

1 Part I: Basic Probability and Statistics

1. (4 pts) Consider an experiment where a coin is tossed repeatedly until the first time a head is observed.

This is a geometric distribution

- a. What is the sample space for this experiment? What is the probability that the coin turns up heads after i tosses?

The sample space is $\{H, TH, TTH, TTTH, \dots\}$

$$(1 - p)^{k-1}p$$

So, the probability will be $(1 - \frac{1}{2})^{i-1} \frac{1}{2} = \frac{1}{2}^i$

- b. Let E be the event that the first time a head turns up is after an even number of tosses. What set of outcomes belong to this event? What is the probability that E occurs?

$(1 - p)^{k-1}p$, where k is even

So, $1/2^2 + 1/2^4 + \dots$

$$a = 1/4, r = 1/4$$

$$\frac{a}{1-r} = \frac{1/4}{3/4} = \frac{1}{3}$$

The sample space is $\{TH, TTTH, TTTTTH, \dots\}$

2. (5 pts) Two standard dice are rolled. Let E be the event that the sum of the dice is odd; let F be the event that at least one of the dice lands on 1; and let G be the event that the sum is 5. Compute the following:

Total events = 36

$E = (1,2), (1,4), (1,6), (2,1), (2,3), (2,5), (3,2), (3,4), (3,6), (4,1), (4,3), (4,5), (5,2), (5,4), (5,6), (6,1), (6,3), (6,5)$

$F = (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (2,1), (3,1), (4,1), (5,1), (6,1)$

$G = (1,4), (2,3), (3,2), (4,1)$

- a. $P(E \cap F)$
 $\{(1,2), (1,4), (1,6), (2,1), (4,1), (6,1)\}$

$$\frac{6}{6^2} = \frac{1}{6}$$

- b. $P(E \cup F)$
 $\frac{23}{36}$

- c. $P(F \cup G)$
 $\frac{13}{36}$

- d. $P(E \cup \neg F)$
 $\frac{31}{36}$

- e. $P(E \cup F \cup G)$

$\frac{23}{36}$

3. (6 pts) A system is built using 3 disks d_1 , d_2 , d_3 having probabilities of failure 0.01, 0.03 and 0.05 respectively. Suppose the disks fail independently.

- a. Let E denote the event of loss of data, which occurs only if two or more disks fail.

Compute $P(E)$, the probability of loss of data.

$$P(\neg E) = 1 \text{ disk fail or no disk fail} = 0.99 * 0.97 * 0.95 + 0.99 * 0.97 * 0.05 + 0.99 * 0.03 * 0.95 + 0.01 * 0.97 * 0.95 = 0.99773$$

$$P(E) = 1 - 0.99773 = 0.00227$$

- b. Instead, let F denote the event that at least one of the following happens: (i) d_1 fails; (ii) d_2 and d_3 both fail. If loss of data only occurs when event F occurs, then what is the probability that there is loss of data?

$$P(F) = P(i \cup ii) = 0.01 * 0.97 * 0.95 + 0.99 * 0.03 * 0.05 - 0.01 * 0.03 * 0.05 = 0.010685$$

- c. Considering the setting of 3b, given that d_3 has failed, what is the conditional probability that event F will occur and there will be loss of data?

G : d_3 has failed

$$P(F | G) = P(F \cap G) / P(G) = 0.99 * 0.03 * 0.05 / (0.99 * 0.97 * 0.05) = 0.0309$$

4. (6 pts) 52% of the students at a particular college are female. 5% of the students in the college are majoring in computer science. 0.55% of the students are women majoring in computer science.

F : female $P(F) = 0.52$

C : CS student $P(C) = 0.05$

$$P(C \cap F) = 0.0055$$

- a. If a student is selected at random, find the conditional probability that the student is female given that they are majoring in computer science. (State this as a conditional probability and show the calculation.)

$$P(F | C) = P(F \cap C) / P(C) = 0.0055 / 0.05 = 0.11$$

- b. If a student is selected at random, find the conditional probability that the student is majoring in computer science given that they are female. (State this as a conditional probability and show the calculation.)

$$P(C | F) = P(F \cap C) / P(F) = 0.0055 / 0.52 = 0.0106$$

- c. Now suppose that the overall proportion of female students increases to 57% and that the conditional probability from 4a changes (i.e., increases or decreases) to 15%. Compute the updated conditional probability that a student is majoring in computer science given that they are female. (Assume that the overall proportion of students majoring in CS stays the same.)

F : female $P(F) = 0.57$

$$P(F | C) = 0.15$$

$$P(C | F) = P(F \cap C) / P(F) = P(F | C) * P(C) / P(F) = 0.15 * 0.05 / 0.57 = 0.0132$$

5. (6 pts) Let X_n be the random variable that equals the number of heads minus the number of tails when n coins are flipped. Each flip has a probability of p of heads, $1 - p$ probability of tails. Do not assume $p = 1/2$.

- a. What is the expected value of X_n ?
 $E \text{ of heads} = np$, let's assume i heads, and $n-i$ tails
 $P(i - (n - i)) = P(2i - n)$; $E(2i - n) = 2E(i) - E(n) = 2np - n$
- b. What is the variance of X_n ?
 $\text{Var} = E(X_n^2) - E(X_n)^2 = 4np(1-p)$
- c. Compute the expected value and variance of X_3 . Plug it in, $n = 3$
 $E(X_3) = 6p - 3$
 $\text{Var}(X_3) = 12p(1-p)$

2 Part II: R

3 Data import and summarization

```
yelp = read.csv("yelp.csv", header = TRUE, quote="\"", comment.char="")
```

- a. (2 pts) Print the names of the columns in the table using `names()`.

```
names(yelp)
```

```
## [1] "business_id"      "name"              "fullAddress"
## [4] "city"             "state"             "latitude"
## [7] "longitude"        "stars"             "reviewCount"
## [10] "checkins"         "open"              "neighborhoods"
## [13] "categories"       "alcohol"            "noiseLevel"
## [16] "attire"           "priceRange"        "delivery"
## [19] "ambience"        "parking"           "dietaryRestrictions"
## [22] "waiterService"   "smoking"           "outdoorSeating"
## [25] "caters"          "recommendedFor"    "goodForGroups"
## [28] "goodForKids"
```

- b. (2 pts) Print a summary of the data using the `summary()` function.

```
summary(yelp)
```

```
##               business_id               name
## __etvGuL2dh_a1LOT0gNYQ:      1 Starbucks : 407
## __kNfrrGoUXoF-BYciMU_Q:      1 McDonald's: 275
## __Y2jjdCFHvq3rzSbpDBlw:      1 Subway    : 256
## __-lEgXrkOlKajCsmasuEgg:      1 Walgreens : 158
## __-6I6VXjr-NiwIBa_luI4A:      1 Taco Bell : 148
## __-9pMxBWtG_x8l4rHWBasg:      1 Wendy's   : 113
## (Other)                      :24807 (Other)   :23456
##
##
Address
## Bellagio Las Vegas\n3600 S Las Vegas Blvd\nThe Strip\nLas Vegas, NV 89109
: 21
```

```

## Las Vegas, NV
: 17
## 5000 S Arizona Mills Cir\nTempe, AZ 85282
: 14
## 3131 Las Vegas Blvd. South\nThe Strip\nLas Vegas, NV 89109
: 13
## Monte Carlo Hotel and Casino\n3770 Las Vegas Blvd S\nThe Strip\nLas Vegas, NV
89109: 13
## 2000 E Rio Salado Pkwy\nTempe, AZ 85281
: 12
## (Other)
:24723
## city state latitude longitude
## Las Vegas : 5256 AZ :9301 Min. :32.88 Min. : -115.370
## Phoenix : 3072 NV :6296 1st Qu.:33.54 1st Qu.: -114.977
## Charlotte : 1993 QC :2389 Median :36.03 Median : -111.924
## Pittsburgh: 1467 NC :2370 Mean :37.53 Mean : -97.298
## Scottsdale: 1296 PA :1613 3rd Qu.:40.41 3rd Qu.: -80.807
## Montral : 1267 WI :1089 Max. :55.99 Max. : 8.549
## (Other) :10462 (Other):1755
## stars reviewCount checkins open
## Min. :1.000 Min. : 3.00 Min. : 3 Mode :logical
## 1st Qu.:3.000 1st Qu.: 8.00 1st Qu.: 16 FALSE:3580
## Median :3.500 Median : 18.00 Median : 48 TRUE :21233
## Mean :3.544 Mean : 49.03 Mean : 166 NA's :0
## 3rd Qu.:4.000 3rd Qu.: 48.00 3rd Qu.: 155
## Max. :5.000 Max. :4578.00 Max. :14203
##
## neighborhoods categories
## [] :15727 ['Mexican', 'Restaurants'] : 1331
## ['The Strip']: 816 ['Food', 'Coffee & Tea'] : 844
## ['Southeast']: 639 ['Pizza', 'Restaurants'] : 831
## ['Downtown'] : 533 ['Chinese', 'Restaurants'] : 776
## ['Westside'] : 526 ['Burgers', 'Fast Food', 'Restaurants']: 549
## ['Eastside'] : 447 ['Restaurants', 'Italian'] : 509
## (Other) : 6125 (Other) :19973
## alcohol noiseLevel attire priceRange
## : 3 : 7947 : 7005 Min. :1.000
## beer_and_wine: 2497 average :10957 casual:17129 1st Qu.:1.000
## full_bar : 7565 loud : 1622 dressy: 640 Median :2.000
## none :14748 quiet : 3562 formal: 39 Mean :1.631
## very_loud: 725 3rd Qu.:2.000
## Max. :4.000
## NA's :903
## delivery ambience parking
## Mode :logical ['casual']:7878 ['lot'] :10348
## FALSE:14471 :7875 [] : 6675
## TRUE :3093 [] :6348 ['street'] : 3046
## NA's :7249 ['divey'] : 716 : 2456
## ['trendy']: 567 ['garage'] : 907
## ['classy']: 320 ['street', 'lot']: 364
## (Other) :1109 (Other) : 1017
## dietaryRestrictions waiterService smoking
## :24696 Mode :logical :21862

```

```
## ['vegan'] : 45 FALSE:6208 no : 904
## ['vegetarian'] : 23 TRUE :10351 outdoor: 1415
## [] : 20 NA's :8254 yes : 632
## ['dairy-free', 'vegetarian']: 7
## ['vegan', 'vegetarian'] : 5
## (Other) : 17
## outdoorSeating caters recommendedFor
## Mode :logical Mode :logical :7859
## FALSE:10989 FALSE:6503 [] :4932
## TRUE :8698 TRUE :5932 ['lunch'] :4324
## NA's :5126 NA's :12378 ['dinner'] :2553
## ['lunch', 'dinner']:1966
## ['breakfast'] :1004
## (Other) :2175
## goodForGroups goodForKids
## Mode :logical Mode :logical
## FALSE:2054 FALSE:506
## TRUE :17078 TRUE :1283
## NA's :5681 NA's :23024
##
##
##
```

c. (2 pts) Print a summary of the noiseLevel attribute and the stars attribute.

```
summary(yelp$noiseLevel)
```

```
##          average      loud      quiet very_loud
##          7947      10957      1622      3562      725
```

```
summary(yelp$stars)
```

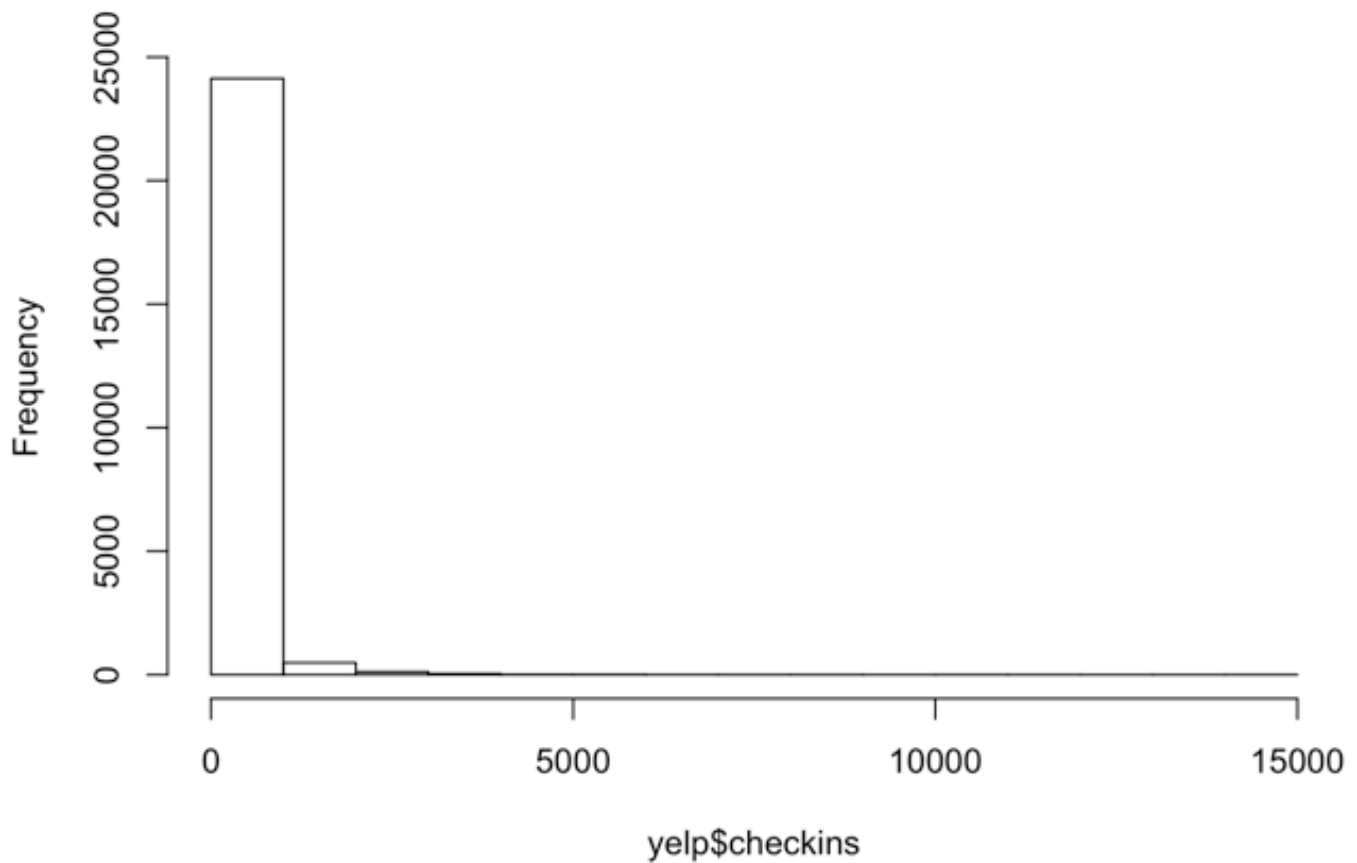
```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      1.000   3.000   3.500   3.544   4.000   5.000
```

4 1D plots

a. (4 pts) Plot a histogram of the checkins attribute. Use the hist() function with its default values and make sure to title the plot with the name of the attribute for clarity.

```
hist(yelp$checkins)
```

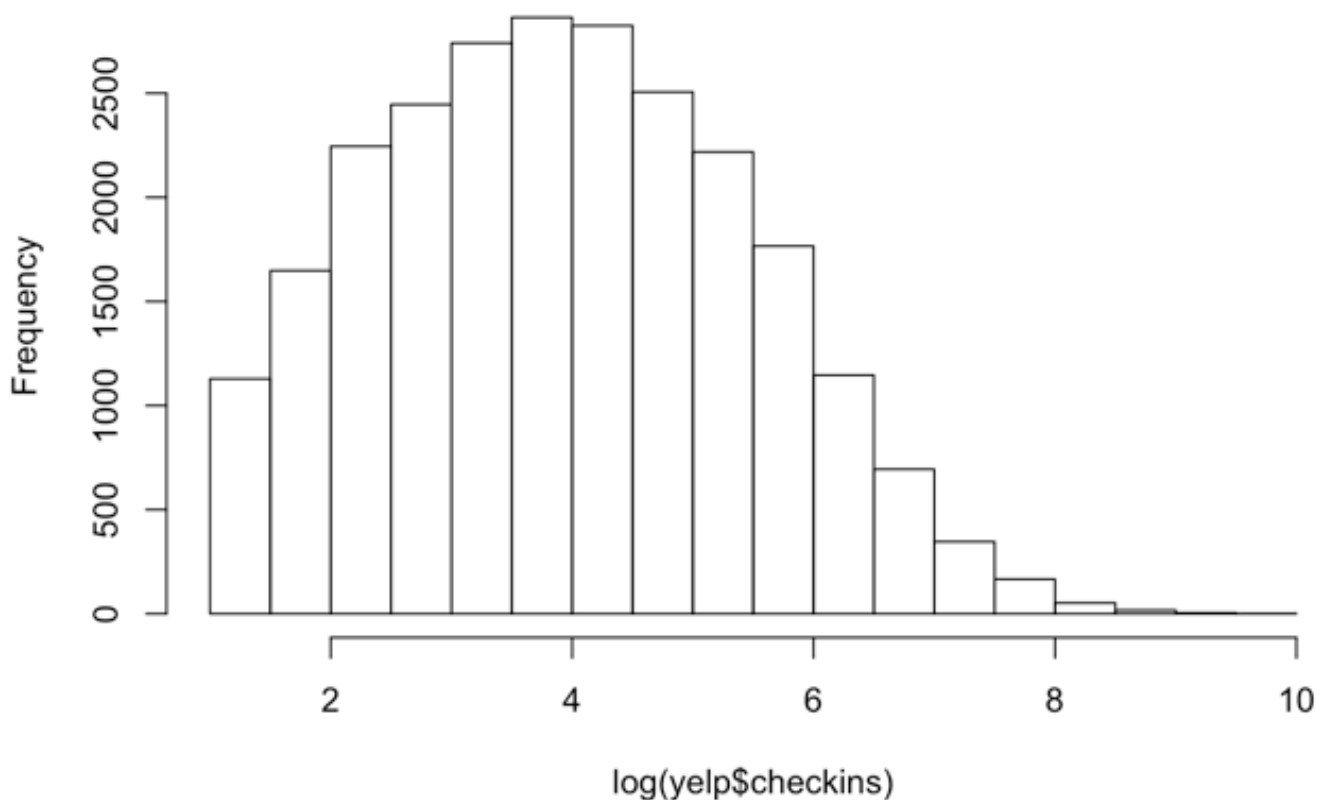
Histogram of yelp\$checkins



(b) (4 pts) Compute the logged values for checkins (you can use `log()` to compute the log of all the values in a vector). Plot a histogram of the logged values.

```
hist(log(yelp$checkins))
```

Histogram of log(yelp\$checkins)



- c. (4 pts) Discuss the differences between the two plots and the information they convey about the distribution of checkins values in the data.

The difference between two plots is obvious. The first plot is skewed as hell, and the log function will help us remove the skewness and it will reveal the more helpful information. Because of the density for the low frequency is too high, so the normal histogram is sort of meaningless.

5 Sampling and transforming data

- a. (4 pts) The attributes categories and recommendedFor each contain a comma separated list of values associated with each restaurant. Compute two new boolean features: isAmerican and goodForDinner with a value of TRUE if the list contains “American” (in categories), “dinner” (in recommendedFor) respectively and FALSE otherwise. You can use the function grepl(str, f\$column name) to check whether the values in column name contain the string str. Append the two new columns to the original data frame, using cbind(), to increase the number of features to 32. Show the output of summary() for those two columns.

```
isAmerican = grepl("American", yelp$categories)
goodForDinner = grepl("dinner", yelp$recommendedFor)
yelp = cbind(yelp, isAmerican, goodForDinner)
summary(yelp$isAmerican)
```

```
##      Mode  FALSE    TRUE   NA's
## logical  21456   3357     0
```

```
summary(yelp$goodForDinner)
```

```
##      Mode   FALSE    TRUE   NA's  
## logical  19670    5143      0
```

b. (4 pts) Print the quantiles (using `quantile()`) for the `reviewCount` attribute.

```
quantile(yelp$reviewCount)
```

```
##      0%   25%   50%   75%  100%  
##       3     8    18    48  4578
```

c. (6 pts) Select a subset of the data with `reviewCount` value \leq 1st quartile (25th percentile). You can use `subset()` or select from the data frame with `[]` operations. Print a summary of the above subset for the following attributes: `reviewCount`, `stars`, `attire`, `priceRange`, `delivery`, `goodForKids`, and compare them to their summary for the full dataset. Discuss any differences in the distributions of the numerical attributes that you find.

```
lowReviewCount = subset(yelp, yelp$reviewCount <= quantile(yelp$reviewCount, 0.25)  
)  
#instead of give summary for individual, I print out the general summary and look  
at the reviewCount, stars, attire, priceRange, delivery, goodForKids individually.  
summary(lowReviewCount)
```

```
##                business_id                name  
## __Y2jjdCFHvq3rzSbpDBlw:    1    Subway      : 213  
## _-1EgXrkOlKajCsmasuEgg:    1    McDonald's  : 174  
## _-6I6VXjr-NiwIBa_luI4A:    1    Starbucks   : 137  
## _-EB8tQzBlM_jLkgtRw4Rg:    1    Walgreens   : 115  
## _04PNAespgMZVXBjrkmbNA:    1    Taco Bell    : 99  
## _0DI4UXAaFC6hOYpBadtIw:    1    Burger King: 80  
## (Other)                   :6954    (Other)    :6142  
##                                fullAddress                city  
## 5000 S Arizona Mills Cir\nTempe, AZ 85282          :    7    Las Vegas :1189  
## 1300 W Sunset Rd\nHenderson, NV 89014      :    6    Phoenix   : 819  
## Las Vegas, NV          :    6    Charlotte  : 553  
## 11025 Carolina Place Pkwy\nPineville, NC 28134      :    5    Montreal   : 514  
## 138, avenue Atwater\nMontreal, QC H4C 2G3      :    5    Pittsburgh: 386  
## 4300 Meadows Ln\nWestside\nLas Vegas, NV 89107      :    5    Montreal   : 347  
## (Other)                   :6926    (Other)    :3152  
##      state      latitude      longitude      stars  
## AZ      :2400    Min.      :32.88    Min.      : -115.352    Min.      :1.000  
## NV      :1479    1st Qu.:33.58    1st Qu.: -112.264    1st Qu.:3.000  
## QC      :1129    Median :36.08    Median : -111.823    Median :3.500  
## NC      : 701    Mean     :38.30    Mean     : -94.056    Mean     :3.418  
## PA      : 440    3rd Qu.:43.07    3rd Qu.: -79.998    3rd Qu.:4.000  
## EDH     : 299    Max.      :55.99    Max.      : 8.485    Max.      :5.000  
## (Other): 512  
##      reviewCount      checkins      open      neighborhoods  
## Min.      :3.000    Min.      : 3.00    Mode :logical    []      :4839
```



```

## 1st Qu.:4.000 1st Qu.: 7.00 FALSE:887 ['Southeast']: 144
## Median :5.000 Median : 13.00 TRUE :6073 ['Downtown'] : 140
## Mean :5.247 Mean : 24.78 NA's :0 ['The Strip']: 136
## 3rd Qu.:7.000 3rd Qu.: 29.00 ['Eastside'] : 133
## Max. :8.000 Max. :694.00 ['Westside'] : 119
## (Other) :1449
## categories alcohol
## ['Burgers', 'Fast Food', 'Restaurants']: 310 : 0
## ['Food', 'Grocery'] : 293 beer_and_wine: 266
## ['Food', 'Coffee & Tea'] : 285 full_bar : 968
## ['Fast Food', 'Restaurants'] : 278 none :5726
## ['Mexican', 'Restaurants'] : 274
## ['Pizza', 'Restaurants'] : 262
## (Other) :5258
## noiseLevel attire priceRange delivery
## :4096 :3248 Min. :1.000 Mode :logical
## average :1549 casual:3581 1st Qu.:1.000 FALSE:2899
## loud : 324 dressy: 107 Median :1.000 TRUE :693
## quiet : 836 formal: 24 Mean :1.546 NA's :3368
## very_loud: 155 3rd Qu.:2.000
## Max. :4.000
## NA's :825
## ambience parking
## :4104 [] :3518
## [] :2550 :1897
## ['casual'] : 226 ['lot'] :1059
## ['divey'] : 36 ['street'] : 333
## ['hipster']: 9 ['garage'] : 59
## ['trendy'] : 7 ['street', 'lot']: 39
## (Other) : 28 (Other) : 55
## dietaryRestrictions
## :6955
## ['vegan']
## : 3
## ['vegetarian']
## : 1
## []
## : 1
## ['dairy-free', 'gluten-free', 'vegan', 'halal', 'soy-free', 'vegetarian']
## : 0
## ['dairy-free', 'gluten-free', 'vegan', 'kosher', 'halal', 'soy-free', 'vegetarian']
## : 0
## (Other)
## : 0
## waiterService smoking outdoorSeating caters
## Mode :logical :6578 Mode :logical Mode :logical
## FALSE:1323 no : 111 FALSE:2672 FALSE:1040
## TRUE :1729 outdoor: 157 TRUE :1370 TRUE :620
## NA's :3908 yes : 114 NA's :2918 NA's :5300
##
##
##

```

```
## recommendedFor goodForGroups goodForKids
## :3832 Mode :logical Mode :logical
## [ ] :2532 FALSE:704 FALSE:15
## ['lunch'] : 249 TRUE :3471 TRUE :31
## ['breakfast'] : 93 NA's :2785 NA's :6914
## ['lunch', 'dinner']: 76
## ['dinner'] : 54
## (Other) : 124
## isAmerican goodForDinner
## Mode :logical Mode :logical
## FALSE:6452 FALSE:6796
## TRUE :508 TRUE :164
## NA's :0 NA's :0
##
##
##
```

summary(yelp)

```
## business_id name
## __etvGuL2dh_a1LOT0gNYQ: 1 Starbucks : 407
## __kNfrrGoUXoF-BYciMU_Q: 1 McDonald's: 275
## __Y2jjdCFHvq3rzSbpDBlw: 1 Subway : 256
## _lEgXrkOlKajCsmasuEgg: 1 Walgreens : 158
## _6I6VXjr-NiwIBa_luI4A: 1 Taco Bell : 148
## _9pMxBWtG_x8l4rHWBasg: 1 Wendy's : 113
## (Other) :24807 (Other) :23456
## full
Address
## Bellagio Las Vegas\n3600 S Las Vegas Blvd\nThe Strip\nLas Vegas, NV 89109
: 21
## Las Vegas, NV
: 17
## 5000 S Arizona Mills Cir\nTempe, AZ 85282
: 14
## 3131 Las Vegas Blvd. South\nThe Strip\nLas Vegas, NV 89109
: 13
## Monte Carlo Hotel and Casino\n3770 Las Vegas Blvd S\nThe Strip\nLas Vegas, NV
89109: 13
## 2000 E Rio Salado Pkwy\nTempe, AZ 85281
: 12
## (Other)
:24723
## city state latitude longitude
## Las Vegas : 5256 AZ :9301 Min. :32.88 Min. : -115.370
## Phoenix : 3072 NV :6296 1st Qu.:33.54 1st Qu.: -114.977
## Charlotte : 1993 QC :2389 Median :36.03 Median : -111.924
## Pittsburgh: 1467 NC :2370 Mean :37.53 Mean : -97.298
## Scottsdale: 1296 PA :1613 3rd Qu.:40.41 3rd Qu.: -80.807
## Montral : 1267 WI :1089 Max. :55.99 Max. : 8.549
## (Other) :10462 (Other):1755
## stars reviewCount checkins open
```

```

## Min.      :1.000   Min.      : 3.00   Min.      : 3   Mode :logical
## 1st Qu.:3.000   1st Qu.: 8.00   1st Qu.: 16   FALSE:3580
## Median :3.500   Median : 18.00   Median : 48   TRUE :21233
## Mean    :3.544   Mean    : 49.03   Mean    : 166   NA's :0
## 3rd Qu.:4.000   3rd Qu.: 48.00   3rd Qu.: 155
## Max.    :5.000   Max.    :4578.00   Max.    :14203
##
## neighborhoods categories
## [] :15727 ['Mexican', 'Restaurants'] : 1331
## ['The Strip']: 816 ['Food', 'Coffee & Tea'] : 844
## ['Southeast']: 639 ['Pizza', 'Restaurants'] : 831
## ['Downtown'] : 533 ['Chinese', 'Restaurants'] : 776
## ['Westside'] : 526 ['Burgers', 'Fast Food', 'Restaurants']: 549
## ['Eastside'] : 447 ['Restaurants', 'Italian'] : 509
## (Other) : 6125 (Other) :19973
## alcohol noiseLevel attire priceRange
## : 3 : 7947 : 7005 Min. :1.000
## beer_and_wine: 2497 average :10957 casual:17129 1st Qu.:1.000
## full_bar : 7565 loud : 1622 dressy: 640 Median :2.000
## none :14748 quiet : 3562 formal: 39 Mean :1.631
## very_loud: 725 3rd Qu.:2.000
## Max. :4.000
## NA's :903
## delivery ambience parking
## Mode :logical ['casual']:7878 ['lot'] :10348
## FALSE:14471 :7875 [] : 6675
## TRUE :3093 [] :6348 ['street'] : 3046
## NA's :7249 ['divey'] : 716 : 2456
## ['trendy']: 567 ['garage'] : 907
## ['classy']: 320 ['street', 'lot']: 364
## (Other) :1109 (Other) : 1017
## dietaryRestrictions waiterService smoking
## :24696 Mode :logical :21862
## ['vegan'] : 45 FALSE:6208 no : 904
## ['vegetarian'] : 23 TRUE :10351 outdoor: 1415
## [] : 20 NA's :8254 yes : 632
## ['dairy-free', 'vegetarian']: 7
## ['vegan', 'vegetarian'] : 5
## (Other) : 17
## outdoorSeating caters recommendedFor
## Mode :logical Mode :logical :7859
## FALSE:10989 FALSE:6503 [] :4932
## TRUE :8698 TRUE :5932 ['lunch'] :4324
## NA's :5126 NA's :12378 ['dinner'] :2553
## ['lunch', 'dinner']:1966
## ['breakfast'] :1004
## (Other) :2175
## goodForGroups goodForKids isAmerican goodForDinner
## Mode :logical Mode :logical Mode :logical Mode :logical
## FALSE:2054 FALSE:506 FALSE:21456 FALSE:19670
## TRUE :17078 TRUE :1283 TRUE :3357 TRUE :5143
## NA's :5681 NA's :23024 NA's :0 NA's :0
##
##

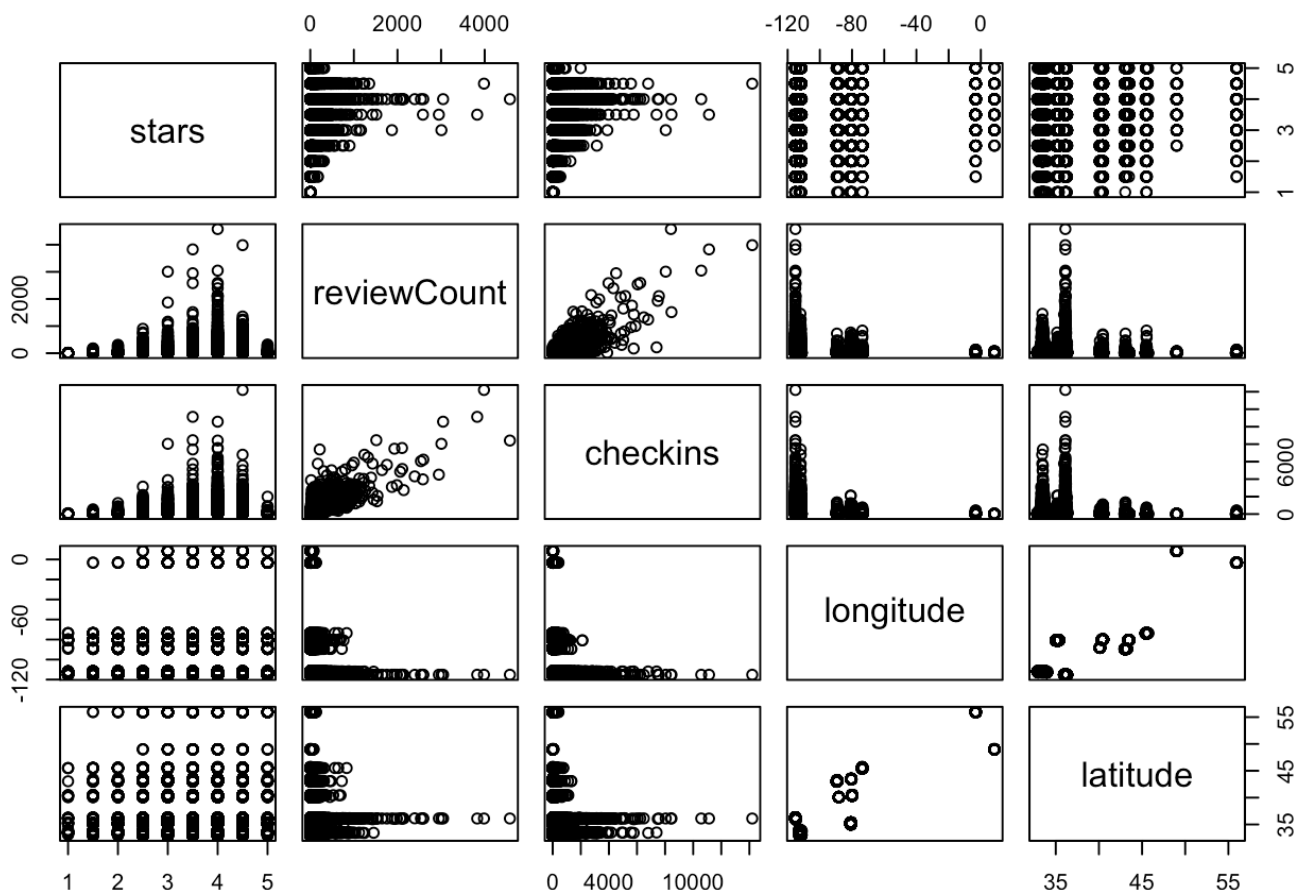
```

According to the different result showed up in the above summary stats: reviewCount: of course the mean review count in the 25 quantile is 5.247, which is much lower than the mean of whole dataset 49.03 stars: The mean of quantiled stars is 3.418 which is similar to the mean of whole dataset 3.544. attire: Although the amount of casual, dressy and formal are different from original dataset to 25 quantile dataset, the general proportion in side of the attire is matched up. priceRange: We could see that the mean price range in 25 quantile is 1.546 which is slightly less than original data's 1.631. However, the NA's in the 25 quantile data set is significant greater portion compare to the original dataset. delivery: The 25 quantile data has similar pattern with the original data in terms of the True, False and NAs distribution inside of the dataset. goodForKids: The NAs in the 25 quantile data is significant higher proportion than the original dataset.

6 2D plots and correlations

- a. (7 pts) Plot a scatterplot matrix (using pairs()) for the five attributes: stars, reviewCount, checkins, longitude, latitude. • Identify which pair of attributes exhibit the most association (as you can determine visually) and discuss if this is interesting or expected, given your domain knowledge.

```
pairs(~ stars + reviewCount + checkins + longitude + latitude, data = yelp)
```



ReviewCount is very related to checkins, which makes a lot of sense in terms of for those customer who reviewed a certain place, they definitely tend to check in already. Another interesting relationship is longitude and latitude, they are strongly associated, I think it makes sense here because we all know that longitude and latitude are related from our instinct.

- b. (7 pts) Calculate the pairwise correlation among the above five attributes using `cor()`. • Identify the pair of attributes with largest positive correlation and the pair with largest negative correlation. Report the correlations and discuss how it matches with your visual assessment in part (a).

```
cor(yelp[,c('stars', 'reviewCount', 'checkins', 'longitude', 'latitude')])
```

```
##           stars reviewCount  checkins  longitude  latitude
## stars      1.00000000  0.10705060  0.09440071  0.1174446  0.12116308
## reviewCount 0.10705060  1.00000000  0.82749365 -0.1294142 -0.09850936
## checkins    0.09440071  0.82749365  1.00000000 -0.1789531 -0.15260462
## longitude   0.11744458 -0.12941420 -0.17895315  1.0000000  0.88110176
## latitude    0.12116308 -0.09850936 -0.15260462  0.8811018  1.00000000
```

Largest pos correlation except the diagonal is latitude and longitude. It definately match up with the graph since they are have a strong correlation. Largest neg correlation is between longitude and checkins, I think it is also true in the graph due to the meaningless cluster of points.

- c. (7 pts) Plot a boxplot (using `boxplot()`) for each of the following four attributes (checkins, reviewCount, longitude, latitude) vs. the goodForGroups attribute. Omit outliers using the outline argument. Make sure to label both axes of the plot with the appropriate attribute names. • Identify the attribute that exhibits the most association with goodForGroups (as you can determine visually) and discuss whether this is interesting or expected, given your domain knowledge. It seems like both checkins and reviewCount are kinda associate with goodForGroups from the boxplot. I'll choose to go with Checkins. And I found that both of the attributes are some what interesting. I can't find any direct relationship of how checkins and reviewCount related to weither a place is good for group or not. I mean they are definately a good decision of weither a place is good or not, but that is not related to group feature from my domain knowledge. • For the attribute identified above, calculate its interquartile range for each value of goodForGroups (i.e., a separate IQR for the TRUE instances and the FALSE instances). You can do this with `subset()` and `quantile()`. Calculate the overlap between the two IQRs. Discuss whether these results support the conclusion you made based on visual inspection.

```
checkinGroup = subset(yelp, goodForGroups==TRUE, select = c(checkins))
checkinNotGroup = subset(yelp, goodForGroups==FALSE, select = c(checkins))
quantile(checkinGroup$checkins)
```

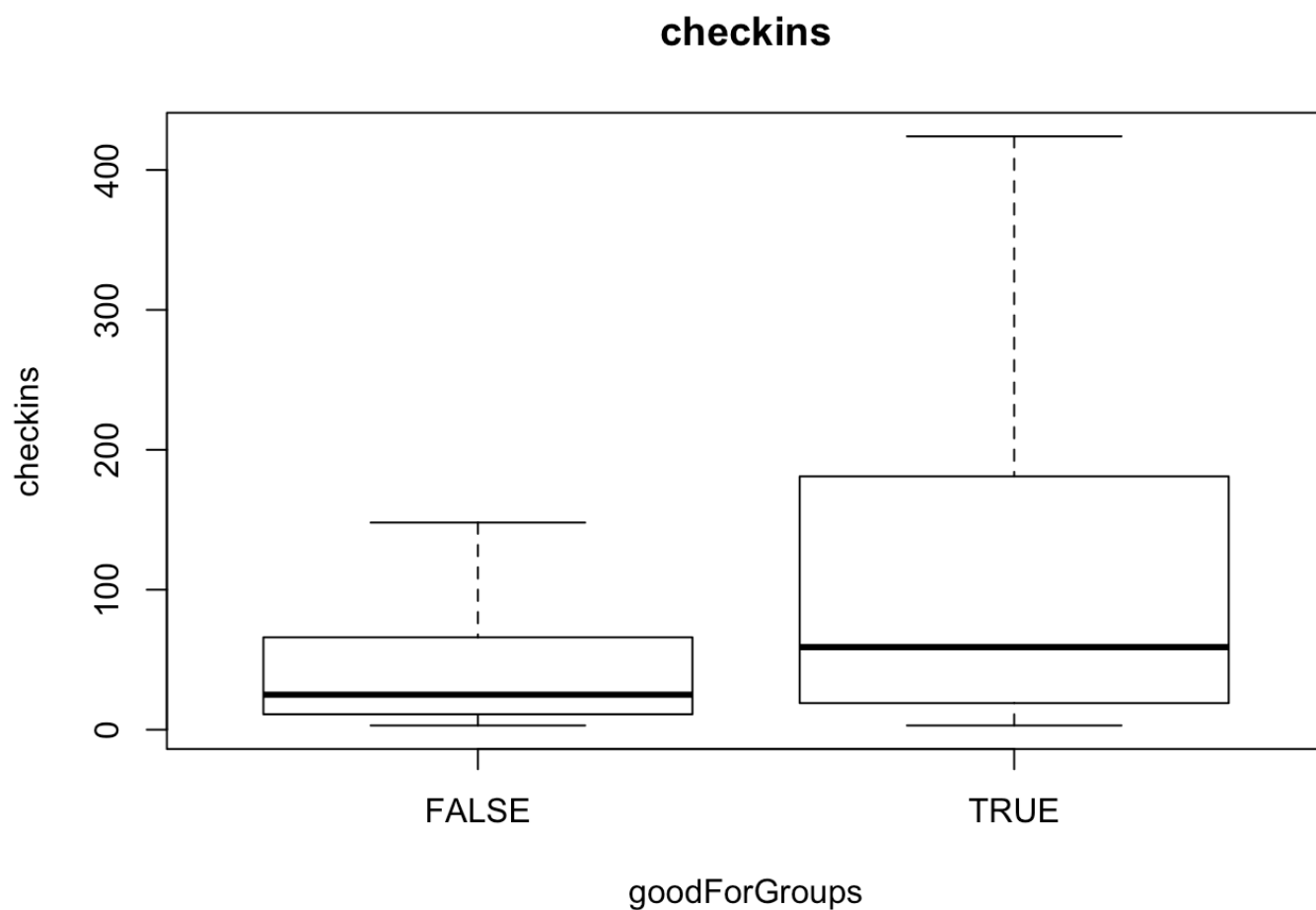
```
##      0%    25%    50%    75%   100%
##      3     19     59    181  14203
```

```
quantile(checkinNotGroup$checkins)
```

```
##      0%    25%    50%    75%   100%
##      3     11     25     66  6485
```

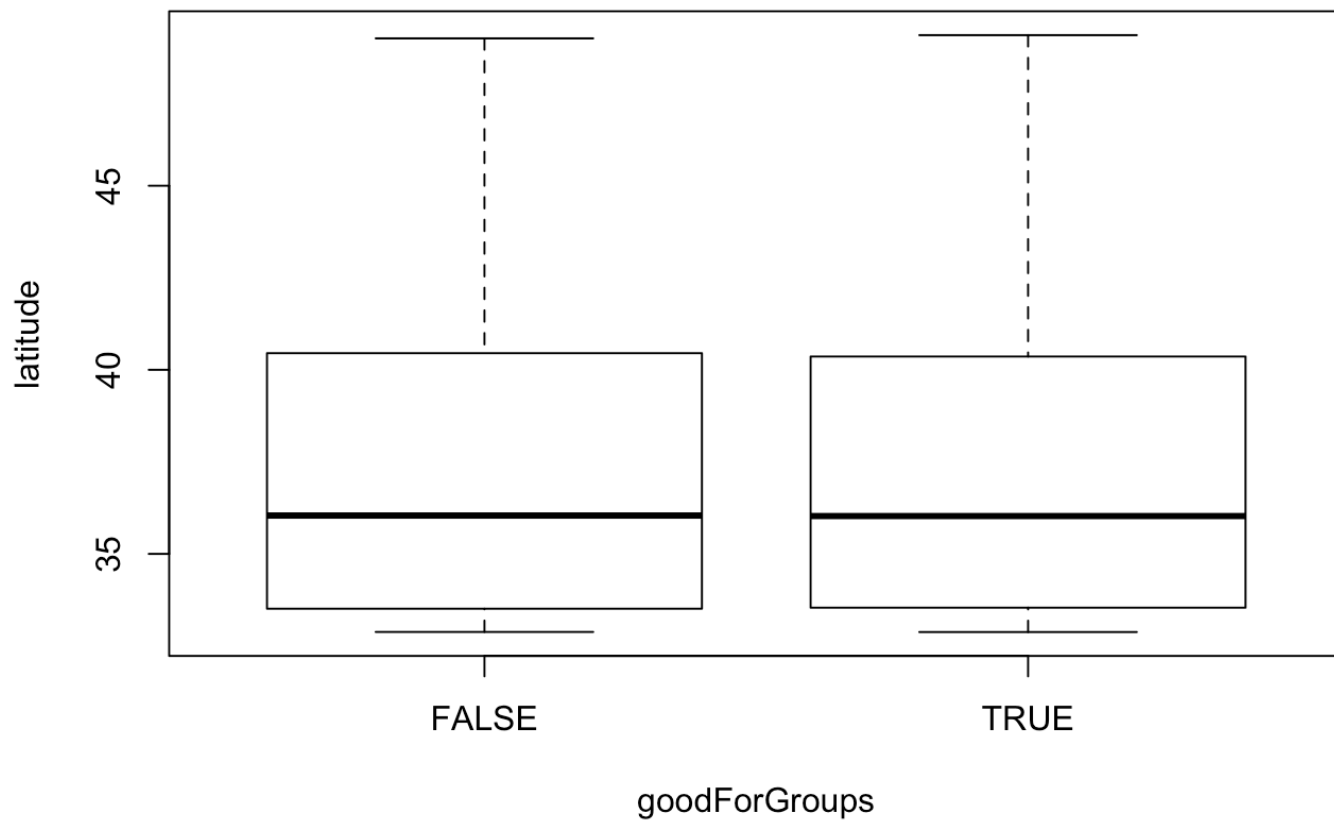
The overlap between those two IQR is $66 - 19 = 47$, which is very minimal compare to the IQR that distinguish the TRUE goodforgroup from false. So, it support the conclusion that I made based on the visual observation.

```
boxplot(checkins ~ goodForGroups, data = yelp, outline = FALSE, main="checkins", x
lab= "goodForGroups", ylab="checkins")
```



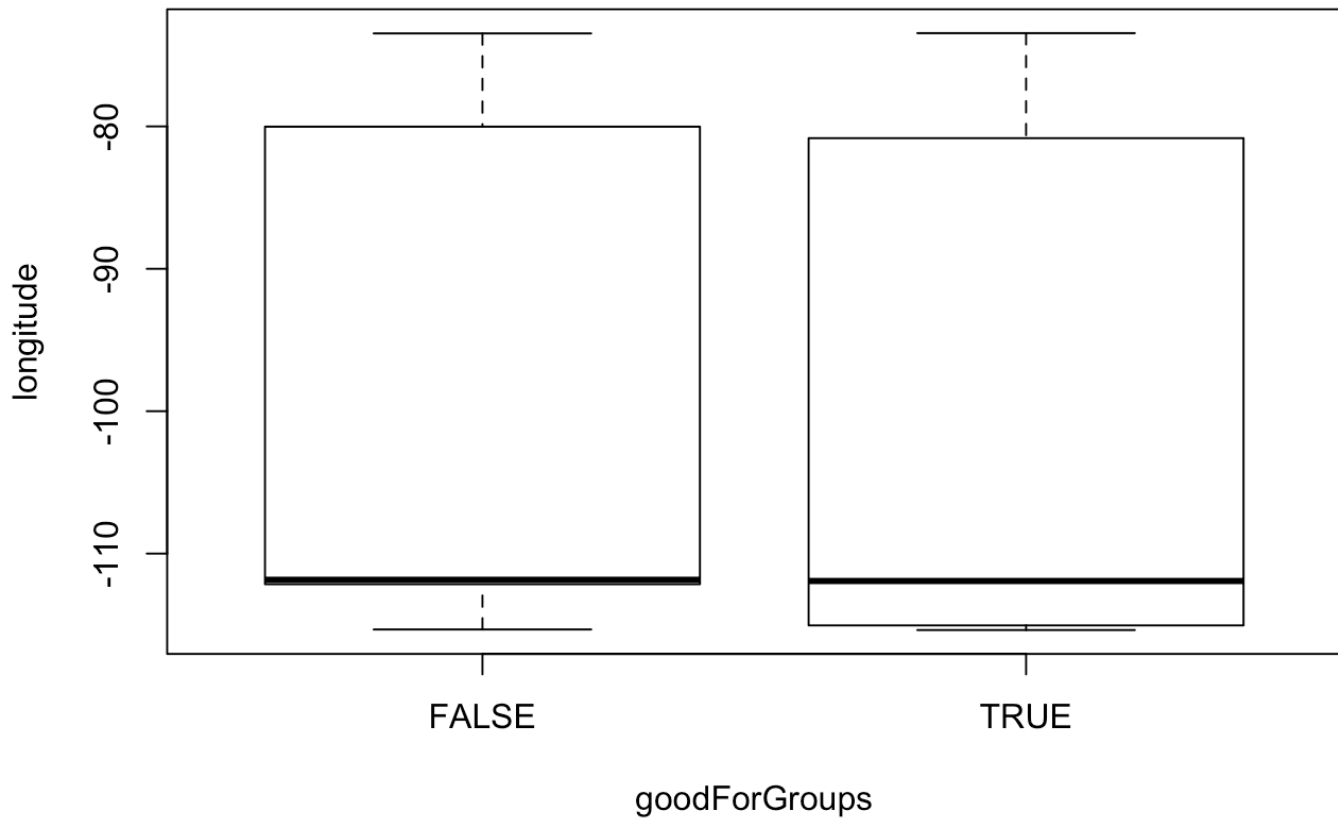
```
boxplot(latitude ~ goodForGroups, data = yelp, outline = FALSE, main="latitude", x
lab= "goodForGroups", ylab="latitude")
```

latitude

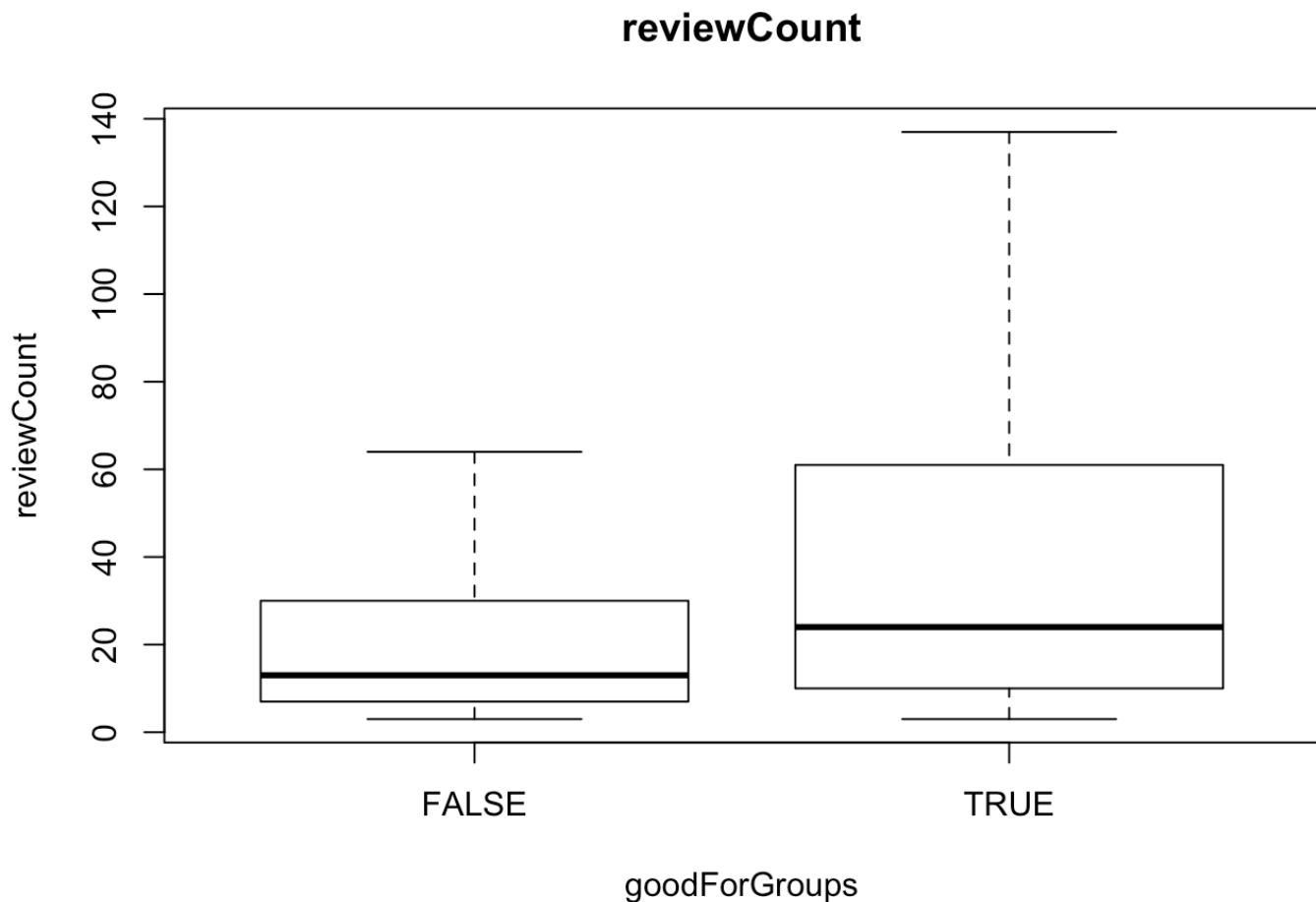


```
boxplot(longitude ~ goodForGroups, data = yelp, outline = FALSE, main="longitude",  
xlab= "goodForGroups", ylab="longitude")
```

longitude



```
boxplot(reviewCount ~ goodForGroups, data = yelp, outline = FALSE, main="reviewCount", xlab= "goodForGroups", ylab="reviewCount")
```

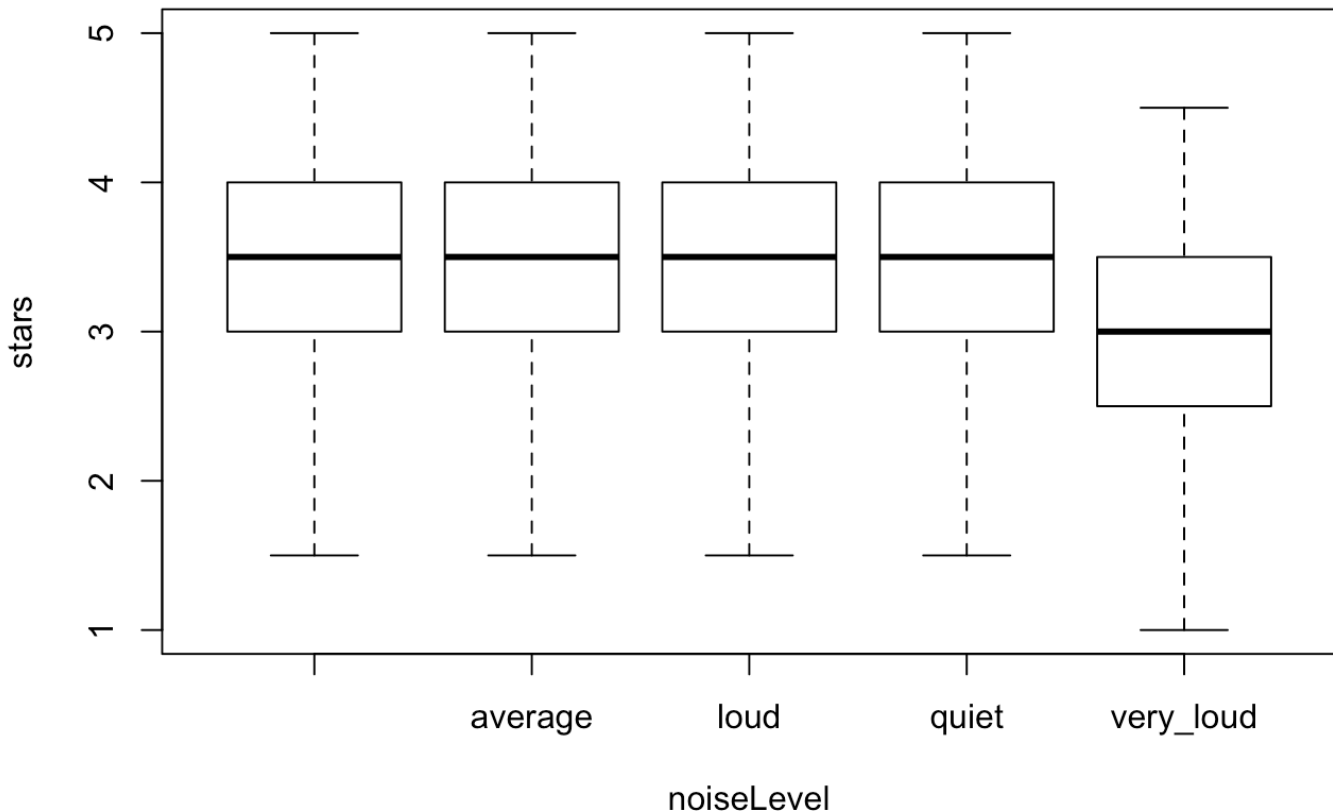
7 Identifying potential hypotheses (20 pts)

During your exploration above, investigate other aspects of the data. Explore relationships between variables by assessing plots, computing correlation, or other numerical analysis. Identify TWO possible relationships in the data (other than the ones specified in earlier questions) and formulate hypotheses based on the observed data. For each of the two identified relationships:

Relationship A:

- a. Include a plot illustrating the observed relationship (between at least two variables).

```
boxplot(stars ~ noiseLevel, data = yelp, outline = FALSE, xlab = "noiseLevel", ylab = "stars")
```

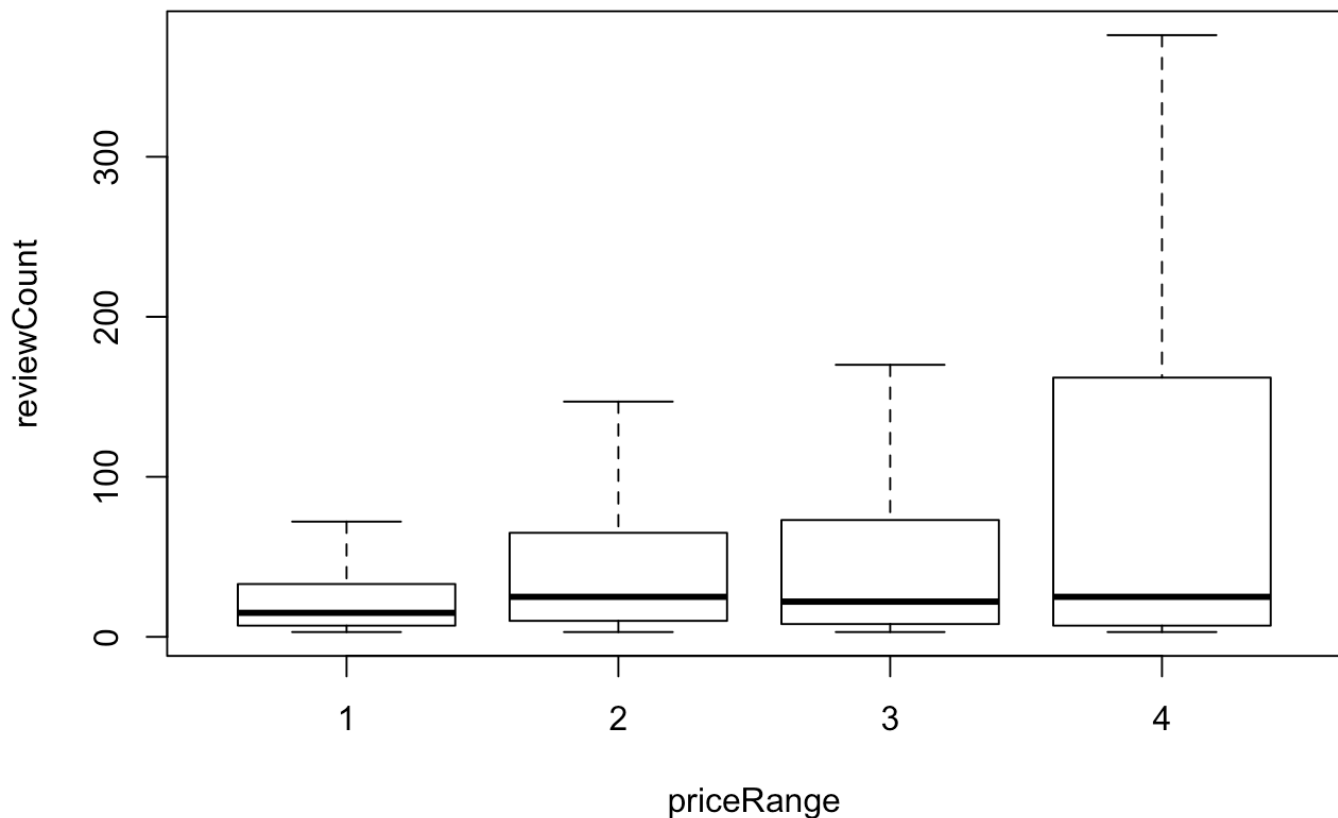


- State whether the variables are discrete or continuous and what type of plot is relevant for comparing these two types of variables. The star is continuous numericle variable, and the noiselevel is discrete catagorical variable. The boxplot that I used before is good for this data.
- Formulateahypothesisabouttheobservedrelationshipasafunctionoftworandom variables (e.g., X is associated with Y). noiseLevel is assosiated with stars.
- Write the hypothesis as a claim in English, relating it to the attributes in the data. The noiseLevel, particularly the very loud noiseLevel will have negative effect on the users review reflecting on the stars of the restaurount.
- Identify the type of hypothesis. Directional-relational

Relationship B:

- Include a plot illustrating the observed relationship (between at least two vari- ables).

```
boxplot(reviewCount ~ priceRange, data = yelp, outline = FALSE, xlab = "priceRange", ylab = "reviewCount")
```



- State whether the variables are discrete or continuous and what type of plot is relevant for comparing these two types of variables. reviewCount is a continuous numerical variable, priceRange seems to be a numerical var, but it is actually a discrete catagorical var.
- Formulate a hypothesis about the observed relationship as a function of two random variables (e.g., X is associated with Y). priceRange is associated with reviewCount
- Write the hypothesis as a claim in English, relating it to the attributes in the data. Higher priceRange of the restaurant will tends to have more reviewCount.
- Identify the type of hypothesis. Directional-relational