```
1 | • • •
      Created on 29 Oct 2014
 2
 3
      @author: bob
 5
 6 import multiprocessing
      import scipy
 8 from workers.worker2 import Worker2 as worker2
      from workers.workerSimple import workerSimple as workerSimple
      from workers.worker_nls import WorkerNLS
10
       import matplotlib.pyplot as plot
11
12
13
       if __name__ == '__main__':
14
                 manager = multiprocessing.Manager()
15
                 return_dict = manager.dict()
16
                 iobs = []
17
                 nb_ofLoopsPerProces = 10
18
                 nb Proces = 8
19
                 Ksqr = [1]
20
                 sigma = scipy.linspace(0.1, 500, nb_ofLoopsPerProces*nb_Proces).tolis
21
                 q = [-1]
22
                 n = 10
23
                 y0=[0.,1.];
24
                 t0=0
25
                 tend=1
26
                 h=0.01
27
                 for i in range(nb Proces):
28
                            name = 'Worker %s'%(i+1)
29
                            filename = 'File%s.txt'%(i+1)
30
                            eigenSys = workerSimple(Ksqr,sigma[nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_ofLoopsPerProces*i:nb_o
31
                            p = multiprocessing.Process(target=eigenSys.task,args=(i+1,return_
32
                            jobs.append(p)
33
                            p.start()
34
                 i = 1;
35
                 for p in jobs:
36
                            p.join()
37
                            print 'Job %s finished, from %s'% (i,len(jobs))
38
39
                  result = scipy.zeros((nb_ofLoopsPerProces*nb_Proces,n+3))
40
                 for i in range(nb Proces):
41
                            result[i*nb_ofLoopsPerProces:(i+1)*nb_ofLoopsPerProces,:] =
42
                 fig = plot.figure()
43
                 fig.suptitle('Dispersion Relation', fontsize=18)
44
                 ax = fig.add_subplot(111)
45
                 fig.subplots_adjust(top=0.85)
46
                 ax.set_xlabel('Sigma', fontsize=16)
47
                 ax.set_ylabel('Omega sqr', fontsize=16)
48
```

```
ax.tick_params(axis='both', which='major', labelsize=14)
49
       for i in range(n):
50
           ax.plot(result[:,1],result[:,3+i])
51
       plot.savefig('../../plot/dispersionsigma.eps')
52
53
       plot.show()
54
55
56
57
58
59
60
```

```
1 | | | | |
2
  Created on 14 Oct 2014
3 @author: bob
4
  class Function(object):
5
6
7
       A class to represent function objects, these functions
       must be able to be evaluated and to be derived at some point.
8
9
       def __init__(self, delta=0.001):
10
11
           Constructor
12
13
           self. DELTA = delta
14
15
       def evaluate(self,x):
16
17
           A method to evaluate the function
18
19
           raise NotImplementedError
20
       def derivative(self,x):
21
22
           A method to calculate the derivative of the function
23
24
           return (self.evaluate(x+self._DELTA/2) - self.evaluate(x-self._DEL
25
  class P(Function):
26
27
       def __init__(self,Ksqr,sigma,g,wsqr):
           Function. init (self)
28
           self.Ksqr = Ksqr
29
           self.sigma = sigma
30
           self.g = g
31
           self.wsqr = wsqr
32
       def evaluate(self, x):
33
           return self.wsqr*(rho0(self.Ksqr,self.sigma,self.g,self.wsqr).eval
34
35
  class O(Function):
36
       def __init__(self,Ksqr,sigma,g,wsqr):
37
           Function. init (self)
38
           self.Ksqr = Ksqr
39
           self.sigma = sigma
40
           self_q = q
41
           self.wsqr = wsqr
42
       def evaluate(self, x):
43
           return self.Ksqr*((rho0(self.Ksqr,self.sigma,self.g,self.wsqr).eva
44
                                (rho0(self.Ksqr,self.sigma,self.g,self.wsqr).de
45
46
  class rho0(Function):
47
       def __init__(self,Ksqr,sigma,g,wsqr):
48
```

```
Function.__init__(self)
self.Ksqr = Ksqr
self.sigma = sigma
self.g = g
self.wsqr = wsqr
def evaluate(self, x):
return (1+self.sigma*x)
```

```
1 \# -*- coding: utf-8 -*-
2
  Created on Wed Oct 8 17:17:48 2014
3
4
  @author: bob
5
  \mathbf{H} \mathbf{H} \mathbf{H}
6
7
  class ODESystem(object):
8
9
       def __init__(self):
10
11
            Constructor for ODE system. Input can take the form that the
12
            subclasses desire. This abstract class is meant to create a commor
13
            interface that can be used by Integrator objects.
14
15
            raise NotImplementedError
16
17
       def f(self,t,y):
18
19
            Return the righthand side of the ODE
20
21
            raise NotImplementedError
22
23
       def y_exact(self,t,y0):
24
25
            Returns the exact solution for the ODE at times t,
26
27
            starting from y0 at time t=0
            0.00
28
            raise NotImplementedError
29
30
31
```

```
1 | • • •
  Created on 29 Oct 2014
2
3
  @author: bob
5
6 import multiprocessing
  import scipy
8 from workers.worker2 import Worker2 as worker2
9 from workers.workerSimple import workerSimple as workerSimple
  from workers.worker_nls import WorkerNLS
10
  import matplotlib.pyplot as plot
11
  from test import plottest
12
13
14
  if __name__ == '__main__':
15
       manager = multiprocessing.Manager()
16
       return dict = manager.dict()
17
       jobs = []
18
       nb_ofLoopsPerProces = 5
19
       nb Proces = 8
20
       Ksqr = scipy.linspace(1, 500, nb_ofLoopsPerProces*nb_Proces).tolist()
21
       sigma = scipy.linspace(1, 1.5, 1).tolist()
22
       g = scipy.linspace(-1, -1.5, 1).tolist()
23
       n = 10
24
       y0=[0.,1.];
25
       t0=0
26
      tend=1
27
       h=0.01
28
       for i in range(nb_Proces):
29
           name = 'Worker %s'%(i+1)
30
           filename = 'File%s.txt'%(i+1)
31
           eigenSys = workerSimple(Ksqr[nb_ofLoopsPerProces*i:nb_ofLoopsPerPr
32
           p = multiprocessing.Process(target=eigenSys.task,args=(i+1,return))
33
           jobs.append(p)
34
           p.start()
35
       i = 1;
36
       for p in jobs:
37
           p.join()
38
           print 'Job %s finished, from %s'% (i,len(jobs))
39
40
       result = scipy.zeros((nb_ofLoopsPerProces*nb_Proces,n+3))
41
       print return_dict
42
       for i in range(nb Proces):
43
           result[i*nb_ofLoopsPerProces:(i+1)*nb_ofLoopsPerProces,:] =
                                                                            retur
44
      ax1 = plot.subplot2grid((1,2), (0,0), colspan=1)
45
       ax7 = plot.subplot2grid((1,2), (0, 1), rowspan=1, colspan=1)
46
47
       ax1.plot(result[:,0],result[:,3])
48
```

```
ax1.plot(result[:,0],result[:,4])
49
      ax1.plot(result[:,0],result[:,5])
50
      ax1.plot(result[:,0],result[:,6])
51
       ax1.plot(result[:,0],result[:,7])
52
      ax1.plot(result[:,0],result[:,8])
53
54
       ax1.plot(result[:,0],result[:,9])
      ax1.plot(result[:,0],result[:,10])
55
      ax1.plot(result[:,0],result[:,11])
56
       ax1.plot(result[:,0],result[:,12])
57
      plottest.PlotWave(data=result,fig = ax7)
58
      plot.savefig('../../plot/mainResult.eps')
59
       plot.show()
60
61
62
63
64
65
66
```

```
1.1.1
1
  Created on 29 Oct 2014
2
3
  @author: bob
  1.1.1
5
6
  import scipy
  from scipy.integrate import odeint
  import function.function as func
  import system.waveSystem as wave
10
11
12
13
  class PlotWave(object):
14
15
       A class to plot the curves for the given parameters.
16
17
       def __init__(self, data,fig=None):
18
           self.fig = fig
19
           for i in range(len(data[:,0])):
20
                self.plotRow(data[i,:])
21
       def f(self,y,t):
22
           return self.vgl.f(t, y)
23
       def plotRow(self,row):
24
           y0 = [0., 1.]
25
           t = scipy.linspace(0, 1., 1000)
26
           Solution = row[3:]
27
           Ksgr = row[0]
28
           sigma = row[1]
29
           q = row[2]
30
           for i in Solution:
31
                funcP = func.P(Ksqr,sigma,g,i)
32
                funcQ = func.Q(Ksqr,siqma,q,i)
33
               # create the ODE
34
                self.vgl = wave.WaveSystem(funcP, funcQ)
35
               # solve the DEs
36
37
                soln = odeint(self.f, y0, t)
               S =soln[:, 0]
38
               # Normalising the solution
39
               MAX = max(S[:])
40
               S = scipy.multiply(1/MAX,S)
41
                self.fig.plot(t,S)
42
43
44
45
46
47
```

```
1 \# -*- coding: utf-8 -*-
2
  Created on Wed Oct 8 17:17:48 2014
3
4
  @author: bob
5
6
7
  import scipy
8
9
  class RungeKutta(object):
10
11
       def __init__(self,ode,A=None,b=None,c=None):
12
13
           Initializes a runge-kutta time integration object for the system of
14
           ODEs specified by the object ode
15
           Input:
16
                ode -- an object of the class ODESystem that contain the ODE 1
17
                integrated
18
19
           Output:
                an object of the class RungeKutta that can integrate
20
                the ODE specified in the object ode
21
22
           #If one of the parameters is left None all the parameters A,b,c wi
23
           #set to the default runge-kutta 4th order sceme (RG4)
24
                   0
25
           1/2
                   1/2
26
27
           1/2
                   0
                        1/2
           1
                              1
28
                   0
                        0
29
           1/6
                   1/3
                          1/3
                                  1/6
30
           .....
31
           if (A==None) or (b==None) or (c==None):
32
               A = [[0 * j *i for i in range(4)] for j in range(4)]
33
               A[1][0] = 1.0/2
34
               A[2][1] = 1.0/2
35
               A[3][2] = 1.0
36
                c = [0 * i for i in range(4)]
37
                c[1] = 1.0/2
38
                c[2] = 1.0/2
39
                c[3] = 1.0
40
                b = [0 * i for i in range(4)]
41
               b[0] = 1.0/6
42
               b[1] = 1.0/3
43
               b[2] = 1.0/3
44
                b[3] = 1.0/6
45
           self_A = A
46
           self_b = b
47
           self.c = c
48
```

```
self.ode = ode
49
50
       def step(self,tn,yn,h):
51
52
           takes a single time step using the runge-kutta method
53
               y_{n+1} = y_n + sum(b_i*k_i)
54
           Input:
55
               tn -- current time
56
               yn -- state at time tn
57
               h - size of time step
58
59
           Output:
               y -- state at time t0+h
60
61
           k = self.kValues(tn,yn,h)
62
           lincombinatie = scipy.zeros(len(yn))
63
           for i in range(len(self.b)):
64
               lincombinatie = scipy.add(scipy.multiply(k[i],self.b[i]*h), li
65
           return yn + lincombinatie
66
       def kValues(self,tn,yn,h):
67
           #Initialise an empty vector k of the same length as b and init the
68
           A = self_A
69
           b = self.b
70
           c = self.c
71
           k = [[0. * i * j for j in range(len(yn))] for i in range(len(b))]
72
           tnew = 0
73
           ynew = scipy.zeros(len(yn))
74
           lincombinatie = ynew
75
           for i in range(len(b)):
76
               tnew = tn + c[i]*h
77
               ynew = scipy.zeros(len(yn))
78
               lincombinatie = scipy.zeros(len(yn))
79
               for j in range(i):
80
                   prod = scipy.multiply(A[i][j]*h,k[j])
81
                   lincombinatie = scipy.add(lincombinatie,prod)
82
               ynew = scipy.add(yn,lincombinatie)
83
               k[i] = scipy.multiply(1,self.ode.f(tnew,ynew))
84
               #k[i] = scipy.multiply(h,self.ode.f(tnew,ynew))
85
           return k
86
       def scalarProductArray(self,sc,ar):
87
           return [x*sc for x in ar]
88
       def sumOfArray(self,ar1,ar2):
89
           if len(ar1) != len(ar2):
90
               raise AttributeError
91
           return [ar1[i]+ar2[i] for i in range(len(ar1))]
92
93
       def integrate(self,y0,t0,tend,h):
94
95
           Integrates using forward Euler time steps
96
```

```
97
            Input:
                t0 -- initial time
98
                y0 -- initial condition at time t0
99
                tend — time horizon of time integration
100
                Dt — size of time step
101
            \mathbf{m}
102
            # obtain the number of time steps
103
            N = int(scipy.ceil(tend/h))
104
            # create a vector of time instances
105
            t = scipy.arange(t0,N*h+h/2.,h)
106
            # obtain the number of equations
107
            D = scipv.size(v0)
108
            # create the matrix that will contain the solutions
109
            y = [[0*i*j for i in range(D)] for j in range(N+1)]
110
            # set the initial condition
111
            y[0]=y0
112
            # perform N time steps
113
            for n in range(N):
114
                y[n+1]=self.step(t[n],y[n],h)
115
            return t,y
116
117
```

```
1.1.1
1
2
  Created on 14 Oct 2014
3
  @author: bob
5
6 import numpy as np
7 import matplotlib.pyplot as plt
8 from scipy.integrate import odeint
9 import function function as func
  import system.waveSystem as wave
10
11 import integrators rungeKutta as rK
12 from math import ceil
  from scipy.io.matlab.mio5_utils import scipy
13
14
  def f(y,t):
15
       return vgl.f(t, y)
16
17
18 | wsqr = 0.1
19 \mid sigma = 1.
20 | Ksqr = 1.
21 | g = 1.
22
23
24 # create the ODE
25 | vql = wave.WaveSystem(func.P(Ksqr,sigma,g,wsqr),func.Q(Ksqr,sigma,g,wsqr))
26
27 # initial condition
28 | y0 = [0.,1.]
29 | t0 = 0
30 | tend = 1.
31 || h = 0.01
32 | NbSteps = ceil((tend-t0)/h)
  t_scipy = np.linspace(t0, tend, NbSteps+1)
34
  # solve the ODE using the integrated solver
35
  soln_scipy = odeint(f, y0, t_scipy)
  solution_scipy = soln_scipy[:, 0]
37
38
39
40 # solve the ODE using the self written runge kutta integrator
41 fe = rK.RungeKutta(vgl)
  t_runge,soln_runge = fe.integrate(y0,t0,tend,h)
  solution_runge = [soln_runge[i][0] for i in range(len(soln_runge))]
43
44
45 # plot results
46 plt.subplot(211)
47 plt.plot(t_runge, solution_runge)
48 plt.plot(t_scipy, solution_scipy)
```

```
# plot the error of the scipy method and the self implemented method
error = [scipy.absolute(solution_runge[i]-solution_scipy[i]) for i in rang
plt.subplot(212)
plt.plot(t_runge,error)

plt.show()
```

```
1 \# -*- coding: utf-8 -*-
2
  Created on Wed Oct 8 17:17:48 2014
3
4
  @author: bob
5
6
  A class to visually check the solutions of the differential equations.
8
  0.000
9
  import numpy as np
10
  import matplotlib.pyplot as plt
11
  from scipy.integrate import odeint
  import system.waveSystem as wave
13
  import function.function as func
14
15
  # A dummy function for the runge kutta solver.
16
  def f(y,t):
17
       return vgl.f(t, y)
18
  # Values for wsgr
19
20 Solution = \begin{bmatrix} 0.1 \end{bmatrix}
21 # Parameters of the differential equations
22 | sigma = 1
23 | Ksqr = 1
24 | q = -1
25 # initial condition
26 | y0 = [0., 1.]
  t = np.linspace(0, 1., 1000)
27
  # Start the calculation of the ode for the different values of wsqr
  for i in Solution:
29
       funcP = func.P(Ksqr,sigma,q,i)
30
       funcQ = func.Q(Ksqr,sigma,q,i)
31
       # create the ODE
32
       vgl = wave.WaveSystem(funcP,funcQ)
33
       # solve the DEs
34
       soln = odeint(f, y0, t)
35
       S =soln[:, 0]
36
       plt.plot(t,S)
37
  # plot results
38
  plt.plot(t,S)
  plt.show()
40
41
42
43
44
45
46
```

```
1 | • • •
  Created on 13 Oct 2014
2
3
  @author: bob
4
5
  import ode_system
  class WaveSystem(ode_system.ODESystem):
8
       def __init__(self,P=None,Q=None):
9
10
           Creates an object to represent a differential equation of the form
11
                d/dx[p(x,w) d/dx e(x)] - q(x,w) e(x) = 0
12
           This equation is internally converted to a system of first order of
13
                x'_1 = x_2
14
                x' = (q(x,w) \times 1 - p(x,w) \times 2)/(p(x,w)')
15
16
           Input:
17
                p -- an object of type function to represent p(x,w) in the equ
18
                q -- an object of type function to represent q(x,w) in the equ
19
           Output:
20
                an object of the class WaveSystem
21
22
           0.00
23
           self.P = P
24
           self.Q = Q
25
26
27
       def f(self,x,y):
28
           Return the righthand side of the ODE
29
30
           P = self.P
31
           Q = self.Q
32
           dy_1 = y[1]/P_evaluate(x)
33
           dy_2 = Q_evaluate(x)*y[0]
34
           return [dy_1, dy_2]
35
36
37
38
39
40
41
```

```
1 | • • •
  Created on 08 Nov 2014
2
3
  @author: bob
4
5
6 from workers.worker import Worker as worker
  import scipy
  from scipy.optimize import anderson
  #from scipy.optimize import newton krylov
10
  GUESS W = 1
11
12
  class WorkerNLS(worker):
13
14
       A class to represent a worker to find the eigenmodes as
15
       a function of K^2, sigma and g
16
17
       def __init__(self, Ksqr=[1],sigma=[1],g=[1],y0=[0.,1.],n=3,t0=0,tend=1
18
19
           The constructor to set up the right parameters and to create
20
           the ode's
21
           1.1.1
22
           super(WorkerNLS, self).__init__(Ksqr, sigma, g, y0, n, t0, tend, h
23
           self.f = open(filename, 'w')
24
           self.filename = filename
25
           self.name = name
26
27
       def search(self,Ksqrnum,sigmanum,gnum,n):
28
           Search for the first n roots.
29
30
           guess = GUESS_W
31
           self.tempKsqrnum = Ksqrnum
32
           self.tempsigmanum = sigmanum
33
           self.tempgnum = gnum
34
           if n ==1:
35
               orde = 1
36
               while(orde!=0):
37
                    oneOnGuess = 1./guess
38
                    print 'Root guess: %s'%(1./oneOnGuess)
39
                    root = (1./scipy.absolute(anderson(self.aid_f, oneOnGuess,
40
                    info = self.zero point info(Ksgrnum, sigmanum, gnum, root)
41
                    orde = info[0]
42
                    print 'Root and order: %s , %s'%(root,orde)
43
                    quess = root*(orde + 1)
44
           else:
45
46
               pass
47
48
```

```
return [root]
49
50
       def aid_f(self,oneonguess):
           return self.endPoint(scipy.absolute(1/oneonguess))
51
52
       def foundAll(self,Nroots):
53
           for root in Nroots:
54
                if (root==0):
55
                    return False
56
           return True
57
       def _nextGuess(self,Nroots,guess,previous=None):
58
59
           A method to do an educated guess for the next omega value
60
61
           # Find index of lowest 0
62
           index = 0
63
           for root in Nroots:
64
                if (root==0):
65
                    break
66
                index = index +1
67
           print '-'*40
68
           print previous
69
           print index
70
           print '-'*40
71
           if (previous!=0 and previous==index):
72
                return (quess/2,index)
73
           newquess = 0
74
75
           count = 1
           nonzero = 0
76
           for root in Nroots:
77
                newguess = newguess + root/count
78
                count = 1 + count
79
                if (root!=0):
80
                    nonzero = nonzero +1
81
           if nonzero!=0:
82
                newguess = (newguess/nonzero)/(index+1)
83
                return (newguess,index)
84
85
           else:
                return (guess/2,index)
86
87
88
89
90
91
92
93
94
95
```

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```
1.1.1
  1
  2
       Created on 14 Oct 2014
  3
       @author: bob
        1.1.1
  5
  6
        import scipy
       import multiprocessing
  8
        import function.function as func
        import system.waveSystem as wave
10
        import integrators.rungeKutta as rK
11
        from scipy.signal import argrelextrema
13
       UPPERZERO = 0.05
14
15
        class Worker(object):
16
17
                    A class to represent a worker
18
                     1.1.1
19
20
21
                    def __init__(self, Ksqr=[1],sigma=[1],g=[1],y0=[0.,1.],n=10,t0=0,tend=
22
23
24
                                 Constructor
                                 1.1.1
25
                                 self.Ksqr = Ksqr
26
                                 self.sigma = sigma
27
                                 self.g = g
28
                                 self.n = n
29
                                 self_y0 = y0
30
                                 self.t0 = t0
31
                                 self.tend = tend
32
                                 self_h = h
33
                                 self.spectrum = scipy.zeros((len(self.Ksqr)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigma)*len(self.sigm
34
                    def task(self,procnum, return_dict):
35
36
                                 Defines the task that has to be preformed for a parallel worker.
37
38
                                 print '%s : started the task '%(self.name)
39
                                 teller = 0
40
                                 for i in range(len(self.Ksqr)):
41
                                             for j in range(len(self.sigma)):
42
                                                         for k in range(len(self.g)):
43
                                                                     Ksqr = self.Ksqr[i]
44
                                                                      sigma = self.sigma[j]
45
                                                                     g = self_g[k]
46
                                                                     eigen_nodes = scipy.zeros(self.n)
47
                                                                      eigen_nodes = self.search(Ksqr,sigma,g,self.n)
48
```

```
49
                                                                                a = scipy.append([Ksqr ,sigma ,g] , eigen_nodes,1)
                                                                                self.spectrum[teller,:] = a
50
                                                                                teller +=1
51
                                                                                print ('%s : Eigen Nodes for (%i,%i,%i) = %s')%(self.r
52
                                      return_dict[procnum] =
                                                                                                                          self.spectrum
53
                       def taskNonParallel(self):
54
55
                                     Creates a task with default proces number.
56
57
                                     manager = multiprocessing.Manager()
58
                                     return_dict = manager.dict()
59
                                     self.task(0, return dict)
60
                                     print return dict
61
                                     return return dict[0]
62
63
                       def search(self,Ksqrnum,sigmanum,gnum,n):
64
65
                                     A method to search for the first n roots given the specified value
66
67
                                     K sigma and g.
68
                                     raise NotImplementedError
69
70
                       def endPoint(self,wguess):
71
                       #Create the ode
72
                                     funcP = func.P(self.tempKsgrnum,self.tempsigmanum,self.tempgnum,wo
73
                                     funcQ = func.Q(self.tempKsqrnum,self.tempsigmanum,self.tempgnum,wg
74
                                     vgl = wave.WaveSystem(funcP,funcQ)
75
                                     fe = rK.RungeKutta(vgl)
76
                                     t_runge, soln_runge = fe.integrate(self.y0, self.t0, self.tend, se
77
                                     # Now we are going to calculate the local minima of the absolute \
78
                                     solution_runge = [soln_runge[i][0] for i in range(len(soln_runge))
79
                                     return solution_runge[len(solution_runge)-1]
80
81
                       def zero_point_info(self,Ksqrnum,sigmanum,gnum,wsqrnum):
82
83
                                     This method will give some information about the zero points of the
84
                                     function.
85
                                     Output:
86
                                                   - nb_of_zero: Holds the number of 0 points
87
                                                   - index_last_min: Holds the index of the last 0 point
88
                                                   - value end point: Holds the value of the endpoint of the equa
89
90
                                     #Create the ode
91
                                     funcP = func.P(Ksqrnum, sigmanum, gnum, wsqrnum)
92
                                     funcQ = func.Q(Ksqrnum, sigmanum, gnum, wsqrnum)
93
                                     vgl = wave.WaveSystem(funcP,funcQ)
94
                                     fe = rK.RungeKutta(vgl)
95
                                     t_runge, soln_runge = fe.integrate(self.y0, self.t0, self.tend, se
96
```

```
# Now we are going to calculate the local minima of the absolute \
97
            solution runge = [soln runge[i][0] for i in range(len(soln runge))
98
            index_local = argrelextrema(scipy.absolute(solution_runge), scipy.
99
            # This will in theory give all the points where the data is zero,
100
            # plus the starting point and possible also the end point.
101
            # But due to the possible un smoothness of the data some points co
102
            # appear several times.
103
            # Seen that we are looking for the first n values of we can safely
104
            # assume that two 0 points should lie at a minimum distance of say
105
           # ceil(tend/h) + 1)/20 = N/20
106
            presision = scipy.ceil(self.tend/self.h)/20
107
            nb of zero = 0
108
           # Count the number real of local 0 points.
109
            end point = solution runge[len(solution runge)-1]
110
            if (len(index local) == 0):
111
                return 0,0,end_point,len(solution_runge)
112
            if index local[0]>presision:
113
                nb\_of\_zero = 1
114
            for i in range(1,len(index_local)):
115
                if ((index_local[i]-index_local[i-1])<presision):</pre>
116
                    # if this is the case the two points are to close to
117
                    # each other and are the same minima.
118
119
                    pass
120
                else:
                    # In this case we check the number of actual 0
121
                    if(solution_runge[index_local[i]] < UPPERZERO):</pre>
122
                        nb_of_zero = nb_of_zero + 1
123
            # nb of zero should now be the number of times the function was 0
124
            index_last_min = index_local[len(index_local)-1]
125
            return nb of zero , index last min , end point , len(solution rund
126
```

```
1 | • • •
2
  Created on 27 Oct 2014
3
  @author: bob
4
5
6
  from workers.worker import Worker as worker
  import scipy
8
  from scipy.signal import argrelextrema
9
10
11
12
  # Global parameters to tweak the algorithm
13
  DIST = 1
14
  GUESS_W = 10
  |UPPERZER0| = 0.05
  PRECISION = 400
17
18
19
20
  class Worker2(worker):
21
       1.1.1
22
       A class to represent a worker to find the eigenmodes as
23
       a function of K^2, sigma and g
24
       1.1.1
25
       def __init__(self, Ksqr=[1],sigma=[1],g=[1],y0=[0.,1.],n=3,t0=0,tend=1
26
27
           The constructor to set up the right parameters and to create
28
29
           the ode's
30
           super(Worker2, self).__init__(Ksqr, sigma, g, y0, n, t0, tend, h)
31
           self.f = open(filename, 'w')
32
           self.filename = filename
33
           self.name = name
34
35
       def search(self,Ksqrnum,sigmanum,gnum,n):
36
37
           A method to search for the first n eigen modes, the hard way.
38
           This method will first guess the value of w. And based on the numb
39
           modes it will find the value for tune thise guess.
40
           If it finds a good value for w it will search for the neigbour val
41
           for w who are eigenmodes.
42
43
           self.tempKsqrnum = Ksqrnum
44
           self.tempsigmanum = sigmanum
45
           self.tempgnum = gnum
46
           N = 100
47
48
           #print w
```

```
49
           fx = scipy.zeros(N)
           nb of eigen = 0
50
           count = 0
51
           solutionW = []
52
           while nb_of_eigen < n:</pre>
53
               count = count + 1
54
               w = scipy.logspace(0.1*count,10*count,N,base=0.5)
55
               count = count+1
56
               for x in xrange(N):
57
                    fx[x] = self.endPoint(w[x])
58
               index_local = argrelextrema(scipy.absolute(fx), scipy.less)[0]
59
               solutW = scipy.zeros(len(index local))
60
               #matplotlib.pyplot.show(block=False)
61
               for i in xrange(len(index local)):
62
                    solutW[i] = w[index local[i]]
63
               nb_of_eigen = len(index_local) + nb_of_eigen
64
               solutionW = scipy.append(solutionW, solutW, 1)
65
               #matplotlib.pyplot.draw()
66
           #matplotlib.pyplot.show(block=False)
67
           return solutW[0:n]
68
69
       def getAnswer(self):
70
           if (self.spectrum==None):
71
                raise RuntimeError('No spectrum calculated')
72
           return self.spectrum
73
74
75
76
77
```

```
1.1.1
1
2
  Created on 08 Nov 2014
3
  @author: bob
4
  1.1.1
5
6
7
   1.1.1
8
  Created on 08 Nov 2014
9
10
  @author: bob
11
12
  from workers.worker import Worker as worker
13
  import scipy
14
15
  GUESS_W = 10
16
  MAX TOL = 0.000001
17
18
  class workerSimple(worker):
19
20
       A class to represent a worker to find the eigenmodes as
21
       a function of K^2, sigma and g
22
23
       def __init__(self, Ksqr=[1],sigma=[1],g=[1],y0=[0.,1.],n=3,t0=0,tend=1
24
25
           The constructor to set up the right parameters and to create
26
           the ode's
27
           1.1.1
28
           super(workerSimple, self).__init__(Ksqr, sigma, g, y0, n, t0, tend
29
           self.f = open(filename, 'w')
30
           self.filename = filename
31
32
           self.name = name
       def search(self,Ksqrnum,sigmanum,gnum,n):
33
           guess = GUESS_W/0.9
34
           self.tempKsqrnum = Ksqrnum
35
           self.tempsigmanum = sigmanum
36
           self.tempgnum = gnum
37
           endP = self.endPoint(guess)
38
           while endP<0:
39
               guess = guess*10
40
               endP = self.endPoint(guess)
41
           guesses = scipy.zeros(n)
42
           positiveGuess = quess
43
           for i in range(n):
44
                teken = (-1)**i
45
               endP = self.endPoint(guess)
46
                shrinksize = 0.9
47
48
                overCount = 1
```

```
while scipy.absolute(endP)>MAX_TOL:
49
                    previous = guess
50
                     guess = previous * shrinksize
51
                    endP = self.endPoint(guess)
52
53
54
                     if (scipy.absolute(endP)<MAX_TOL):</pre>
                         break
55
                     if (teken*endP<0):</pre>
56
                         overCount = overCount +1
57
                         shrinksize = shrinksize + 9./(10**overCount)
58
                         guess = positiveGuess
59
                         guess = guess/shrinksize
60
                     elif (teken*endP>0):
61
                         positiveGuess = guess
62
                guesses[i] = guess
63
                while (scipy.absolute(endP)<MAX_TOL ):</pre>
64
                    quess = positiveGuess
65
                    guess = guess/shrinksize
66
                    endP = self.endPoint(guess)
67
                    pass
68
            return guesses
69
70
71
72
73
74
75
76
77
78
```

```
1 | • • •
  Created on 15 Oct 2014
2
3
  @author: bob
4
5
  This task tests the worker class in more detail.
6
   1.1.1
7
8
  from workers.worker2 import Worker2 as worker2
9
  import scipy
10
  from matplotlib import pyplot as plot
11
12
  if __name__ == '__main__':
13
       Ksqr = scipy.linspace(0.5, 1.5, 1).tolist()
14
       sigma = scipy.linspace(0.5, 1.5,10).tolist()
15
       g = scipy.linspace(0.5, 1.5, 1).tolist()
16
       n = 3
17
       y0=[0.,1.];
18
       t0=0
19
       tend=1
20
       h=0.01
21
       eigenSys = worker2(Ksqr,sigma,q,y0,n,t0,tend,h)
22
       data = eigenSys.taskNonParallel()
23
       print data
24
       plot.plot(data[:,1],data[:,3])
25
       plot.show()
26
27
28
29
```

```
1.1.1
1
  Created on 15 Oct 2014
2
3
  @author: bob
4
5
6
  A test file for the worker class.
8
  1.1.1
9
10
  from workers.workerSimple import workerSimple as workerSimple
11
  import system.waveSystem as wave
  import function.function as func
13
  import integrators.rungeKutta as rK
14
  import matplotlib.pyplot as plt
16
  Ksqr = [1]
17
  sigma = [1]
18
19 || q = [1]
20 n = 10
21 || y0 = 0
  | t0 = 1
22
  tend = 1
24
  h = 0.01
25
  \#wsqrnum = 0.3-0.285
26
  wsqrnum = 0.015*(1+23./50)
27
  wsgrnum = wsgrnum*(1+7./50)
28
  wsqrnum = 0.001
29
30
  class rho0(func.Function):
31
       def __init__(self,Ksqr,sigma,g,wsqr):
32
           func.Function. init (self)
33
           self.Ksqr = Ksqr
34
           self.sigma = sigma
35
           self.g = g
36
           self.wsqr = wsqr
37
       def evaluate(self, x):
38
           return (1+self.sigma*x)
39
  # Create the two objects to represent the functions P and Q
40
  class P(func.Function):
41
       def __init__(self,Ksqr,sigma,g,wsqr):
42
           func.Function. init (self)
43
           self.Ksqr = Ksqr
44
           self.sigma = sigma
45
           self.g = g
46
           self.wsqr = wsqr
47
       def evaluate(self, x):
48
```

```
return self.wsgr*rho0(self.Ksgr,self.sigma,self.g,self.wsgr).evalu
49
  class Q(func.Function):
50
       def __init__(self,Ksqr,sigma,g,wsqr):
51
           func.Function.__init__(self)
52
           self.Ksqr = Ksqr
53
           self.sigma = sigma
54
           self_q = q
55
           self.wsqr = wsqr
56
       def evaluate(self, x):
57
           return -self.Ksqr*(rho0(self.Ksqr,self.sigma,self.g,self.wsqr).eva
58
                               rho0(self.Ksqr,self.sigma,self.g,self.wsqr).der
59
60
61
  def plot ode(Ksqr, sigma, q, wsqr):
62
       funcP = P(Ksqr,sigma,g,wsqr)
63
       funcQ = Q(Ksqr,sigma,g,wsqr)
64
       vgl = wave.WaveSystem(funcP, funcQ)
65
       fe = rK.RungeKutta(vgl)
66
       t_runge, soln_runge = fe.integrate(y0,t0,tend,h)
67
       solution_runge = [soln_runge[i][0] for i in range(len(soln_runge))]
68
       plt.plot(t_runge, solution_runge)
69
       plt.show()
70
71
       pass
72
73
  def nb0fZerosnumber_of_zeros():
74
       eigenSys = workerSimple(Ksqr,sigma,g,y0,n,t0,tend,h)
75
       print eigenSys.zero point info(Ksgrnum=1, sigmanum=1, gnum=1, wsgrnum=
76
77
  def find eigen mode():
78
       w = wsqrnum
79
       eigenSys = workerSimple(Ksqr,sigma,g,y0,n,t0,tend,h)
80
       nb_of_zero , index_last_min , end_point , length_Set = eigenSys.zero_p
81
       newW = w
82
       while (nb_of_zero==0):
83
           newW = (newW + 0.0)/2
84
           nb_of_zero , index_last_min , end_point , length_Set = eigenSys.ze
85
       print nb of zero , index last min , end point , length Set
86
87
       print newW
88
89
       previousW = newW
       counter = 0
90
       while(abs(end_point)>0.001):
91
           counter = counter +1
92
           nb_of_zero_new , index_last_min_new , end_point_new , length_Set_r
93
           print counter, newW , nb_of_zero_new , index_last_min_new , end_pot
94
           if (abs(end_point_new)<0.001):</pre>
95
               break
96
```

```
97
            if (nb of zero new>=nb of zero):
                # Vergroot w
98
                previousW = newW
99
                newW = newW*(1+((length Set-index last min new)+0.0)/index last
100
            if (nb_of_zero_new < nb_of_zero):</pre>
101
                # Nu weten we dat het vorige punt wel nog achter het nulpunt 1
102
                # gemmidelde tussen het slechte punt en het vorige goede punt.
103
                newW = ((newW+previousW)+0.0)/2
104
        print newW
105
        plot ode(Ksqr=1, sigma=1, g=1, wsqr=newW)
106
107
   def task():
108
        eigenSys = workerSimple(Ksqr,sigma,q,y0,n,t0,tend,h)
109
        eigenSys.task()
110
        pass
111
112
   if name == ' main ':
113
        Ksqr = [1]
114
        sigma = [1]
115
        q = [1]
116
        n = 10
117
        y0 = 0
118
        t0 = 1
119
        tend = 1
120
        h = 0.1
121
        Ksqr=[1]; sigma=[1]; g=[1]; y0=[0.,1.]; n=10; t0=0; tend=1; h=0.01
122
        #nb0fZerosnumber_of_zeros()
123
        #find eigen mode()
124
        #plot_ode(Ksqr=1, sigma=1, g=1, wsqr=wsqrnum)
125
        task()
126
127
128
129
130
```