

Please upload your solution to Problem 3 to canvas for marking after the workshop.

### Problem 1

A 0.150 kg particle moves along an x axis according to  $x(t) = 13.00 + 2.00t + 4.00t^2 - 3.00t^3$ , with x in meters and t in seconds. In unit-vector notation, what is the net force acting on the particle at  $t = 3.40$  s?

### Problem 2

In a laboratory simulation, a standard wood toothpick was shot by pneumatic gun into an oak branch. The toothpick's mass was 0.13 g, its speed before entering the branch was  $220 \text{ ms}^{-1}$ , and its penetration depth was 15 mm. If its speed was decreased at a uniform rate, what was the magnitude of the force of the branch on the toothpick?

### Problem 3

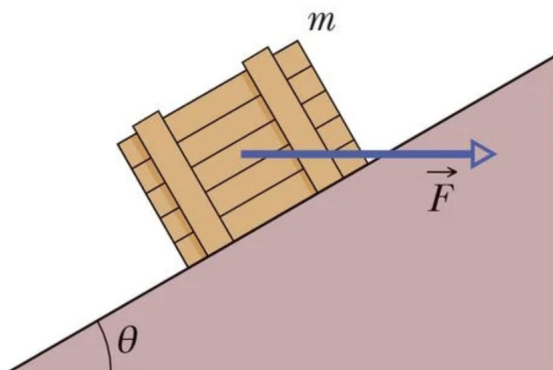
A 200-m-wide river flows due east at a uniform speed of  $2.0 \text{ ms}^{-1}$ . A boat with a speed of  $8.0 \text{ ms}^{-1}$  relative to the water leaves the south bank pointed in a direction  $30^\circ$  west of north.

- (a) What is the magnitude of the boat's velocity relative to the ground?
- (b) What is the direction of the boat's velocity relative to the ground?
- (c) How long does the boat take to cross the river?

### Problem 4

In the figure below, a crate of mass  $m = 100 \text{ kg}$  is pushed at constant speed up a frictionless ramp ( $\theta = 30.0^\circ$ ) by a horizontal force.

- (a) What is the magnitude of  $\vec{F}$ ?
- (b) What is the magnitude of the force on the crate from the ramp?



### Want more practice?

Further problems on relative motion: Chapter 4.6, 4.7

Further problems on Newton's Laws: Chapter 5.1

Further problems on Forces: Chapter 5.2, 5.3

## Problem 1

A 0.150 kg particle moves along an x axis according to  $x(t) = 13.00 + 2.00t + 4.00t^2 - 3.00t^3$ , with x in meters and t in seconds. In unit-vector notation, what is the net force acting on the particle at  $t = 3.40$  s?

$$x(t) = 13 + 2t + 4t^2 - 3t^3$$

$$\dot{x}(t) = 2 + 8t - 9t^2$$

$$\ddot{x}(t) = 8 - 18t$$

$$m = 0.15 \text{ kg}$$

$$\Sigma F = ma = (0.15)(8 - 18t)$$

$$\text{@ } t = 3.4 \text{ s} \quad , \quad \Sigma F = (0.15)(8 - (18)(3.4)) = -7.98 \text{ N}$$

## Problem 2

smallest nsf = 2

In a laboratory simulation, a standard wood toothpick was shot by pneumatic gun into an oak branch. The toothpick's mass was 0.13 g, its speed before entering the branch was  $220 \text{ ms}^{-1}$ , and its penetration depth was 15 mm. If its speed was decreased at a uniform rate, what was the magnitude of the force of the branch on the toothpick?

$$m_t = 0.13 \text{ g} = 1.3 \times 10^{-1} \text{ g} = 1.3 \times 10^{-4} \text{ kg}$$

$$u_t = 220 \text{ ms}^{-1}$$

$$s_t = 15 \text{ mm} = 15 \times 10^{-3} \text{ m} = 1.5 \times 10^{-2} \text{ m}$$

$$a_t = \text{constant} \rightarrow \text{can use suvat}$$

$$v_t = 0$$

$t$  is unknown.

$$\begin{aligned} a &= \frac{1}{2s} (v^2 - u^2) \\ &= \frac{1}{1.5 \times 10^{-2}} (0 - 220^2) \end{aligned}$$

(They don't have to show this)

$$\text{Rearrange suvat 2: } v = u + at \therefore t = \frac{v-u}{a}$$

$$\text{Sub into suvat 1: } s = ut + \frac{1}{2}at^2$$

$$= u\left(\frac{v-u}{a}\right) + \frac{1}{2}a\left(\frac{v-u}{a}\right)^2$$

$$= \frac{uv - u^2}{a} + \frac{1}{2a}(v^2 + u^2 - 2uv)$$

$$= \frac{1}{a}(\cancel{uv} - u^2 + \frac{v^2}{2} + \frac{u^2}{2} - \cancel{uv})$$

$$= \frac{1}{2a}(v^2 - u^2)$$

$$\therefore a = -3.2 \dots \times 10^6 \text{ ms}^{-2}$$

$$\therefore F = ma = -4.2 \times 10^2 \text{ N to 2SF}$$

This is the force ON the toothpick.

### Problem 3

A 200-m-wide river flows due east at a uniform speed of  $2.0 \text{ ms}^{-1}$ . A boat with a speed of  $8.0 \text{ ms}^{-1}$  relative to the water leaves the south bank pointed in a direction  $30^\circ$  west of north.

- What is the magnitude of the boat's velocity relative to the ground?
- What is the direction of the boat's velocity relative to the ground?
- How long does the boat take to cross the river?

$$\mathbf{B_G} = \mathbf{B_W} + \mathbf{W_G}$$


200m : y-displacement, BW and BG ( $S_y, W_y = 0$ )

$2.0 \text{ ms}^{-1}$  : x-velocity, WG

$8 \text{ ms}^{-1}$  : mag velocity, BW

$30^\circ$  west of North = angle, BG

BG



$S_y = 200 \text{ m}$

$\theta = 30^\circ \text{ W. of N.}$

$$S = \frac{S_y}{\cos 30} \sim 231 \text{ m}$$

$$S_x = S \sin \theta \sim 115 \text{ m}$$

BW

$S_y = 200 \text{ m}$

$v = 8 \text{ ms}^{-1}$

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$S = (8 \text{ ms}^{-1}) t$

$S_x^2 = S^2 - S_y^2$

WG

$v_x = 2 \text{ ms}^{-1}$

$v_y = 0$

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$S_y = 0$

$S_x = (2 \text{ ms}^{-1}) t$

$$v_{x, BG} = v_{x, BW} + v_{x, WG}$$

$$v_{y, BG} = v_{y, BW} + v_{y, WG}$$

$$S_{x, BG} = S_{x, BW} + S_{x, WG}$$

$$115 \text{ m} = \sqrt{(8 \text{ ms}^{-1})^2 t^2 + 200^2 \text{ m}^2} \rightarrow \text{solve for } t$$

$$t = \sqrt{(115^2 + 200^2) / 8^2} = 118 \text{ s}$$

Then

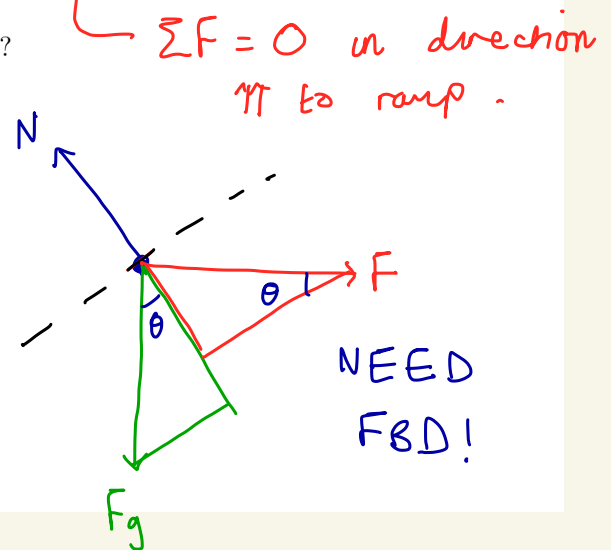
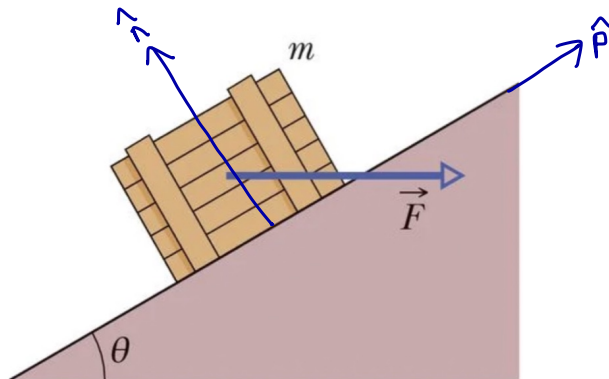
$$v_{BG} = S_{BG} / t = 231 / 118 = 1.96 \text{ ms}^{-1}$$

And  $\theta_{BG} \text{ is } 30^\circ$  (given)

### Problem 4

In the figure below, a crate of mass  $m = 100 \text{ kg}$  is pushed at constant speed up a frictionless ramp ( $\theta = 30.0^\circ$ ) by a horizontal force.

- (a) What is the magnitude of  $\mathbf{F}$ ?  
 (b) What is the magnitude of the force on the crate from the ramp?



$$\vec{F}_g = F_g \cos \theta \hat{p} - F_g \sin \theta \hat{n}$$

$$\vec{F}_{app} = F_{app} \sin \theta \hat{p} - F_{app} \cos \theta \hat{n}$$

$$\Sigma \vec{F}_p = F_g \cos \theta + F_{app} \sin \theta = 0 \quad \text{ANGLES SKETCH HELPS.}$$

$$\Sigma \vec{F}_n = -F_g \sin \theta - F_{app} \cos \theta = 0$$

$$\therefore F_{app,p} = -F_g \frac{\cos \theta}{\sin \theta} \approx -1700 \text{ N}$$

and

$$F_{app,n} = -F_g \frac{\sin \theta}{\cos \theta} \approx -566 \text{ N}$$

$$\therefore F_{app} = \sqrt{1700^2 + 566^2} \approx 1792 \text{ N}$$

Ramp provides NORMAL FORCE  $N = -F_g \sin \theta - F_{app} \cos \theta$

$$N \approx -2042 \text{ N} \quad \text{magnitude } N = 2042 \text{ N}$$