# COSC4337\_Manual Neural Network

## 1 Manual Neural Network

1.0.1 Quick Note on Super() and OOP

```
[1]: class SimpleClass():
         def __init__(self,str_input):
             print("SIMPLE"+str_input)
[2]: class ExtendedClass(SimpleClass):
         def __init__(self):
             print('EXTENDED')
[3]: s = ExtendedClass()
    EXTENDED
[4]: class ExtendedClass(SimpleClass):
         def __init__(self):
             super().__init__(" My String")
             print('EXTENDED')
[5]: s = ExtendedClass()
    SIMPLE My String
    EXTENDED
    1.1 Operation
```

```
[6]: class Operation():
```

```
An Operation is a node in a "Graph". TensorFlow will also use this concept \sqcup
\hookrightarrow of a Graph.
   This Operation class will be inherited by other classes that actually \sqcup
\hookrightarrow compute the specific
   operation, such as adding or matrix multiplication.
   def __init__(self, input_nodes = []):
       Intialize an Operation
       self.input_nodes = input_nodes # The list of input nodes
       self.output_nodes = [] # List of nodes consuming this node's output
       # For every node in the input, we append this operation (self) to the
\hookrightarrow list of
       # the consumers of the input nodes
       for node in input_nodes:
            node.output_nodes.append(self)
       # There will be a global default graph (TensorFlow works this way)
       # We will then append this particular operation
       # Append this operation to the list of operations in the currently_
\rightarrow active default graph
       _default_graph.operations.append(self)
   def compute(self):
       This is a placeholder function. It will be overwritten by the actual \sqcup
\hookrightarrow specific operation
        that inherits from this class.
        11 11 11
       pass
```

#### 1.2 Example Operations

#### 1.2.1 Addition

```
[7]: class add(Operation):

def __init__(self, x, y):

super().__init__([x, y])
```

```
def compute(self, x_var, y_var):
    self.inputs = [x_var, y_var]
    return x_var + y_var
```

### 1.2.2 Multiplication

```
[8]: class multiply(Operation):
    def __init__(self, a, b):
        super().__init__([a, b])

    def compute(self, a_var, b_var):
        self.inputs = [a_var, b_var]
        return a_var * b_var
```

## 1.2.3 Matrix Multiplication

```
[9]: class matmul(Operation):
    def __init__(self, a, b):
        super().__init__([a, b])

    def compute(self, a_mat, b_mat):
        self.inputs = [a_mat, b_mat]
        return a_mat.dot(b_mat)
```

#### 1.3 Placeholders

```
[10]: class Placeholder():
    """
    A placeholder is a node that needs to be provided a value for computing the
    →output in the Graph.
    """

    def __init__(self):
        self.output_nodes = []
        _default_graph.placeholders.append(self)
```

#### 1.4 Variables

```
class Variable():
    """
    This variable is a changeable parameter of the Graph.
    """

def __init__(self, initial_value = None):
    self.value = initial_value
    self.output_nodes = []

_default_graph.variables.append(self)
```

#### 1.5 Graph

```
class Graph():

    def __init__(self):
        self.operations = []
        self.placeholders = []
        self.variables = []

    def set_as_default(self):
        """
        Sets this Graph instance as the Global Default Graph
        """
        global _default_graph
        _default_graph = self
```

#### 1.6 A Basic Graph

$$z = Ax + b$$

With A=10 and b=1

$$z = 10x + 1$$

Just need a placeholder for x and then once x is filled in we can solve it!

```
[13]: g = Graph()
[14]: g.set_as_default()
[15]: A = Variable(10)
```

```
[16]: b = Variable(1)
[17]: # Will be filled out later
      x = Placeholder()
[18]: y = \text{multiply}(A, x)
[19]: z = add(y,b)
      1.7 Session
[20]: import numpy as np
     1.7.1 Traversing Operation Nodes
[21]: def traverse_postorder(operation):
          PostOrder Traversal of Nodes. Basically makes sure computations are done in
           the correct order (Ax first , then Ax + b). Feel free to copy and paste\sqcup
       \hookrightarrow this code.
           It is not super important for understanding the basic fundamentals of deep_{\sqcup}
       \hookrightarrow learning.
           11 11 11
          nodes_postorder = []
          def recurse(node):
               if isinstance(node, Operation):
                   for input_node in node.input_nodes:
                        recurse(input_node)
               nodes_postorder.append(node)
          recurse(operation)
          return nodes_postorder
[22]: class Session:
          def run(self, operation, feed_dict = {}):
                 operation: The operation to compute
                 feed_dict: Dictionary mapping placeholders to input values (the data)_{\sqcup}
               11 11 11
               # Puts nodes in correct order
               nodes_postorder = traverse_postorder(operation)
```

for node in nodes\_postorder:

```
if type(node) == Placeholder:
                      node.output = feed_dict[node]
                  elif type(node) == Variable:
                      node.output = node.value
                  else: # Operation
                      node.inputs = [input_node.output for input_node in node.
       →input_nodes]
                      node.output = node.compute(*node.inputs)
                  # Convert lists to numpy arrays
                  if type(node.output) == list:
                      node.output = np.array(node.output)
              # Return the requested node value
              return operation.output
[23]: sess = Session()
[24]: result = sess.run(operation=z,feed_dict={x:10})
[25]: result
[25]: 101
[26]: 10*10 + 1
[26]: 101
     ** Looks like we did it! **
[27]: g = Graph()
      g.set_as_default()
      A = Variable([[10,20],[30,40]])
      b = Variable([1,1])
      x = Placeholder()
      y = matmul(A,x)
```

```
z = add(y,b)
[28]: sess = Session()
[29]: result = sess.run(operation=z,feed_dict={x:10})
[30]: result
[30]: array([[101, 201],
             [301, 401]])
     1.8 Activation Function
[31]: import matplotlib.pyplot as plt
      %matplotlib inline
[32]: def sigmoid(z):
          return 1/(1+np.exp(-z))
[33]: sample_z = np.linspace(-10,10,100)
      sample_a = sigmoid(sample_z)
[34]: plt.plot(sample_z,sample_a)
[34]: [<matplotlib.lines.Line2D at 0x212d8295d08>]
               1.0
               0.8
               0.6
               0.4
               0.2
               0.0
```

0.0

2.5

5.0

7.5

10.0

-10.0 -7.5

-5.0

-2.5

Sigmoid as an Operation

```
[35]: class Sigmoid(Operation):

    def __init__(self, z):
        # a is the input node
        super().__init__([z])

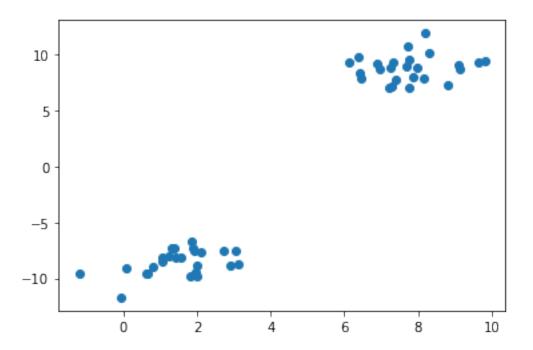
    def compute(self, z_val):
        return 1/(1+np.exp(-z_val))
```

#### 1.9 Classification Example

```
[36]: from sklearn.datasets import make_blobs
     data = make_blobs(n_samples = 50,n_features=2,centers=2,random_state=75)
[38]:
      data
[38]: (array([[ 7.3402781,
                              9.36149154],
              9.13332743,
                              8.74906102],
              1.99243535,
                             -8.85885722],
                7.38443759,
                              7.72520389],
              [ 7.97613887,
                              8.80878209],
              [ 7.76974352,
                              9.50899462],
              [ 8.3186688 ,
                              10.1026025 ],
              [ 8.79588546,
                              7.28046702],
              [ 9.81270381,
                              9.46968531],
              [ 1.57961049,
                             -8.17089971],
              [ 0.06441546,
                              -9.04982817],
              [ 7.2075117 ,
                              7.04533624],
              [ 9.10704928,
                              9.0272212 ],
              [ 1.82921897,
                             -9.86956281],
               7.85036314,
                              7.986659 ],
              [ 3.04605603,
                             -7.50486114],
              1.85582689,
                              -6.74473432,
                2.88603902,
                              -8.85261704],
              [-1.20046211,
                             -9.55928542],
              [ 2.00890845,
                             -9.78471782],
              [ 7.68945113,
                              9.01706723],
              [ 6.42356167,
                              8.33356412],
              [ 8.15467319,
                              7.87489634],
              [ 1.92000795,
                              -7.50953708],
                1.90073973,
                              -7.24386675],
              [ 7.7605855 ,
                              7.05124418],
```

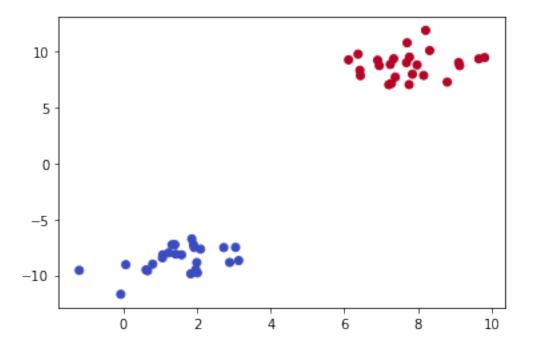
```
[ 6.90561582,
                              9.23493842],
              [ 0.65582768,
                             -9.5920878],
              [ 1.41804346,
                             -8.10517372],
              [ 9.65371965,
                              9.35409538],
              [ 1.23053506,
                             -7.98873571],
              [ 1.96322881,
                             -9.50169117],
              [ 6.11644251,
                              9.26709393],
              [ 7.70630321,
                             10.78862346],
              [ 0.79580385,
                             -9.00301023],
              [ 3.13114921,
                             -8.6849493 ],
              [ 1.3970852 ,
                             -7.25918415],
              [ 7.27808709,
                              7.15201886],
              [ 1.06965742,
                             -8.1648251 ],
              [ 6.37298915,
                              9.77705761],
                              8.85834104],
              [ 7.24898455,
              [ 2.09335725,
                             -7.66278316],
              [ 1.05865542,
                             -8.43841416],
              [ 6.43807502,
                              7.85483418],
              [ 6.94948313,
                              8.75248232],
              [-0.07326715, -11.69999644],
              [ 0.61463602,
                             -9.51908883],
              [ 1.31977821,
                             -7.2710667 ],
              [ 2.72532584,
                             -7.51956557],
              [ 8.20949206, 11.90419283]]),
      array([1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1,
             1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 1, 0, 0, 1,
             1, 0, 0, 0, 0, 1]))
[39]: features = data[0]
      plt.scatter(features[:,0],features[:,1])
```

[39]: <matplotlib.collections.PathCollection at 0x212dde03a08>



```
[40]: labels = data[1] plt.scatter(features[:,0],features[:,1],c=labels,cmap='coolwarm')
```

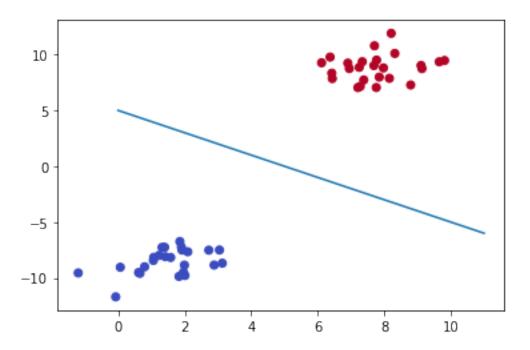
[40]: <matplotlib.collections.PathCollection at 0x212dde6a508>



```
[41]: # DRAW A LINE THAT SEPERATES CLASSES

x = np.linspace(0,11,10)
y = -x + 5
plt.scatter(features[:,0],features[:,1],c=labels,cmap='coolwarm')
plt.plot(x,y)
```

## [41]: [<matplotlib.lines.Line2D at 0x212ddea6908>]



## 1.10 Defining the Perceptron

$$y = mx + b$$

$$y = -x + 5$$

$$f1 = mf2 + b, m = 1$$

$$f1 = -f2 + 5$$

$$f1 + f2 - 5 = 0$$

#### 1.10.1 Convert to a Matrix Representation of Features

$$w^T x + b = 0$$

$$(1,1)f - 5 = 0$$

Then if the result is > 0 its label 1, if it is less than 0, it is label=0

## 1.10.2 Example Point

Let's say we have the point f1=2, f2=2 otherwise stated as (8,10). Then we have:

$$(1,1)\begin{pmatrix}8\\10\end{pmatrix} + 5 =$$

[42]: np.array([1, 1]).dot(np.array([[8],[10]])) - 5

[42]: array([13])

Or if we have (4,-10)

[43]: np.array([1,1]).dot(np.array([[4],[-10]])) - 5

[43]: array([-11])

#### 1.10.3 Using an Example Session Graph

[44]: g = Graph()

[45]: g.set\_as\_default()

[46]: x = Placeholder()

[47]: w = Variable([1,1])

[48]: b = Variable(-5)

[49]: z = add(matmul(w,x),b)

[50]: a = Sigmoid(z)

[51]: sess = Session()

[52]: sess.run(operation=a,feed\_dict={x:[8,10]})

[52]: 0.999997739675702

[53]: sess.run(operation=a,feed\_dict={x:[0,-10]})

[53]: 3.059022269256247e-07

# 2 Great Job!