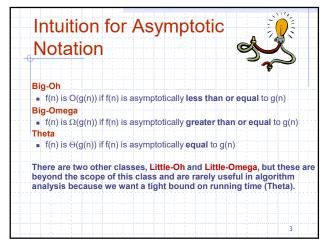
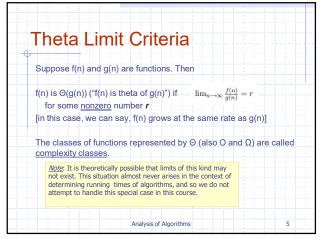
Asymptotic Notation in Practice The fastest algorithm in practice or for practical size input data sets is not always revealed!!! Because Constants are dropped Low-order terms are dropped Algorithm efficiencies on small input sizes are not considered However, asymptotic notation is very effective for comparing the scalability of different algorithms as input sizes become large



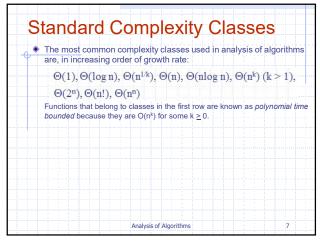


Theta and Big-omega

If f(n) grows at least as fast as g(n), we say f(n) is Ω(g(n)) ("big-omega")

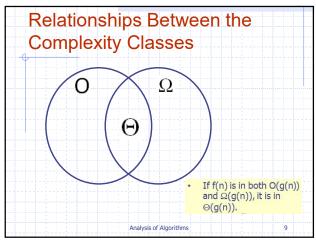
That is, f(n) is Ω(g(n)) if g(n) is O(f(n)).

If f(n) grows at same rate as g(n), we say f(n) is Θ(g(n)) ("theta")



Examples

• Both 2n + 1 and $3n^2$ are $O(n^2)$ • Both $2n^2 + 1$ and $3n^2$ are $O(n^2)$ • Both $2n^2 - 1$ and $4n^3$ are $O(n^2)$



Lecture 2: Stacks, Queues, Lists

Pure Knowledge Has
Infinite Organizing Power

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Wholeness Statement

Knowledge of data structures allows us to pick the most appropriate data structure for any computer task, thereby maximizing efficiency.

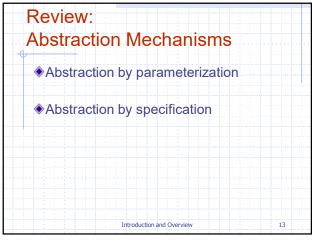
Science of Consciousness: Pure knowledge has infinite organizing power, and administers the whole universe with minimum effort.

Review:
Decomposition & Abstraction

What do we mean by decomposition?

What do we mean by abstraction?

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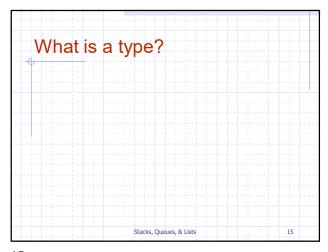


Kinds of Abstractions

1. Procedural abstraction introduces new functions/operations
2. Data abstraction introduces new types of data objects (ADTs)
3. Iteration abstraction allows traversal of the elements in a collection without revealing the details of how the elements are obtained
4. Type hierarchy allows us to create families of related types

All members have data and operations in common that were defined in (inherited from) the supertype

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Algorithms and Data Structures

Closely linked

Algorithm (operation)

a step by step procedure for performing and completing some task in a finite amount of time

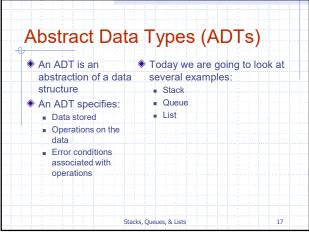
Data structure

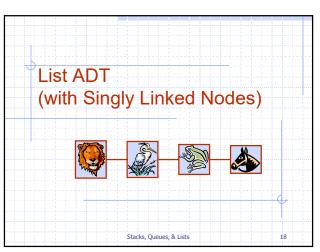
an efficient way of organizing data for storage and access by an algorithm

An ADT provides services to other algorithms

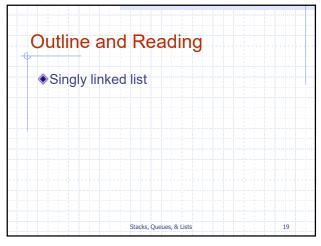
E.g., operations (algorithms) are embedded in the data structure (ADT)

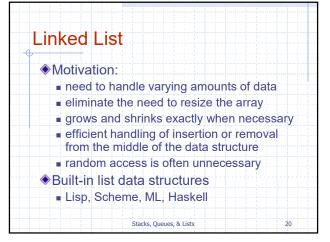
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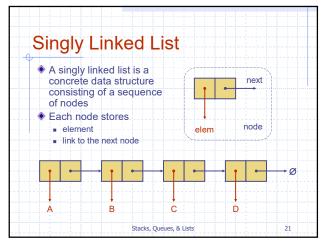


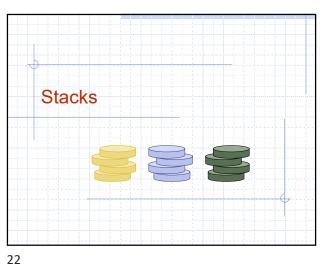
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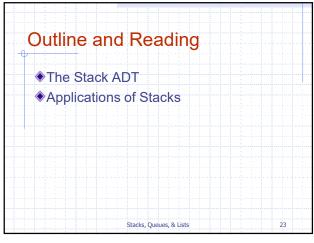


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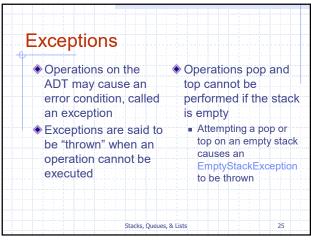


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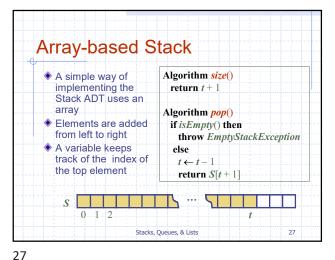
The Stack ADT Auxiliary stack The Stack ADT stores arbitrary objects operations: Insertions and deletions object top(): returns the follow the last-in first-out last inserted element (LIFO) scheme without removing it Like a spring-loaded plate • integer size(): returns the dispenser number of elements Main stack operations: boolean isEmpty(): void push(object): inserts an indicates whether no element object pop(): removes and returns the last inserted elements are stored Stacks, Queues, & Lists

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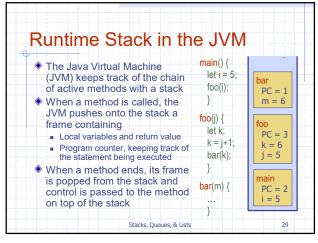
Applications of Stacks Direct applications Page-visited history in a Web browser Undo sequence in a text editor Chain of method calls in the Java Virtual Machine Evaluate an expression Indirect applications Auxiliary data structure for algorithms Component of other data structures Linked List Implementation is straightforward Stacks, Queues, & Lists

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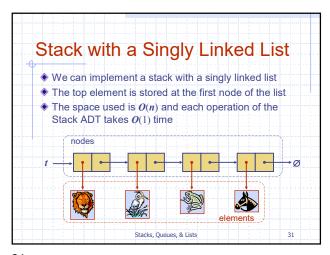


Array-based Stack (cont.) The array storing the stack elements may Algorithm push(o) become full if t = S.length - 1 then A push operation will throw StackFullException then throw a else StackFullException $t \leftarrow t + 1$ Limitation of the arraybased implementation $S[t] \leftarrow o$ Not intrinsic to the Stack ADT Stacks, Queues, & Lists

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Performance and Limitations Performance ■ Let *n* be the number of elements in the stack ■ The space used is O(n)■ Each operation runs in time *O*(1) Limitations ■ The maximum size of the stack must be defined at creation and cannot be changed Trying to push a new element onto a full stack causes an implementation-specific exception Stacks, Queues, & Lists



Main Point

1. Stacks are data structures that allow very specific and orderly insertion, access, and removal of their individual elements, i.e., only the top element can be inserted, accessed, or removed.

Science of Consciousness: The infinite dynamism of the unified field is responsible for the orderly changes that occur continuously throughout creation.

Stacks, Queues, & Lists

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Queues

Outline and Reading

◆The Queue ADT

◆Implementation with a circular array

◆Queue interface in Java

Queue interface in Java

Stacks, Queues, & Lists

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The Queue ADT ♦ The Queue ADT stores arbitrary
♦ Auxiliary queue objects operations: Insertions and deletions follow object front(): returns the the first-in first-out (FIFO) element at the front without removing it Insertions are at the rear of the integer size(): returns the number of elements stored queue and removals are at the boolean isEmpty(): front of the queue indicates whether no Main queue operations: elements are stored ■ void enqueue(object): inserts an ◆ Exceptions element at the end of the queue Attempting the execution of object dequeue(): removes and returns the element at the front remove or front on an empty queue throws an of the queue Stacks, Queues, & Lists

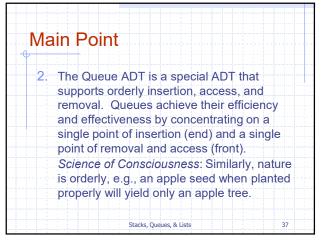
Applications of Queues

Direct applications

Waiting lists, bureaucracy
Access to shared resources (e.g., printer)

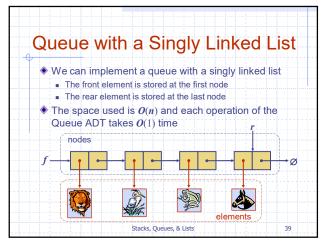
Multiprogramming (OS)
Indirect applications
Auxiliary data structure for algorithms
Component of other data structures

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◆Are there any ADT's that could be implemented efficiently with a linked list?
Stacks, Queues, & Lists
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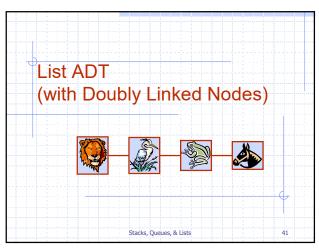
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Queue ADT Implementation

Can be based on either an array or a linked list
Linked List
Implementation is straightforward
Array
Need to maintain pointers to index of front and rear elements
Need to wrap around to the front after repeated insert and remove operations
May have to enlarge the array

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Outline and Reading

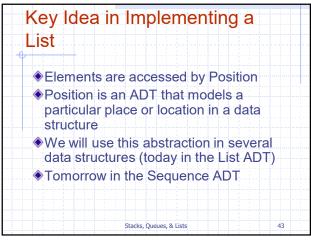
Position ADT and List ADT

Doubly linked list

Stacks, Queues, & Lists

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Position ADT

The Position ADT models the notion of place within a data structure where a single object is stored

It gives a unified view of diverse ways of storing data, such as

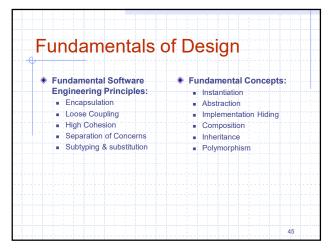
a cell of an array

a node of a linked list or tree

Just one method:

object element(): returns the element stored at the position

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List ADT The List ADT models a Accessor methods: sequence of positions first(), last() storing arbitrary objects before(p), after(p) It establishes a Update methods: before/after relation replaceElement(p, e), between positions swapElements(p, q) insertBefore(p, e), Generic methods: insertAfter(p, e), size(), isEmpty() insertFirst(e). Query methods: insertLast(e) isFirst(p), isLast(p) remove(p) Stacks, Queues, & Lists

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Doubly Linked List

A doubly linked list provides a natural implementation of the List ADT

Nodes implement Position and store:

element

ink to the previous node

link to the next node

Special header and trailer nodes

header

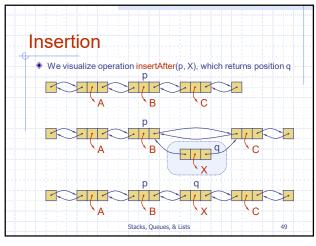
nodes/positions trailer

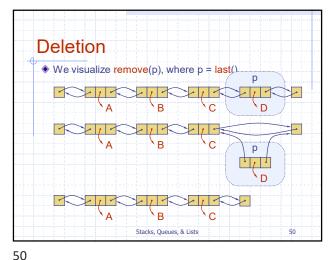
JavaScript Position ADT

class NPos {
#elem;
#prev;
#next;
constructor (elem, prev, next) {
// inserts this new node between prev and next
this #elem = elem;
this #prev = prev;
this #prev = next;
if (prev != null) {
 prev.fmext = this;
}
if (next != null) {
 next.#prev = this;
}
element() {
 return this #elem;
}

Stacks, Queues, & Lists 48

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Performance of Linked List implementation of List ADT Generic methods: Update methods: size(), isEmpty() replaceElement(p, e), swapElements(p, q) Query methods: insertBefore(p, e), isFirst(p), isLast(p) insertAfter(p, e), Accessor methods: insertFirst(e), first(), last() insertLast(e) before(p), after(p) remove(p) Stacks, Queues, & Lists

Performance

In the implementation of the List ADT by means of a doubly linked list

The space used by a list with *n* elements is *O(n)*The space used by each position of the list is *O(1)*All the operations of the List ADT run in *O(1)* time

Operation element() of the Position ADT runs in *O(1)* time

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Exercise on List Generic methods: Generic methods:

integer size()

boolean isEmpty()

objectiterator elements()

Accessor methods:

position first()

position last()

position last()

position after(p)

Query methods:

boolean isErist(p)

boolean isLast(p)

Uddate methods: Exercise: Write a method to calculate the sum of the integers in a list of Only use the methods in the list to the left. Update methods: swapElements(p, q)
 object replaceElement(p, o)
 insertFirst(o) Algorithm sum(L) insertLast(o) insertBefore(p, o) insertAfter(p , o) remove(p)

Main Point

3. The algorithm designer needs to consider how a sequence of objects is going to be used because linked lists are much more efficient than arrays (vectors) when many insertions or deletions need to be made to random parts of a sequence (or list).

Science of Consciousness: Nature always functions with maximum efficiency and minimum effort.

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Operation	Position
first(), last()	
before(p), after(p)	
replaceElement(p, o), swapElements	s(p, q)
insertFirst(o), insertLast(o)	
insertAfter(p, o), insertBefore(p, o)	
remove(p)	

List Complexity

Operation

first(), last()

before(p), after(p)

replaceElement(p, o), swapElements(p, q)

insertFirst(o), insertLast(o)

insertAfter(p, o), insertBefore(p, o)

remove(p)

Stacks, Queues, & Lists

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Exercise on List ADT	
Generic methods: integer size() boolean isEmpty() objectiterator elements() Accessor methods: position first() position before(p) position before(p) position after(p) Query methods: boolean isFirst(p) boolean isLast(p) Update methods: swapElements(p, q) object replaceElement(p, o) insertFirst(o) insertLast(o) insertAfter(p, o) remove(p)	Exercise: Given a List L, write a method to find the Position that occurs in the middle of L Specifically, find middle as follows: when the number of elements is over that the same number of nodes occur when number of elements is even find p such that there is one more element that cours before p than after Do this without using a counter of any kind Algorithm findMiddle(L)

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Connecting the Parts of Knowledge with the Wholeness of Knowledge 1. The List ADT may be used as an allpurpose class for storing collections of objects with only sequential access to its elements. 2. The underlying implementation of an ADT determines its efficiency depending on how that data structure is going to be used in practice.

3. Transcendental Consciousness is the unbounded, silent field of pure order and efficiency.

4. Impulses within Transcendental Consciousness: Within this field, the laws of nature continuously organize and govern all activities and processes in creation.

5. Wholeness moving within itself: In Unity Consciousness, when the home of all knowledge has become fully integrated in all phases of life, life is spontaneously lived in accord with natural law for maximum achievement with minimum effort.

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