

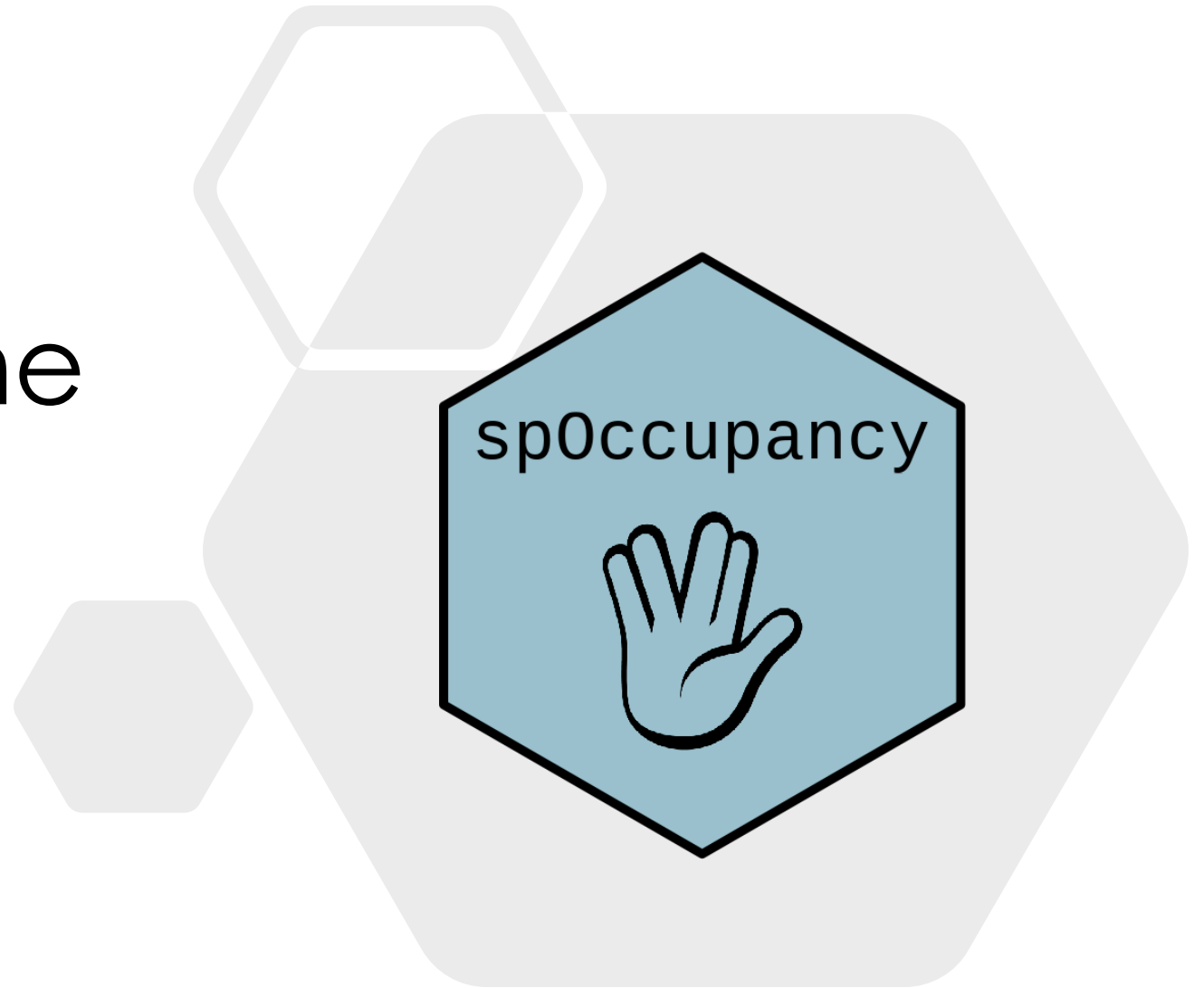
Spatially-explicit occupancy modeling with the spOccupancy R package

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Michigan State University

TWS 2023

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Course Website

- <https://doserjef.github.io/TWS23-spOccupancy/>
- Single-species non-spatial/spatial occupancy models
- Multi-species non-spatial/spatial occupancy models
- Multi-season non-spatial/spatial occupancy models

Occupancy Models

Ecological Motivation

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 - Spatial autocorrelation

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Presence-absence data

Site	Survey
1	1
2	0
3	1
4	1
5	0
6	0

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Assuming no false positives, if we detect the species, we know it exists at the site

An arrow originates from the text block and points to the first row of the table, specifically to the 'Survey' column value '1' for 'Site' 1.

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A 0 (or nondetection) could mean:

1. The species does not exist at the site
2. The species exists at the site, but we failed to detect it.

Occupancy modeling

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- **Fundamental concept:** obtain "repeated surveys" at a given site during some period of closure
 - Key assumption: the species does not move in or out of the site during this time period
- "Repeated surveys" usually come in the form of multiple visits to a site during some time period, but can also take different forms (e.g., multiple observers, spatial replicates)

Data for occupancy modeling

Detection-nondetection matrix (y)

$k \longrightarrow$

$j \downarrow$

Site	Survey 1	Survey 2	Survey 3	Survey 4
1	1	0	0	1
2	0	0	0	0
3	1	1	0	NA
4	1	NA	0	NA
5	0	1	1	1
6	0	0	0	1

$y_{j,k}$

- J sites with K_j replicate surveys at each site j
- Assume no false positives
- Any variation in the observed data values across surveys is assumed to arise from imperfect detection.

Occupancy model structure

- Two distinct sub-models
 1. Model occupancy probability as a function of site-level covariates

Occupancy model structure

- Two distinct sub-models
 1. Model occupancy probability as a function of site-level covariates
 2. Model detection probability as a function of site and/or survey-level covariates
 - Can only detect a species if it truly occupies a site
 - Detection probability is modeled "conditional" on true occupancy

Single-species occupancy model

Occupancy (ecological) sub-model

$j = 1, \dots, J$ (site)

$k = 1, \dots, K_j$ (replicate)

$$z_j \sim \text{Bernoulli}(\psi_j)$$

$$\text{logit}(\psi_j) = \beta_1 + \beta_2 \cdot X_{2,j} + \dots + \beta_r \cdot X_{r,j}$$

z_j True occurrence of the species at site j

ψ_j Occurrence probability at site j

$X_{r,j}$ The r th covariate at site j (e.g., habitat variable)

Single-species occupancy model

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$y_{j,k}$ Detection-nondetection data at site j during replicate k

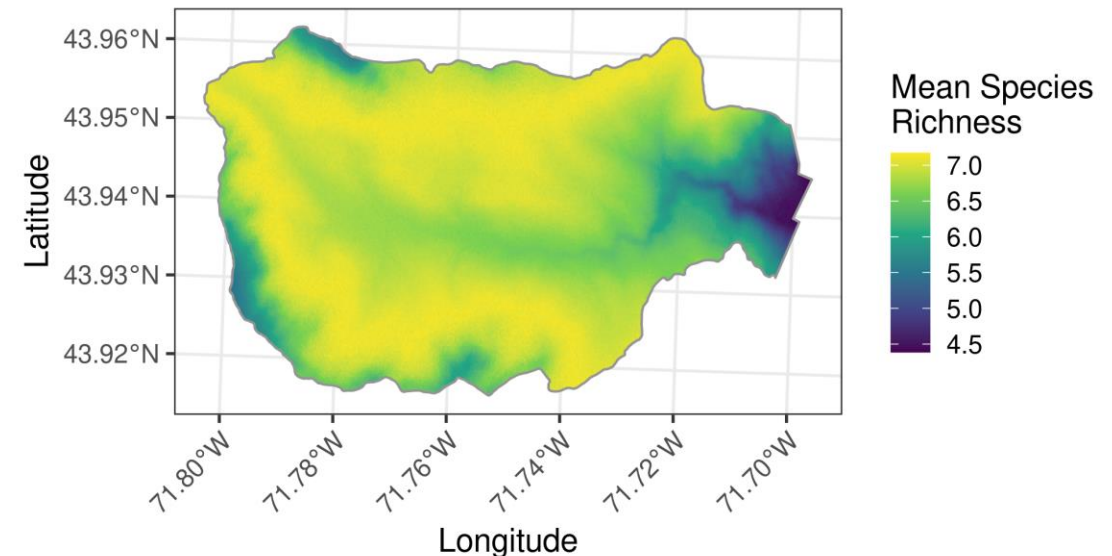
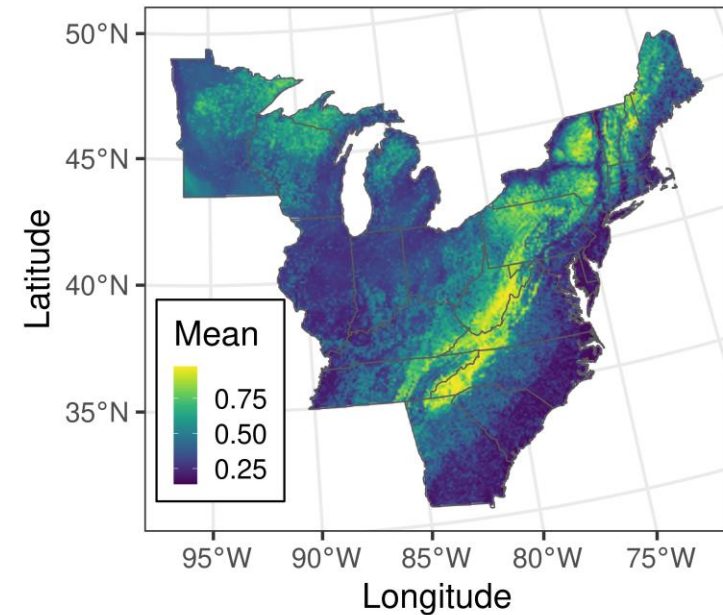
$p_{j,k}$ Detection probability at site j during replicate k

$V_{r,j,k}$ Covariate affecting detection at site j during replicate k

Spatial Occupancy Models

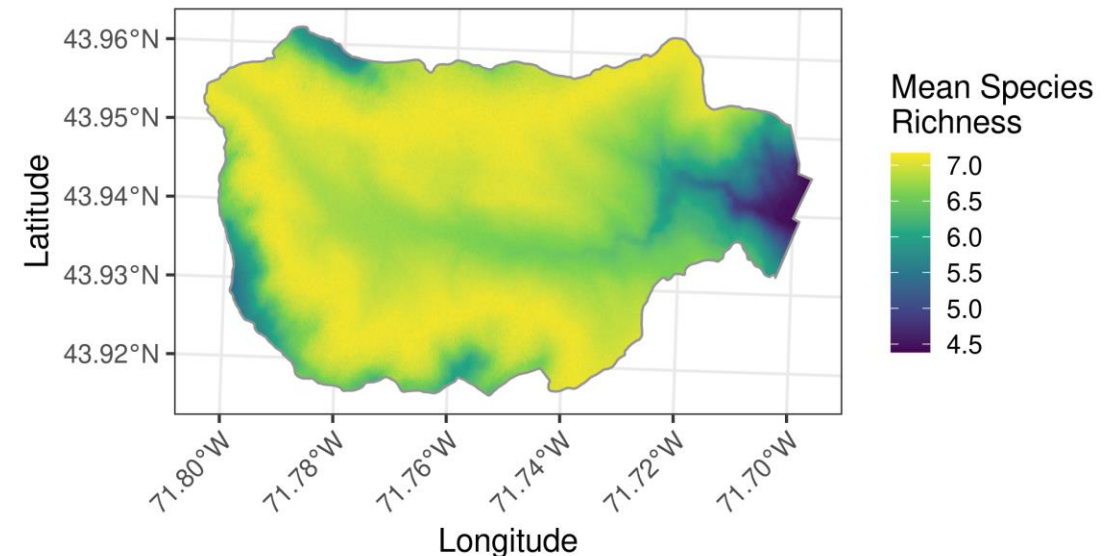
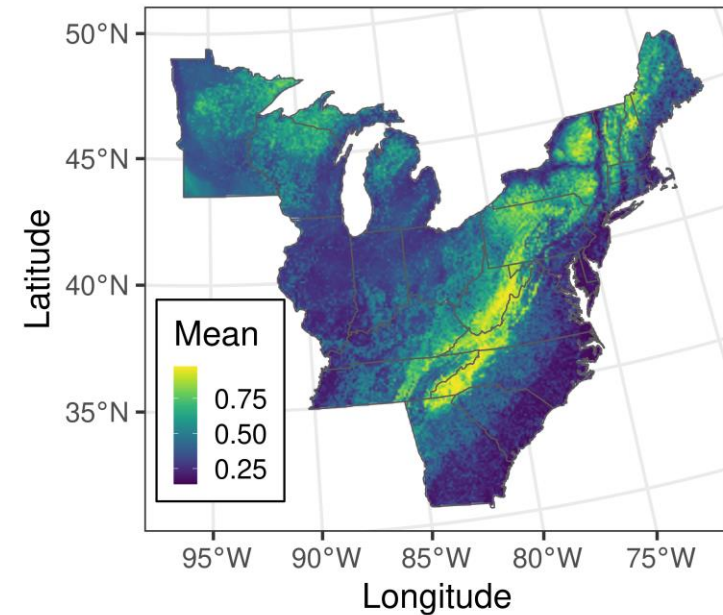
Spatial autocorrelation

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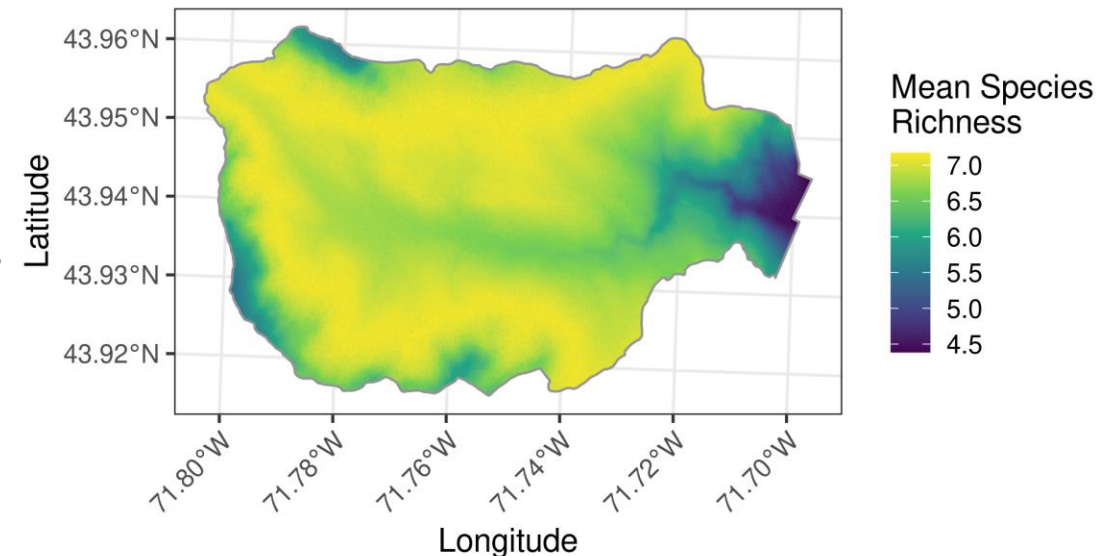
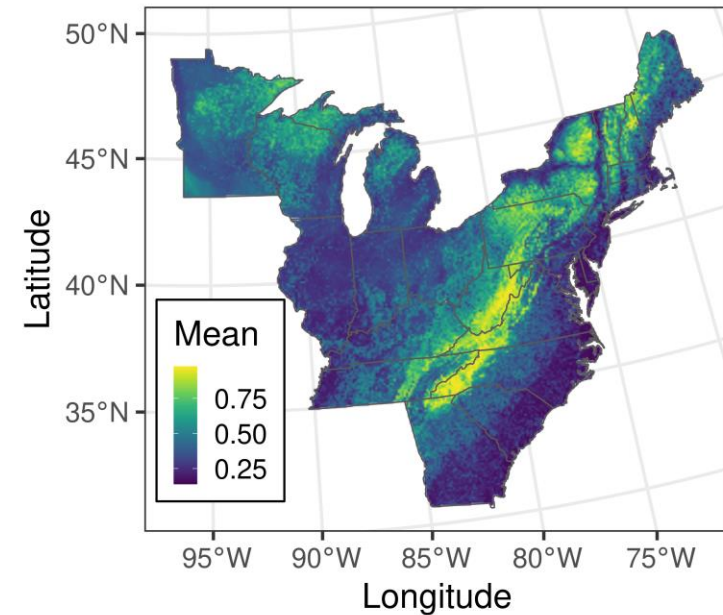
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- What leads to spatial autocorrelation in species distributions?
 - Environmental drivers, habitat requirements
 - Biotic factors (dispersal, conspecific attraction)
- Initial approach: attempt to explain spatial variation in species distributions with covariates (e.g., forest cover, temperature, elevation)



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Residual spatial autocorrelation

- Spatial correlation in occupancy probability *after* including spatial covariates
- Often arises from missing/unavailable covariates
- Can lead to bias if unaddressed
- Account for using spatial random effects
 - Each site has a local adjustment in occupancy probability
 - The local adjustments are given a spatial structure
 - Estimated parameters: spatial variance and spatial decay

Single-species spatial occupancy model

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- spOccupancy supports four covariance functions: **exponential**, Gaussian, spherical, Matérn
- Covariance between site A and site B using exponential covariance function:

$$\Sigma(d_{A,B}, \sigma^2, \phi) = \sigma^2 \exp(-\phi d_{A,B})$$

Intuition on spatial covariance

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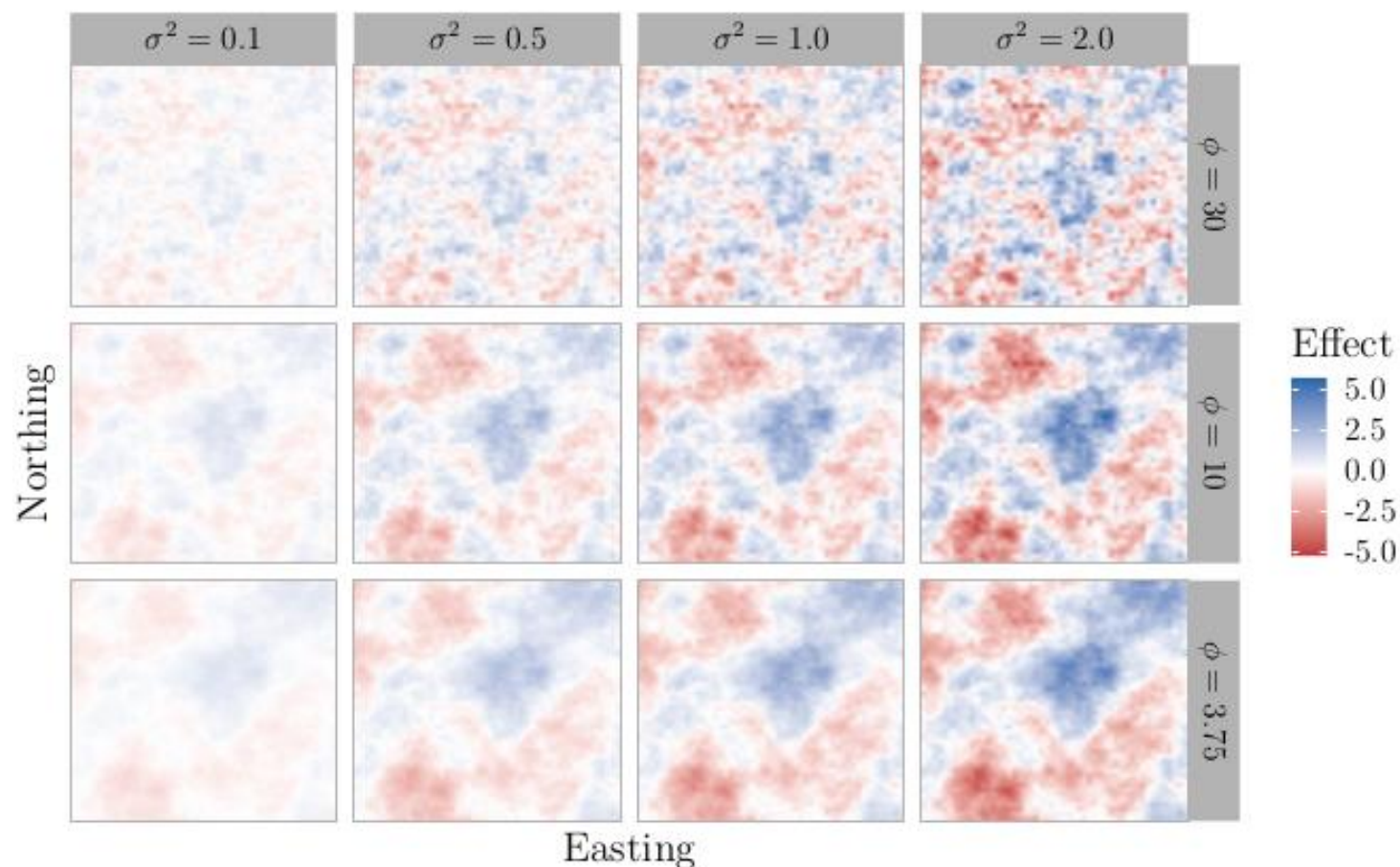
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- σ^2 Spatial variance. Controls magnitude of random effects
- ϕ Spatial decay. Controls how quickly the correlation between sites decays across space
- $\frac{3}{\phi}$ "Effective spatial range" when using an exponential covariance function. This is the distance at which the spatial correlation between two sites is essentially negligible (0.05)

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- Flexible, non-parametric approach to account for spatial autocorrelation
- But... becomes extremely slow as the number of sites increases
- Not practical for data sets with hundreds of data points, let alone thousands.
- Computational bottleneck: dealing with a large, dense $J \times J$ matrix
- Need a more efficient approach...

Nearest Neighbor Gaussian Processes (NNGPs)

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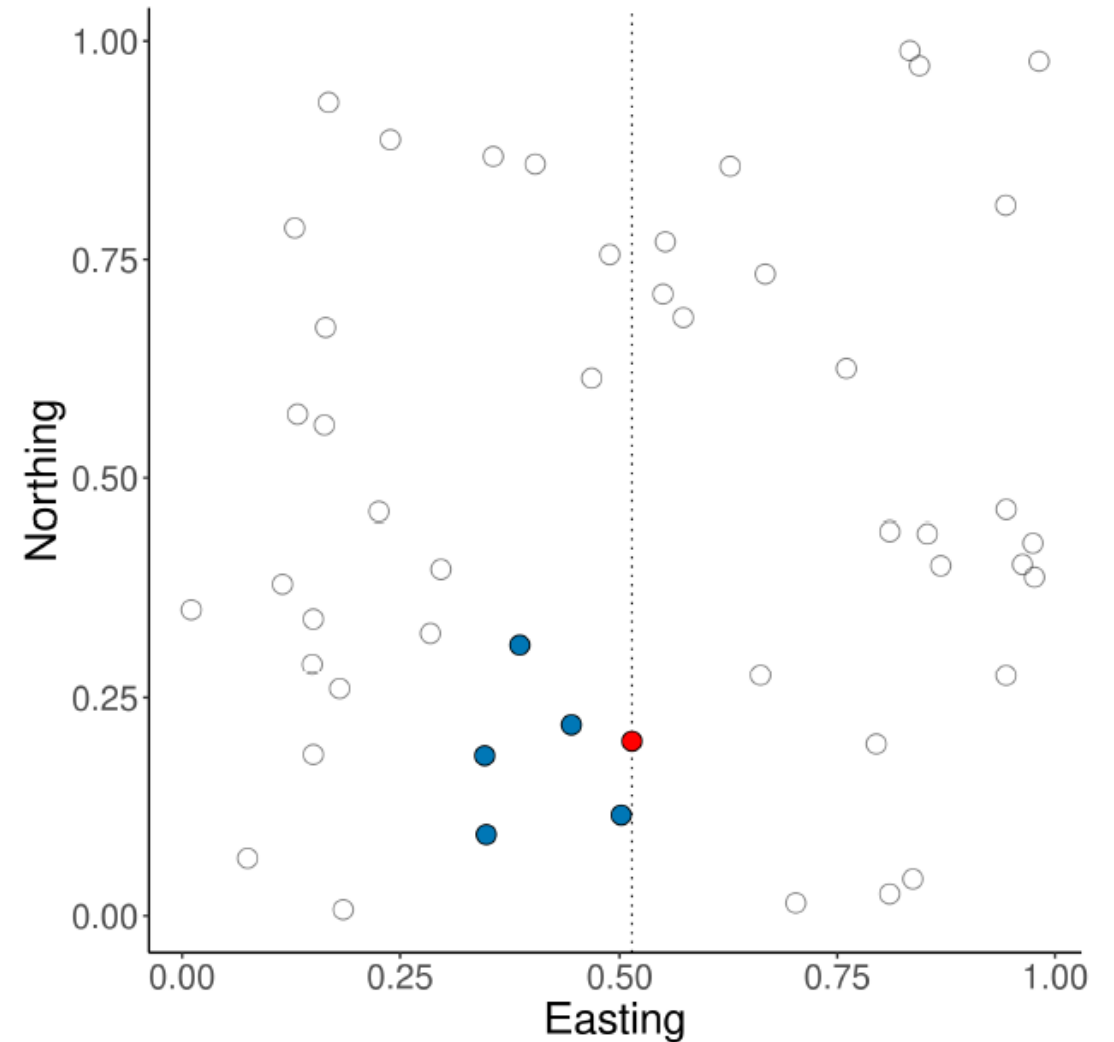
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 3. The spatial random effect at each site only depends on values of its m nearest neighbors and is conditionally independent of all other values

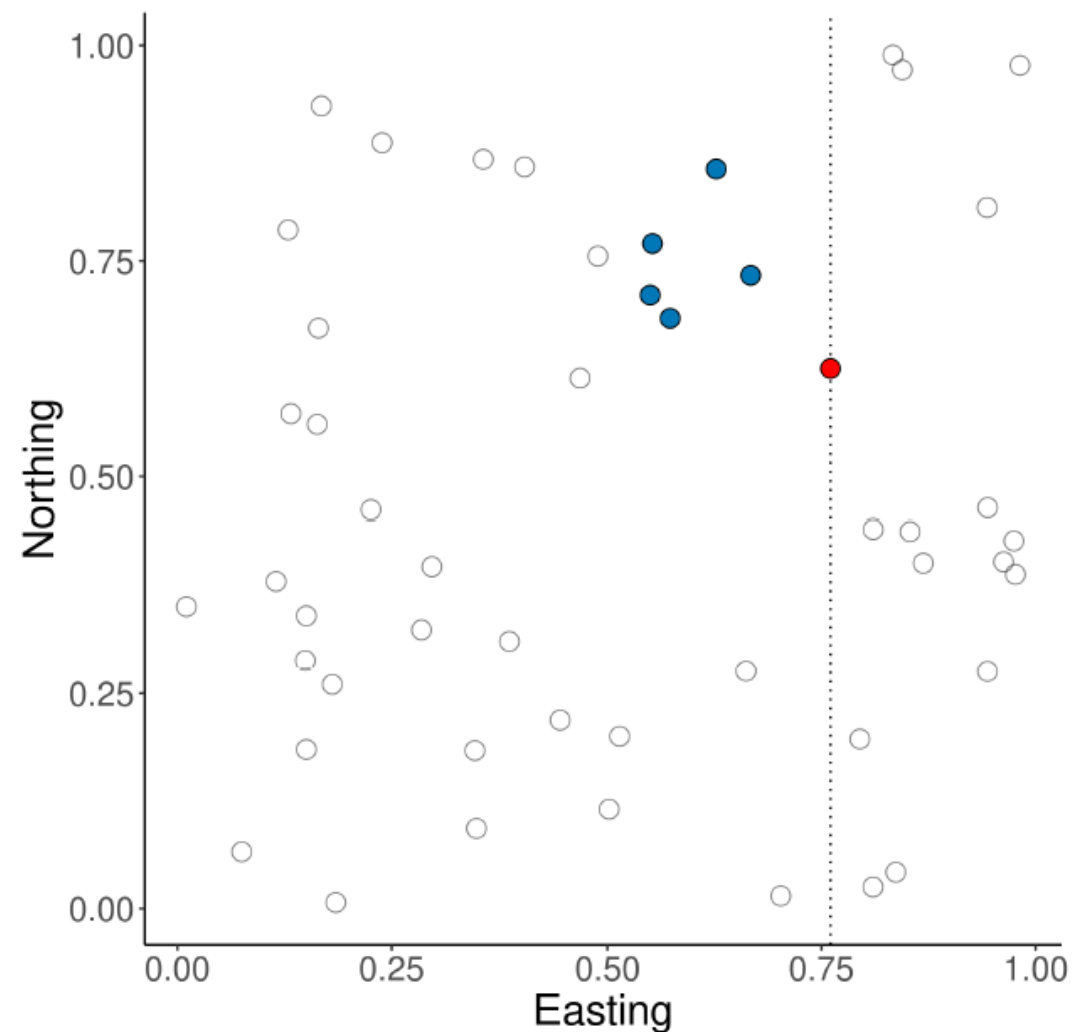
Choosing the neighbors

- spOccupancy orders sites along the horizontal axis (i.e., Easting)
- Example: NNGP with 5 neighbors
- Red point denotes the current site
- Blue points denote sites in the "neighbor set"



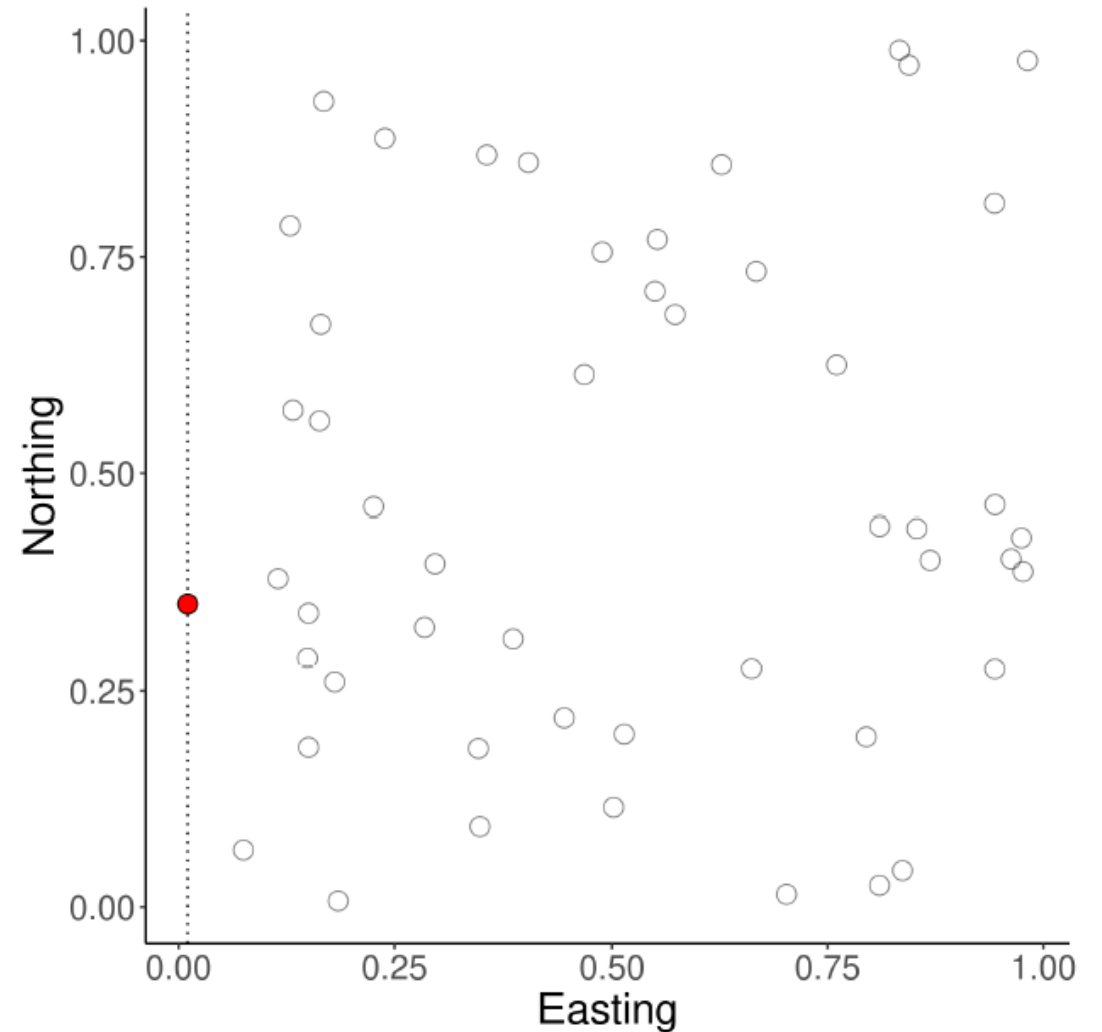
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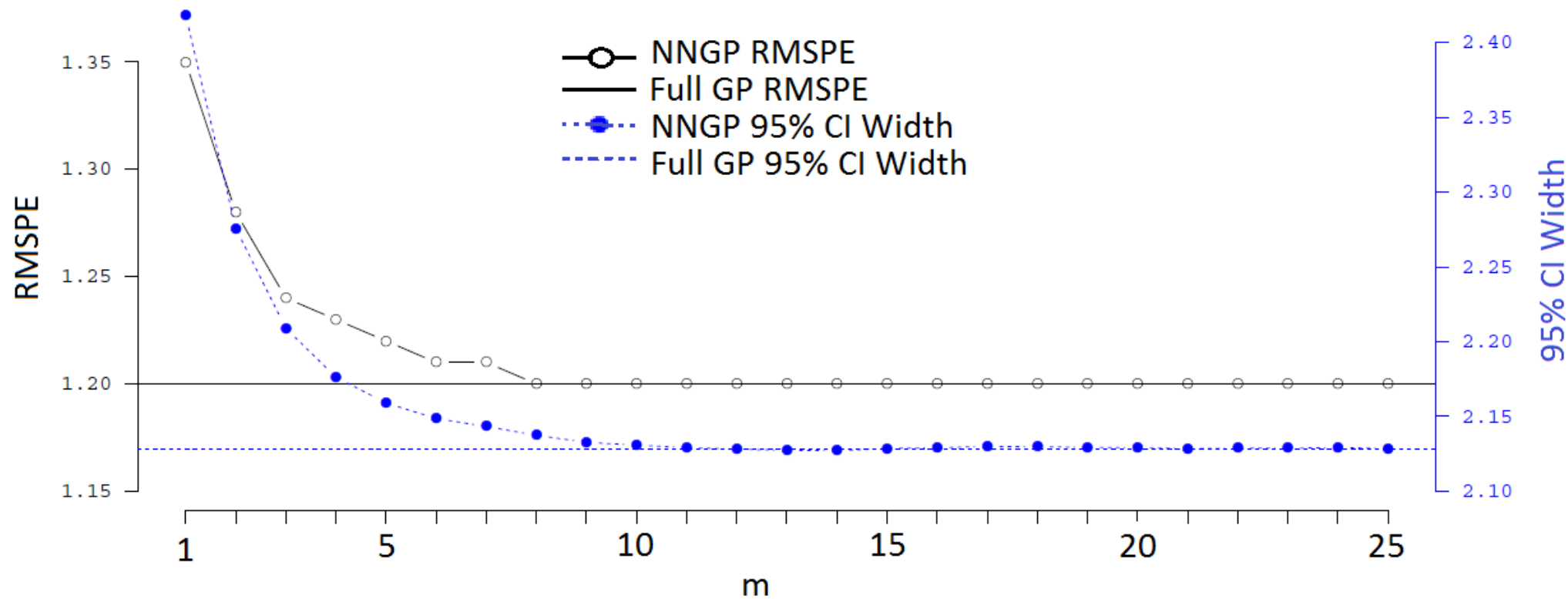


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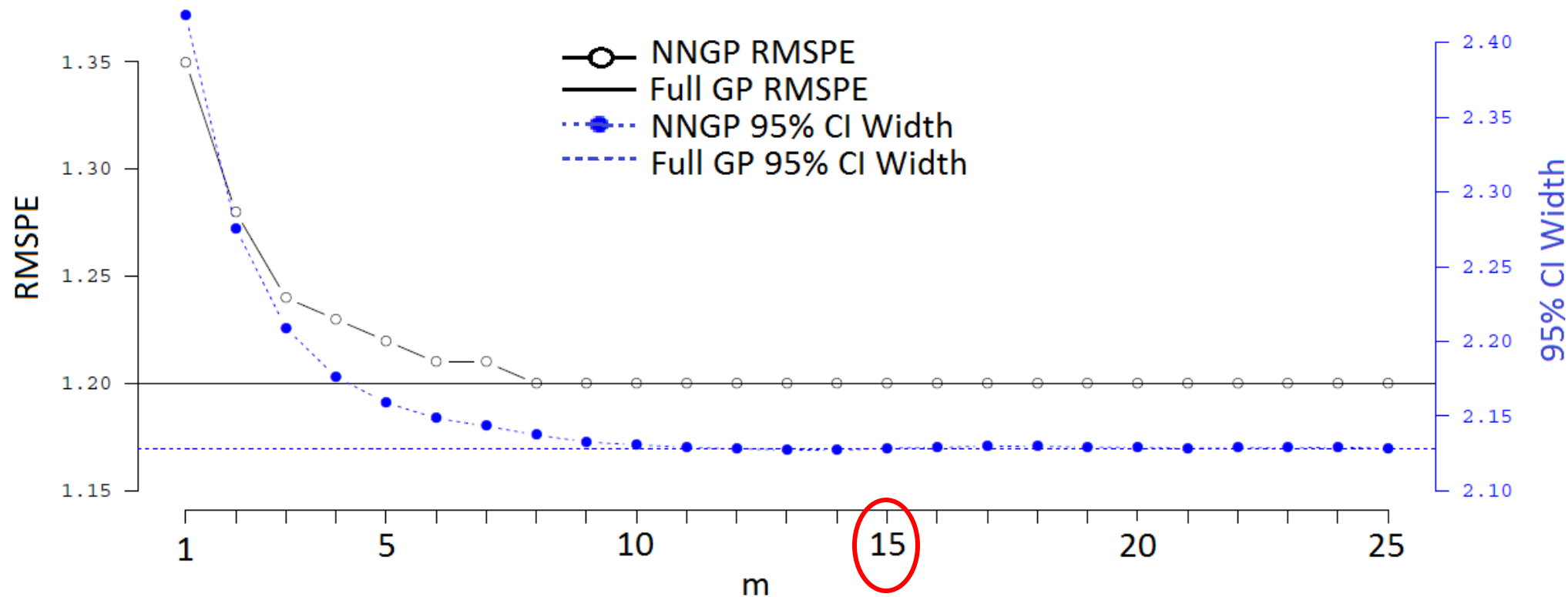
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How many neighbors?



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- $m=15$ neighbors is often adequate (spOccupancy default)
- Can compare smaller m using WAIC

Pros/cons of spatial models

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- More accurate species distribution maps (improved predictions)
- More accurate uncertainty estimates
- Provide insights on underlying drivers
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Cons

- Slower (but NNGPs help a lot!)
- Spatial confounding (Hanks et al. 2015, Mäkinen et al. 2022)
- More data hungry

Bayesian Basics

Why Bayesian for spatial occupancy models?

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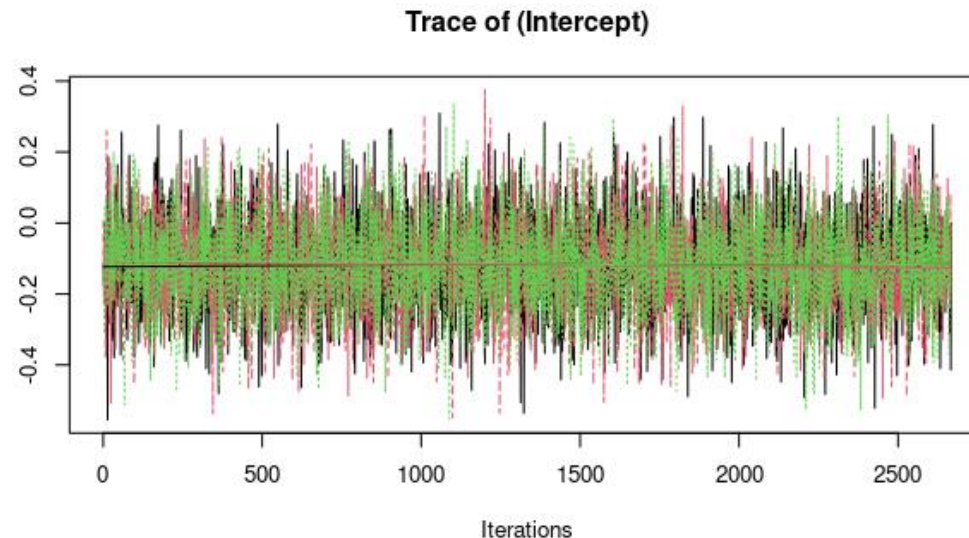
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Why Bayesian for spatial occupancy models?

1. Interpretation
2. More flexible to accommodate spatial autocorrelation
3. Easy to extend to multispecies frameworks/integrate multiple data sources
4. Fully propagate uncertainty in all estimates (and derived quantities)

Bayesian basics: what to know to get started in spOccupancy

- Markov chain Monte Carlo (MCMC)
- MCMC chains eventually converge to a posterior distribution
 - Assess convergence by running multiple chains with different starting values



MCMC Step 1: Specify prior distributions

$$\beta \sim \text{Normal}(\mu_\beta, \sigma_\beta^2)$$

$$\alpha \sim \text{Normal}(\mu_\alpha, \sigma_\alpha^2)$$

$$\sigma^2 \sim \text{Inverse-Gamma}(a_{\sigma^2}, b_{\sigma^2})$$

$$\phi \sim \text{Uniform}(a_\phi, b_\phi)$$

MCMC Step 2: Set initial values

- Set different values for each chain
- spOccupancy will set initial values by default
- Can be important for more complicated models (e.g., spatially-varying coefficient models)

MCMC Step 3: Propose new value

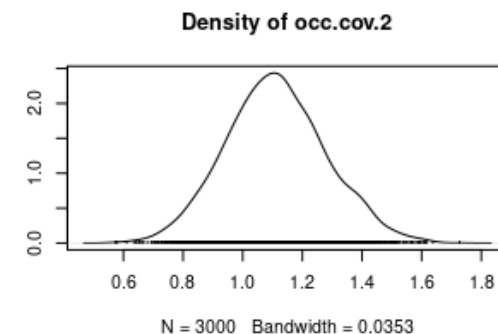
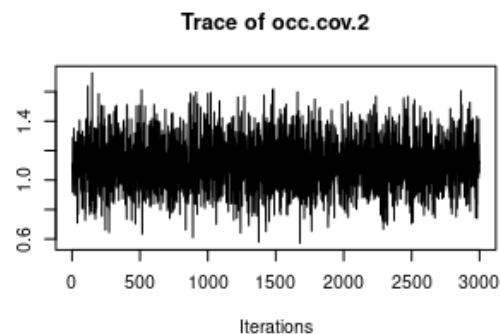
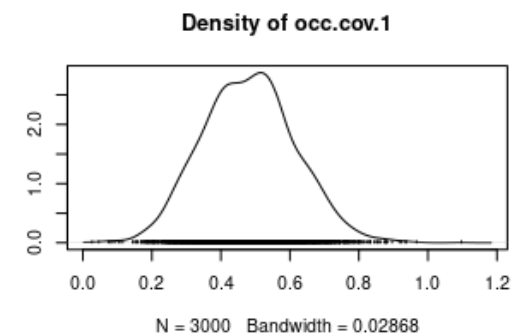
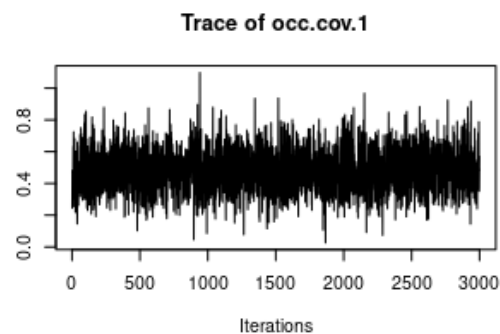
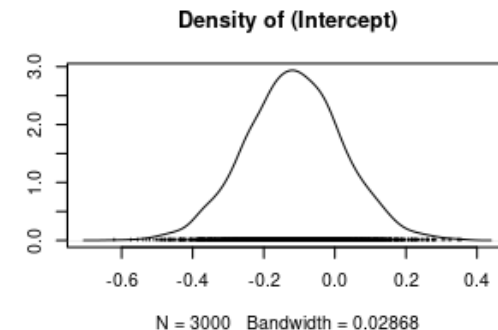
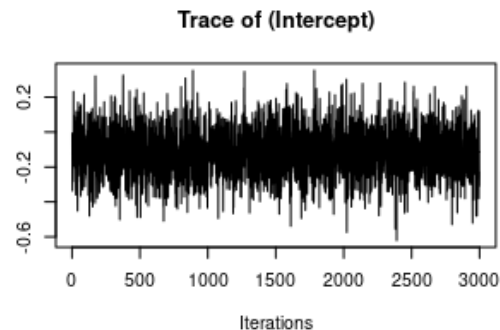
- Propose a new value for each parameter one at a time based on a statistical algorithm.
- For some parameters, we always accept the proposed value because our algorithm is efficient.
- For parameters with less efficient algorithms, we will accept the new value with some probability p .

MCMC Step 4: Repeat

- Repeat step 3 "many" times to generate a set of samples from the posterior distribution for each parameter.

MCMC Step 5: Summarize

- Point estimate: mean, median, mode
- Uncertainty: 95% credible (e.g., 2.5 and 97.5% quantiles of the samples)



What do you need to specify?

- Prior distribution (optional)
- Initial values (optional)
- Number of samples/iterations
- Burn-in: initial part of the MCMC chain that we throw away
- Thinning rate: how often do you want to save a sample?

spOccupancy

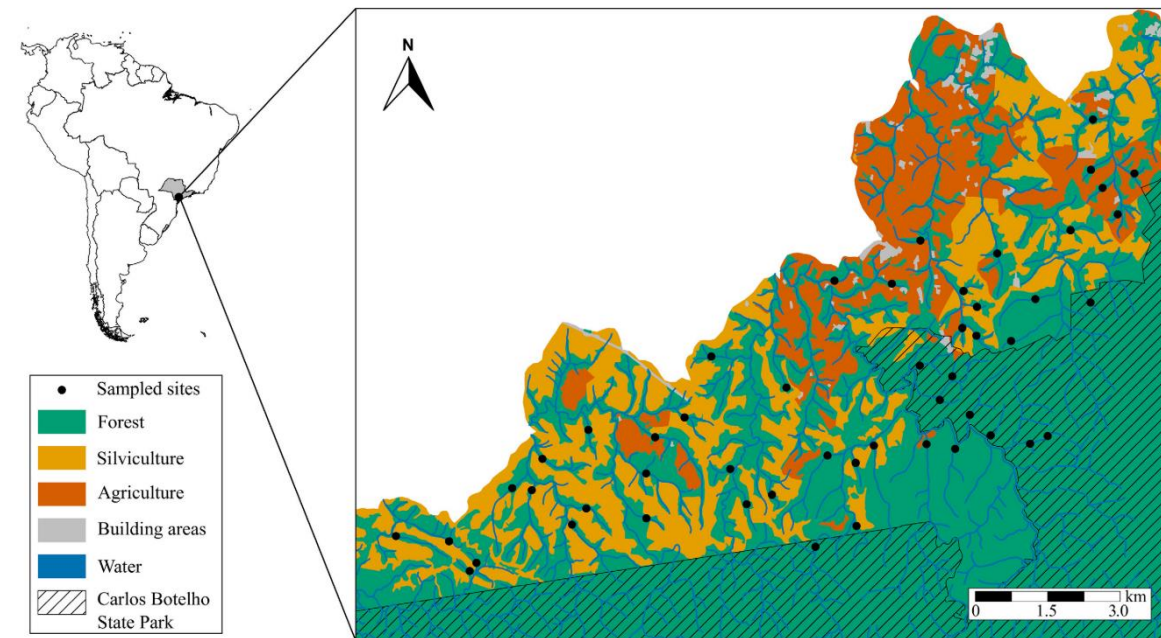
spOccupancy



- Designed to fit Bayesian single-species and multi-species occupancy models
- Efficient options (NNGPs) to account for spatial autocorrelation
- Workflow completely in R (no Bayesian programming languages necessary)
- PGOcc -> single-species occupancy model
- spPGOcc -> spatial single-species occupancy model
- The "PG" stands for Pólya-Gamma (Polson et al. 2013)

Exercise 1: Amphibian occupancy in Brazil

- Data from [Ribeiro Jr. Et al \(2018\) Eco Apps](#)
- 50 sites along a gradient of landscape characteristics
- 3 ARU recordings at each site (repeat surveys/visits)
- 36 amphibian species analyzed
- Focus on *Crossodactylus caramaschii*



spOccupancy workflow

1. Data simulation/prep
2. Model fitting
3. Model validation
4. Model comparison
5. Posterior summaries
6. Prediction

Multi-species occupancy models

Multi-species detection-nondetection data

- Many types of multi-species inventories:
 - Point count surveys
 - Acoustic recording units
 - Camera traps
 - Citizen science checklists

Species	Site 1	Site 2	Site 3	Site 4
A	1	0	0	1
B	0	0	1	0
C	1	1	0	0
D	1	0	0	0
E	0	1	1	1
F	0	0	0	1

Multi-species detection-nondetection data

Visit 1				Visit 2				Visit 3				
								Species	Site 1	Site 2	Site 3	Site 4
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B	0	0		B	0	NA		D	0	0	0	NA
C	1	1		C	1	NA		E	0	0	1	NA
D	1	0		D	0	NA		F	0	0	0	NA
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F	0	0		F	0	NA		0	0			
							</					

Ecological Motivation

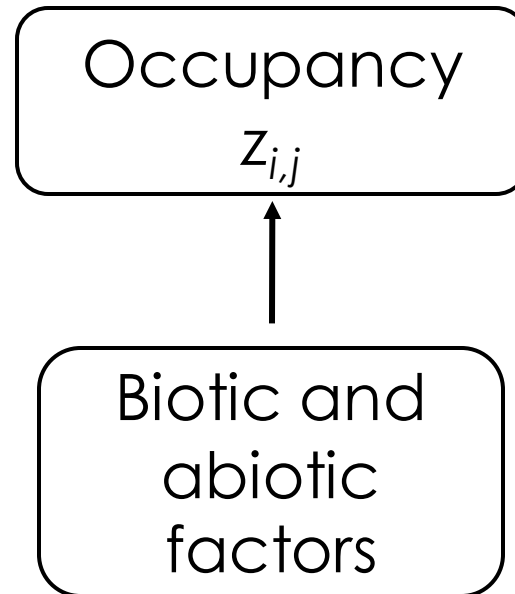
- Management has historically focused on individual species.
- Increased interest in multi-species management
- Biodiversity conservation
- Species are not independent of each other

Statistical Motivation

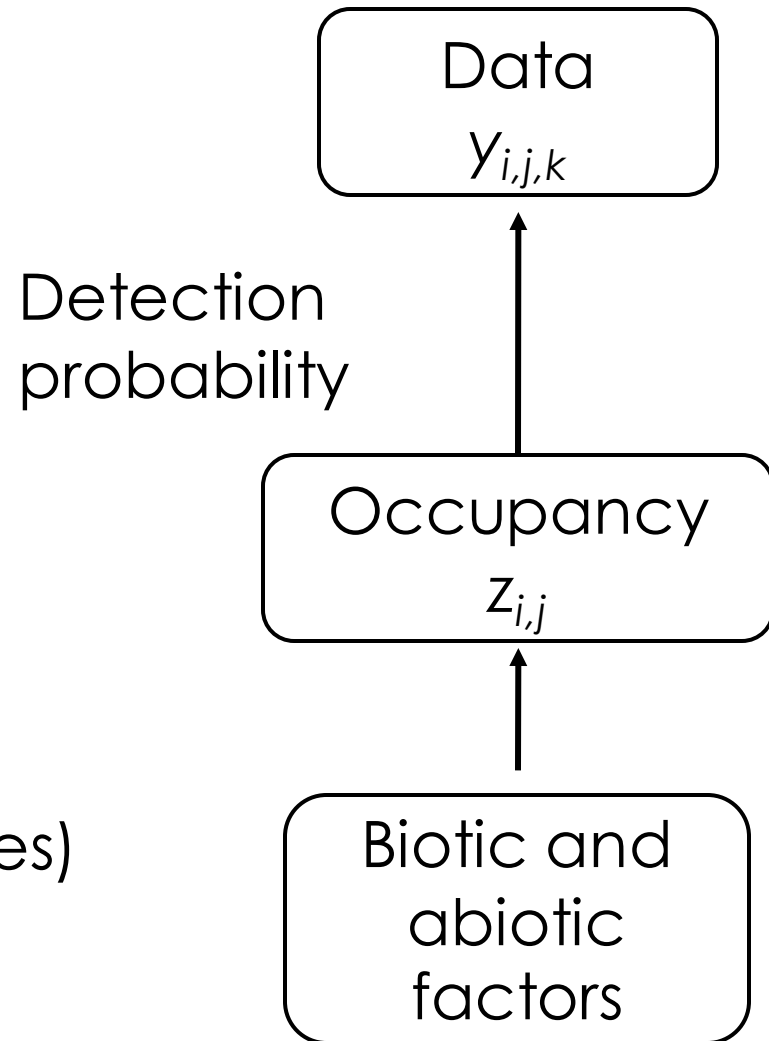
- Species of interest (e.g., SGCNs) are often the rarest species.
- Occupancy models are hard to fit when the number of detections is low
- Multi-species models can:
 - Improve ability to model rare species
 - Provide inference at both species and community-levels
 - Use information from other species to improve species-specific estimates

Multi-species occupancy model

$i = 1, \dots, N$ (species)
 $j = 1, \dots, J$ (sites)
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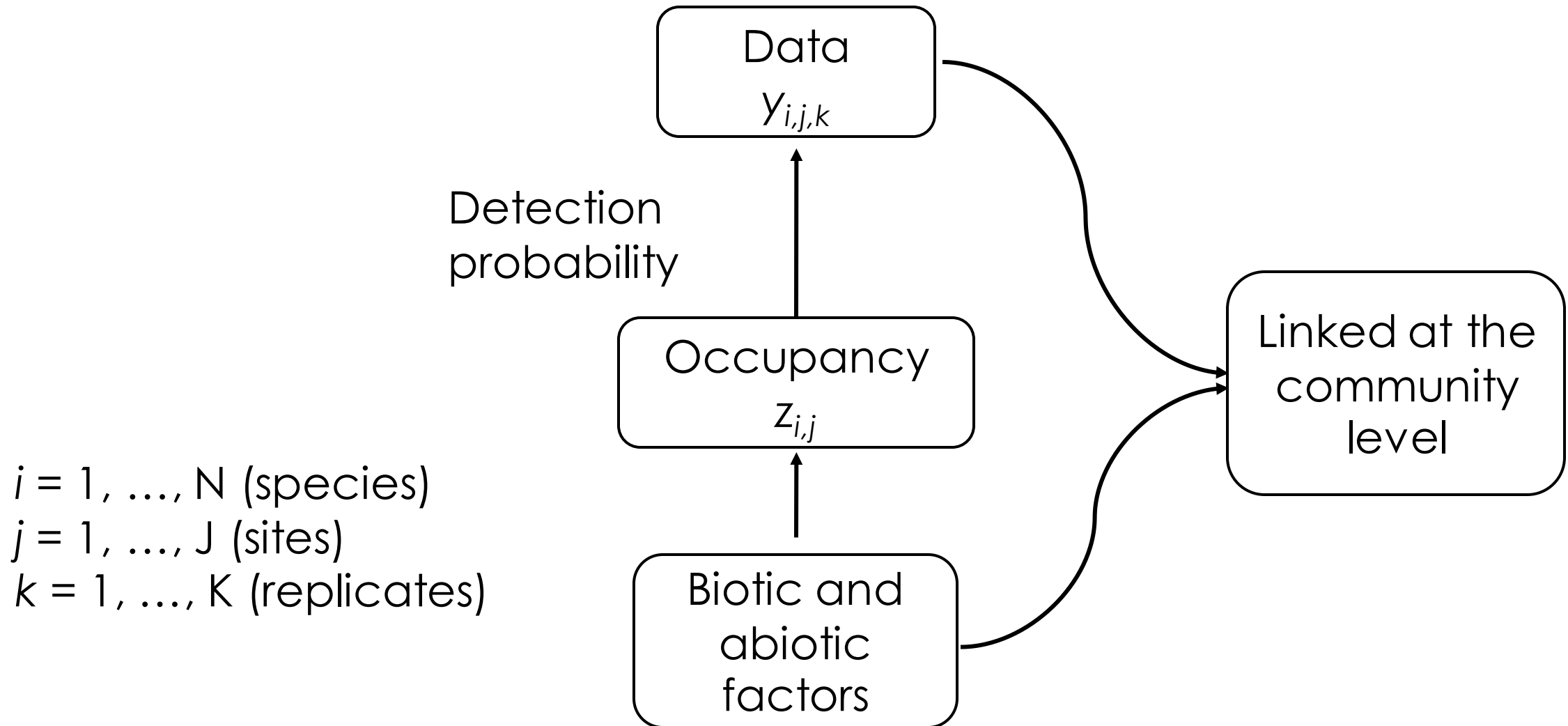


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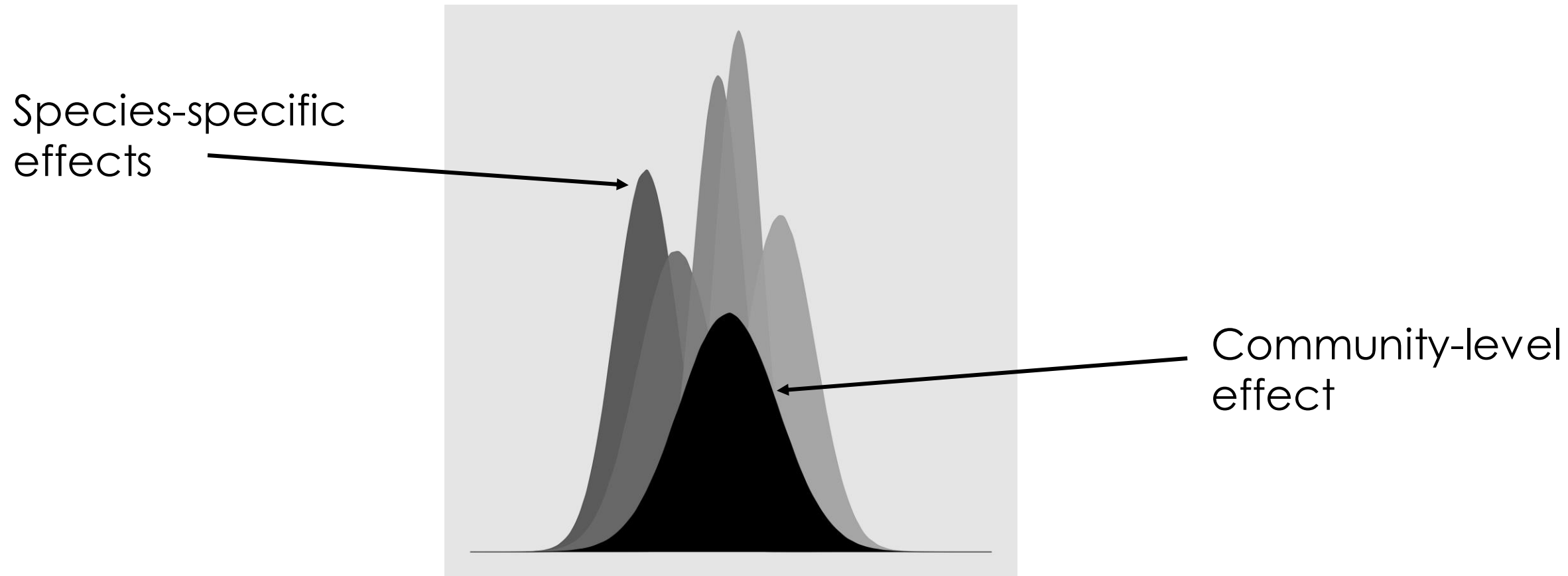
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Multi-species occupancy model



Species-specific and community effects



Species-specific effects are drawn from a common, community-level distribution

Multi-species occupancy model

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$$\beta_{r,i} \sim \text{Normal}(\mu_{\beta_r}, \tau_{\beta,r}^2)$$

Detection (observation) sub-model

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Multi-species occupancy model

Occupancy (ecological) sub-model

$i = 1, \dots, N$ (species)

$j = 1, \dots, J$ (sites)

$k = 1, \dots, K$ (replicates)

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Multi-species occupancy model

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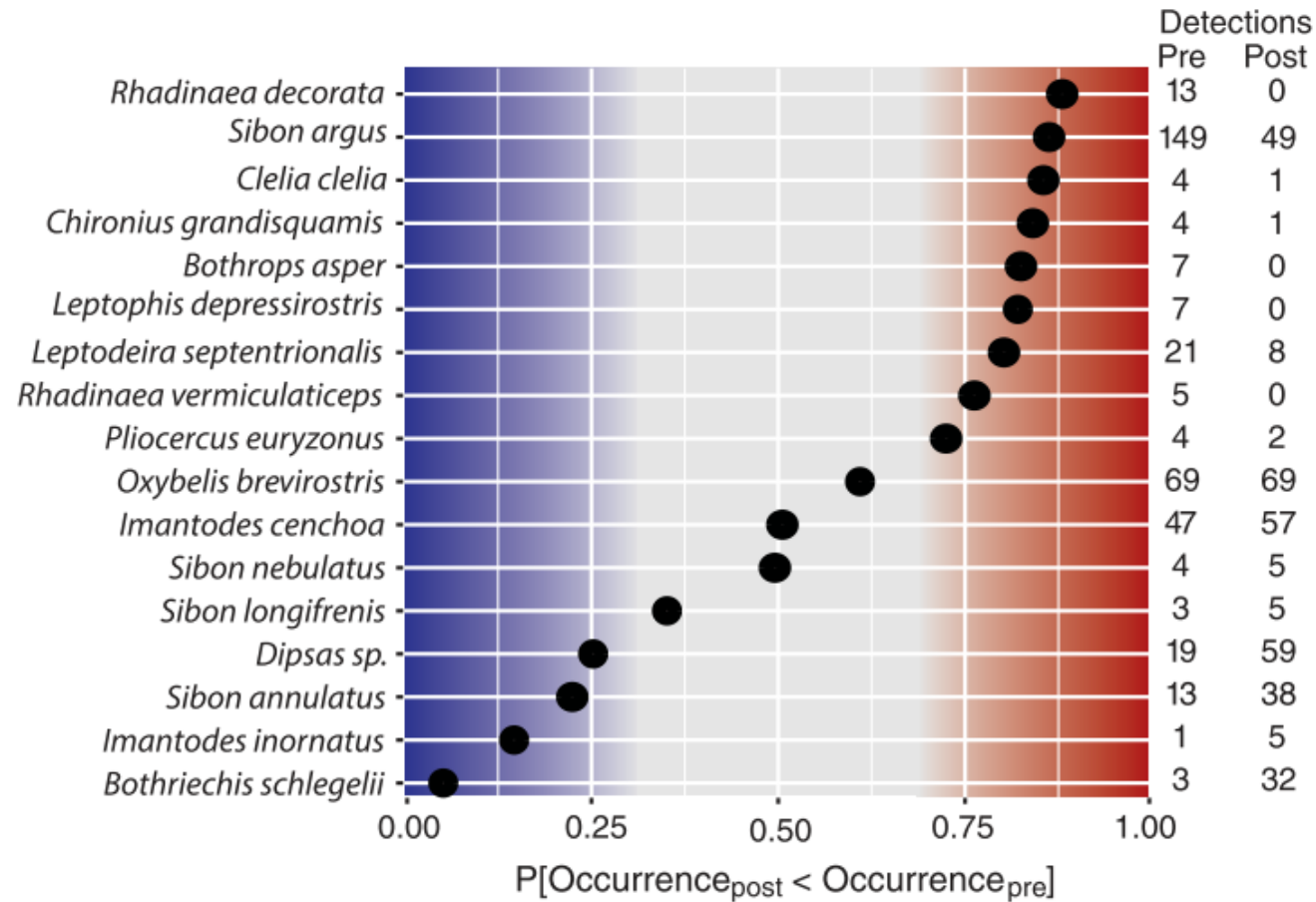
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Random slopes!!

Why multi-species occupancy modeling?

Improved ability to model rare species



Potential downsides

- Longer model run times
- Coding often involves working with multi-dimensional arrays (but spOccupancy simplifies this!)
- Defining a "community" is not always straightforward:
 - [Pacifi et al. 2014 Ecology and Evolution](#)
- May not be ideal for the rarest of the rare species:
 - [Erickson and Smith, 2023 Ecography](#)

Spatial multi-species occupancy models

Spatial autocorrelation in multi-species models

- Spatial autocorrelation may be more relevant in multi-species models since different species are driven by different variables.

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- Each w is estimated using an NNGP as before
- Model run times become huge with even a moderate number of species (e.g., 10)

Alternative approach: spatial factor models

- Basic idea: species-specific residual spatial autocorrelation can be explained by a set of common underlying "factors"

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- View the factors as "missing covariates" with a spatial structure
- Each species has a unique effect of each "missing covariate"
 - Called a "factor loading"
- This is a form of "factor analysis" (similar to PCA)

Spatial factor models

- Example: one covariate and two factors ("missing covariates")

$$\text{logit}(\psi_{i,j}) = \beta_{1,i} + \beta_{2,i} \cdot X_{2,j} + \lambda_{i,1} \cdot w_{1,j} + \lambda_{i,2} \cdot w_{2,j}$$

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"Missing covariates" that
account for residual
spatial autocorrelation

Spatial factor models

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Effects of the missing covariates

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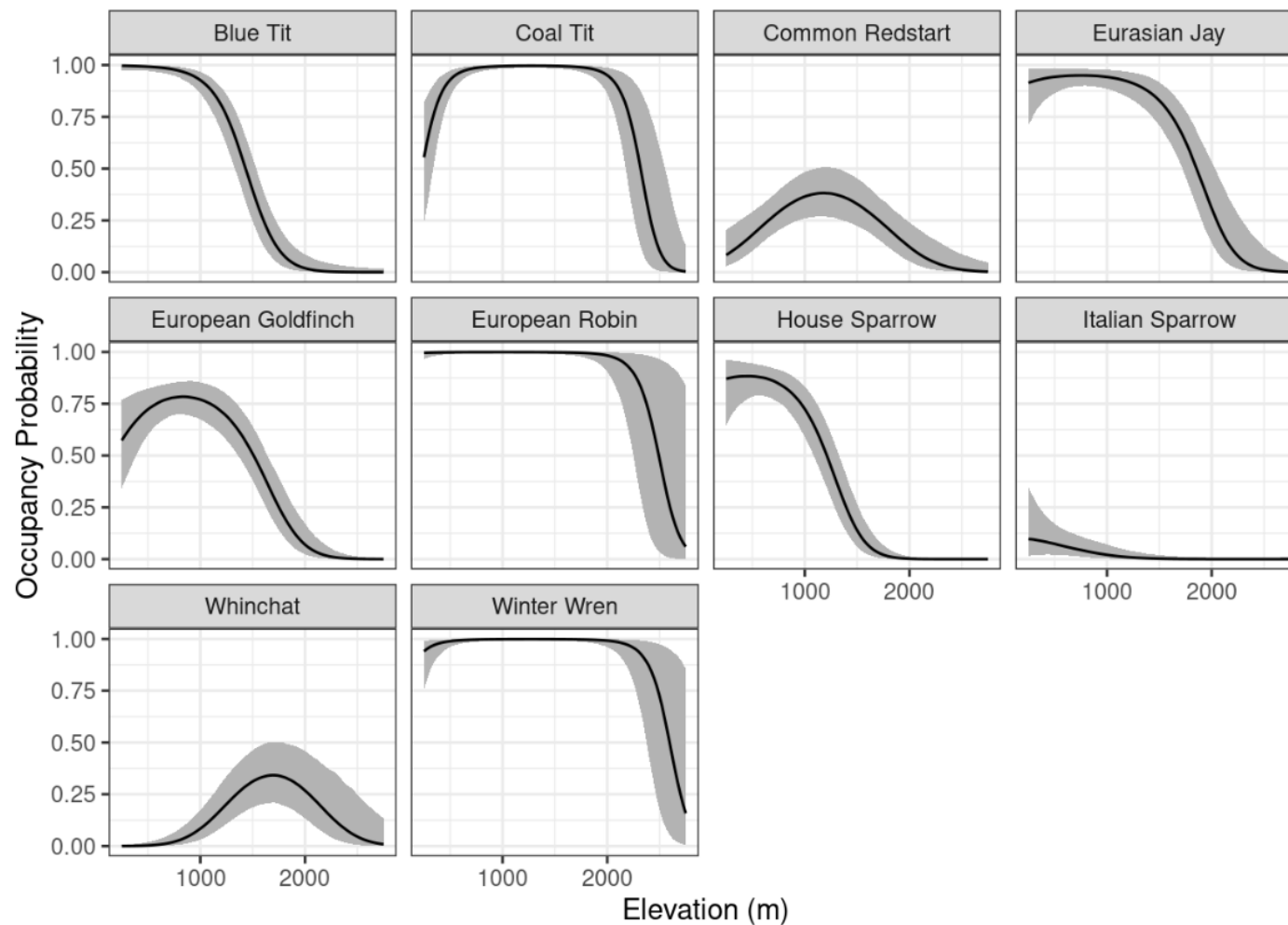
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- Downsides
 - Convergence can be tricky (see linked vignette above)
 - Requires more data than non-spatial multi-species models

Exercise 2: Swiss songbirds

- Data from the Swiss Breeding Bird Survey
- 3 visits at 267 1km squares across Switzerland
- We will focus on 10 passerine species



Multi-season occupancy models

Ecological Motivation

- How are species distributions shifting across space and time?

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- Assessment of occupancy trends over time:
 - Detection-nondetection data are easier to collect than count data
 - Occupancy-abundance relationship
 - Exact interpretation of occupancy trends depends on how data are collected ([Steenweg et al. 2018 Ecology](#))

Multi-season detection-nondetection data

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- Seasons are sometimes referred to as "primary replicates" and repeat visits within season as "secondary replicates"

Multi-species detection-nondetection data

- Example: 6 sites, 2 seasons, 3 surveys within a season

Season 1

Site	Survey 1	Survey 2	Survey 3
1	1	0	0
2	0	0	0
3	1	1	0
4	1	NA	0
5	0	1	1
6	0	0	0

Season 2

Site	Survey 1	Survey 2	Survey 3
1	0	1	NA
2	1	0	0
3	1	1	0
4	1	1	0
5	NA	NA	NA
6	0	0	1

Dynamic vs. multi-season occupancy models

Dynamic models

Multi-season models

Dynamic vs. multi-season occupancy models

Dynamic models

- Estimate colonization and survival/extinction

Multi-season models

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Dynamic vs. multi-season occupancy models

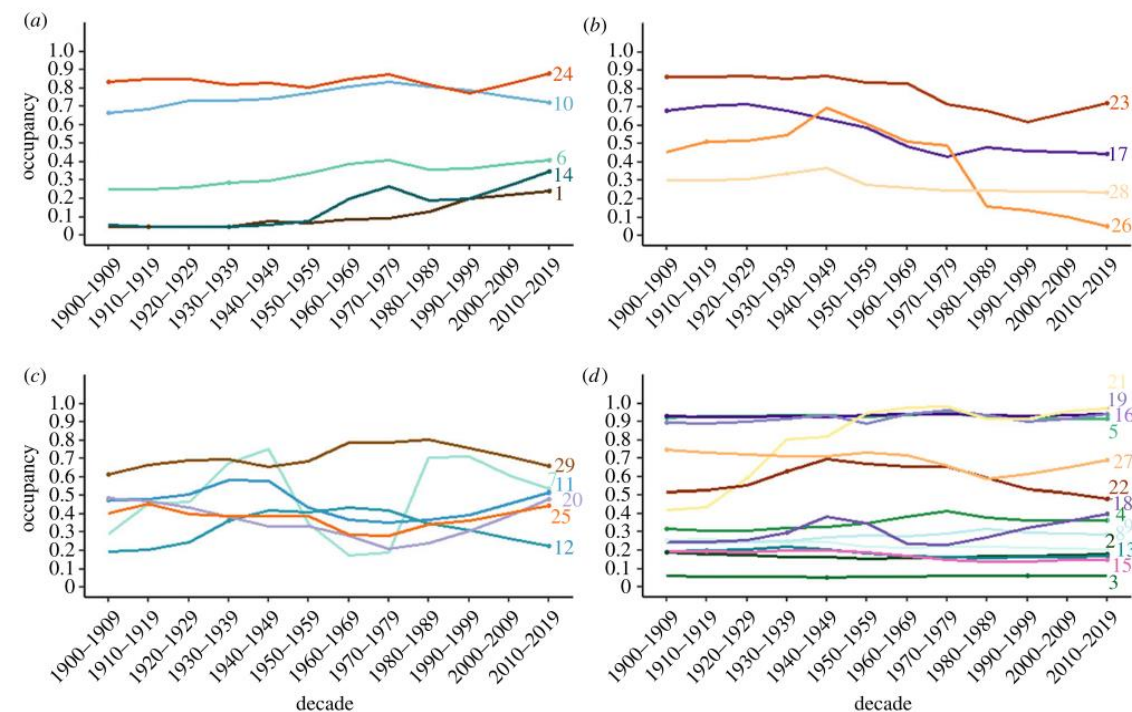
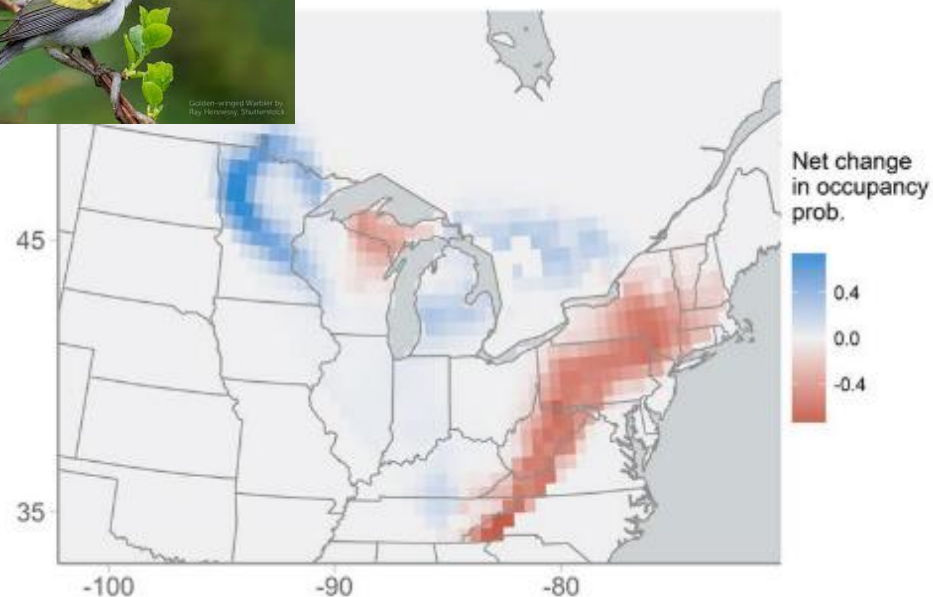
Dynamic models

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- Non-spatial versions in [ubms package](#)
- [MacKenzie et al. 2003 Ecology](#)

Multi-season models

- Estimate occupancy probability per season
- Less mechanistic
- Easier to fit and less data hungry
- In spOccupancy
- [Package vignette](#)
- Sometimes called "stacked" occupancy models

Examples of multi-season occupancy models



[Rushing et al. \(2019\) Sci Rep](#)

[Rushing et al. \(2020\) PNAS](#)

[Sheard et al. \(2021\) Curr Bio](#)



Multi-season occupancy model

$j = 1, \dots, J$ (site)

$t = 1, \dots, T$ (season)

Occupancy (ecological) sub-model

$k = 1, \dots, K_{j,t}$ (replicate)

$$z_{j,t} \sim \text{Bernoulli}(\psi_{j,t})$$

$$\text{logit}(\psi_{j,t}) = \mathbf{x}_{j,t}\boldsymbol{\beta} + w_j + \eta_t$$

$z_{j,t}$ True occurrence of the species at site j in season t

$\psi_{j,t}$ Occurrence probability at site j in season t

$\mathbf{x}_{j,t}$ Site and/or season-varying covariates

w_j Site-level random effect

η_t Season-level (temporal) random effect

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1. Unstructured -> a typical random intercept with the form:

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2. Spatial NNGP -> same as before. This is the "spatial multi-season occupancy model"

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 1. Unstructured -> a typical random intercept with the form:

$$\eta_t \sim \text{Normal}(0, \sigma_T^2)$$

2. AR(1) -> random temporal effects follow an autoregressive structure. Covariance between two time points is:

$$\sigma_T^2 \rho^{|t-t'|}$$

Multi-season occupancy model

$j = 1, \dots, J$ (site)

$t = 1, \dots, T$ (season)

$k = 1, \dots, K_{j,t}$ (replicate)

Detection (observation) sub-model

$$y_{j,t,k} \sim \text{Bernoulli}(p_{j,t,k} \cdot z_{j,t})$$

$$\text{logit}(p_{j,t,k}) = \mathbf{v}_{j,t,k} \cdot \boldsymbol{\alpha}$$

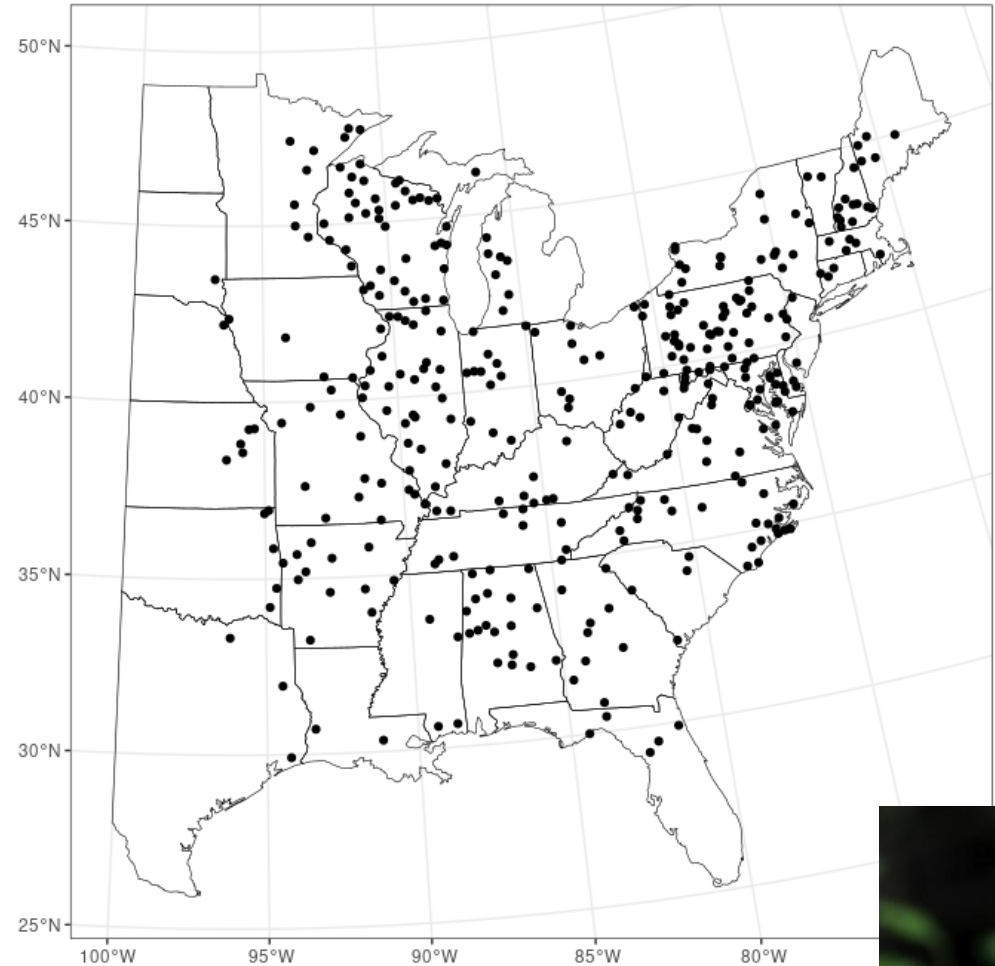
$y_{j,t,k}$ Detection-nondetection data at site j during replicate k and season t

$p_{j,t,k}$ Detection probability at site j during replicate k and season t

$\mathbf{v}_{j,t,k}$ Covariates affecting detection at site j during replicate k and season t

Exercise 3: Wood Thrush trend in eastern US

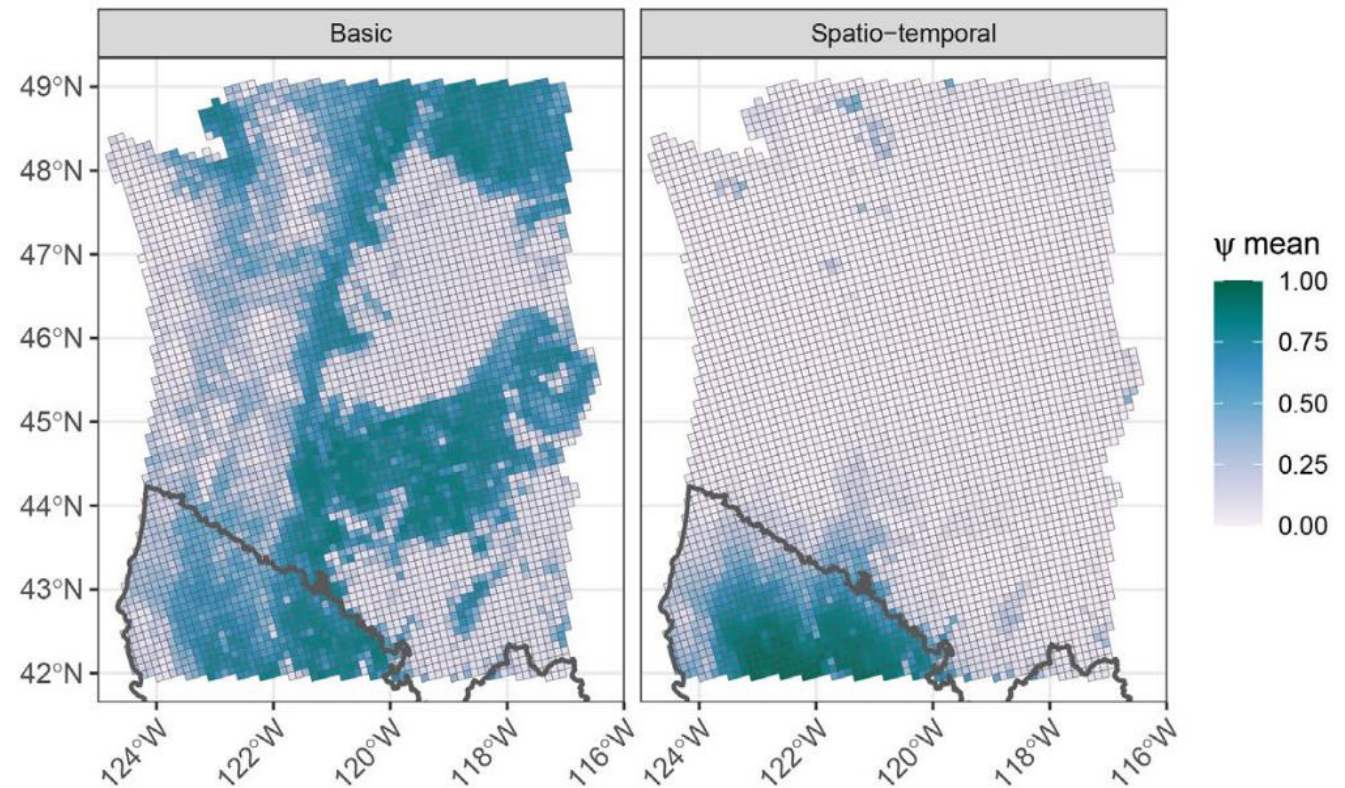
- Wood Thrush (*Hylocichla mustelina*) data from North American Breeding Bird Survey
- Replicates are spatial replicates (5 replicates per route)
- Each replicate is a group of 10 stops
- Data from 368 routes sampled in 2000-2009



Additional topics and
resources

Multi-season multi-species occupancy models

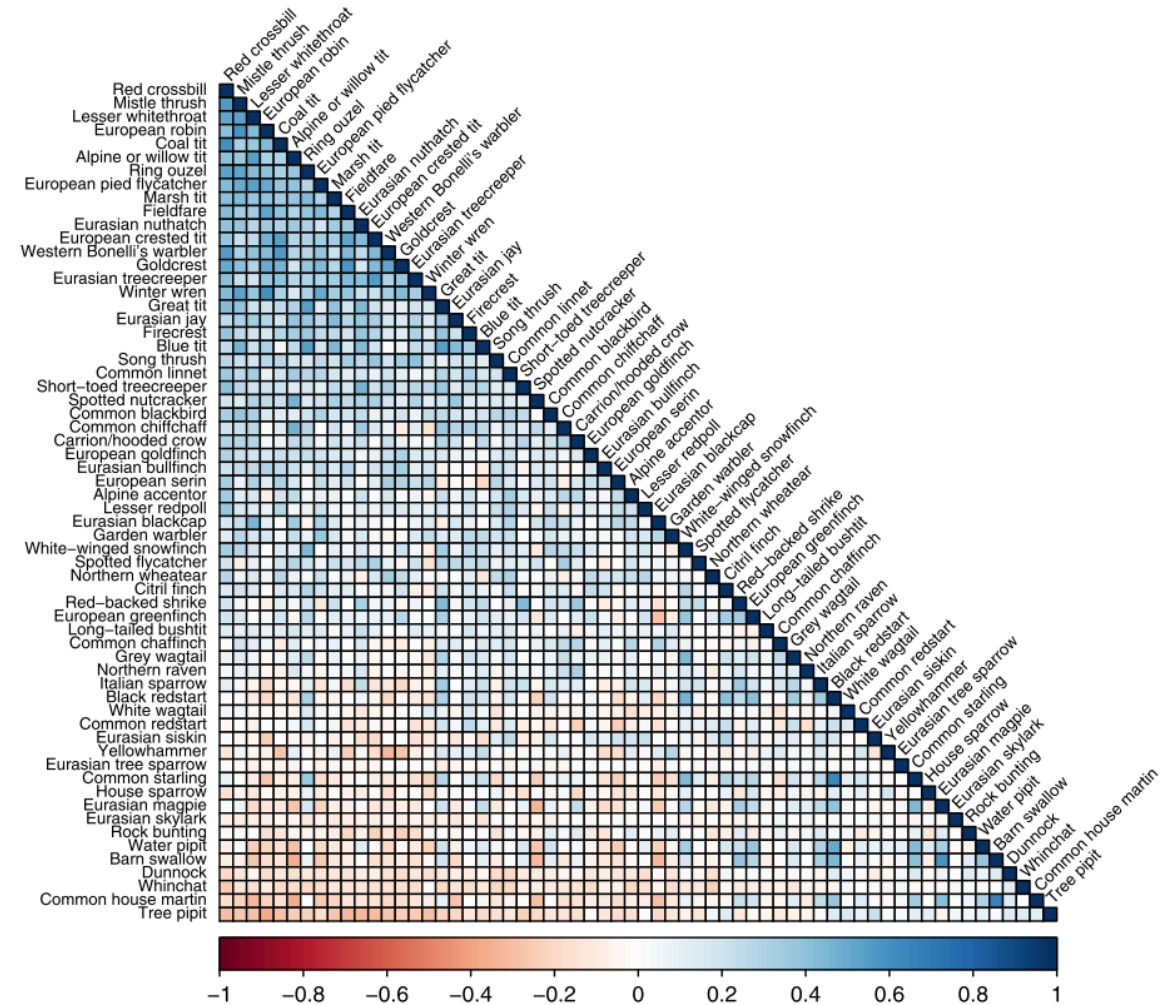
- Model spatio-temporal occupancy patterns for multiple species simultaneously
- Can help estimate trends for very rare species
- See functions `tMsPGOcc()` and `stMsPGOcc()`
- Data formatted in a four-dimensional array



[Wright et al. \(2021\) Eco and Evo](#)

Species correlations


- The factor modeling approach for multi-species models inherently accounts for residual species correlations ([vignette](#))
- Can derive a species x species correlation matrix
- This is a spatially-explicit joint species distribution model (JSDM) with imperfect detection
- See `lfMsPGOcc()` function for a non-spatial JSDM




[Tobler et al. \(2019\) Ecology](#)

Spatially-varying coefficient occupancy models

- Allow the effects of covariates to vary spatially in addition to the intercept
- Applications: spatially-varying trends, quantify "nonstationarity" in covariate effects
- [Vignette](#)

Guidelines for the use of spatially-varying coefficients in species
distribution models 

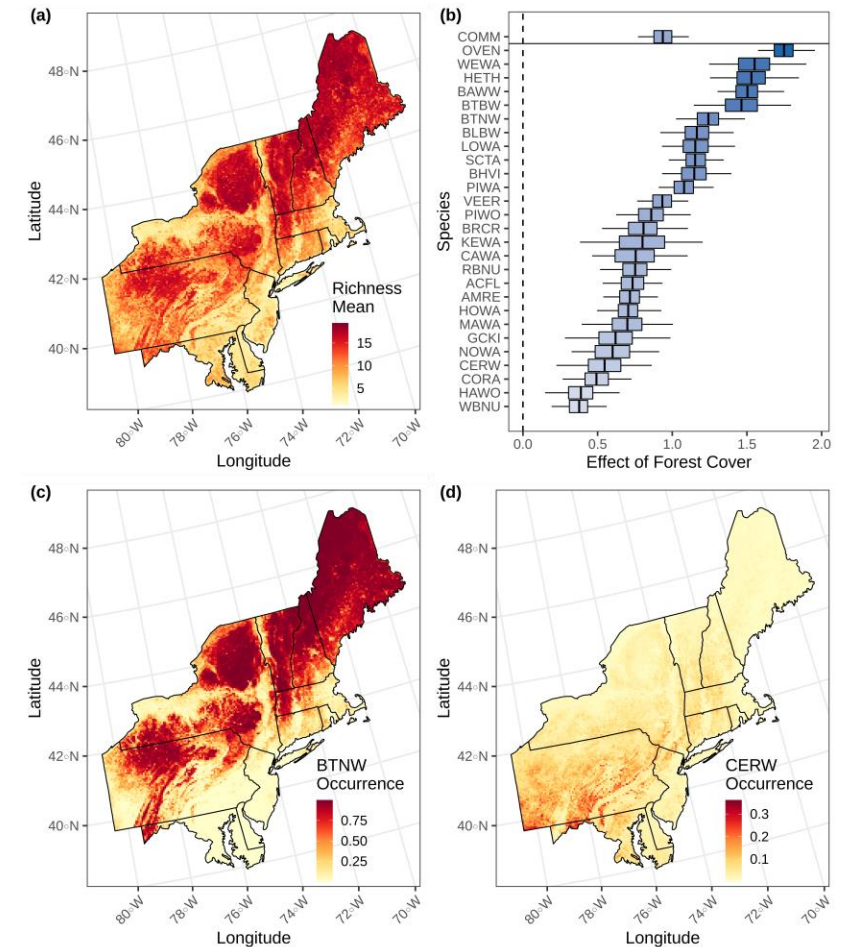
Jeffrey W. Doser^{1, 2}, Marc Kéry³, Sarah P. Saunders⁴, Andrew O. Finley^{2,5,6}, Brooke L. Bateman⁴, Joanna Grand⁴, Shannon Reault⁴, Aaron S. Weed⁷, Elise F. Zipkin^{1, 2}

Modeling complex species-environment relationships through
spatially-varying coefficient occupancy models 

Jeffrey W. Doser^{1, 2}, Andrew O. Finley^{2, 3, 4}, Sarah P. Saunders⁵, Marc Kéry⁶, Aaron S. Weed⁷, Elise F. Zipkin^{1, 2}

Integrated occupancy models

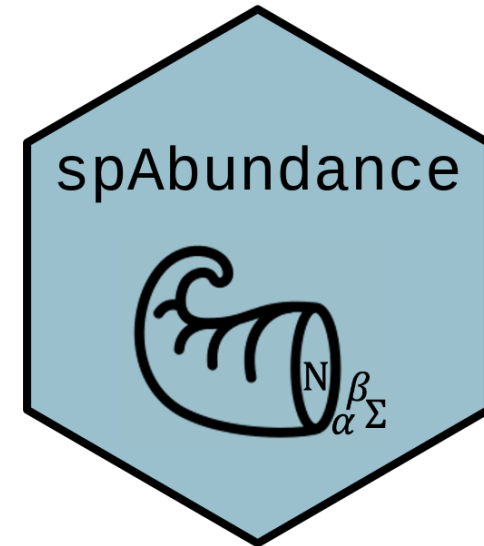
- Fit occupancy models using multiple data sources
- Single-species: spatial and non-spatial models
- Multi-species: non-spatial models only (spatial coming soon)
- Examples:
 - Vignette for [single-species](#) and [multi-species](#)
 - [Code for single-species example with bottlenose dolphins](#)
 - [Code for multi-species example with eBird and BBS data](#)



[Zipkin et al. \(2023\) JAE](#)

spAbundance

- Spatial and nonspatial N-mixture models, hierarchical distance sampling models, and GLMMs
- Single-species and multi-species models
- Syntax nearly identical to spOccupancy
- [Website](#) and [preprint](#)



Additional resources

Articles



Fit occupancy models

[Introduction to spOccupancy](#)

Learn how to get started with the core spOccupancy functionality

[Formatting data for use in spOccupancy](#)

Learn how to format raw data to fit occupancy models in spOccupancy

[Joint species distribution models with imperfect detection in spOccupancy](#)

Learn how to account for species correlations within multi-species occupancy models

[Multi-season occupancy models for assessing species trends and spatio-temporal occurrence patterns \(PDF\)](#)

[Multi-season occupancy models for assessing species trends and spatio-temporal occurrence patterns](#)

Learn how to fit multi-season occupancy models in spOccupancy

[Fitting occupancy models with random intercepts in spOccupancy](#)

Learn how to include random effects in spOccupancy

[Spatially varying coefficient models in spOccupancy](#)

Learn how to fit spatially varying coefficient models to quantify spatially varying trends and species-environment relationships

[Integrated multi-species occupancy models in spOccupancy](#)

Learn how to fit multi-species occupancy models with multiple data sources

[Convergence diagnostics and other considerations when fitting spatial occupancy models](#)

Ideas related to convergence, identifiability, priors, and other potential problem areas in spatial occupancy models

[Exploring model identifiability with a stress-testing framework](#)

- Website:
 - <https://www.jeffdoser.com/files/spoccupancy-web/>
- GitHub development page
 - <https://github.com/doserjef/spOccupancy>
- Package updates announced on Twitter/X (@jeffdoser18)
- Email: doserjef@msu.edu