

1. Derive the strain transformation matrix,  $[T]_\epsilon$ , from the equation given below:

$$\begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \epsilon_{12} \end{bmatrix} = [T] \begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_{xy} \end{bmatrix}$$

2. Derive  $\eta_{y,xy}$  and  $\eta_{xy,x}$  as a function of engineering constants in principal material coordinates.

3. Write a MATLAB function to import the lamina properties given below from an Excel spreadsheet and plot the elastic constants as a function of lamina orientation,  $\theta$ .

$$E_1 = 135 \text{ GPa}, E_2 = 10 \text{ GPa}, G_{12} = 5 \text{ GPa}, \nu_{12} = 0.3$$

- Plot  $E_x$  as a function of  $\theta$  (normalize the y axis with  $E_1$ )
- Plot  $G_{xy}$  as a function of  $\theta$  (normalize the y axis with  $G_{12}$ )
- Plot  $E_y$  as a function of  $\theta$  (normalize the y axis with  $E_2$ )
- Plot  $\nu_{xy}$  as a function of  $\theta$  (normalize the y axis with  $\nu_{12}$ )
- Plot  $\eta_{y,xy}$  as a function of  $\theta$

4. Write a short paragraph for each plot stating your interpretation of the plot.