



MRC  
Biostatistics  
Unit



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# Designing Phase I Single Agent Dose-Escalation Studies

*Lecture 5: Introduction to crmPack*

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# Why we wrote `crmPack`

- More flexible than commercial software (FACTS, East, Addplan DF)
- Wish to adopt and implement new designs quickly
- Other R-packages on CRAN (`bcrm`, `dfcrm`, `CRM`) are not (easily) extensible
- `crmPack` development started in 2014
- Package is available on CRAN since 2016 (latest version: 0.2.7)

# Differences to other packages

- Allows inclusion of placebo control
- Implements bivariate methods (safety and efficacy)
- Is based on S4 classes and methods
- It can make nice plots . . .

- Identify real objects and operations on them that are interesting
- Examples:
  - ▶ Object: cdf or pdf
  - ▶ Method: mean, median, skewness,...
- Objects should know how to deal with all relevant operations
  - ▶ cdf should know how to find a mean, but not how to fit a linear model

# Class structure in `crmPack`

NextBest

- How to identify the next dose given the model and data

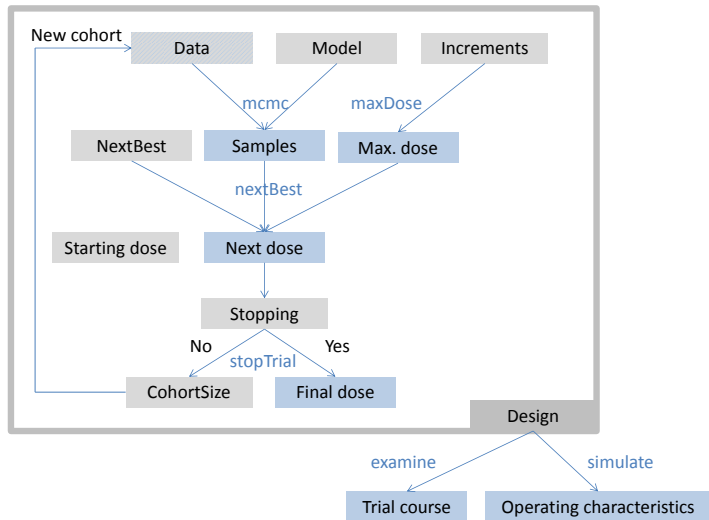
Stopping

- conditions under which the dose escalation is stopped

CohortSize

- Determines number of patients in the next cohort of the trial

# crmPack classes and methods



# Data object

Contains dose grid and current data



- Load package

```
library(crmPack)
```

```
Loading required package: ggplot2
```

```
Type crmPackHelp() to open help browser
```

```
Type crmPackExample() to open example
```

- Create dose grid

```
> doseGrid <- seq(from=40, to=200, by=10)
```

```
> doseGrid
```

```
[1] 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 200
```

# Data object

Contains dose grid and current data



- Create data object
  - ▶ 2 patients on 40mg without DLTs
  - ▶ 2 patients on 50mg with one DLT

```
> data <- Data(x=c(40,40,50,50), y=c(0,0,1,0),  
+             doseGrid=doseGrid)
```

Warning messages:

```
1: In Data(x = c(40, 40, 50, 50), y = c(0, 0, 1, 0), doseGrid = doseGrid) :  
  Used default patient IDs!
```

```
2: In Data(x = c(40, 40, 50, 50), y = c(0, 0, 1, 0), doseGrid = doseGrid) :  
  Used best guess cohort indices!
```

```
> data@ID
```

```
[1] 1 2 3 4
```

```
> data@cohort
```

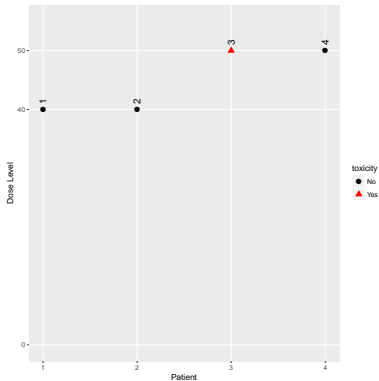
```
[1] 1 1 2 2
```



# Data object

Contains dose grid and current data

```
> plot(data)
```



Data

# Model object

## Specification

The following model for the probability of toxicity at dose  $x$ ,  $\phi(x)$ , is used:

Model

$$\text{logit}(\phi(x)) = \alpha_0 + \alpha_1 * \log(x)$$

and prior distribution is

$$(\alpha_0, \log(\alpha_1))^T \sim N \left( \begin{pmatrix} -4.47 \\ 0.0033 \end{pmatrix}, \begin{pmatrix} \sigma_0^2 & \rho\sigma_0\sigma_1 \\ \rho\sigma_0\sigma_1 & \sigma_1^2 \end{pmatrix} \right)$$

with  $\sigma_0 = 1.0278$ ,  $\sigma_1 = 1.65$ ,  $\rho = 0.5$ .

NOTE: No reference dose used!

# Model object

## Specification

Can use `LogisticLogNormal` as a readily available model

Model

```
> sigma0 <- 1.0278
> sigma1 <- 1.65
> rho <- 0.5
> cov <- matrix(c(sigma0^2, rho*sigma0*sigma1,
+                 rho*sigma0*sigma1, sigma1^2),
+               nrow=2, ncol=2)
> model <- LogisticLogNormal(mean = c(-4.47, 0.0033),
+                             cov = cov, refDose = 1)
```

# Obtaining samples

- The usual MCMC options

```
> mcmcOptions <- McmcOptions()  
  ► 10,000 burn-in iterations  
  ► step size 2  
  ► target sample size 10,000
```
- For prior use empty dataset

```
> emptyData <- Data(doseGrid=doseGrid)
```
- Run the sampler (normal distribution)

```
> set.seed(12)  
> priorSamples <- mcmc(emptyData, model,  
+                        mcmcOptions)
```

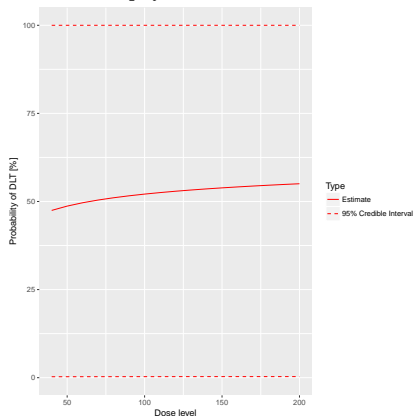
- Similar for posterior samples

```
> set.seed(92)
> postSamples <- mcmc(data, model,
+                      mcmcOptions)
```

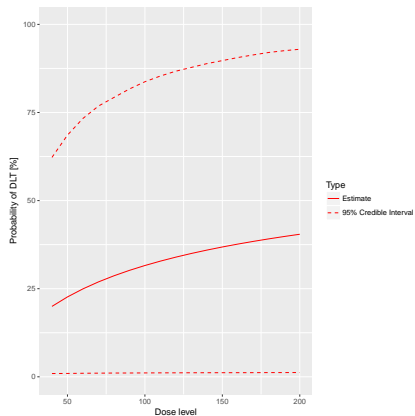
- Internally JAGS (Just another Gibbs Sampler) is used for sampling

# Plotting the models

```
> plot(priorSamples,  
+ model, emptyData)
```



```
> plot(postSamples,  
+ model, data)
```



# Increments object

## Specification

### Increments

- Define that dose can increase by 100% at most

```
> increments <- IncrementsRelative(interval=0,  
+                                increments=1)
```

► `interval` specifies the range of doses that applies to

- The increments rule is used by `maxDose` to obtain the maximum allowable dose given the current data:

```
> maxDose(increments, data)  
[1] 100
```

# NextBest object

## Specification

- In order to use the CRM with target toxicity interval from 16% to 33%, and a maximum overdosing probability of 25%, we specify<sup>1</sup>:

NextBest

```
> ncrm <- NextBestNCRM(target = c(0.16, 0.33),  
+                       overdose = c(0.33, 1),  
+                       maxOverdoseProb = 0.25)
```

- The NextBest rule is used by the nextBest function in order to calculate the dose recommendation:

```
> doseRec <- nextBest(ncrm,  
+                     doselimit = maxDose(increments, data),  
+                     postSamples, model, data)  
> doseRec$value  
[1] 40
```

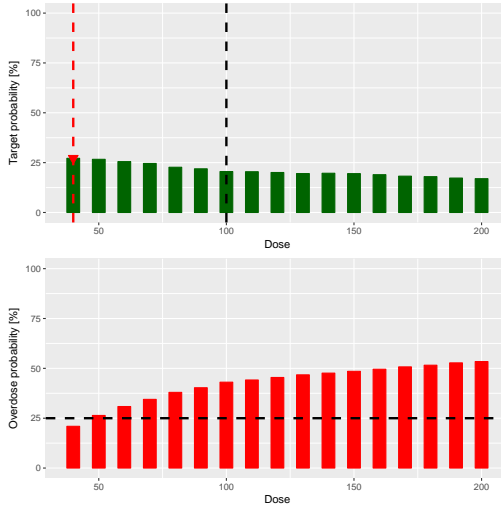
---

<sup>1</sup>NCRM called in the package, because Neuenschwander and colleagues first published this method.



# Summary plot

```
> doseRec$plot
```



# Cohort size and stopping rules

Always 3 patients in a cohort:

```
cohort <- CohortSizeConst(size = 3)
```

CohortSize

# Cohort size and stopping rules

Always 3 patients in a cohort:

```
cohort <- CohortSizeConst(size = 3)
```

CohortSize

We would like to stop the trial if:

- there are at least 2 cohorts at the MTD and
- at least 6 cohorts in total

Stopping

OR the maximum sample size of 30 has been reached.

```
> stop1 <- StoppingCohortsNearDose(nCohorts = 2, percentage = 0)
# percentage specifies doses that are considered similar
> stop2 <- StoppingMinCohorts(nCohorts = 6)
> stop3 <- StoppingMinPatients(nPatients = 30)
> stopRule <- (stop1 & stop2) | stop3
```

We can check if stopping criterion is fulfilled using `stopTrial`

```
stopTrial(stopRule, doseRec$value, postSamples, model, data)
[1] FALSE
attr(,"message")
attr(,"message")[[1]]
attr(,"message")[[1]][[1]]
[1] "1 cohorts lie within 0% of the next best dose 40.
    This is below the required 2 cohorts"

attr(,"message")[[1]][[2]]
[1] "Number of cohorts is 2 and thus below the prespecified
    minimum number 6"

attr(,"message")[[2]]
[1] "Number of patients is 4 and thus below the prespecified minimum
    number 30"
```

- We bundle all parts of the design in the Design object:

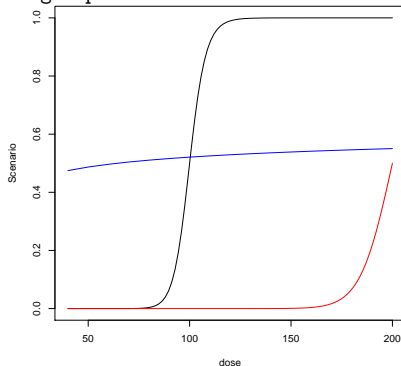
```
> design <- Design(model=model, stopping=stopRule,  
+                 increments=increments,  
+                 nextBest=ncrm,  
+                 cohortSize=cohort,  
+                 data=emptyData,  
+                 startingDose=40)
```

- Scenario is given in terms of ED50 and slope:

```
> scenario <- function(dose, ED50, alpha1){  
+   alpha0 <- qlogis(0.5)-alpha1*log(ED50)  
+   model@prob(dose,alpha0=alpha0, alpha1 = alpha1)  
+ }
```

# Scenarios

```
> curve(scenario(dose, ED50=100, alpha1=25), from=40, to=200,  
+       xname="dose",ylab="Scenario") # Scenario 1  
> curve(scenario(dose, ED50=200, alpha1=25), from=40, to=200,  
+       xname="dose", add=TRUE, col="red") # Scenario 2  
> # Prior model  
> lines(fit(priorSamples, model, emptyData), col="blue")  
# Use fit function to get prior model fit
```



- Generate 10 hypothetical trials ( $\sim 10$  secs)

```
> sims1 <- simulate(design, nsim=10,  
+   seed = 456, truth=scenario, args=list(ED50=100, alpha1=25),  
+   mcmcOptions = mcmcOptions,  
+   parallel = TRUE)
```

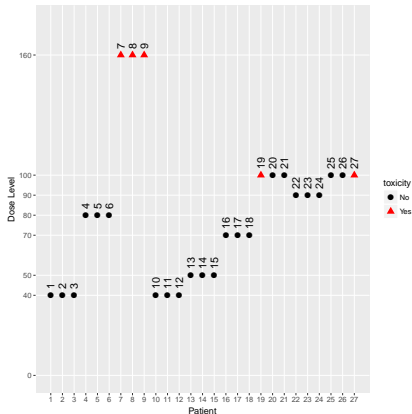
- Analogously for the second scenario:

```
> sims2 <- simulate(design, nsim=10,  
+   seed = 457, truth=scenario, args=list(ED50=200, alpha1=25),  
+   mcmcOptions = mcmcOptions,  
+   parallel = TRUE)
```

# Plotting simulated trials

```
plot(sims1@data[[3]])
```

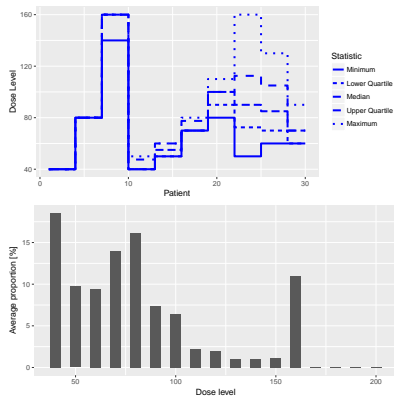
# 3rd run Scenario



1

```
plot(sims1)
```

# Summary





# Summarizing simulations

```
> summary(sims1, truth=scenario,  
+ target=ncrm@target, ED50=100, alpha1=25)  
Summary of 10 simulations
```

Target toxicity interval was 16, 33 %

Target dose interval corresponding to this was 93.6, 97.2

Intervals are corresponding to 10 and 90 % quantiles

Number of patients overall : mean 28 (24, 30)

Number of patients treated above target tox interval : mean 7 (6, 9)

Proportions of DLTs in the trials : mean 21 % (18 %, 24 %)

Mean toxicity risks for the patients on active : mean 22 % (18 %, 26 %)

Doses selected as MTD : mean 79 (68, 100)

True toxicity at doses selected : mean 11 % (0 %, 50 %)

Proportion of trials selecting target MTD: 0 %

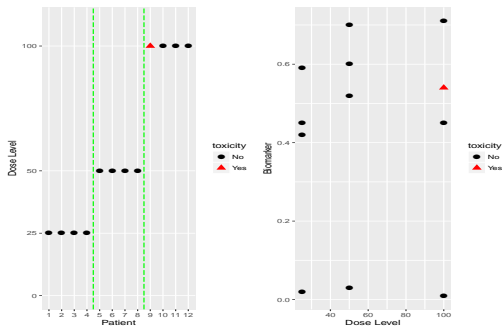
Dose most often selected as MTD: 70

Observed toxicity rate at dose most often selected: 0 %

Fitted toxicity rate at dose most often selected : mean 21 % (18 %, 23 %)

# Dual Endpoints

```
> PL <- 0.001
> data2 <- DataDual(x = c(PL, 25, 25, 25, PL, 50, 50, 50,
+                          PL, 100, 100, 100),
+                  y = c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0),
+                  w = c(0.02, 0.42, 0.59, 0.45, 0.03, 0.7, 0.6, 0.52,
+                      0.01, 0.71, 0.54, 0.45),
+                  cohort = c(1, 1, 1, 1, 2, 2, 2, 3, 3, 3, 3),
+                  doseGrid = c(PL, seq(25, 300, 25)), ID = 1:12, placebo = TRUE)
> plot(data2, blind=TRUE)
```



# Two models and a gain function

## Safety and efficacy model

```
> emptydata2 <- DataDual(doseGrid = data2@doseGrid, placebo = TRUE)
> DLTmodel <- LogisticIndepBeta(binDLE = c(1.05, 1.8),
+                               DLEweights = c(3, 3), DLEdose = c(25, 300),
+                               data = emptydata2)
> Effmodel <- Effloglog(Eff = c(1.223, 2.513), Effdose = c(25, 300),
+                        nu = c(a = 1, b = 0.025), data = emptydata2, c = 2)
```

Gain function depends on safety and efficacy parameters which will be estimated using posterior modal estimates

```
> newDLTmodel <- update(object = DLTmodel, data = data2)
> newEffmodel <- update(object = Effmodel, data = data2)
> GainNextBest <- NextBestMaxGain(DLEDuringTrialtarget = 0.35,
+                                 DLEEndOfTrialtarget = 0.3)
```

- A more advanced increment rule

```
> myIncrements <- IncrementsRelative(intervals = c(0, 125, 200),  
+                                     increments = c(1, 0.75, 0.5))
```

A maximum increase of 100% for doses below 125 mg, 75% for doses in the range from 125 mg to 200 mg, and 50% for doses equal or above 200 mg

- Identify maximum next dose

```
> nextMaxDose <- maxDose(myIncrements, data2)  
> nextMaxDose  
[1] 200
```

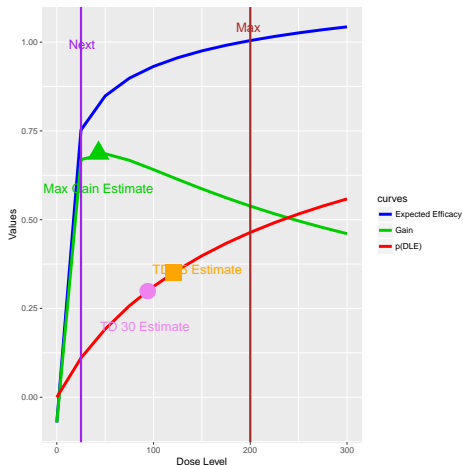
## Finding the next dose

```
> doseRecGain <- nextBest(GainNextBest, doselimit = nextMaxDose,  
+                          model = newDLTmodel, Effmodel = newEffmodel,  
+                          data = data2)  
> nextDoseVal <- doseRecGain$nextdose  
> nextDoseVal  
[1] 25
```

- After new data are observed `newDLTmodel` and `newEffmodel` need to be updated
- No MCMC used here

# Plotting the decision

```
> doseRecGain$plot
```



- Stop when maximum number of patients are observed
- The optimal dose can be estimated precisely enough

```
> stop4 <- StoppingGstarCIRatio(targetRatio = 5,  
+                               targetEndOfTrial = GainNextBest@DLEndOfTrialtarget)  
> myStoppingDual <- stop3 | stop4
```

- Define design object

```
> design2 <- DualResponsesDesign(nextBest = GainNextBest,  
+                               model = DLTmodel, Effmodel = Effmodel,  
+                               data = emptydata2,  
+                               stopping = myStoppingDual,  
+                               increments = myIncrements,  
+                               cohortSize = cohort, startingDose = 25)
```

- Define scenarios

```
> trueDLT<- function(dose){DLTmodel@prob(dose,  
+                                       phi1 = -53, phi2 = 10)}  
> trueEff<- function(dose){Effmodel@ExpEff(dose,  
+                                       theta1 = -4.8, theta2 = 3.7)}  
> trueGain <- function(dose){trueEff(dose) * (1 - trueDLT(dose))}
```



- Simulate

```
> sims3 <- simulate(object = design2, args = NULL,  
+                   trueDLE = trueDLT, trueEff = trueEff,  
+                   trueNu = 1 / 0.025, nsim = 100,  
+                   seed = 19, parallel = TRUE)
```

- Summarize and plot

```
> mean(sims3@FinalOptimalDose)  
[1] 149.0867  
> summary(sims3,trueDLE=trueDLT,trueEff=trueEff)  
> plot(sims3@data[[90]])  
> plot(sims3)
```

# Simulation plots

