# Digital Image Processing COSC 6380/4393

Lecture – 10

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Slides from Dr. Shishir K Shah and Frank (Qingzhong) Liu

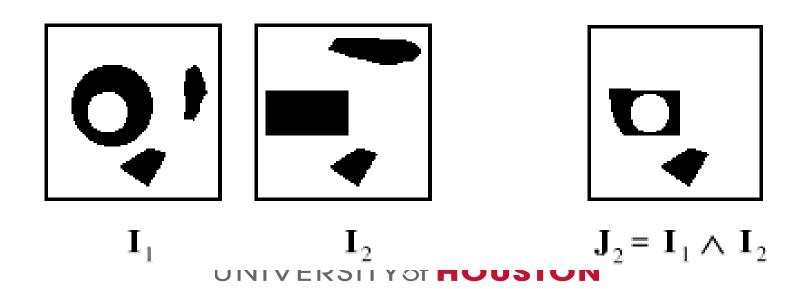
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#### **Review: THE BASIC LOGICAL OPERATIONS**

- We will use only a **few simple** logical operations
- Suppose that  $X_1, ..., X_n$  are binary variables
- For example, pixels from one or more binary images
- Here is the notation we will use:
- Logical Complement:  $NOT(X_1) = complement of X_1$
- Logical AND: AND $(X_1, X_2) = X_1 \wedge X_2$
- Logical OR:  $OR(X1, X2) = X1 \vee X2$
- Binary Majority:  $MAJ(X_1, X_2, ..., X_n) = 1$  if more 1's than 0's = 0 if more 0's than 1's

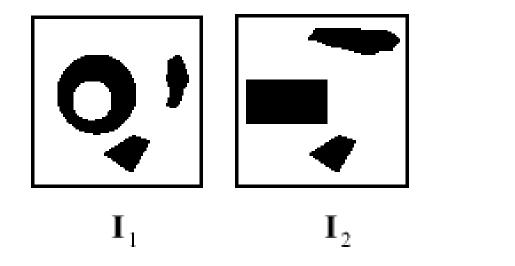
#### **Review: BINARY AND**

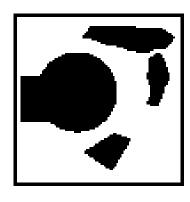
- The AND or intersection of two images:
- $J_2 = AND(I_1, I_2) = I_1 \wedge I_2 \text{ if } J_2(i, j) =$  $AND[I_1(i, j), I_2(i, j)] \text{ for all } (i, j)$
- Shows the overlap of BLACK regions in  $I_1$  and  $I_2$



### **Review:** BINARY OR

- The OR or union of two images:
- $J_3 = OR(I_1, I_2) = I_1 \vee I_2$ if  $J_3(i, j) = OR[I_1(i, j), I_2(i, j)]$  for all (i, j)
- Shows the **overlap** of the WHITE regions in  $I_1$  and  $I_2$

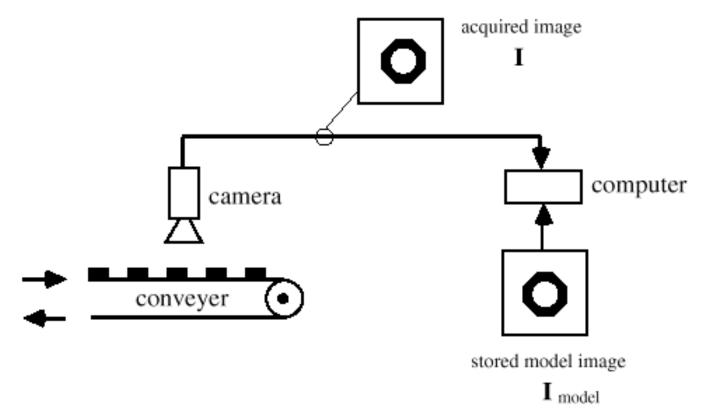




$$\mathbf{J}_3 = \mathbf{I}_1 \vee \mathbf{I}_2$$

# **Review: EXAMPLE**

• An assembly-line image inspection system. Similar to many marketed by industry:

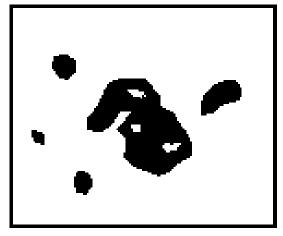


• Objective: Numerically compare the stored image  $I_{model}$  and the acquired image I

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# **Review: BLOB COLORING**

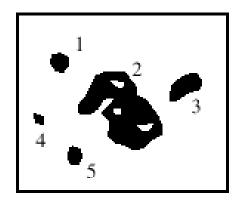
- A simple technique for region classification and correction
- **Motivation**: Gray-level image thresholding **usually** produces an imperfect binary image:
  - Extraneous blobs or holes due to noise
  - Extraneous blobs from thresholded objects of little interest
  - Nonuniform object/background surface reflectances



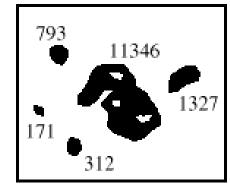
typical thresholded image result

#### **EXAMPLE**

Using blob coloring



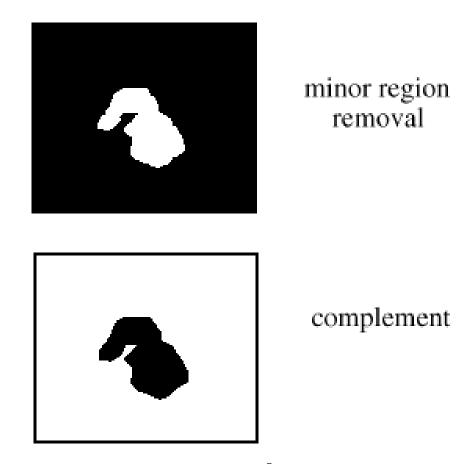
blob coloring result



blob counting result

• "Color" of largest blob: 2

#### **EXAMPLE**



• Simple and effective, but doesn't "cure" everything

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# **BINARY MORPHOLOGY**

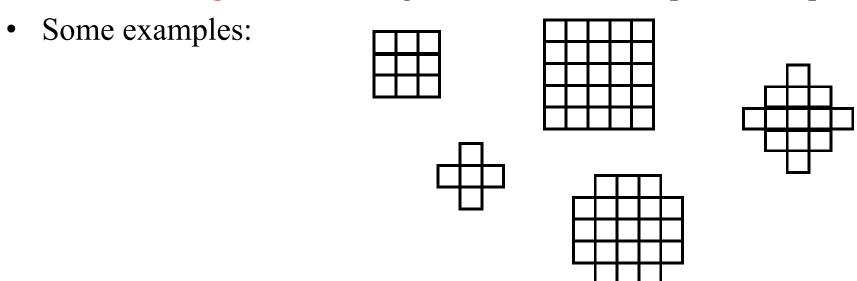
- The most powerful class of binary image operators
- A general framework known as mathematical morphology

#### morphology = shape

- Morphological operations affect the shapes of objects and regions in binary images
- All processing is done on a **local basis** region or blob shapes are affected in a local manner
- Morphological operators
  - Expand (dilate) objects
  - Shrink (erode) objects
  - Smooth object boundaries and eliminate small regions or holes
  - Fill gaps and eliminate 'peninsulas'
- All is accomplished using local logical operations

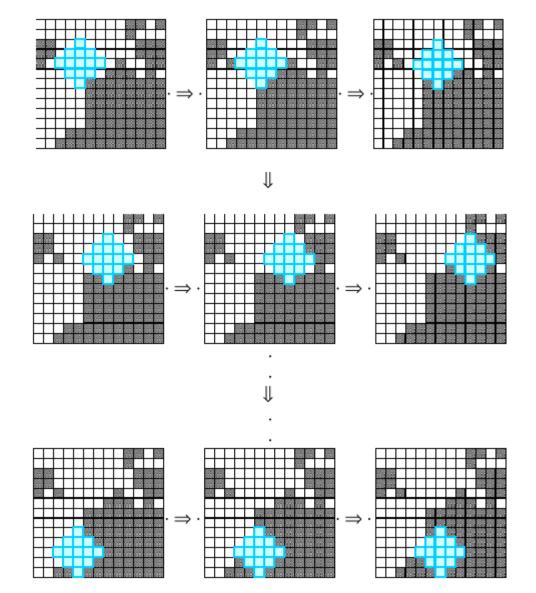
#### STRUCTURING ELEMENTS OR WINDOWS

• A structuring element is a geometric relationship between pixels



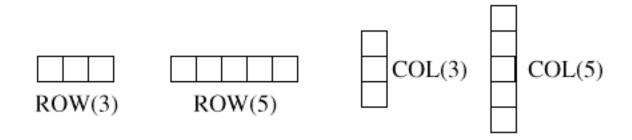
• Morphological operations are defined (conceptually) by moving a structuring element over the image to be modified, in such a way that it is centered over every image pixel at some point

# STRUCTURING ELEMENTS



# WINDOWING

Some typical windows:

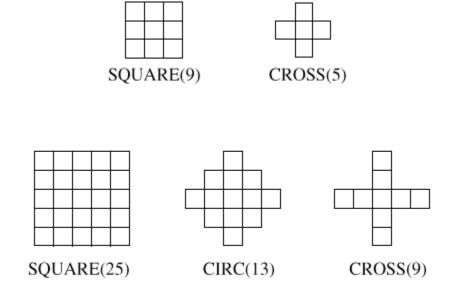


1-D windows ROW(2M+1) and COL(2M+1).

- These operate on rows and columns only
- A window will always cover an **odd number** of pixels **2M+1**:
  - pairs of adjacent pixels, plus the center pixel
- Filtering operations are defined symmetrically this way

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### TWO-DIMENSIONAL WINDOWS



2-D windows SQUARE(2M+1), CROSS(2M+1), CIRC(2M+1)

- Again, 2M+1 denotes the **odd** number of pixels covered by the window
- Can generalize to arbitrary-size windows covering 2M+1 pixels
- These are the **most common** window shapes

Structuring element



1	0	0	1	0
0	1	0	0	0
1	1	1	1	0
1	0	1	0	1
0	1	0	1	0

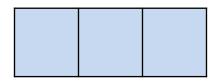
Structuring element



Apply OR binary operation

1	0	0	1	0
0	1	0	0	0
1	1	1	1	0
1	0	1	0	1
0	1	0	1	0

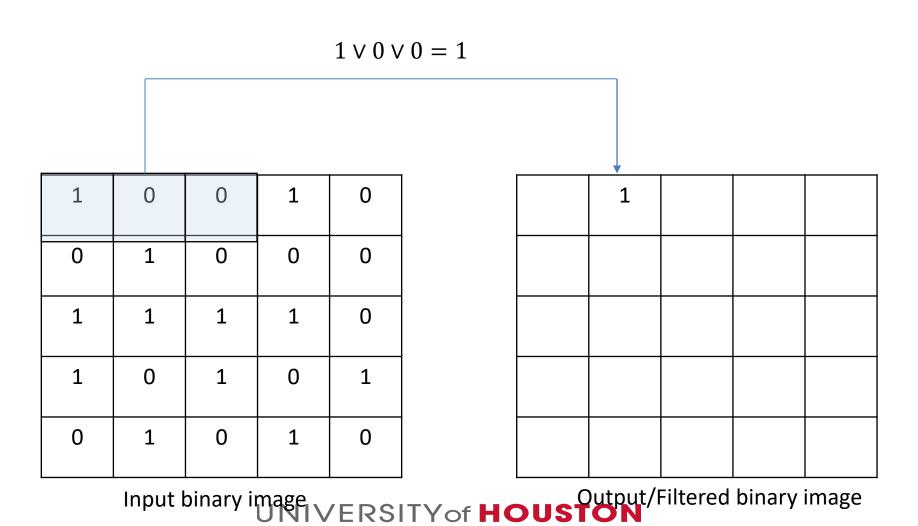
Input binary image VERSITY of HOUSTON

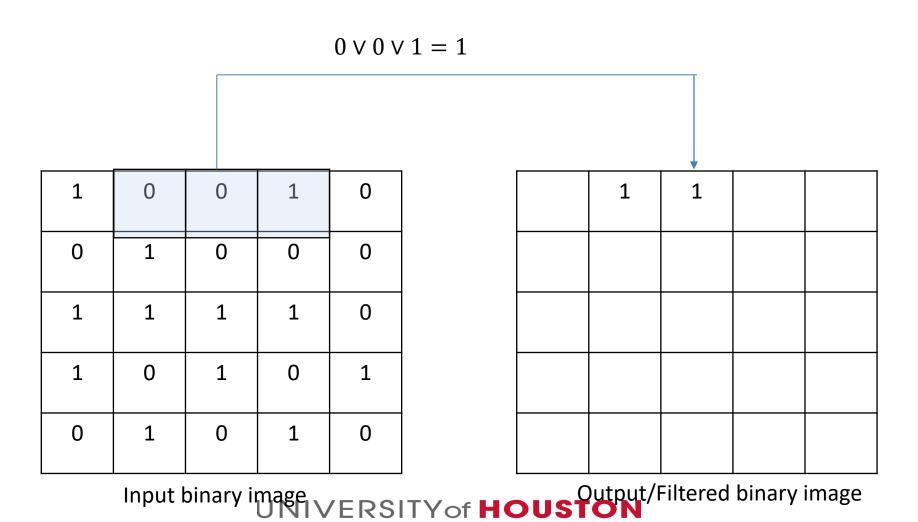


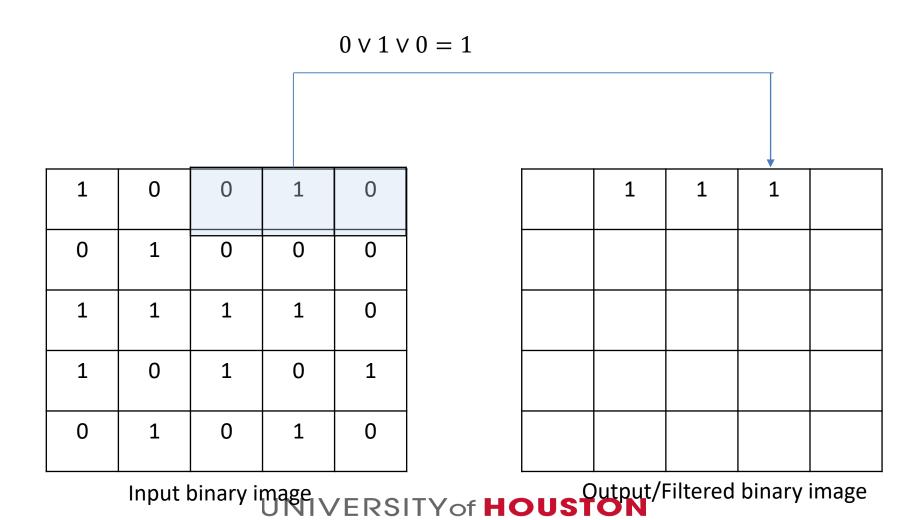
1	0	0	1	0
0	1	0	0	0
1	1	1	1	0
1	0	1	0	1
0	1	0	1	0

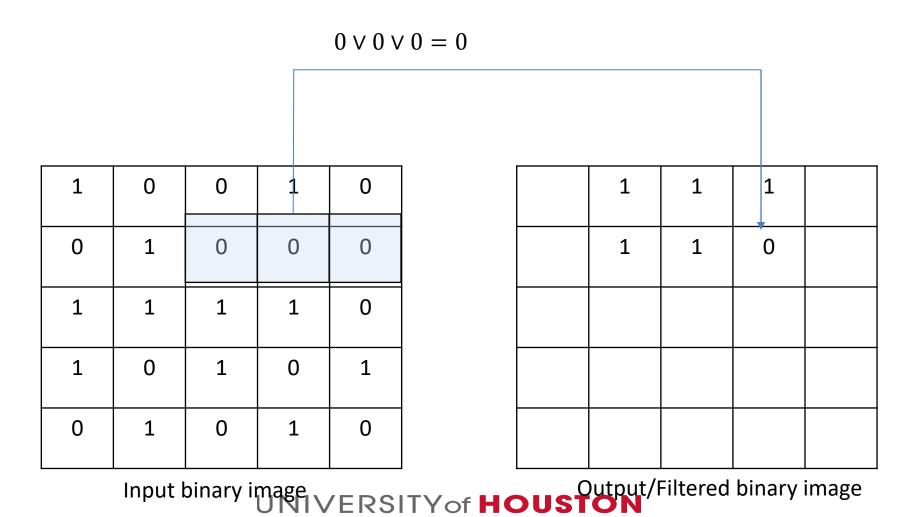
1	0	0	1	0
0	1	0	0	0
1	1	1	1	0
1	0	1	0	1
0	1	0	1	0

Input binary image Output/Filtered binary image Output/Filtered binary image



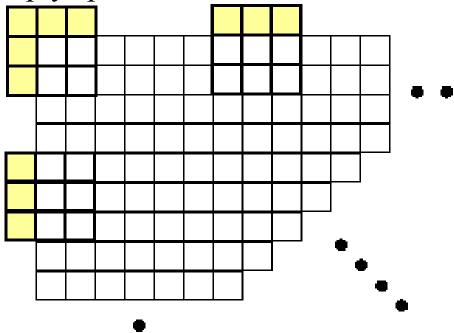






# **EDGE-OF-IMAGE PROCESSING**

Window overlapping "empty space" :



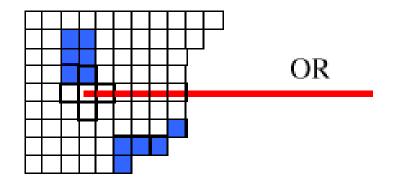
• Convention: fill the "empty" window slots by the nearest image pixel. This is called replication

# DILATION, EROSION AND MEDIAN (MAJORITY)

- <u>DILATION</u>: Given a window **B** and a binary image **I**:
- $J_1 = DILATE(I, B)$  Apply OR operations within the moving window
- <u>EROSION</u>: Given a window **B** and a binary image **I**:
- $J_2 = \text{ERODE}(I, B)$  Apply AND operation within the moving window
- MEDIAN: Given a window **B** and a binary image **I**:
- $J_3 = MEDIAN(I, B)$  Apply MAJ operation within the moving window

# **DILATION**

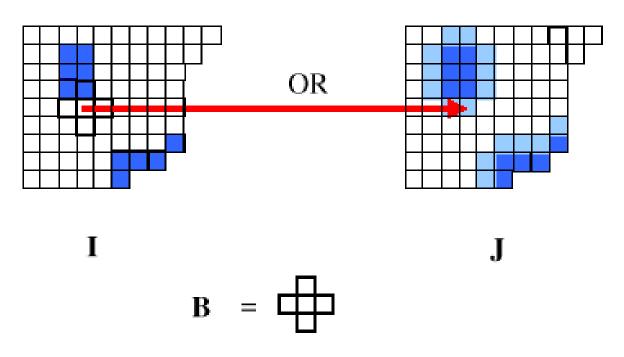
- So-called because this operation **increases** the size of BLACK objects in a binary image
- Local Computation: J = DILATE(I, B)



Ι

# **DILATION**

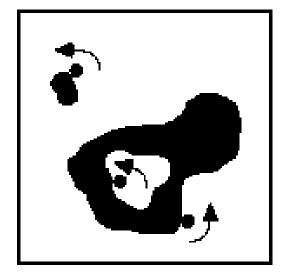
- So-called because this operation **increases** the size of BLACK objects in a binary image
- Local Computation: J = DILATE(I, B)



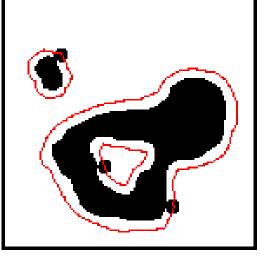
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### **DILATION**

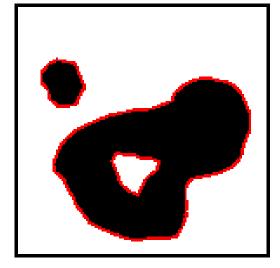
#### • Global Effect:



It is useful to think of the structuring element as rolling along all of the boundaries of all BLACK objects in the image.



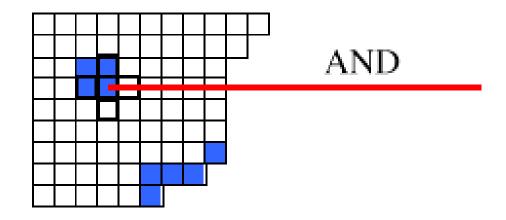
The center point of the structuring element traces out a set of paths.



That form the boundaries of the dilated image.

# **EROSION**

- So-called because this operation **decreases** the size of BLACK objects in a binary image
- Local Computation: J = ERODE(I, B)

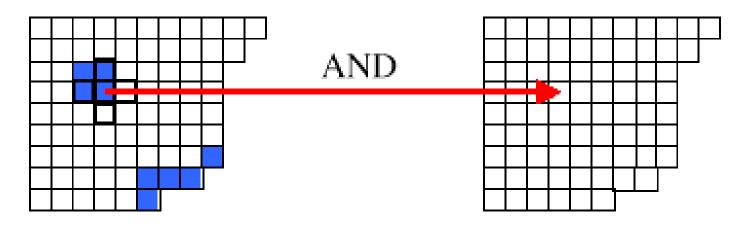


Ι

J

# **EROSION**

- So-called because this operation **decreases** the size of BLACK objects in a binary image
- Local Computation: J = ERODE(I, B)

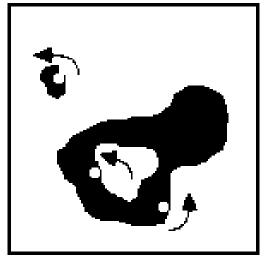


в =

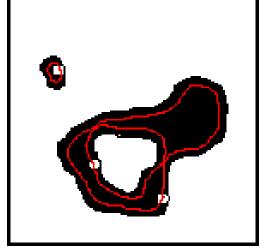
J

# **EROSION**

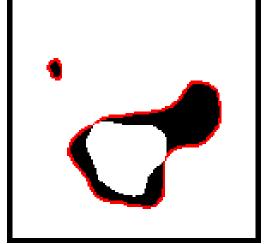
#### • Global Effect:



It is useful to think of the structuring element as rolling inside of the boundaries of all BLACK objects in the image.



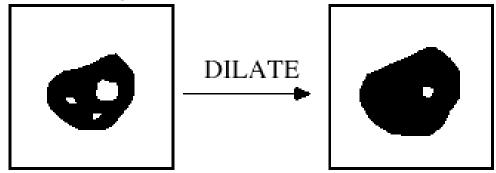
The center point of the structuring element traces out a set of paths.



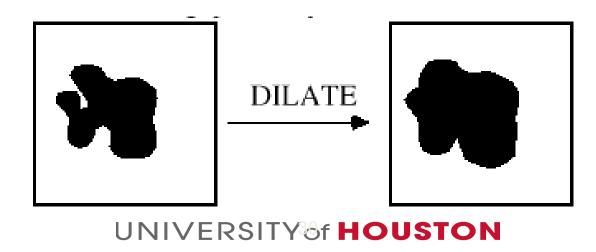
That form the boundaries of the eroded image.

# QUALITATIVE PROPERTIES OF DILATION

• Dilation removes object holes of too-small size:

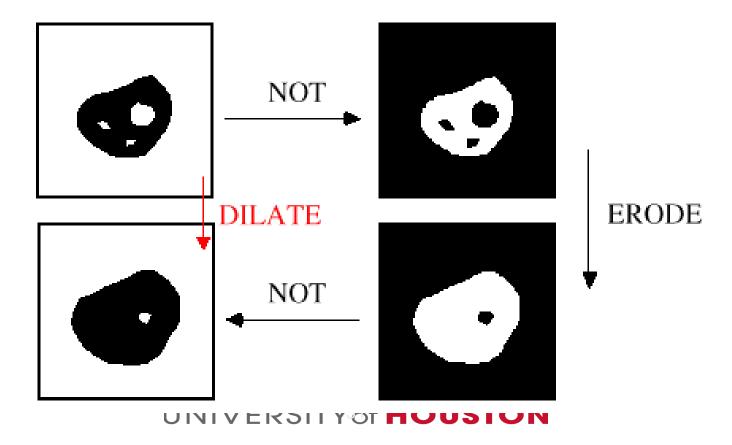


• Dilation also removes gaps or bays of too-narrow width:



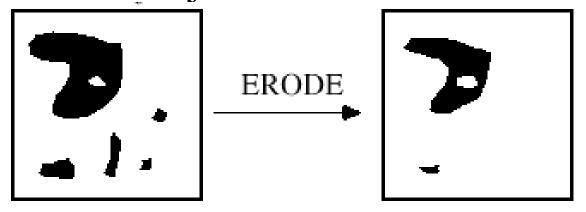
# QUALITATIVE PROPERTIES OF DILATION

• Dilation of the BLACK part of an image is the same as erosion of the WHITE part!

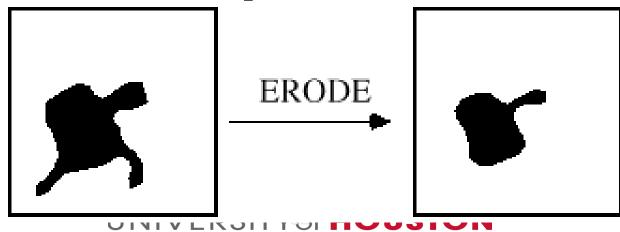


# QUALITATIVE PROPERTIES OF EROSION

• Erosion removes objects of too-small size:

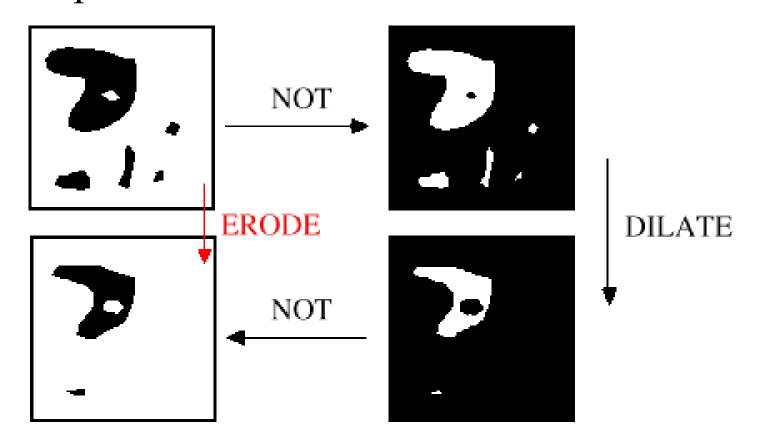


• Erosion also removes peninsulas of too-narrow width:



# QUALITATIVE PROPERTIES OF EROSION

• Erosion of the BLACK part of an image is the same as dilation of the WHITE part!

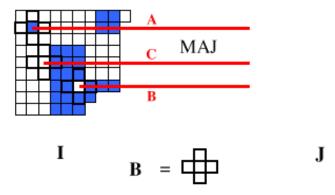


# RELATING EROSION AND DILATION

- Erosion and dilation are actually the same operation they are just **dual** operations with respect to **complementation**
- Erosion and dilation are only **approximate** inverses of one another
- Dilating an eroded image rarely yields the original image
- In particular, dilation cannot
  - Recreate peninsulas eliminated by erosion
  - Recreate small objects eliminated by erosion
- Eroding a dilated image rarely yields the original image
- In particular, erosion cannot
  - Unfill holes filled by dilation
  - Recreate gaps or bays filled by dilation

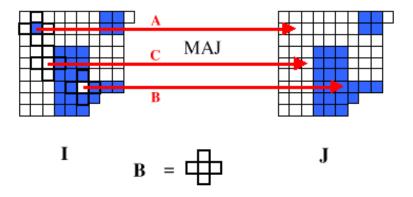
# **MEDIAN**

- Actually **majority**. A special case of the gray-level **median filter**
- Possesses qualitative attributes of both dilation and erosion, but does not generally change the **size** of objects or background
- Local Computation: J = MEDIAN(I, B)



### **MEDIAN**

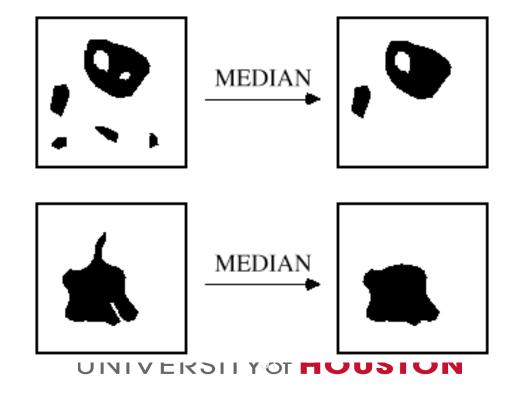
- Actually **majority**. A special case of the gray-level **median filter**
- Possesses qualitative attributes of both dilation and erosion, but does not generally change the **size** of objects or background
- Local Computation: J = MEDIAN(I, B)



• The median removed the small **object** A and the small **hole** B, but did not change the boundary (**size**) of the larger region C

# QUALITATIVE PROPERTIES OF MEDIAN

• Median removes both objects and holes of too-small size, as well as both gaps (bays) and peninsulas of too-narrow width



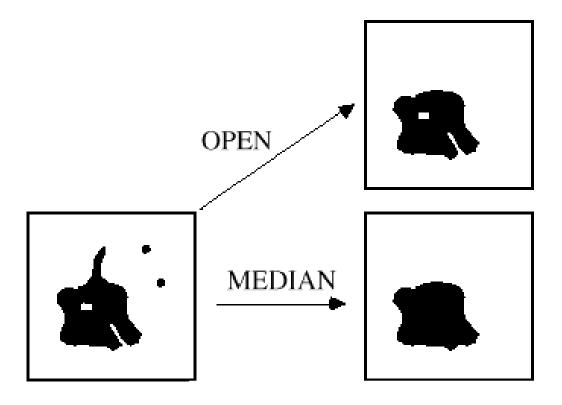
## QUALITATIVE PROPERTIES OF MEDIAN

- Note that median does not generally change the size of objects (although it does alter them)
- Median is its own dual, since
  MEDIAN [ NOT(I) ] = NOT [ MEDIAN(I) ]
- Thus, the median is a shape smoother. It is a filter
- We can define other shape smoothers as well.

# **OPENing**

- We can define **new** morphological operations by performing the basic ones in sequence
- Given an image I and window B, define
  OPEN(I, B) = DILATE [ERODE(I, B), B]
- In other words,
  OPEN = erosion (by B) followed by dilation (by B)

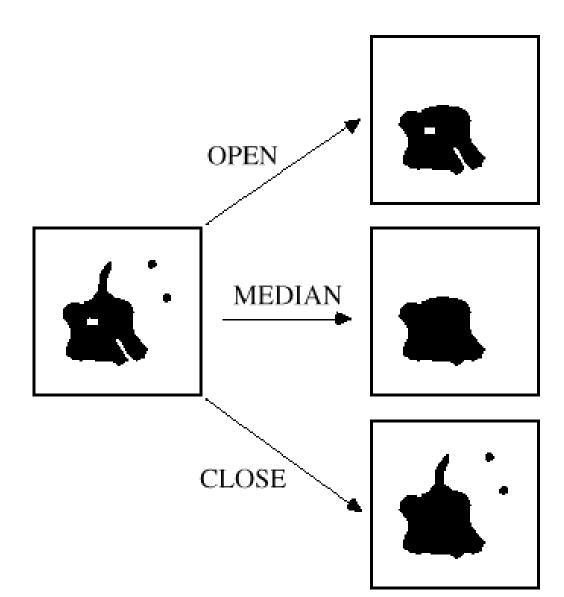
# **EXAMPLES**



# **OPENing and CLOSing**

- We can define **new** morphological operations by performing the basic ones in sequence
- Given an image I and window B, define OPEN(I, B) = DILATE [ERODE(I, B), B]
   CLOSE(I, B) = ERODE [DILATE(I, B), B]
- In other words,
- OPEN = erosion (by  $\bf B$ ) followed by dilation (by  $\bf B$ )
- CLOSE = dilation (by **B**) followed by erosion (by **B**)

# **EXAMPLES**



# **OPENing and CLOSing**

- OPEN and CLOSE are very similar to MEDIAN:
- OPEN removes too-small objects/fingers (more effectively than MEDIAN), but not holes, gaps, or bays
- CLOSE removes too-small holes/gaps (more effectively than MEDIAN) but not objects or peninsulas
- OPEN and CLOSE generally do not affect object size
- OPEN and CLOSE are used when too-small BLACK and WHITE objects (respectively) are to be removed
- Thus OPEN and CLOSE are more specialized smoothers

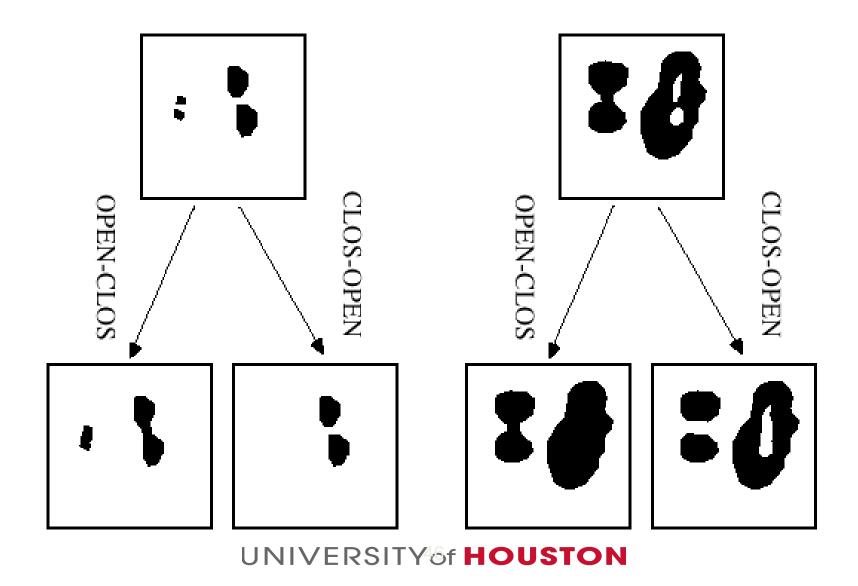
# **Open-Close and Close-Open**

- Very effective smoothers can be obtained by sequencing the OPEN and CLOSE operators:
- For an image I and structuring element B, define
  OPEN-CLOS(I, B) = OPEN [CLOSE (I, B), B]
  CLOS-OPEN(I, B) = CLOSE [OPEN (I, B), B]
- These operations are quite similar (not mathematically identical)

# **Open-Close and Close-Open**

- Both remove too-small structures without affecting size much
- Both are similar to the median filter except they smooth **more** (for a given structuring element **B**)
- One notable difference between OPEN-CLOS and CLOS-OPEN:
- OPEN-CLOS tends to link neighboring objects together
- CLOS-OPEN tends to link neighboring holes together

## **EXAMPLES**

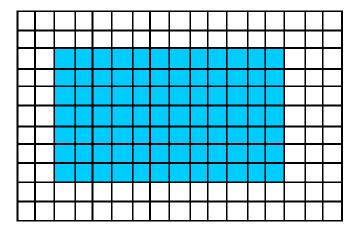


### **SKELETONIZATION**

• A way of obtaining an image's medial axis or skeleton

### **EXAMPLE**

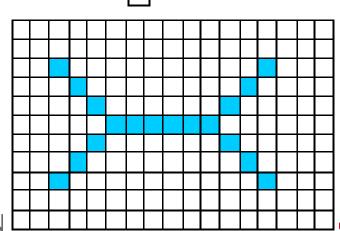
• Image  $I_0$ :



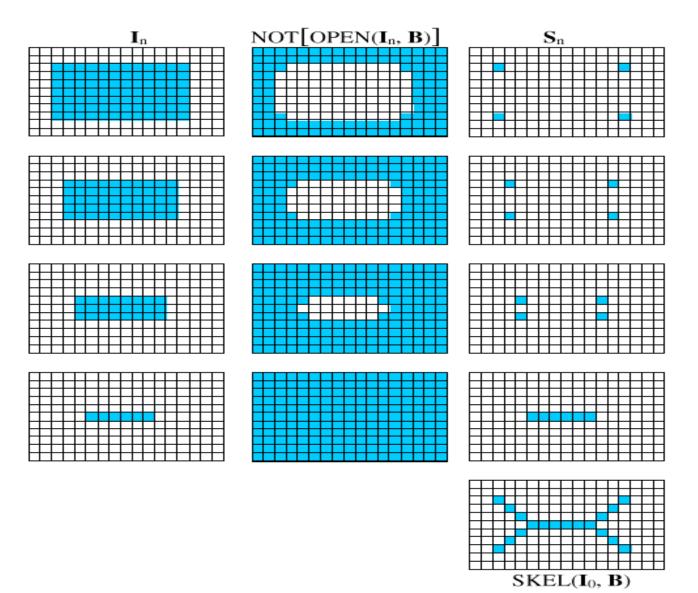
• Structuring Element **B**:



• SKEL(**I**<sub>0</sub>, **B**):



### THE STEPS



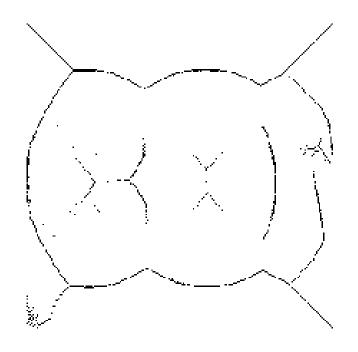
### **SKELETONIZATION**

- A way of obtaining an image's medial axis or skeleton
- Given an image  $I_0$  and window B, the skeleton is SKEL( $I_0$ , B)
- Obtaining the skeleton requires a fairly complex iteration:
- Define I<sub>n</sub> = ERODE [··· ERODE [ERODE(I<sub>0</sub>, B), B], ···
  B ] (n consecutive EROSIONS of I<sub>0</sub> by B)
- $N = \max \{ n: I_n \cdot \phi \} \phi = \text{empty set}$
- (the largest number of erosions before  $I_n$  "disappears")
- $S_n = I_n \land NOT[OPEN(I_n, B)]$
- Then SKEL( $\mathbf{I}_0$ ,  $\mathbf{B}$ ) =  $\mathbf{S}_1 \vee \mathbf{S}_2 \vee \cdots \vee \mathbf{S}_N$

## **EXAMPLE**



binary image



skeleton (of background)

### **APPLICATION EXAMPLE**

- Simple Task: Measuring Cell Area
- Simple processing steps:
  - (i) Find general cell region by **simple thresholding**
  - (ii) Apply region correction techniques:
    - Blob coloring
    - Minor region removal
    - CLOS-OPEN
  - (iii) Display cell boundary for operator verification
  - (iv) Compute image cell area by counting pixels
  - (v) Compute actual cell area using perspective projection

### **COMMENTS**

- Previous manual measurement techniques required >
  1 hour per cell image to analyze
- Algorithm runs in less than a second.
- Published in CRC Press's *Image Analysis in Biology* as the standard for "Automated Area Measurement."

# Compression: RUN LENGTH CODING

- The number of bits required to store an N x N binary image is  $N^2$
- This can be significantly reduced in many cases.
- Run-length coding works well if the WHITE and BLACK regions are generally not small.

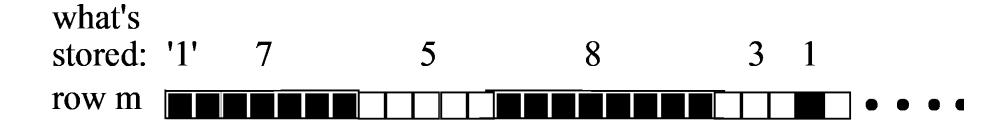
### **EXAMPLE**

what's stored:

row m



### **EXAMPLE**



#### **HOW DOES IT WORK?**

- Binary images are stored (or transmitted) on a line-by-line (row-by-row) basis
- For each image row numbered *m*:
  - Store the first pixel value ('0' or '1') in row m as a reference
  - Set run counter c = 1
  - For each pixel in the row:
    - Examine the next pixel to the right
    - If same as current pixel, set c = c + 1
    - If different from current pixel, **store** c and set c = 1
    - Continue until end of row is reached
- Each run-length is stored using b bits.

#### **COMMENTS**

- Can yield excellent lossless compressions on some images.
- This will happen if the image contains lots of runs of 1's and 0's.
- If the image contains only very short runs, then run-length coding can actually **increase** the required storage.

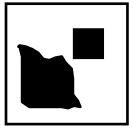
#### **WORST CASE**

- In this worst-case example the storage increases **b-fold**!
- Rule of thumb: the average run-length L should satisfy:

$$L > b$$
.

#### **CONTOUR REPRESENTATION & CHAIN CODING**

• We can distinguish between two general types of binary image: **region images** and **contour images**.

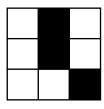




region image

contour image

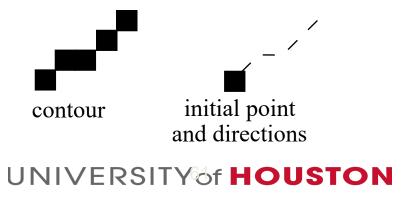
- We will require contour images to be special:
- Each BLACK pixel in a contour image must have at most two BLACK 8-neighbors
- a BLACK pixel and its 8-neighbors –



 Contour images are composed only of single-pixel width contours (straight or curved) and single points.

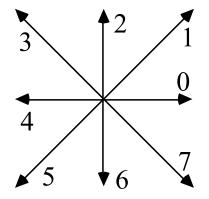
#### CHAIN CODE

- The chain code is a highly efficient method for coding contours
- Observe that if the initial (i, j) coordinate of an 8-connected contour is known, then the rest of the contour can be coded by giving the directions along which the contour propagates



#### CHAIN CODE

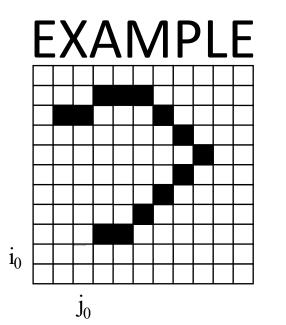
• We use the following 8-neighbor direction codes:



• Since the numbers 0, 1, 2, 3, 4, 5, 6, 7 can be coded by their 3-bit binary equivalents:

000, 001, 010, 011, 100, 101, 110, 111

the location of each point on the contour **after** the initial point can be coded by 3 bits.



 $\Box$  = initial point

Its chain code: (after recording the initial coordinate (i0, j0)
 1, 0, 1, 1, 1, 1, 3, 3, 3, 4, 4, 5, 4

=

#### **COMMENTS**

- The compression obtained can be quite significant: coding the contour by M-bit coordinates (M = 9 for 512 x 512 images) requires 6 times as much storage
- The technique is effective in many computer vision and pattern recognition applications, e.g. character recognition
- For closed contours, the initial coordinate can be chosen arbitrarily. If the contour is **open**, then it is usually an **end point** (one 8-neighbor).