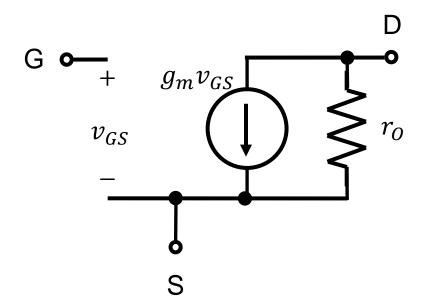
Lecture14: Impedance

Sung-Min Hong (smhong@gist.ac.kr)

Semiconductor Device Simulation Lab.
School of Electrical Engineering and Computer Science
Gwangju Institute of Science and Technology

Small-signal MOSFET model

- Small-signal MOSFET model
 - Two branches are related with two partial derivatives.



Simple math

- Following relations are useful.
 - Sine and cosine functions can be expanded with $e^{+j\omega t}$ and $e^{-j\omega t}$.

$$\sin \omega t = -\frac{j}{2}e^{+j\omega t} + \frac{j}{2}e^{-j\omega t}$$
$$\cos \omega t = \frac{1}{2}e^{+j\omega t} + \frac{1}{2}e^{-j\omega t}$$

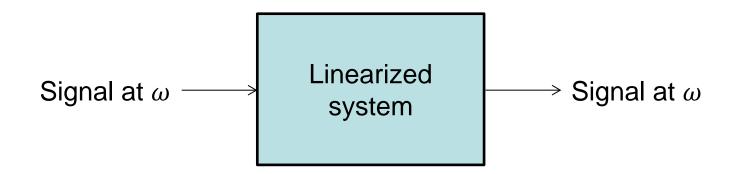
- Therefore, for a function of $f(t) = f_s \sin \omega t + f_c \cos \omega t$, the expansion is

$$f(t) = \left(-j\frac{f_s}{2} + \frac{f_c}{2}\right)e^{+j\omega t} + \left(+j\frac{f_s}{2} + \frac{f_c}{2}\right)e^{-j\omega t}$$

- A single complex number, $-j\frac{f_s}{2} + \frac{f_c}{2}$, is enough to represent f(t).

Linearized system

- Our circuit is nonlinear in general.
- However, we have <u>linearized</u> it.
 - When the input signal has an angluar frequency, ω , the output signal has the same one.
 - It is sufficient to consider the input-output relation at ω .



Impedance

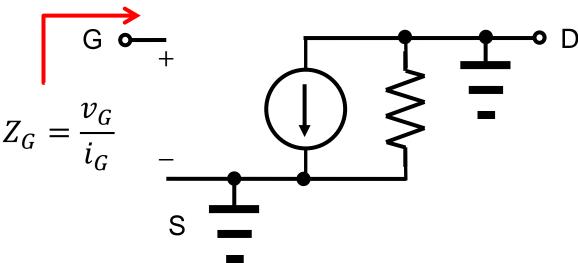
- Resistance, V(t) = R I(t)
 - It is assumed that V(t) and I(t) are in the same phase.
- Impedance, $V(\omega) = Z(\omega)I(\omega)$
 - Consider $V(t) = V_0 \sin \omega t$ and $I(t) = I_0 \cos \omega t$. (Different phases)
 - We introduce a phasor voltage, $V(\omega)$, and a phasor current, $I(\omega)$.
 - The relation between V(t) and $V(\omega)$ is $V(t) = Re[V(\omega)e^{j\omega t}]$.
 - When $V(t) = V_0 \sin \omega t$, the phasor voltage is $V(\omega) = -jV_0$.
 - When $I(t) = I_0 \cos \omega t$, the phasor voltage is $I(\omega) = I_0$.
 - In this example, $Z(\omega) = -j\frac{V_0}{I_0}$. A purely imaginary number.

Multi-terminal devices

- When the number of terminals is 3,
 - We can define 9 (= 3 X 3) different impedances.
- Termination condition is important.
 - Depending on the termination condition, the impedance can be heavily changed.
 - In many cases, it is obvious from the problem.

Impedances of MOSFET

- "Looking into the <u>TERMINAL</u>," we see the impedance of the <u>TERMINAL</u>.
 - Example) Looking into the gate. The source and drain are acgrounded.

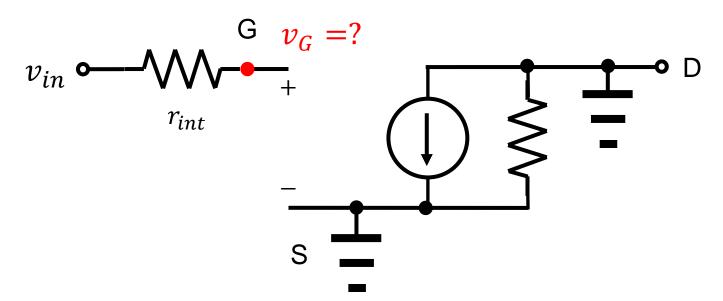


Similar for other terminals

Input impedance

- Consider a input signal with a finite internal resistance.
 - Usually, the internal resistance is small, but not zero.
 - The actual small-signal voltage applied to the gate terminal is given by

$$v_G(\omega) = v_{in} \frac{Z_G(\omega)}{r_{int} + Z_G(\omega)}$$



Homework#6

- Due: 09:00, April 29 (Mon)
- Solve the following problems of the <u>2019</u> mid-term exam.
 - P9, P11, P14, P16, P18, P24, P26, P29, P32, P33, P34, P35, P37,P39, and P40
 - In total, 15 problems.