

SAT Solving with distributed local search

Master Thesis of

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Abstract

Stochastic local search (SLS) is an elementary technique for solving combinational problems. Probsat is an algorithm paradigm of the simplest SLS solvers for Boolean Satisfiability Problem (SAT), in which the decisions only based on the probability distribution. In the first section of this paper, we introduce an efficient Probsat heuristic. We experimentally evaluate and analyze the performance of our solver in a combination of different techniques, including simulated annealing and WalkSAT. With the approach of formula partition, we introduce a parallel version of our solver in the second section. The parallelism improves the Efficiency of the solver. Using different random generator and other parameter settings in solving the sub-formula can bring further improvement in performance to our parallel solver.

Zusammenfassung

Stochastische lokale Suche (SLS) stellt eine elementare Technik zur Lösung von komplizierten kombinatorischen Problemen dar. Probsat ist einer der einfachsten SLS-Solver für das Erfüllbarkeitsproblem der Aussagenlogik (SAT), bei dem die Entscheidungen nur auf der Wahrscheinlichkeitsverteilung basieren. Im ersten Teil dieser Arbeit stellen wir eine effiziente Probsat-basierte Heuristik vor. Die Leistung unseres Algorithmus in einer Kombination verschiedener Techniken, einschließlich simulierter Abkühlung und WalkSAT wurde auch experimentell bewertet und analysiert. Mit dem Ansatz der Formelpartition wird im zweiten Teil eine parallele Version unseres Algorithmus eingeführt, die die Effizienz des Löses verbessert. Die flexible Parametereinstellungen bei der Lösung der Teil-formeln kann eine weitere Verbesserung unseres Algorithmus bringen.

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1 Introduction

1.1 Problem/Motivation

The *propositional satisfiability problem* (*SAT*) is the first proven NP-complete problem [1]. The problem is to determine whether an assignment of Boolean values to variables in a Boolean formula such that the expression evaluates to true. Hard combinational problems can be resolved with appropriate Encoding as a sat problem. The SAT problem has many applications in computer science like chip model checking [2], software verification [3] or in automated planning and scheduling in artificial intelligence [4]. Formula partition is one of the promising approaches in DPLL-like solvers [5]. By giving the order to the variables according to a good formula partition, the search gets a relatively balanced decision tree. But formula partition is rarely used in a local search for the SAT problem. How to combine the formula partition with local search, will the local search benefit from the partitioning, if the formula partitioning can guide a parallel local search, are still open questions.

1.2 Content

The SAT problem, as a well-known NP-complete problem, has received a great deal of attention and different local search heuristics have been developed. This paper is a survey on the stochastic local search on SAT problem with a guide of formula partition.

In section 1, we summarize the formal concept and introduces techniques used in this paper. One class of the most straightforward but efficient stochastic local search algorithms Probsat is the algorithm basic in our paper. Probsat was proposed in 2012 by Adrian Balint and Uwe Schoening [6]. Section 2 describes our Probsat algorithm and discusses our attempts to improve the original algorithm. By experimentally evaluation and comparison, some techniques turned out to be more efficient than the simple Probsat search. With the partition of variables and its corresponding formulas, the problem can be separated into two subproblems of similar size. In section 3, we search the potential benefit of formula partition in a parallel search. Section 4 describes the details in experiments and several empiric results mentioned in section 2 and section 3. Section 5 concludes the paper with further works.

1.3 Definitions and Notations

Propositional Satisfiability Problem

A variable with two possible logical values *TRUE* or *False* is a *propositional variable*, which will be referred to as *variable* in this paper. A *literal* is an atomic formula in propositional logic. A literal can either be a *positive literal* v as the variable v or a *negative literal* \bar{v} as negation of v . A *clause* is a disjunction of literals. A formula in conjunctive normal form (CNF) is a conjunction of clauses. We refer it as *CNF-formula* or simply as *formula* in this paper. An *assignment* a as a function $a: V \rightarrow \{True, False\}$ assigns the truth value to each variable v in the formula. We say the assignment satisfies a formula if the truth value of the formula with this assignment turns out to be true. Specifically, an assignment satisfies a clause, if one literal in the clause with value *True* in this assignment. A formula is a satisfying formula if one assignment exists satisfies all its clauses. We say an assignment a satisfying assignment if it satisfies the formula. Otherwise, we say there are conflicts in some clauses with this assignment, or some clauses are unsatisfying clauses with this assignment. The SAT

problem is to determine whether a satisfying assignment exists for the given formula. If so, we denote the formula a *satisfiable formula*.

Set

A set is a container of unique elements. A set of 3 objects a, b, c is written as $\{a, b, c\}$. The size of a set is the number of elements in the set.

Local Search

For instance I of a hard combinatorial Problem P , there is a set of solutions S . According to the constraints of the problem, an object function (score or cost) Γ is used to evaluate the candidate solutions. The Goal of the local search is to find the solution of minimum cost (or the solution with the maximal score).

A local search starts with an initial complete solution. According to some heuristic, the local search makes local changes to its current solution iteratively, hence the name *local search*. Starts from an initial solution, the search will evaluate the solutions which can be reached by applying a local change to the current solution and choose one of the neighbor solutions with local optimization. The search applies local moves until the optimal solution is reached, or in some cases, a generally good solution is reached. Local search is widely used in hard combinatorial problems such as the traveling salesman problem [13] and the graph coloring problem [14].

Local Search in SAT Problem

In the Boolean satisfiability problem, a local search operates primarily as follows: The search start from a randomly generated assignment as the initial solution. If this current assignment satisfied the formula, the search stops with success. Otherwise, a variable is chosen depends on some criterion. This selection is called *pickVar*. By change the assignment of the selected variable v , a neighbor assignment of our current solution A is reached in next step, which is also called *flip*(A, v). A local search will move in the space of the assignments by making the variable flipping until a satisfying assignment is reached by the search.

The heuristic used for the flipping variable selection *pickVar* is based on some scores of the variables in the current assignment. Consider the assignment \hat{A} reached by taking a flip of the variable in the current assignment A . The number of clauses satisfied in A , but not in \hat{A} is called the *breakcount* of the local move from A to \hat{A} . Accordingly, the number of clauses, which become satisfying because of the flipping, is the *makecount*. The number of newly satisfying clauses (*makecount*) minus the number of newly unsatisfying clauses (*breakcount*), which is denoted as *diffscore*, represents the local improvement of the corresponding flipping. Apart from this, other aspects like the repetition number of one flip or the number of occurrences of the variables can be considered in a selection heuristic. An example is the unit propagation embedded local solver *EagleUp*, which prefers flipping of variables with the highest number of occurrences in a formula to creates new unit clauses sooner. To get local improvement effectively, man can only consider variables in unsat clauses for the flipping selection. This process is called a *focused local search* and commonly used.

Algorithm 1: Focused Local Search

```

input      : A CNF Formula F
parameter: Timeout
output     : a satisfying assignment A
1 A  $\leftarrow$  random generated assignment A;
2 while ( $\exists$  unsatisfied clause  $\wedge$  Timeout does not occur) do
3   c  $\leftarrow$  random selected unsatisfied clause ;
4   x  $\leftarrow$  pickVar(A, c)
5   A  $\leftarrow$  flip(A, x);

```

By choosing the variable with best score in *pickVal*, the search will get greedy local improvement. The initial hope of the local search is that through iterative greedy local improvement the optimal global solution can be found. The typical problem of the local search is that the greedy local searches be trapped in local unattractive local optimal solution. To avoid this, some random flips are picked or even a worse solution will be chosen for the next step (***uphill moves***). There are some techniques following used in local search to avoid getting stuck in local optimum.

Stochastic Local Search (SLS)

The stochastic local search will use the probability distribution of the scores of candidate solutions instead of the static decision. For the candidate moves, the probability of being chosen $p(\Gamma(s))$ corresponds to the score $\Gamma(s)$ of the solution s . In this way, the advantage a move is, the probability of choosing it as the next step is higher. This randomization will avoid the stuck of the search in a local minimum and decrease the misleading of the heuristic in specific situations.

Tabu Local Search

Tabu search is created by Fred W. Glover in 1986 [15] and formalized in 1989. For recognize the loop in a suboptimal region, the search trace is recorded in the process by mark the recently reached neighboring assignments as tabu. The tabu moves will not be touched in the further search to discourage getting stuck in a region.

Simulated Annealing

Simulated Annealing is an approach of local search solver to difficult combinatorial optimization problems proposed by Kirkpatrick, Gelatt, and Vecchi [7]. This approach is inspired by the metallic process annealing of shaping the material by heating and then slowly cooling the material. This approach works as a local optimization algorithm guided by a controlling parameter ***temperature***. By high temperature, an uphill move is allowed with high probability while only small steps are allowed in low temperature. The temperature is varying according to the score of the current situation. For a current solution with a nearly optimal score, the temperature is near zero. For an unattractive local extreme with a poor score, the active search is tending to make uphill moves in high temperature.

WalkSAT

WalkSAT is a focused random local search strategy to solve SAT problem, which is originally introduced in 1994 [8]

. WALKsat may ignore the greedy flipping and flip a random variable in chosen unsatisfied clause with probability p . By introducing these "uphill noises", the WalkSAT combines greedy local search and random walk to get an effective and robust random solver.

Algorithm 2: pickVar in WalkSAT

input : current assignment A , unsatisfied clause c
parameter: probability p
output : a variable x in c for flipping
1 **for** v *in* c **do**
2 | Evaluate v with function $\Gamma(A, v)$;
3 with probability p : $x \leftarrow v$ with maximum $\Gamma(A, v)$;
4 with probability $1 - p$: $x \leftarrow$ randomly selected v in c .

The Probsat

Probsat is a class of SLS sat solver, which was introduced in 2012 by Adrian Balint and Uwe Schoening [6]. In a probsat solver, the score of a candidate flip is solely based on the make and break score. The paradigm is as follows: At first, a completely random assignment is set as the initial assignment. The algorithm performs local moves by flip a variable in a random chosen unsatisfying clause and stops as soon as there are no unsatisfied clauses exists, which means a satisfying assignment is found. The probability $p(v)$ of flipping the variable v in the chosen clause proportionate to the score of v , which is calculated in a function $\Gamma(v, A)$ based on break score of v in the current assignment A .¹ The idea behind this selection heuristic is to give the advantageous flipping relative high score, but the other flipping with small score has chance to be chosen. There are two kinds of score functions are considered in the paper of Adrian Balint:

$$\Gamma(v, A) = (c_b)^{break(v, A)} \text{ (break-only-exp-function)}$$

$$\Gamma(v, A) = (\epsilon + break(v, A))^{-c_b} \text{ (break-only-poly-function)}$$

The pseudo code of a typical Probsat is shown below:

Algorithm 3: pickVar in probSAT

input : current assignment A , unsatisfied clause c
output : a variable x in c for flipping
1 **for** v *in* c **do**
2 | Evaluate v with function $\Gamma(A, v)$;
3 $x \leftarrow$ randomly selected variable v in c with probability $p(v) = \frac{\Gamma(A, v)}{\sum_{u \in c} \Gamma(A, u)}$;

1.4 The Competitors

Our heuristic is based on the probSAT paradigm. To evaluate the performance of our algorithm, we compare our heuristic with the original ProbSAT. Another random SAT solver used for a comparison with our algorithm is yalSAT, which is the champion in random track category in SAT competition 2017 [9].

probSAT²

The authors of the original Paper implement the ProbSAT. We compare our Solver with this original code³.

¹As mentioned in the probsat paper, it turns out in experiments that the influence of make is rather weak in selection functions, so the one parameter functions depends on *breakScore* can also lead to an efficient algorithm.

²<https://github.com/adrianopolus/probSAT>

³Using same parameter settings our implementation gets similar performance to the original code

In this original code, there are two implementation variants available. In the incremental approach, the breakScores of variables are calculated in the initialization phase and only updated in the further search. The other straightforward approach is to compute breakScores of the variables in consideration of flipping. This method is called non-incremental approach in original paper. As suggested in Experiments, we take the non-incremental approach for the 3SAT problems and incremental method for 5SAT and 7SAT to get optimal results of the probSAT solver.

The parameters of ProbSAT in our Experiments have been set as suggested in the original paper:

k SAT ^a	score Γ	c_b	ϵ	variants
3SAT	break-only-poly	2.06	0.9	non-incremental
5SAT	break-only-exp	3.7	-	incremental
7SAT	break-only-exp	5.4	-	incremental

Table 1: Parameter setting for competitor probSAT

^ak is the maximum length of the clause

yalSAT⁴

We use the version 03 submitted to the 2017 SAT competition of the yalSAT solver in our experiments. Armin Biere implements it as a reimplement with extensions of probSAT. With the implementation of different variants of probSAT, the yalSAT uses a different variant of probSAT randomly in the restart of a round of search. In our comparison, we use the default settings of the yalSAT with specific seeds.

⁴<https://baldur.iti.kit.edu/sat-competition-2017/solvers/random/>

2 Our local Solver

Our algorithm is a typical focused SLS algorithm, which solves the SAT problem with the basic shema:

Algorithm 4: Our Local Search

```

input      : A CNF Formula F
parameter: Timeout
output     : a satisfying assignment A
1 A  $\leftarrow$  initAssign(F)
2 while ( $\exists$  unsatisfied clause  $\wedge$  Timeout does not occur) do
3   c  $\leftarrow$  pickCla(A) ;
4   x  $\leftarrow$  pickVar(A, c)
5   A  $\leftarrow$  flip(A, x);

```

In the following, we will describe the methods used in our local search.

2.1 *initAssign*(F)

In our algorithm, we have three variants to make assignment initialization. One is the *RandomInit* which is the random initiation like in the original probsat suggests. Two alternatives to this random assignment are with the consideration of number of literal occurrences. with the method *BiasInit* we assign *True* to a variable if the number of occurrences of its positive literal is more than its negative literal. Otherwise, a variable is assigned initially with *False*. *Bias – RandomInit* combines the two initializations above, in which the assignment is generated bias randomly based on the occurrences of literals. In Experiment 1 we compare these three alternatives based on the probsat algorithm. Our local search uses *RandomInit* for 3SAT problems and *BiasInit* for other problems.

2.2 *pickCla*(A)

$numT(c)$, the number of *True* values in each clause *c*, are counted in Initilization phase and maintained in further search. The unsatisfying clauses will be cached in a set *UNSAT*. During the local flipping, these numbers will be updated when the flipping variable is in the clauses. Comparing to the $numT$, the *UNSAT* is updated lazily. After Flipping, if the $numT$ of one clause is decreased to zero, it will be added in the *UNSAT*. To select an unsat clause in *pickCla*(*A*), man needs to select a clause from the *UNSAT* and Ocheck if it is still unsat with its $numT$ is zero. Otherwise, if the chosen clause *c* with $numT(c)$ as zero, it will be removed from the *UNSAT* set. This step *pickCla*(*A*) will be repeated until one unsatisfied clause is found or the *UNSAT* set is empty, which means the current Assignment *A* is a satisfying assignment.

2.3 pickVar(A,c)

Inspired by probSAT and walkSAT, Our pickVar combines the random walk and stochastic selection. We analyze experimentally the following variants for *pickVar*.

1. *Varinat: COMBINE*

In observation of the experiments of the probSAT, this stochastic search bases its selection on a random heuristic. Even the search is very close to a satisfying assignment, and the probability of the critical flipping is exceptionally high, it is possible that the stochastic search make uphill moves and leave then the region of the global minimum. To prevent this besides the stochastic way, we pick greedy flip with zero *breakScore* with a certain probability p . With probability $1 - p$, we choose the variable for flipping using the probSAT heuristic.

Algorithm 5: COMBINE

input : current assignment A , unsatisfied clause c
parameter: probability p
output : a variable x in c for flipping

- 1 greedyVs $\leftarrow \emptyset$;
- 2 for all v in c do
- 3 if ($break(A,v) = 0 \wedge Permit(v)$) then
- 4 greedyVs = greedyVs + $\{v\}$
- 5 with probability p : $x \leftarrow$ randomly selected variable $v \in$ greedyVs;
- 6 with probability $1 - p$: $x \leftarrow$ randomly selected variable v in c with probability $\frac{\Gamma(A,v)}{\sum_{u \in c} \Gamma(A,u)}$;

2. *Varinat: WALK*

Instead of using a constant probability p to choose between a greedy Literal without clause break and the random Literal using probSAT flipping directly, we see a list, called statistic list S to record how many times each variable is chosen for flipping. To avoid cycling, we see the variable v_i with a high value of $S[i]$ to be disadvantages for flipping. After selecting a variable using the ProbSAT stochastic distribution, we make the choice randomly according to the statistic values of these two variables.

Algorithm 6: WALK

input : current assignment A , unsatisfied clause c
parameter: probability p
output : a variable x in c for flipping

- 1 greedyVs $\leftarrow \emptyset$;
- 2 for all v in c do
- 3 if ($break(A,v) = 0 \wedge Permit(v)$) then
- 4 greedyVs = greedyVs + $\{v\}$
- 5 $greedyV \leftarrow$ randomly selected variable $v \in$ greedyVs ;
- 6 $randomV \leftarrow$ randomly selected variable v in c with probability $\frac{\Gamma(A,v)}{\sum_{u \in c} \Gamma(A,u)}$;
- 7 with probability $p = \frac{s(greedyV)}{s(greedyV) + s(randomV)}$: $x \leftarrow$ randomV;
- 8 with probability $1 - p$: $x \leftarrow$ greedyV;

3. Varinat: TieBreak**Algorithm 7: TieBreak**

```

input      : current assignment  $A$ , unsatisfied clause  $c$ 
parameter: probability  $p$ 
output     : a variable  $x$  in  $c$  for flipping
1 greedyVs  $\leftarrow \emptyset$ ;
2 for all  $v$  in  $c$  do
3   if ( $break(A,v) = 0 \wedge Permit(v)$ ) then
4     greedyVs = greedyVs +  $\{v\}$ 
5 if ( $greedyVs$  is not empty) then
6    $x \leftarrow$  selected variable  $v$  in  $greedyVs$  at random
7 else
8    $x \leftarrow$  randomly selected variable  $v$  in  $c$  with probability  $\frac{\Gamma(A,v)}{\sum_{u \in c} \Gamma(A,u)}$ ;
9
```

2.4 Simulated Annealing**2.5 Data structures*****Occurrences***

In the process of initialization, the numbers of occurrences of one variable will be compared. In our implementation, we use a list to count and record these occurrences numbers. This list with size of $2 * numClauses$ is denoted as Occurrences List OL. For the variable with index i , the $OL[2i]$ is the number of literal vs occurrences; The $OL[2i+1]$ is for its negative occurrences.

Literals

Local search is a search where only small changes are made in each step. In our Situation, only the clauses include the flipping variables are involved in the flipping step. The most time in our solver is spent to update the $numTs$ of these involving clauses. To find the involving clauses of one Variable, two 2D Array $posL$ and $negL$ is made to record the clauses of positive and negative literals. For variable v_i , the $posL[i]$ record the indexes of clauses containing the positive literal v_i . The ones with negative literal $-v_i$ are in by $negL[i]$. To implement the flipping of the variable v_i , we update the $numTs$ of clauses with indexes in $posL[i]$ and $negL[i]$.

LookUp

The most time used in the search is the repeated calculation of the polynomial or exponential decay function Γ . With this observation in our experiments, we calculate the $\Gamma(x)$ with x from 0 to $0.5 * numCs$ and keep the value in a list *LookUp*. In our implementation, we use this Table lookup to get the values instead of the reputation of time-consuming exponential operation.

Solution

A Solution in our implementation includes the boolean Assignment and three other structures to record information about the current assignment. The Solution is computed after assignment initialization and is updated during each flipping :

Name	Structure	Size	Meaning
<i>Assignment</i>	list	numVs	boolean assignment to variables
<i>NumTs</i>	list	numCs	number of <i>True</i> values in each clause
<i>NumUnsat</i>	natural number	-	the number of unsatisfied clauses
<i>UNSAT</i>	set	-	indexes of unsatisfied clauses ^a

Table 2: Parameter setting for competitor probSAT

^aThis UNSAT is updated in flipping phase lazily by only adding new unsatisfied clauses and remove the clause chosen in *pickCla*.

3 Our Parallel Algorithm

3.1 1st Approach: The pure portfolio approach (no partition)

3.2 2nd Approach: Star

3.3 3rd Approach: Hope

3.4 4th Approach: future

4 Evaluation

4.1 DIMACS standard format

All the benchmark CNF formula used in experiments are encoded in the DIMACS standard format [?]. This format is used to test and compare SAT solver in SAT competition. A DIMACS file contains the description of an instance using three types of lines⁵:

1. Comment line: Comment lines give information about the graph for human readers, like the author of the file or the seed used in generation. A comment line starts with a lower-case character *c* and will be ignored by programs:

c this is an example of the comment line

2. Problem line: The problem line appears exactly once in each DIMACS format file. The problem line is signified by a lower-case character *p*. For a formula with nV variables and nC clauses ,the problem line in its DIMACS file is:

p cnf nV nC

3. Clause Descriptor: An clause $\{v_1, v_2, , v_n\}$ in the graph is described in an edge Descriptor:

e v_1 v_2 v_n

⁵Only clause unweighted simple instances are tested in our experiments. For other descriptors and details of the DIMACS format

```
c This is a DIMACS file of the graph in Figure 6
p edge 7 11
e 1 3
e 1 2
e 2 7
e 2 6
e 1 6
e 1 4
e 1 5
e 4 5
e 3 5
e 5 6
e 6 7
```

Figure 1: A DIMACS file example of the problem in Figure ??

4.2 Benchmarks

The benchmark instances used in experiments are the 180 uniform instances (unif) in random benchmark categories in SAT competition 2017 [10]. In an unif problem file, all the clause have the same length. The suffix 'k' denotes the length of clauses. The r indicates the clause-to-variable ratio. The c and v are for the number of clauses and variables, while s is for the seed used in the generation process. Without filtering, there are at least 60 (33%) problems from our 180 benchmark collections are unsatisfiable.

4.3 Used plots and tables

the results of the following experiments are all shown in comparison table and illustrated in cactus plot.

Comparison Table

See Table ?? for example.

A comparison table compares the performance of different algorithms. The first column contains the 2-factor penalized runtime ⁶ of solving a set of benchmark problems. The fields of a comparison table in the following columns corresponds to the coloring sizes found with an algorithm.

Cactus Plot

See Figure ?? for an example.

A cactus plot shows the performance of different algorithms. The y-axis shows the time in second used to solve the benchmark graphs. The x-axis is for the number of solved problems by a certain time. Each algorithm corresponds to a curve in different colors. The point (u, v) on a curve means by v seconds the corresponding algorithm have solved u problems.

⁶Not like the PAR-2 scheme in SAT competition, we only assign a 2-factor time limit penalization for each unsolved benchmark which has been solved by another solver in the comparison.

4.4 Random seeds used in Experiments

To make our experiments results reproducible and robust, we repeat our tests with three specific seeds. We produce the seeds in experiments as follows: First, we use the sum of characters of the name of the solver to seed the pseudo-random generator in c++. Then we use this reinitialized generator to produce three random values, which are the seeds used later in our experiments.

solver	name	1.seed	2.seed	3.seed
probSAT	probsat	1988822874	338954226	858910419
yalsat	yalsat	1851831967	280788293	1956345180
our local solver	local	1962042455	1112841915	566263966
our parallel solver	parallel	1749729997	68910537	473644167

Table 3: Parameter setting for competitor probSAT

4.5 Automatic parameter optimization

4.6 Experiments

4.6.1 Experiment 1: initAssign(F)

k	<i>RandomInit</i>	<i>BiasInit</i>	<i>Bias-RandomInit</i>
3	11187.15 (112)	11754.82 (109)	11858.93 (110)
5	11006.72 (167)	6023.1(175)	6692.79 (175)
7	5941.4(119)	4097.48 (118)	6387.73 (117)

5 Conclusion

5.1 Further work

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