

Plate is 14 inches diameter

Archimedes Spiral

$$\text{Dia} := 14 \cdot 2.54 \quad \text{Dia} = 35.56$$

$$\Delta := 1 \quad \text{gap between turns}$$

$$R_o := \frac{\text{Dia}}{2} - 1.5 \quad \text{Outer radius, cm} \quad R_o = 16.28$$

$$R_i := 1 \quad \text{Inner Radius, cm}$$

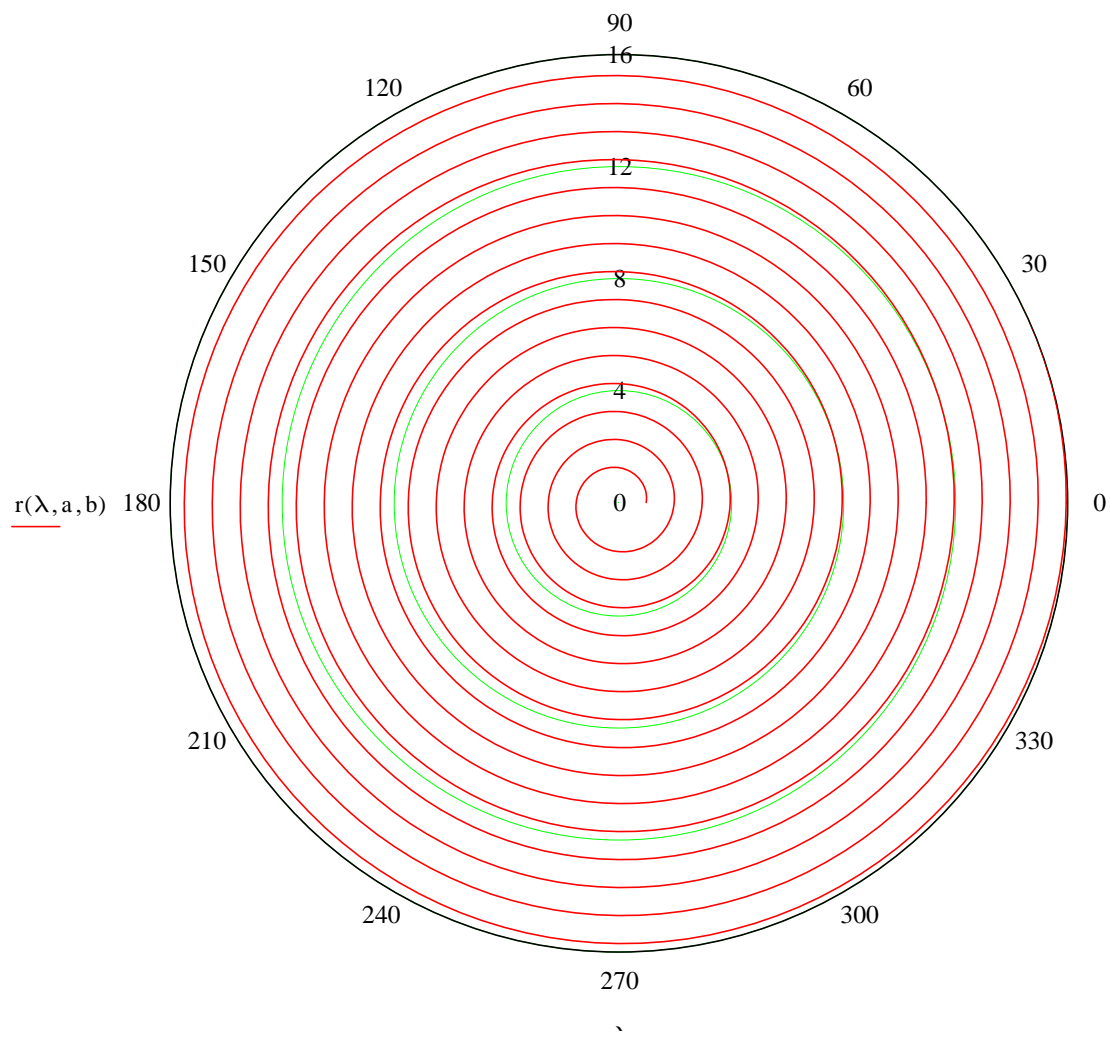
$$N := \frac{R_o - R_i}{\Delta} \quad \text{number of turns} \quad N = 15.28$$

$$r(\theta, a, b) := a + b \cdot \theta \quad \text{Archimedes Spiral}$$

$$a := R_i \quad \text{Start radius}$$

$$b := \frac{\Delta}{2 \cdot \pi} \quad b = 0.159$$

$$\lambda := 0, \frac{\pi}{60} \dots N \cdot 2 \cdot \pi$$



λ

Solve for length

$$L(N, a, b) := \int_0^{N \cdot 2 \cdot \pi} \sqrt{(a + b \cdot \theta)^2 + \left[\frac{d}{d\theta} (a + b \cdot \theta) \right]^2} d\theta$$

$$L(N, a, b) = 829.723 \quad \text{cm}$$

Solve for the diameter and hence the wires gage

$$\text{Watts} := 250 \quad \text{Volts} := 23$$

$$R_s := \frac{\text{Volts}^2}{\text{Watts}} \quad R_s = 2.116$$

$$N_i := \frac{1 \cdot 10^{-6}}{.917} \quad \text{Ohm} - \text{meters}$$

$$A(N, a, b, R_s) := \frac{N_i \cdot \frac{L(N, a, b)}{100}}{R_s}$$

Heater requirements

Required Resistance

Resistivity of Nichrome, Adjusted to man data for 80/20 nichrome wire

Area as a function of N,a,b and resistance

$$D(N,a,b,R_s) := \sqrt{\frac{A(N,a,b,R_s) \cdot 4}{\pi}} \cdot 39.37 \quad \text{Inches}$$

Diameter as a function of length and resistance

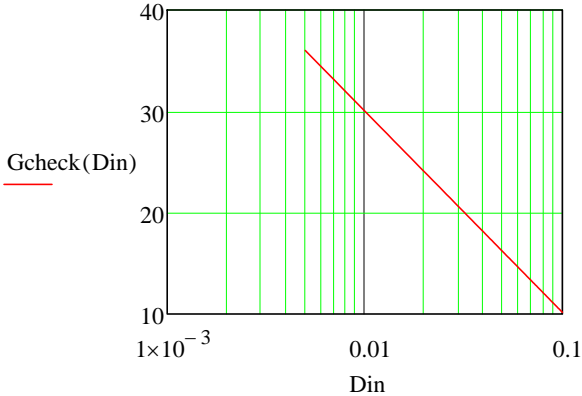
$$D(N,a,b,R_s) = 0.092$$

$$G(N,a,b,R_s) := \frac{\ln(D(N,a,b,R_s)) + 1.12436}{-.11594} \qquad G(N,a,b,R_s) = 10.894$$

wire gage
eguation, in inches

12 ga wire is a bit big

$$Gcheck(Din) := \frac{\ln(Din) + 1.12436}{-.11594} \qquad Din := .005, .006 \dots .1$$



Solve graphically for a smaller gage

$$\text{ga}(\Delta, \text{Ro}, \text{Ri}, \text{Rs}) :=$$

$$\begin{array}{l} N \leftarrow \frac{(\text{Ro} - \text{Ri})}{\Delta} \\ a \leftarrow \text{Ri} \\ b \leftarrow \frac{\Delta}{2 \cdot \pi} \\ Q \leftarrow G(N, a, b, \text{Rs}) \\ Q \end{array}$$

$$r(\theta, a, b) := a + \theta \cdot b$$

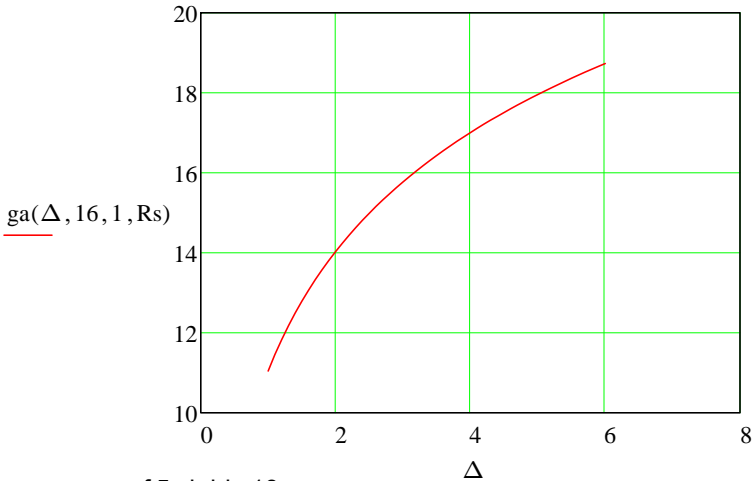
$$\lambda := 0, \frac{\pi}{100} .. 6 \cdot 2 \cdot \pi$$

more than enough radians

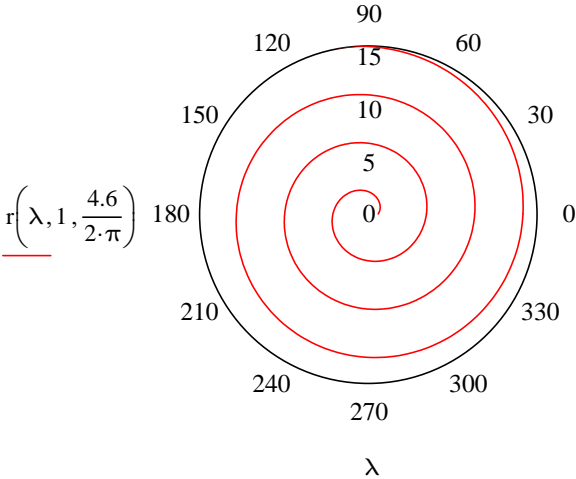
$$\Delta := 1, 1.1 .. 6$$

$$L\left(\frac{\text{Ro} - \text{Ri}}{5}, \text{Ri}, \frac{5}{2 \cdot \pi}\right) = 166.983$$

cm of 18 ga



a gap of 5 yields 18 ga



a 5 cm gap may be too big for even heating of glass, especially

Consider nested spirals

$$ga(1, 16, 1, Rs) = 11.045$$

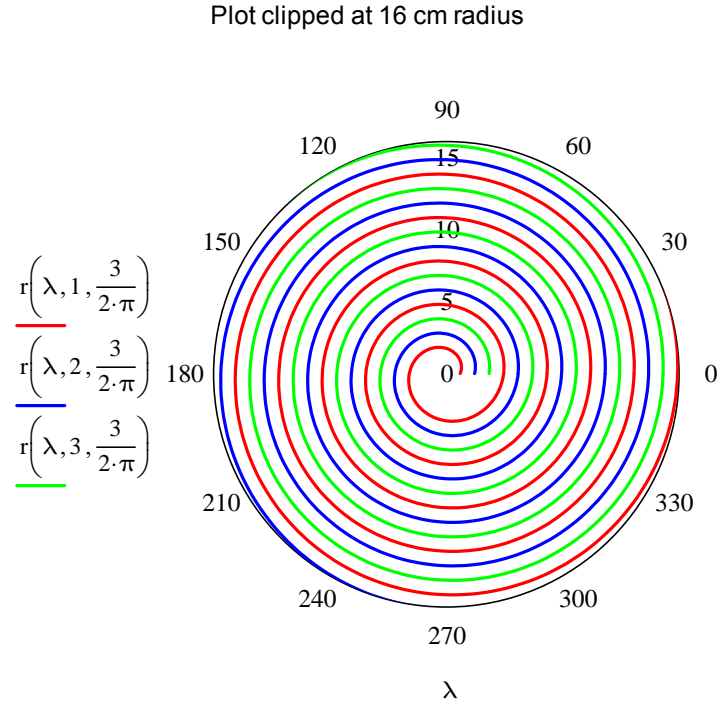
$$ga(3, 16, 1, Rs \cdot 3) = 20.511$$

$$ga(3, 16, 2, Rs \cdot 3) = 20.564$$

three spirals of about 21 gage

$$ga(3, 16, 3, Rs \cdot 3) = 20.652$$

Three spirals



$$L\left(\frac{16-3}{3}, 1, \frac{3}{2 \cdot \pi}\right) = 204.827$$

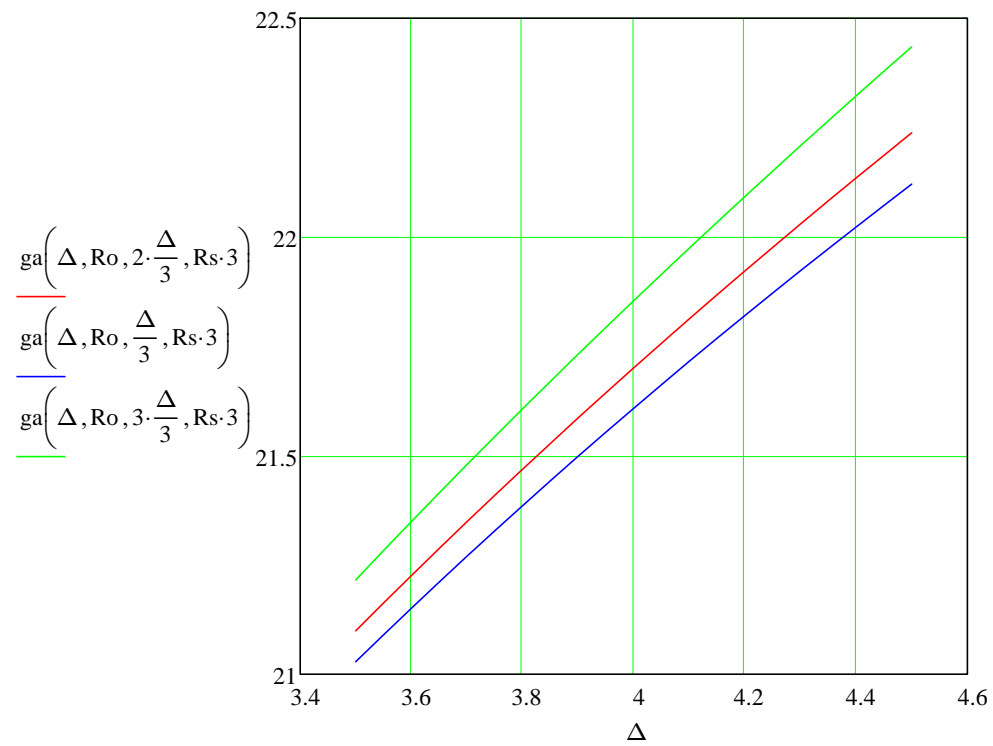
$$L\left(\frac{16-2}{3}, 2, \frac{3}{2 \cdot \pi}\right) = 264.389$$

$$L\left(\frac{16-1}{3}, 3, \frac{3}{2 \cdot \pi}\right) = 330.294$$

This solution will use three spirals of different length, in parallel.

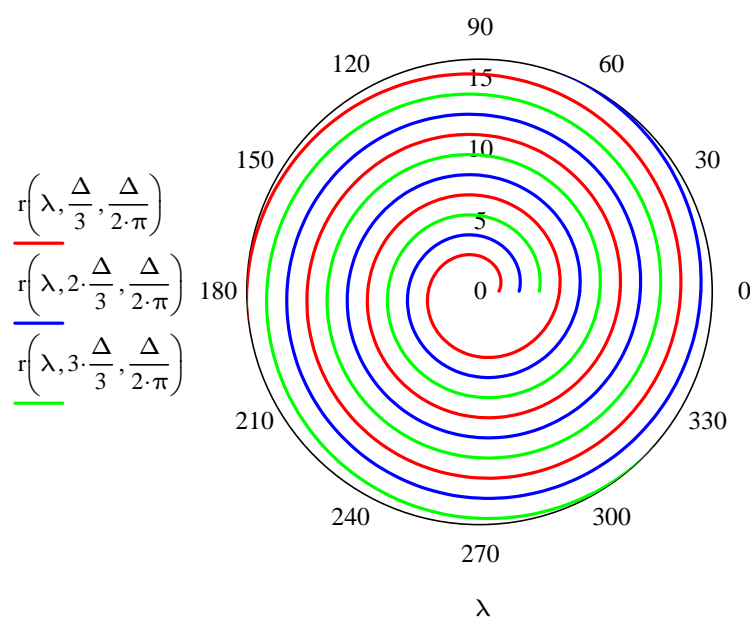
$$\Delta := 3.5, 3.55 \dots 4.5$$

A gap of 4.3 yields 22 ga for the middle sprial



$$\Delta := 4.25$$

Plot clipped at Ro cm radius



$$L\left(\frac{Ro - 3 \cdot \frac{\Delta}{3}}{\Delta}, \Delta, \frac{\Delta}{2 \cdot \pi}\right) = 183.017$$

$$L\left(\frac{Ro - 2 \cdot \frac{\Delta}{3}}{\Delta}, 2 \cdot \frac{\Delta}{3}, \frac{\Delta}{2 \cdot \pi}\right) = 190.571$$

$$L\left(\frac{Ro - \frac{\Delta}{3}}{\Delta}, \frac{\Delta}{3}, \frac{\Delta}{2 \cdot \pi}\right) = 195.249$$

This solution will use three spirals of different length, in parallel, of 22 ga.

$$\frac{\text{Ni} \cdot \frac{\text{L} \left(\frac{\text{Ro} - 3 \cdot \frac{\Delta}{3}}{\Delta}, \Delta, \frac{\Delta}{2 \cdot \pi} \right)}{100}}{\frac{.326}{10^6}} = 6.122$$

$$\frac{190 \cdot 3}{2.54 \cdot 12} = 18.701 \quad \text{feet}$$

$$\frac{1}{\frac{\text{Ni} \cdot \frac{\text{L} \left(\frac{\text{Ro} - \Delta}{\Delta}, \Delta, \frac{\Delta}{2 \cdot \pi} \right)}{100}}{\frac{.326}{10^6}} + \frac{1}{\frac{\text{Ni} \cdot \frac{\text{L} \left(\frac{\text{Ro} - 2 \cdot \frac{\Delta}{3}}{\Delta}, \frac{\Delta \cdot 2}{3}, \frac{\Delta}{2 \cdot \pi} \right)}{100}}{\frac{.326}{10^6}} + \frac{1}{\frac{\text{Ni} \cdot \frac{\text{L} \left(\frac{\text{Ro} - \frac{\Delta}{3}}{\Delta}, \frac{\Delta}{3}, \frac{\Delta}{2 \cdot \pi} \right)}{100}}{\frac{.326}{10^6}}} = 2.113$$

Check on resistivity

$$Ni = 1.091 \times 10^{-6}$$

$$A(N, a, b, Rs) := \frac{Ni \cdot \frac{L(N, a, b)}{100}}{Rs}$$

Expresion to find the required area(m^2) from length(cm) and resistance

$$Acheck(L, Rs) := \frac{Ni \cdot L}{100 \cdot Rs}$$

$$\frac{Acheck(100, 138.8) \cdot 10^6}{.007845} = 1.001$$

mm²

Close to man data

$$\frac{Acheck(100, 6.835) \cdot 10^6}{.1590} = 1.003$$

mm²

Close to man data

$$Acheck(100, .1542) \cdot 10^6 = 7.072$$

$$\frac{Acheck(100, .1542) \cdot 10^6}{7.089} = 0.998$$

$$Acheck(265, 2.1) \cdot 10^6 = 1.376$$

Serpentine path

Assume a serpentine path. The long runs are chords of the circle, the first run is a distance away from the perimeter termed the versine or sagitta (S). Each of N runs after that are evenly gapped by G. The last run is again S from the perimeter. The chords end a distance away from the perimeter defined by the chord and an intersection of a smaller circle of radius R. The runs are then full chords of the smaller circle R. The connectors will be treated as straight lines connecting the runs.

Equation for the length of a chord

Solve for the chord

$$r = \frac{c^2}{8s} + \frac{s}{2} \quad \text{the radius of a circle that just encloses a chord of length C with sagitta S}$$

$$c(r, s) := 2 \cdot \sqrt{s \cdot \sqrt{2 \cdot r - s}} \quad \text{the length of a chord of a circle r with sagitta s}$$

$$N(D, \Delta, s) := \frac{D - 2 \cdot s}{\Delta} + 1 \quad \text{Number of runs in a circle of diameter D, sagitta s and gap } \Delta$$

From the Openscad code that makes the jig

$$\text{arcangle}(\text{radc}, g, W) := \left| \begin{array}{l} Q \leftarrow W - \left[\frac{g}{2 \cdot \pi \cdot \text{radc}} + \frac{g}{2 \cdot \pi \cdot (\text{radc} + g)} \right] \cdot 360 \\ Q \leftarrow 45 \text{ if } Q < 45 \\ Q \end{array} \right.$$

$$\text{Ls}(g, \text{rm}, W) := \left| \begin{array}{l} \text{arclen} \leftarrow 0 \\ N \leftarrow \text{floor}\left(\frac{\text{rm}}{g}\right) \\ \text{for } k \in 0..N-1 \\ \quad \left| \begin{array}{l} \text{radm} \leftarrow \text{rm} - g \cdot k \\ \text{radc} \leftarrow \text{radm} - \frac{g}{2} \\ \text{arcang} \leftarrow \text{arcangle}\left(\text{radc}, g, \frac{360}{W}\right) \\ \text{conang} \leftarrow \frac{g \cdot 360}{2 \cdot \pi \cdot \text{radc}} \\ \text{arclen} \leftarrow \text{arclen} + \frac{\text{arcang}}{360} \cdot \text{radm} \cdot 2 \cdot \pi \\ Q_k \leftarrow \frac{\text{arcang}}{360} \cdot \text{radm} \cdot 2 \cdot \pi \end{array} \right. \\ \text{conlen} \leftarrow N \cdot \pi \cdot \frac{g}{2} \\ \text{arclen} + \text{conlen} \end{array} \right.$$

rm is the radius if the heater

g is the gap between the wires

W is the number of wedges

$$\text{Gas}(\text{rm}, \text{g}, \text{W}, \text{Rs}) := \left| \begin{array}{l} \text{Lsercm} \leftarrow \frac{\text{Ls}(\text{g}, \text{rm}, \text{W})}{10} \\ \text{Aser} \leftarrow \text{Acheck}(\text{Lsercm}, \text{Rs} \cdot \text{W}) \\ \text{Dser} \leftarrow \sqrt{\frac{\text{Aser} \cdot 4}{\pi}} \cdot 39.37 \\ \text{Gser} \leftarrow \text{Gcheck}(\text{Dser}) \\ \text{Gser} \end{array} \right.$$

$$\text{Ls}(20, 170, 4) = 1.203 \times 10^3$$

$$\sqrt{\frac{\text{Acheck}(120.3, 8.4) \cdot 4}{\pi}} \cdot 39.37 \cdot 25.4 = 0.446$$

$$\text{Ls}(10, 170, 4) = 2.345 \times 10^3$$

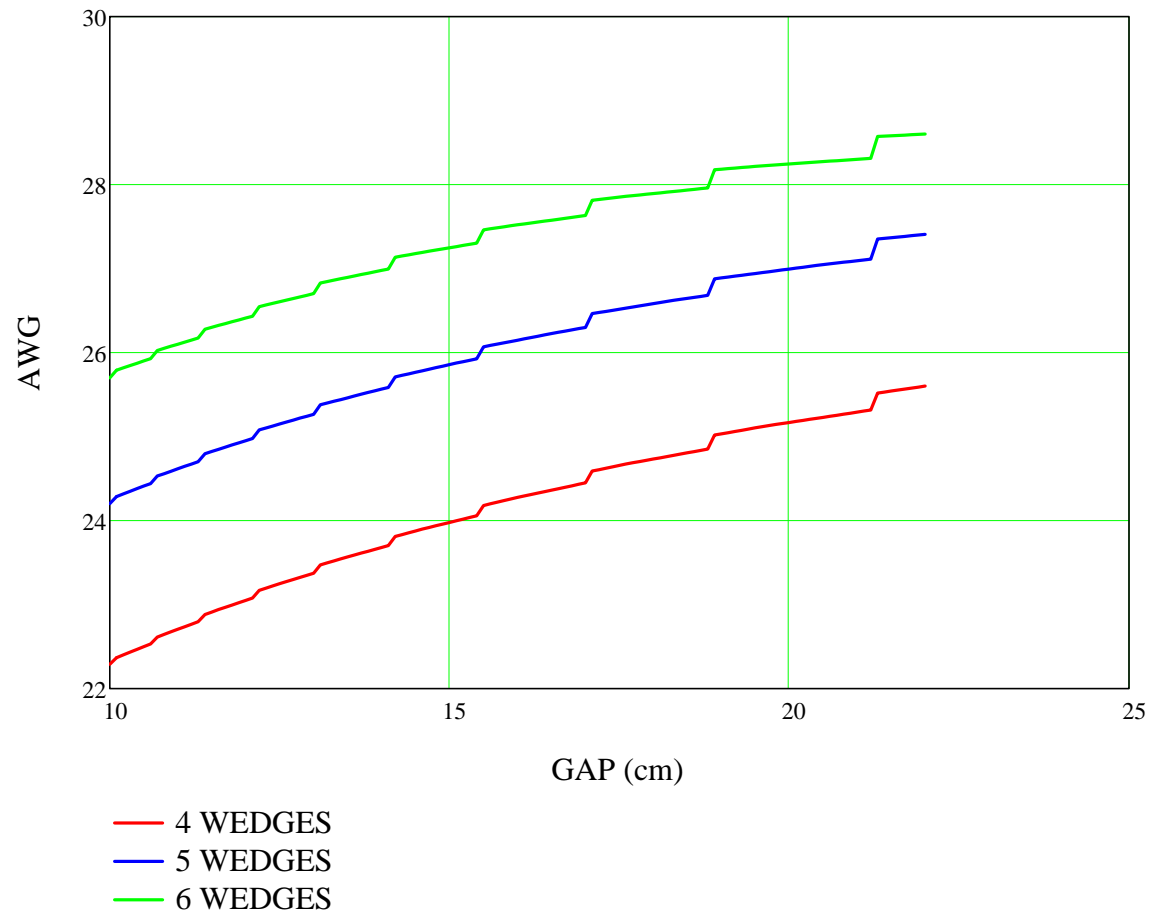
$$\text{Gas}(170, 10.2, 4, 2.1) = 22.402$$

$$\text{Gtry} := 10, 10.1 \dots 22$$

$$\text{Rad} := 170$$

$$\text{Rs} := 2.1$$

WIRE GAGE VS GAP, FOR VARIOUS WEDGE NUMBERS



$$\text{arcangle}(\text{radc}, g, W) := \left| \begin{array}{l} Q \leftarrow W - \left[\frac{g}{2 \cdot \pi \cdot \text{radc}} + \frac{g}{2 \cdot \pi \cdot (\text{radc} + g)} \right] \cdot 360 \\ Q \leftarrow 45 \quad \text{if } Q < 45 \\ Q \end{array} \right.$$

$$\text{Ls}(g, \text{rm}, W) := \left| \begin{array}{l} \text{arclen} \leftarrow 0 \\ N \leftarrow \text{floor} \left(\frac{\text{rm}}{g} \right) \\ \text{for } k \in 0..N-1 \\ \quad \left| \begin{array}{l} \text{radm} \leftarrow \text{rm} - g \cdot k \\ \text{radc} \leftarrow \text{radm} - \frac{g}{2} \\ \text{arcang} \leftarrow \text{arcangle} \left(\text{radc}, g, \frac{360}{W} \right) \\ \text{conang} \leftarrow \frac{g \cdot 360}{2 \cdot \pi \cdot \text{radc}} \\ \text{arclen} \leftarrow \text{arclen} + \frac{\text{arcang}}{360} \cdot \text{radm} \cdot 2 \cdot \pi \\ Q_k \leftarrow \frac{\text{arcang}}{360} \cdot \text{radm} \cdot 2 \cdot \pi \end{array} \right. \\ \text{conlen} \leftarrow N \cdot \pi \cdot \frac{g}{2} \\ \text{arclen} + \text{conlen} \end{array} \right.$$

patient + control