

$$2) a) H(X|X) = - \sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) p(x|y) \log p(x|y) = 0$$

$\uparrow \quad \uparrow$   
 $= 0$

$p(x|y)$  : probability of  $x$  given  $y$  is 1

$$H(X|X) = 0$$

when the two random variable under comparison is the same, then there is no extra information required for communicating  $Y$  given  $X$ .

b)  $I(X; Y)$  = mutual information. = how much reduction in uncertainty given info about  $Y$

$$I(X; Y) = H(X) - H(X|Y)$$

If  $X$  &  $Y$  are independent then  $H(X|Y) = H(X)$

$\therefore$  having the additional info ~~from~~ ~~the~~ given  $Y$  will not provide you with any additional info

$$I(X; Y) = H(X) - H(X) = 0 \quad \text{i.f.f. } X, Y \text{ independent}$$

$$3) a) p(X_A=0, X_B=1) = \frac{N_B - N_{AB}}{N}$$

$$p(X_A=0, X_B=0) = \frac{N - (N_A + N_B - N_{AB})}{N} = \frac{N - N_A - N_B + N_{AB}}{N}$$

