

Publishing Maxima Results Via SageMath With SageTeX

The Pain And The Glory



A how-to presented for the sanity
of all users of Maxima,
Sage and SageTeX



Dedicated To Those Who Toiled In Obscurity To Reveal The Light
Of Knowledge

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1 Calling Maxima From Sage

```
maxima('load("/home/fraser/projects/Math/maxima/cmt_struct_sage_test_102.mac")')
```

1.1 First Block Of Sage and Maxima Code

1.2 Equations From CMT Book

1.2.1 Gathering Latex Code Of Example Equations

Note: These equations are not generated, they are pure latex

Purpose Of These Equations Once enough equations are included, latex code of their component parts can be stored in maxima structures. Each maxima variable, expression and equation will be given an elegant latex display form. This latex is stored in a structure containing the variable name, value/content and a nested list of latex strings for display.

Maxima Implementation Details All maxima structures are stored in a hash array. The key for each variable, function, expression, lemma, axiom in it's respective hash array is the name of that artifact

Roadmap For Development A full explanation of the system internals as well as instructions for use of the system will be given in an appendix as this document evolves.

1.2.2 Raw Latex Code Of Equations

Latex Code has been entered manually to build a library of latex code snippets. These will be stored in a database. Maxima, Sage and Sympy code will be used to perform derivations dynamically, then publish the results in latex documents. The states of derivations will also be stored as reference material for larger derivations and proofs.

Multifrequency Power Relations Of Lossless Waveguiding Systems (1.2.2)

$$\frac{\partial}{\partial z} \sum_{s=-\infty}^{\infty} \sum_{p=-\infty}^{\infty} P_{s,p} = 0 \quad (1.1)$$

$$\omega_1 \frac{\partial}{\partial z} \sum_{p=-\infty}^{\infty} \sum_{s=-\infty}^{\infty} \frac{s P_{s,p}}{s \omega_1 + p \omega_2} + \omega_2 \frac{\partial}{\partial z} \sum_{s=-\infty}^{\infty} \sum_{p=-\infty}^{\infty} \frac{p P_{s,p}}{s \omega_1 + p \omega_2} \quad (1.2)$$

$$\frac{\partial}{\partial z} \sum_{s=-\infty}^{\infty} \sum_{p=-\infty}^{\infty} P_{s,p} = 0 \quad (1.3)$$

$$\sum_{p=-\infty}^{\infty} \sum_{s=-\infty}^{\infty} \frac{s P_{s,p}}{s \omega_1 + p \omega_2} = 2 \sum_{p=-\infty}^{\infty} \sum_{s=1}^{\infty} \frac{s P_{s,p}}{s \omega_1 + p \omega_2} \quad (1.4)$$

$$\omega_1 \frac{\partial}{\partial z} \sum_{p=-\infty}^{\infty} \sum_{s=1}^{\infty} \frac{s P_{s,p}}{s \omega_1 + p \omega_2} + \omega_2 \frac{\partial}{\partial z} \sum_{s=-\infty}^{\infty} \sum_{p=1}^{\infty} \frac{p P_{s,p}}{s \omega_1 + p \omega_2} = 0 \quad (1.5)$$

$$\frac{\partial}{\partial z} \sum_{p=-\infty}^{\infty} \sum_{s=1}^{\infty} \frac{s P_{s,p}}{s \omega_1 + p \omega_2} = 0 \quad (1.6)$$

$$\frac{\partial}{\partial z} \sum_{s=-\infty}^{\infty} \sum_{p=1}^{\infty} \frac{p P_{s,p}}{s \omega_1 + p \omega_2} = 0 \quad (1.7)$$

Manley-Rowe Power Relations For Parametric Waveguiding Systems (1.2.3)

Parametric Amplitude Levels In parametric systems the amplitude of the signal input at frequency ω_1 (ω_s) is much less than the amplitude of the pump at frequency ω_2 (ω_p). The signal amplitude is so small that parametric system is linear w.r.t the signal but nonlinear w.r.t the pump. The pump modes will experience nonlinear effects while the signal modes will experience linear ones.

$$\omega_{0,p} = p \omega_p \text{ (for } s = 0 \text{) and } \omega_{\pm 1,p} = \pm \omega_s + p \omega_p \text{ (for } s = \pm 1 \text{)}$$

Multifrequency Parametric Systems

$$\frac{\partial}{\partial z} \sum_{p=-\infty}^{\infty} \frac{P_{+1,p}}{\omega_s + p\omega_p} = 0 \quad (1.8)$$

$$\frac{\partial}{\partial z} \sum_{p=1}^{\infty} p \left(\frac{P_{0,p}}{p\omega_p} + \frac{P_{+1,p}}{\omega_s + p\omega_p} - \frac{P_{+1,-p}}{\omega_s - p\omega_p} \right) = 0 \quad (1.9)$$

$s = -1, P_{-1,p} = P_{+1,-p}$ then

Now the pump index p will be replaced by pump index ν

$$\omega_s + p\omega \rightarrow \omega_s + p\omega_\nu \text{ and } P_{+1,p} = P_{+1,\nu} \rightarrow P^{(\nu)}$$

The final form of the Manley-Rowe relations for parametric systems are:

$$\frac{\partial}{\partial z} \sum_{\nu=-\infty}^{\infty} \frac{P^{(\nu)}}{\omega_\nu} = 0 \quad (1.10)$$

$$\frac{\partial}{\partial z} \sum_{\nu=1}^{\infty} \nu \left(\frac{P^{(\nu)}}{p\omega_\nu} + \frac{P^{-\nu}}{\omega_{-\nu}} = \frac{1}{\omega_\nu} \frac{\partial P_{pump}}{\partial z} \right) \quad (1.11)$$

where $P_{pump} = \sum_{p=1}^{\infty} P_{0,p}$ is the total power supplied by the pump signal

Three Frequency Parametric Systems Where there are 3 components at frequencies $\omega_p(pump), \omega_s(signal)$ and one of $\omega_{\pm 1} = \omega_s \pm \omega_p$. The case of difference frequency $\omega_{-1} = \omega_s - \omega_p = \omega_i$ includes the case of $\omega_{+1} = \omega_s + \omega_p$. In order to show this re-write the general relations (1.8) and (1.9). This takes into account the presence of only three pump frequencies $\nu = 0, \nu = +1, \nu = -1$.

$$\frac{\partial}{\partial z} \left(\frac{P^{(0)}}{\omega_0} + \frac{P^{(+)}}{\omega_{+1}} + \frac{P^{(-1)}}{\omega_{-1}} \right) = 0 \quad (1.12)$$

$$\frac{\partial}{\partial z} \left(\frac{P^{(pump)}}{\omega_p} + \frac{P^{(+1)}}{\omega_{+1}} + \frac{P^{(-1)}}{\omega_{-1}} \right) = \frac{1}{\omega_p} \frac{\partial P_{pump}}{\partial z} \quad (1.13)$$

Equation Library Parts Going forward, only the math and equations will entered - the goal is to build a large library of latex equation parts. Equations from other sources will be included here, including sources for Nonlinear Optics, Quantum Optics, Quantitative Finance, statistics and Electrodynamics. The components will be extracted and stored as above. A search of github and other sites will be made for any software that can create latex documents automatically from code meant for computer algebra systems.