long Lake-Crampton Lake
                                      -5.0842215 -6.5591700 -3.6092730 0.0000000
## Hummingbird Lake-Crampton Lake
                                      -4.5786109 -7.0538088 -2.1034131 0.0000004
## Paul Lake-Crampton Lake
                                      -1.5376312 -2.8916215 -0.1836408 0.0127491
## Peter Lake-Crampton Lake
                                      -2.0356263 -3.3842699 -0.6869828 0.0000999
## Tuesday Lake-Crampton Lake
                                      -4.2826611 -5.6895065 -2.8758157 0.0000000
## Ward Lake-Crampton Lake
                                      -0.8932661 -3.3684639 1.5819317 0.9714459
## West Long Lake-Crampton Lake
                                      -3.7732318 -5.2378351 -2.3086285 0.0000000
## Hummingbird Lake-East Long Lake
                                       0.5056106 -1.7364925
                                                             2.7477137 0.9988050
## Paul Lake-East Long Lake
                                       3.5465903 2.6900206
                                                             4.4031601 0.0000000
## Peter Lake-East Long Lake
                                       3.0485952 2.2005025
                                                             3.8966879 0.0000000
## Tuesday Lake-East Long Lake
                                       0.8015604 -0.1363286
                                                             1.7394495 0.1657485
## Ward Lake-East Long Lake
                                                 1.9488523
                                                             6.4330585 0.0000002
                                       4.1909554
## West Long Lake-East Long Lake
                                       1.3109897
                                                  0.2885003
                                                             2.3334791 0.0022805
## Paul Lake-Hummingbird Lake
                                       3.0409798 0.8765299
                                                             5.2054296 0.0004495
## Peter Lake-Hummingbird Lake
                                       2.5429846 0.3818755
                                                             4.7040937 0.0080666
## Tuesday Lake-Hummingbird Lake
                                       0.2959499 -1.9019508
                                                             2.4938505 0.9999752
## Ward Lake-Hummingbird Lake
                                       3.6853448 0.6889874
                                                             6.6817022 0.0043297
## West Long Lake-Hummingbird Lake
                                       0.8053791 -1.4299320
                                                             3.0406903 0.9717297
## Peter Lake-Paul Lake
                                      -0.4979952 -1.1120620 0.1160717 0.2241586
## Tuesday Lake-Paul Lake
                                      -2.7450299 -3.4781416 -2.0119182 0.0000000
## Ward Lake-Paul Lake
                                      0.6443651 -1.5200848 2.8088149 0.9916978
## West Long Lake-Paul Lake
                                      -2.2356007 -3.0742314 -1.3969699 0.0000000
## Tuesday Lake-Peter Lake
                                      -2.2470347 -2.9702236 -1.5238458 0.0000000
## Ward Lake-Peter Lake
                                      1.1423602 -1.0187489 3.3034693 0.7827037
## West Long Lake-Peter Lake
                                      -1.7376055 -2.5675759 -0.9076350 0.0000000
## Ward Lake-Tuesday Lake
                                       3.3893950 1.1914943 5.5872956 0.0000609
## West Long Lake-Tuesday Lake
                                      0.5094292 -0.4121051 1.4309636 0.7374387
## West Long Lake-Ward Lake
                                      -2.8799657 -5.1152769 -0.6446546 0.0021080
NTL_LTR_HSD <- HSD.test(NTL_anova, "lakename", group = TRUE)</pre>
NTL_LTR_HSD
## $statistics
##
     MSerror
              Df
                                 CV
                     Mean
##
     54.1016 9719 12.72087 57.82135
##
## $parameters
##
             name.t ntr StudentizedRange alpha
                                4.387504 0.05
##
     Tukey lakename
##
## $means
##
                     temperature C
                                                             Q25
                                                                   Q50
                                                                          Q75
                                        std
                                               r Min Max
                          17.66641 4.196292
                                            128 8.9 26.8 14.400 18.40 21.000
## Central Long Lake
## Crampton Lake
                          15.35189 7.244773 318 5.0 27.5 7.525 16.90 22.300
## East Long Lake
                          10.26767 6.766804 968 4.2 34.1
                                                          4.975 6.50 15.925
## Hummingbird Lake
                          10.77328 7.017845 116 4.0 31.5
                                                          5.200 7.00 15.625
## Paul Lake
                          13.81426 7.296928 2660 4.7 27.7
                                                          6.500 12.40 21.400
## Peter Lake
                          13.31626 7.669758 2872 4.0 27.0 5.600 11.40 21.500
                         11.06923 7.698687 1524 0.3 27.7
## Tuesday Lake
                                                           4.400 6.80 19.400
## Ward Lake
                          14.45862 7.409079 116 5.7 27.6
                                                          7.200 12.55 23.200
                         11.57865 6.980789 1026 4.0 25.7 5.400 8.00 18.800
## West Long Lake
```

##

```
## $comparison
## NULL
##
## $groups
##
                      temperature_C groups
## Central Long Lake
                           17.66641
## Crampton Lake
                           15.35189
                                         ab
## Ward Lake
                           14.45862
                                         bc
## Paul Lake
                           13.81426
                                          c.
## Peter Lake
                           13.31626
                                          С
## West Long Lake
                           11.57865
                                          d
## Tuesday Lake
                           11.06923
                                         de
## Hummingbird Lake
                           10.77328
                                         de
## East Long Lake
                           10.26767
                                          е
##
## attr(,"class")
## [1] "group"
# running the tukey hsd test
```

16. From the findings above, which lakes have the same mean temperature, statistically speaking, as Peter Lake? Does any lake have a mean temperature that is statistically distinct from all the other lakes?

Answer:Peter and Ward lakes have a P value of .78 and Peter and Paul lakes have a P value of .224, meaning they are statistically similar. No lake had a mean temperature that was statistically distinct from all the other lakes

17. If we were just looking at Peter Lake and Paul Lake. What's another test we might explore to see whether they have distinct mean temperatures?

Answer: Since we would only have two variables for Peter and Paul lake we could do a two sample ${\mathcal T}$ test .

18. Wrangle the July data to include only records for Crampton Lake and Ward Lake. Run the two-sample T-test on these data to determine whether their July temperature are same or different. What does the test say? Are the mean temperatures for the lakes equal? Does that match you answer for part 16?

```
NTL_LTR_finalwrangle <- NTL_LTR_wrangled %>%
    filter(lakename == "Crampton Lake" | lakename == "Ward Lake") %>%
    select("lakename", "year4", "daynum", "depth", "temperature_C")
# wrangling the data to just be for Crampton and Ward lake
t.test(NTL_LTR_finalwrangle$temperature_C ~ NTL_LTR_finalwrangle$lakename, alternative = "two.sided")
##
##
   Welch Two Sample t-test
##
## data: NTL_LTR_finalwrangle$temperature_C by NTL_LTR_finalwrangle$lakename
## t = 1.1181, df = 200.37, p-value = 0.2649
## alternative hypothesis: true difference in means between group Crampton Lake and group Ward Lake is:
## 95 percent confidence interval:
## -0.6821129 2.4686451
## sample estimates:
## mean in group Crampton Lake
                                   mean in group Ward Lake
                      15.35189
                                                  14.45862
# running the two sided t.test
```

Answer: The mean temperatures for the lake are not equal, the test says the P value between

Crampton and Ward is .2649 This does not match what we found in question 16 since the Tukey test provided us with an adjusted P value.