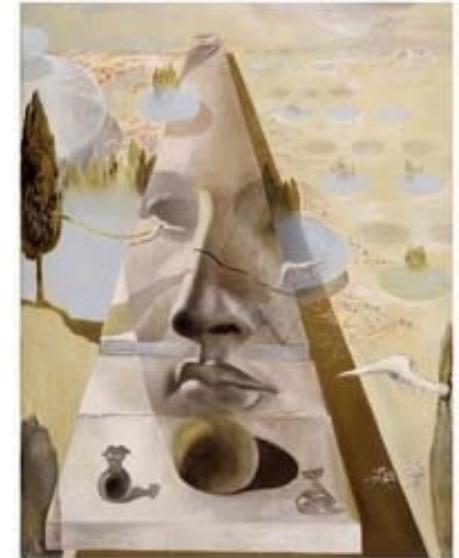


Lecture 13

Segmentation and Scene understanding



- Introduction
- Mean-shift
- Graph-based segmentation
- Top-down segmentation

Segmentation

- Compact representation for image data in terms of a set of **components**



Segmentation

- Compact representation for image data in terms of a set of **components**



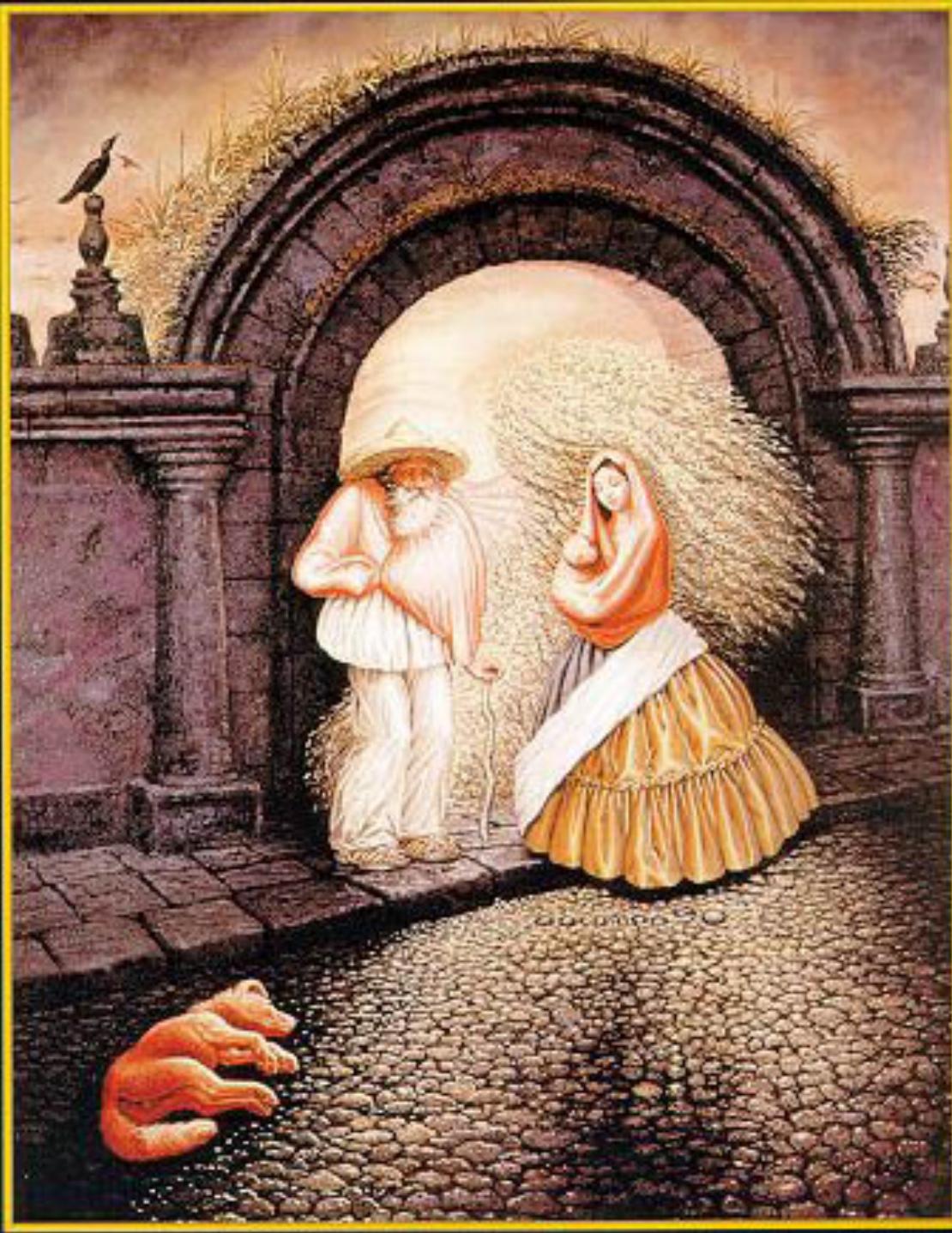
Segmentation

- Compact representation for image data in terms of a set of **components**
- Components share common properties



Segmentation

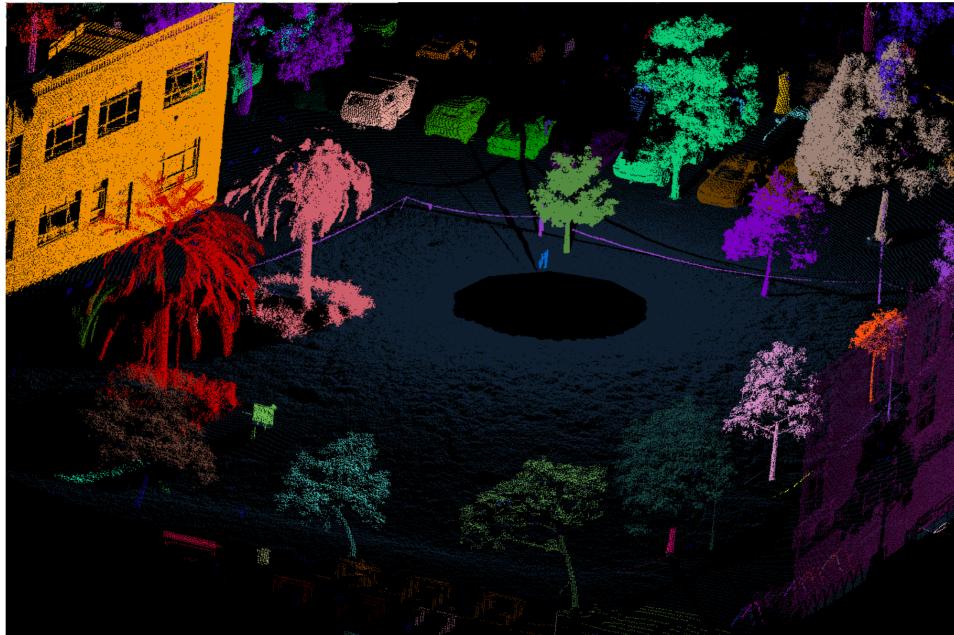
- Compact representation for image data in terms of a set of **components**
- Components share common properties
- Properties can be defined at different level of abstractions



Segmentation

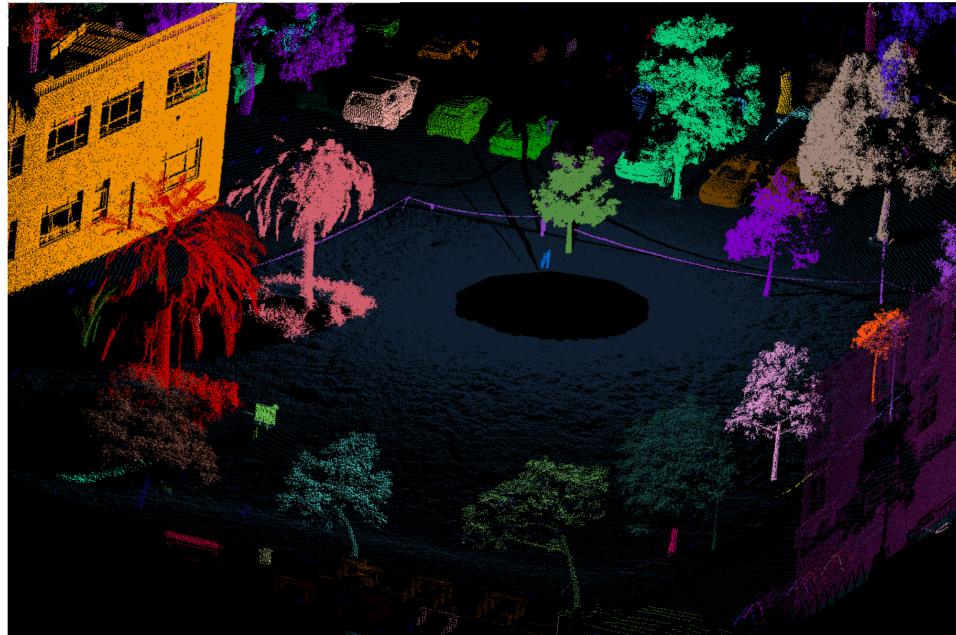


Segmentation

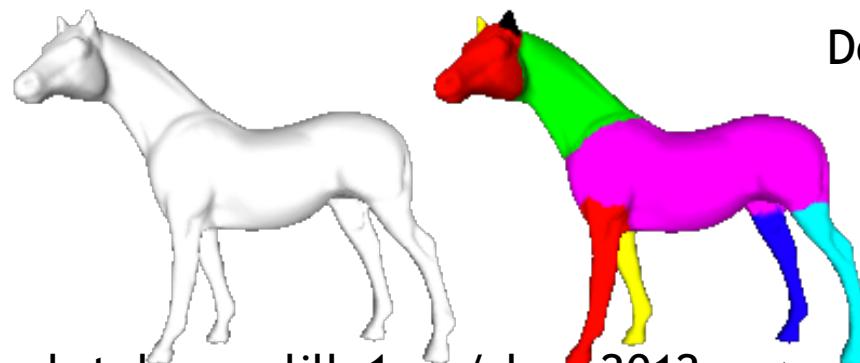


Douillard, et al. ICRA 2011

Segmentation



Douillard, et al. ICRA 2011



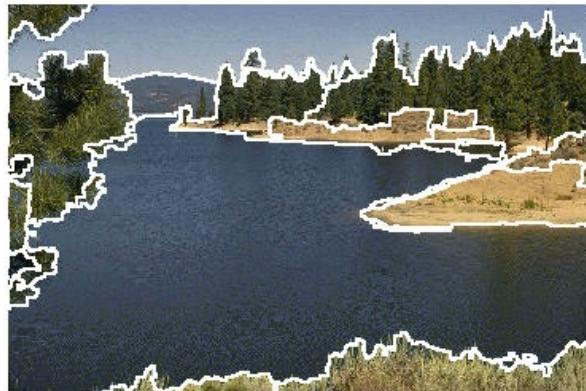
General ideas

- Bottom up segmentation
 - tokens belong together because they are locally coherent



General ideas

- Bottom up segmentation
 - tokens belong together because they are locally coherent



- Top down segmentation
 - tokens belong together because they lie on the same visual entity (object, scene...)



Why Segmentation?

- Segments are building blocks of other vision tasks.
- Complexity
- Boundary



Basic ideas of grouping in human vision

- Gestalt properties
- Figure-ground discrimination
- Emergence

Gestalt psychology or gestaltism

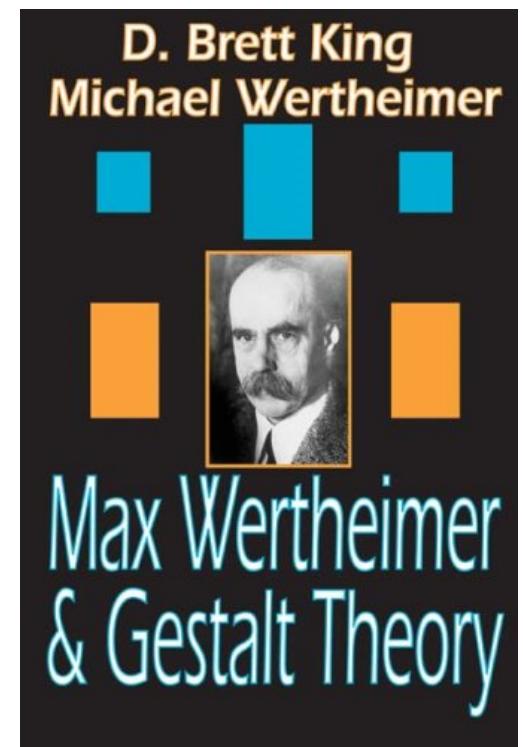
German: *Gestalt* - "form" or "whole"

Berlin School , early 20th century, Carl Stumpf

Kurt Koffka, Max Wertheimer, and Wolfgang Köhler

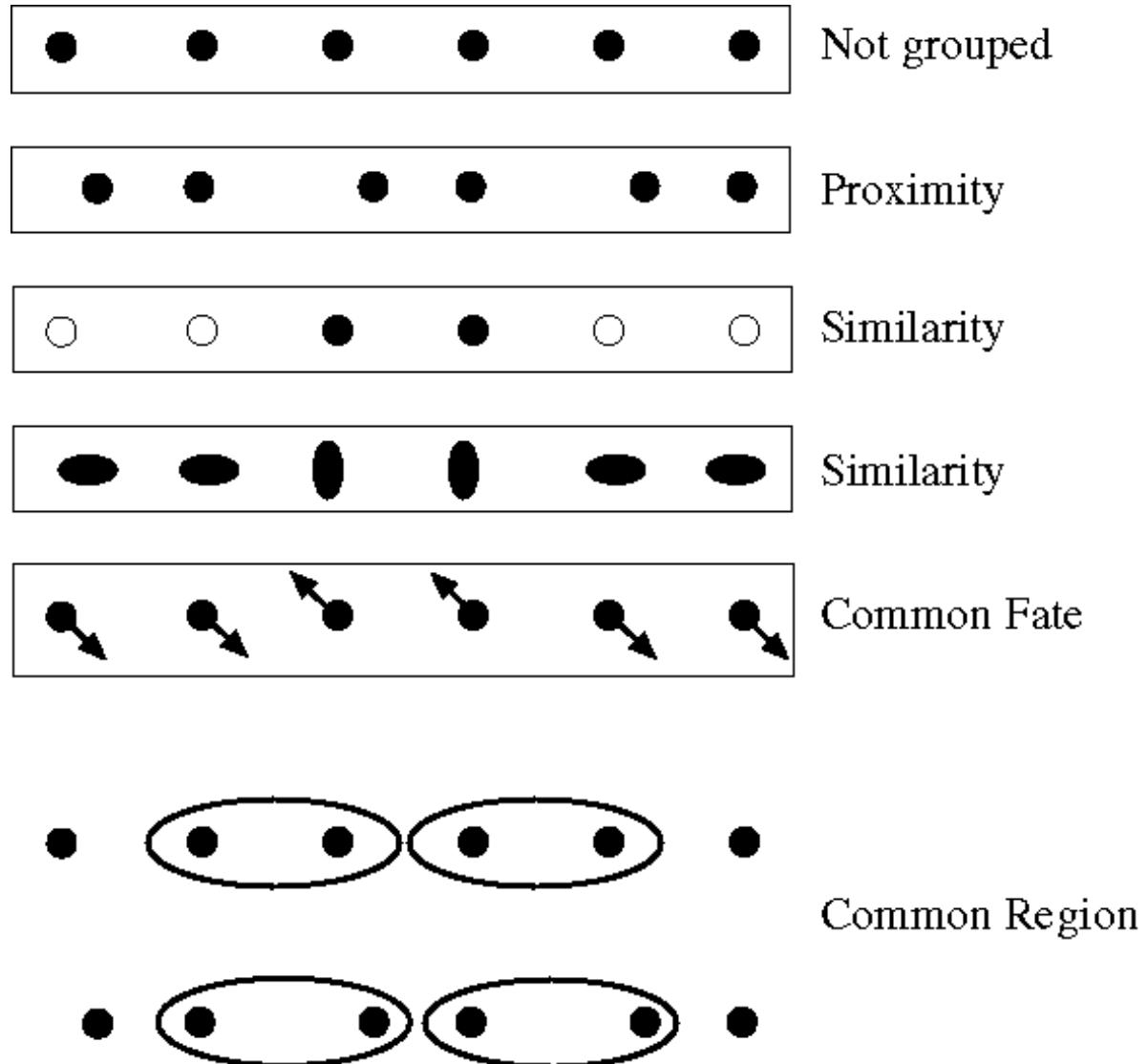
Advocate brain is holistic

Whole is greater than the sum of its parts.



Gestalt properties

-A series of factors affect whether elements should be grouped together



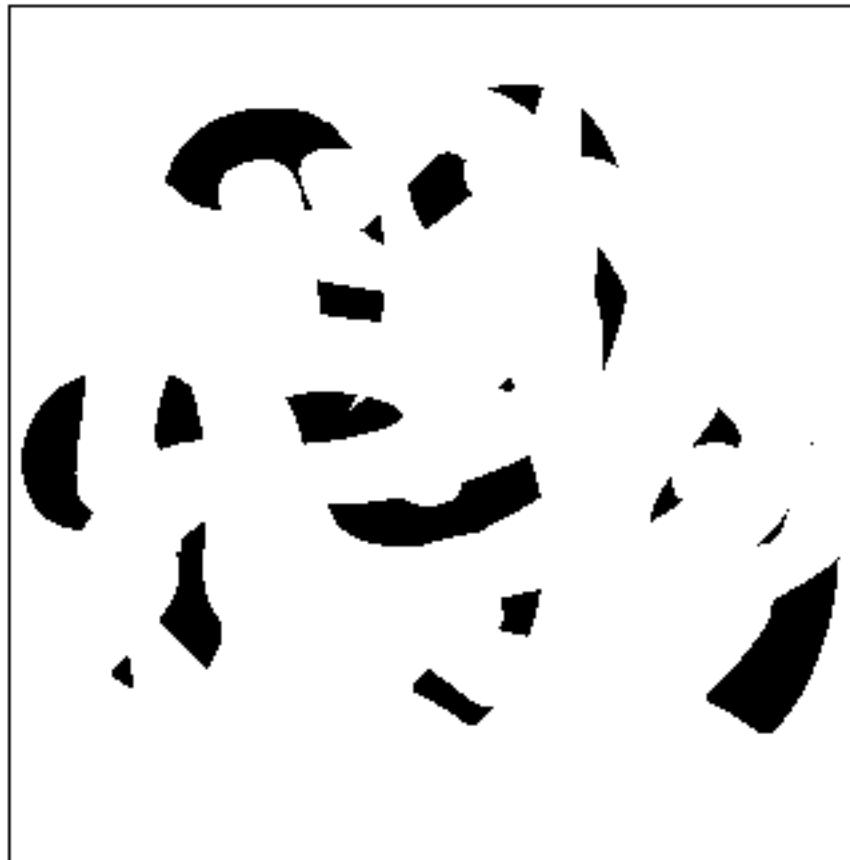
Gestalt properties

Grouping
by occlusions



Gestalt properties

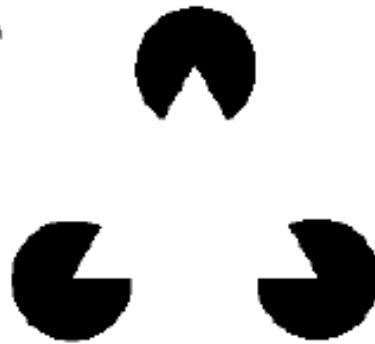
Grouping
by occlusions



Gestalt properties

Grouping
by invisible
completions

A



B



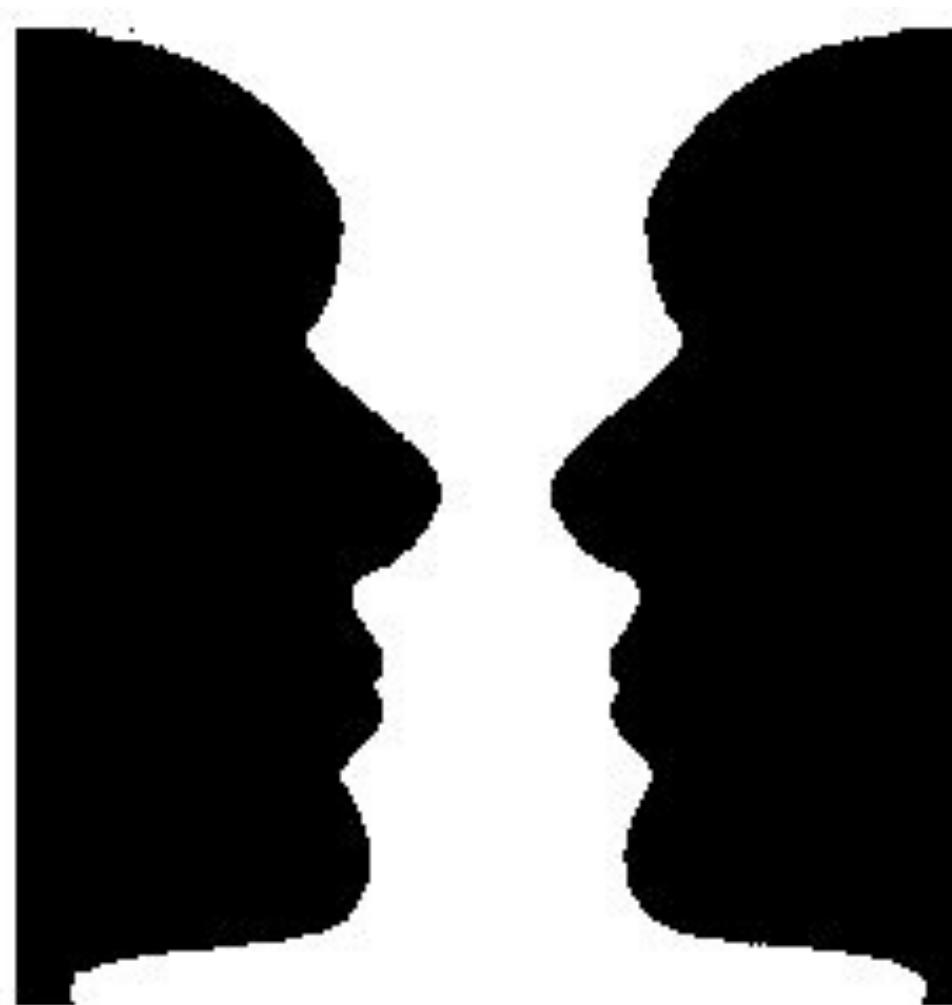
C



D



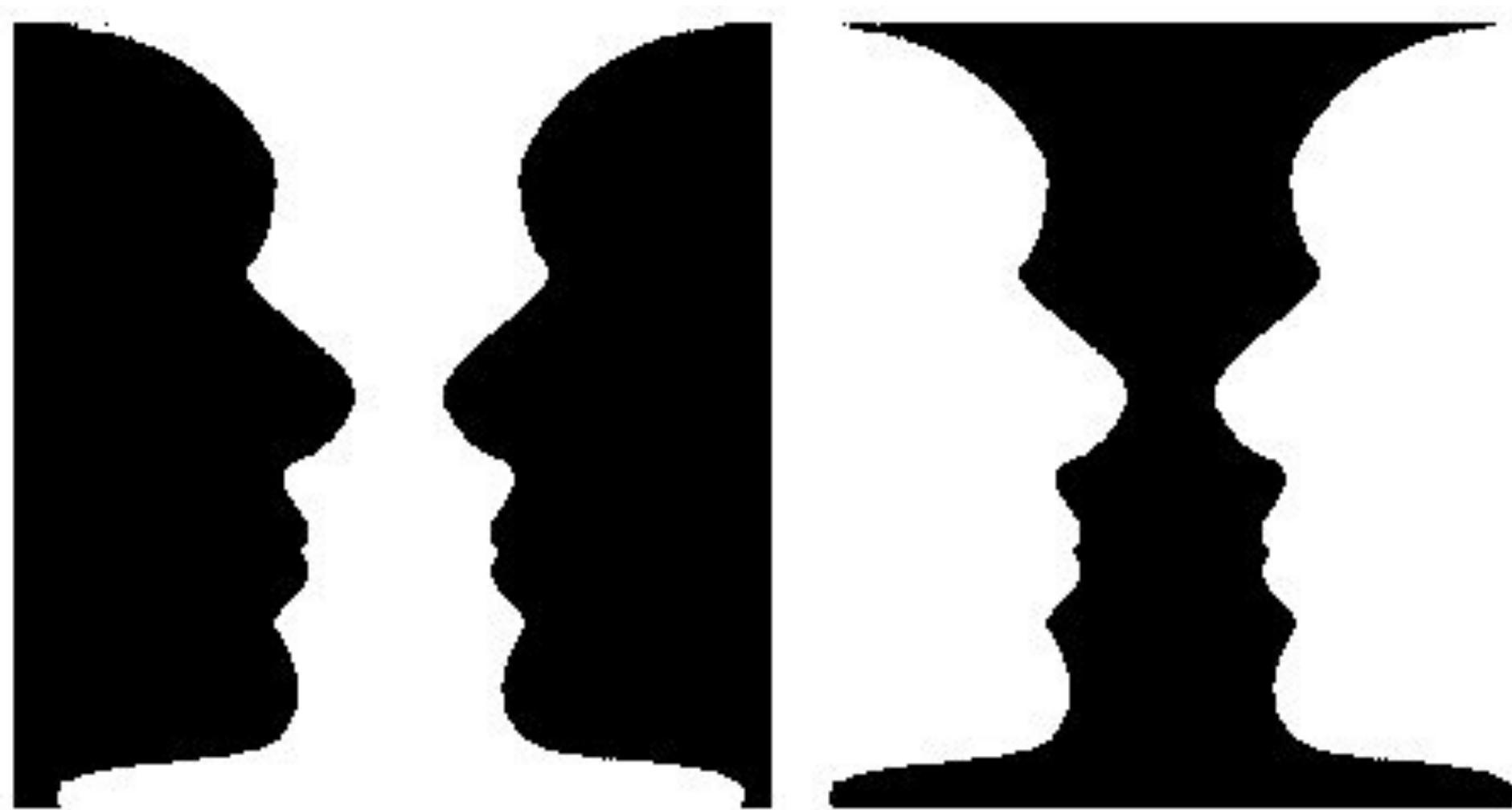
Figure-ground discrimination



–Grouping can be seen in terms of allocating some elements to a figure, some to ground

–Can be based on local bottom-up cues or high level recognition

Figure-ground discrimination

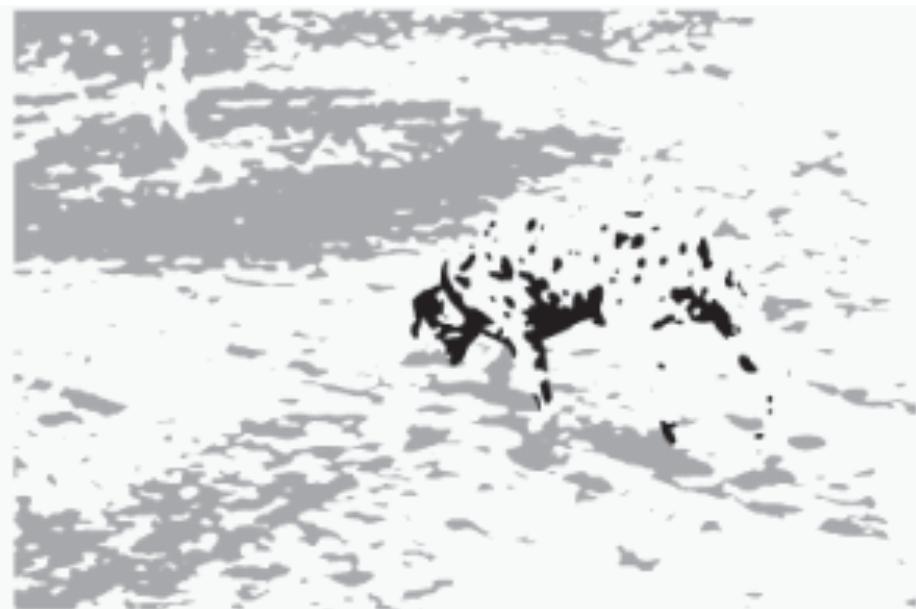


Emergence

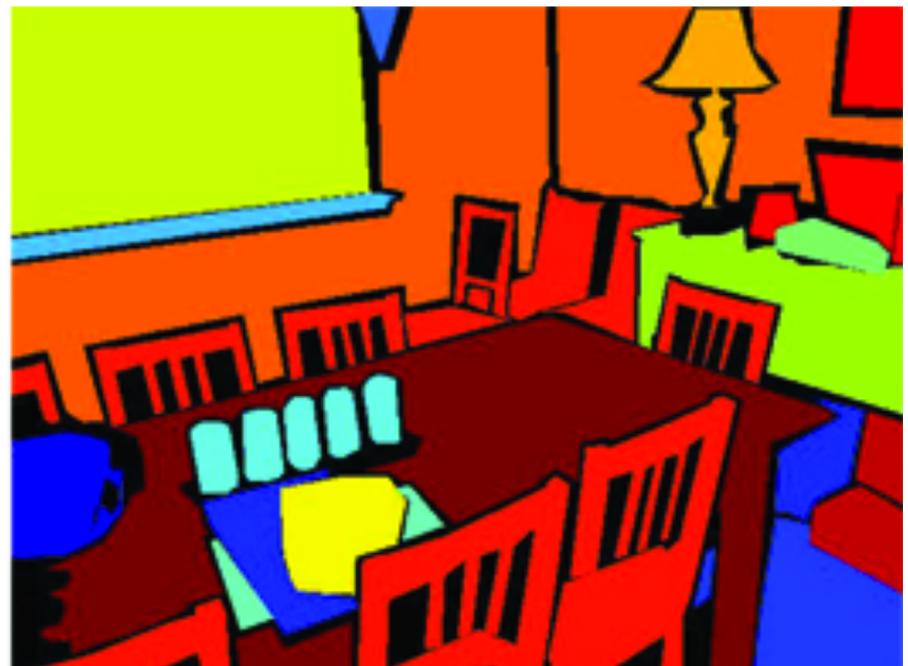


Emergence

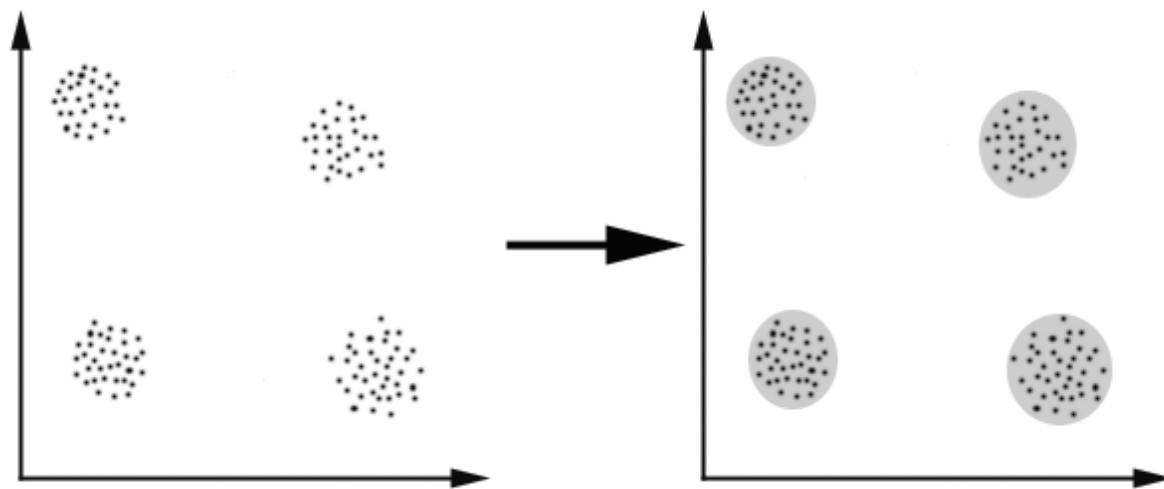
- aggregate information from meaningless pieces, and to perceive a meaningful whole.



How would you do it?



Clustering



Segmentation as clustering

Cluster together tokens that share similar visual characteristics

- **K-means**
- **Mean-shift**

Segmentation as clustering

Cluster together tokens that share similar visual characteristics

- **K-means** } See CS131A, CS 229
- **Mean-shift**

Segmentation as clustering

Cluster together tokens that share similar visual characteristics

- **K-means** } See CS131A, CS 229
- **Mean-shift** } This lecture

Segmentation as clustering

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 - Must specify number of clusters K in advance
 - Assumes clusters are spherical
- **Mean-shift** } This lecture

Segmentation as clustering

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 - Slow
 - Discovers arbitrary number of clusters
 - No a priori assumptions about cluster shapes

Segmentation as clustering

Cluster together tokens that share similar visual characteristics

- **K-means** } See CS131A, CS 229
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Lecture 13

Segmentation and Scene understanding



- Introduction
- Mean-shift
- Graph-based segmentation
- Top-down segmentation

Mean shift segmentation

D. Comaniciu and P. Meer, Mean Shift: A Robust Approach toward Feature Space Analysis, PAMI 2002.

- A versatile technique for clustering-based segmentation

Segmented "landscape 1"



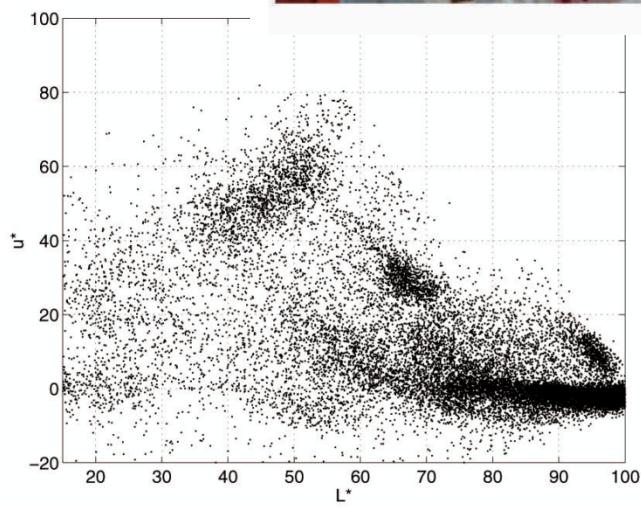
Segmented "landscape 2"



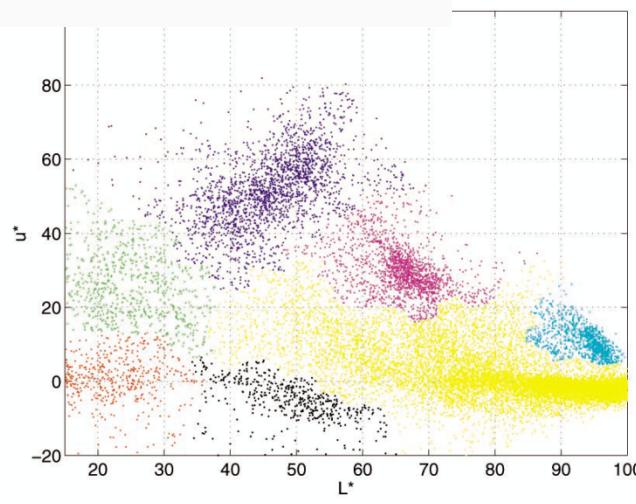
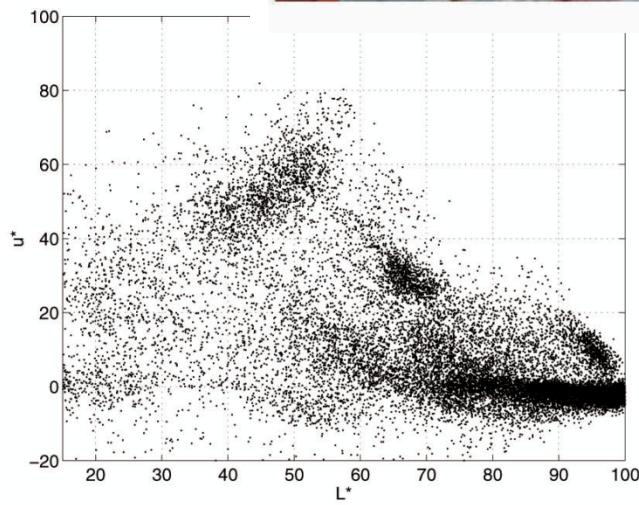
Mean shift segmentation



Mean shift segmentation



Mean shift segmentation



Mean shift algorithm

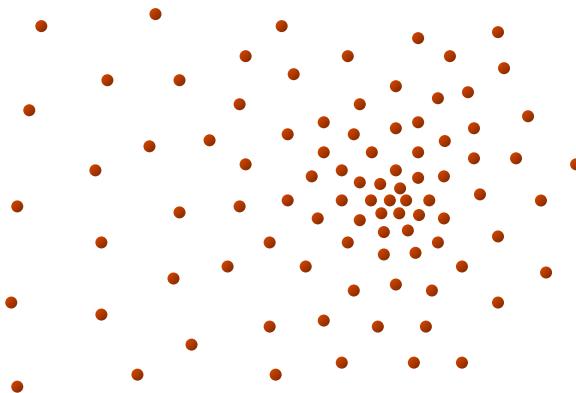
Fukunaga, Keinosuke; Larry D. Hostetler (January 1975). "The Estimation of the Gradient of a Density Function, with Applications in Pattern Recognition". *IEEE Transactions on Information Theory* (IEEE) **21** (1): 32–40

- The mean shift algorithm seeks the *modes* or local maximums of density of a given distribution

Mean shift algorithm

Fukunaga, Keinosuke; Larry D. Hostetler (January 1975). "The Estimation of the Gradient of a Density Function, with Applications in Pattern Recognition". *IEEE Transactions on Information Theory* (IEEE) **21** (1): 32–40

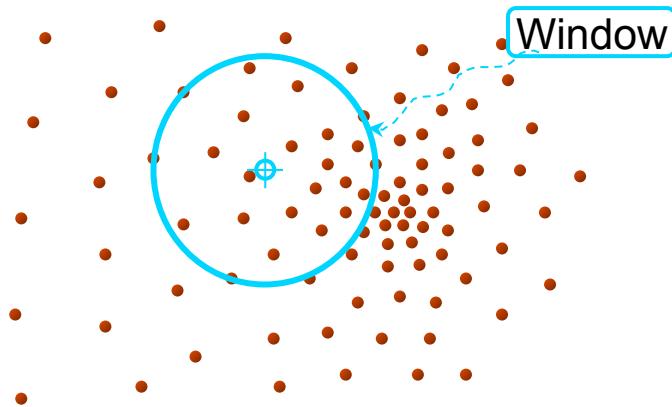
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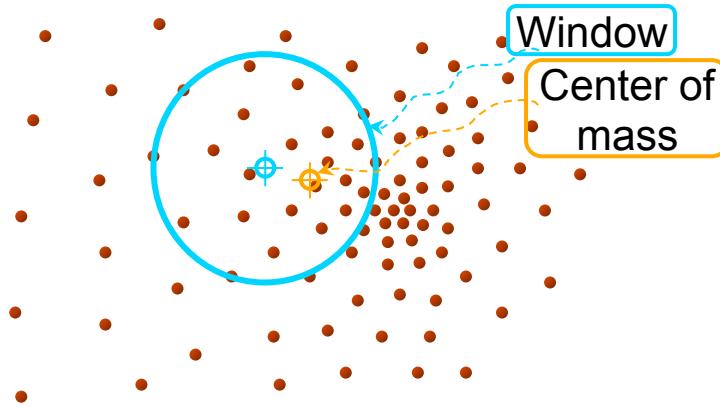
- The mean shift algorithm seeks the *modes* or local maximums of density of a given distribution
 - Choose a search window (size and location)



Mean shift algorithm

Fukunaga, Keinosuke; Larry D. Hostetler (January 1975). "The Estimation of the Gradient of a Density Function, with Applications in Pattern Recognition". *IEEE Transactions on Information Theory* (IEEE) **21** (1): 32–40

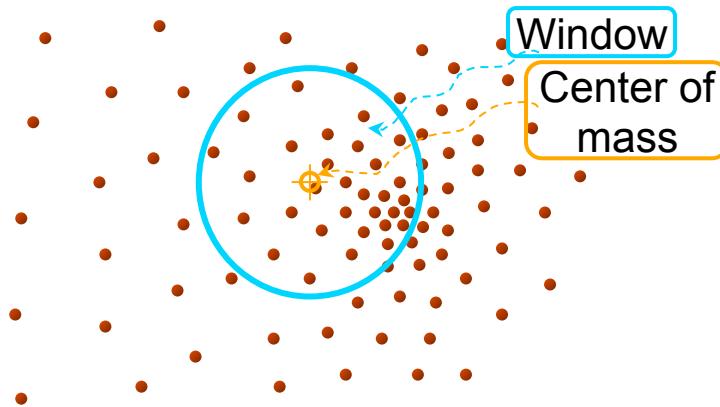
- The mean shift algorithm seeks the *modes* or local maximums of density of a given distribution
 - Choose a search window (size and location)
 - Compute the mean of the data in the search window



Mean shift algorithm

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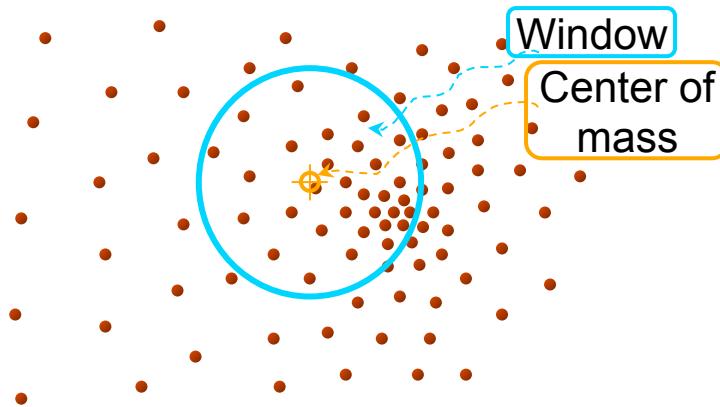
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 - Choose a search window (size and location)
 - Compute the mean of the data in the search window
 - Center the search window at the new mean location



Mean shift algorithm

Fukunaga, Keinosuke; Larry D. Hostetler (January 1975). "The Estimation of the Gradient of a Density Function, with Applications in Pattern Recognition". *IEEE Transactions on Information Theory* (IEEE) **21** (1): 32–40

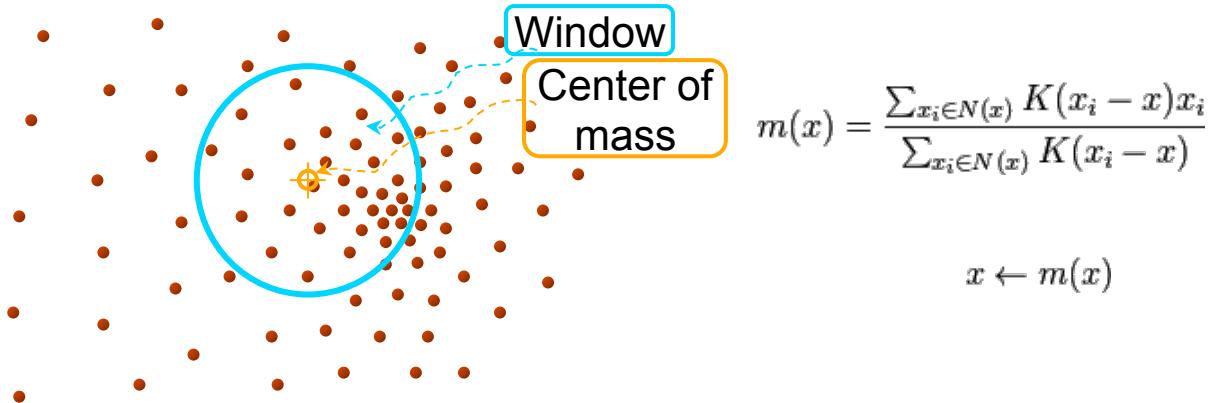
- The mean shift algorithm seeks the *modes* or local maximums of density of a given distribution
 - Choose a search window (size and location)
 - Compute the mean of the data in the search window
 - Center the search window at the new mean location
 - Repeat until convergence

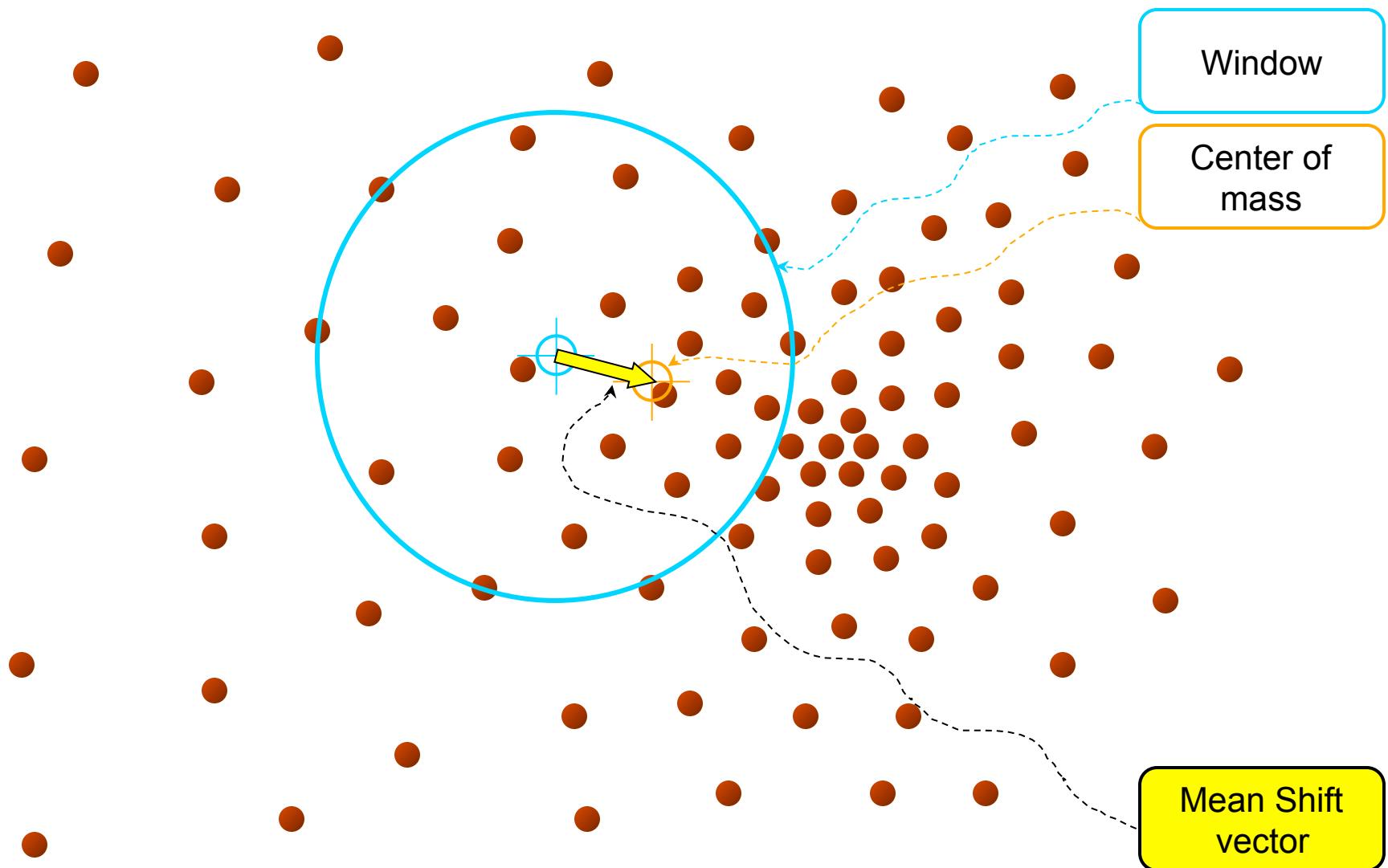


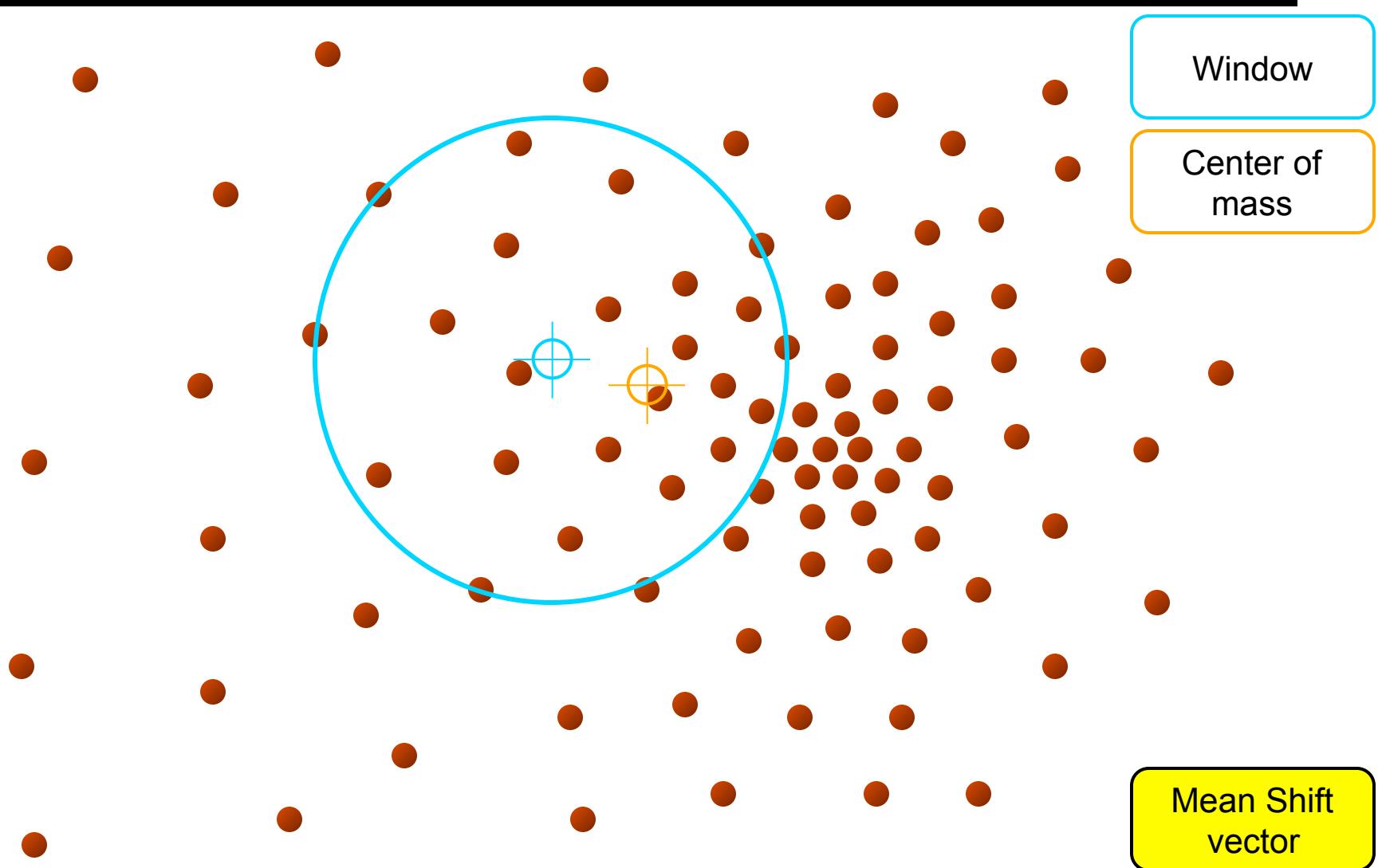
Mean shift algorithm

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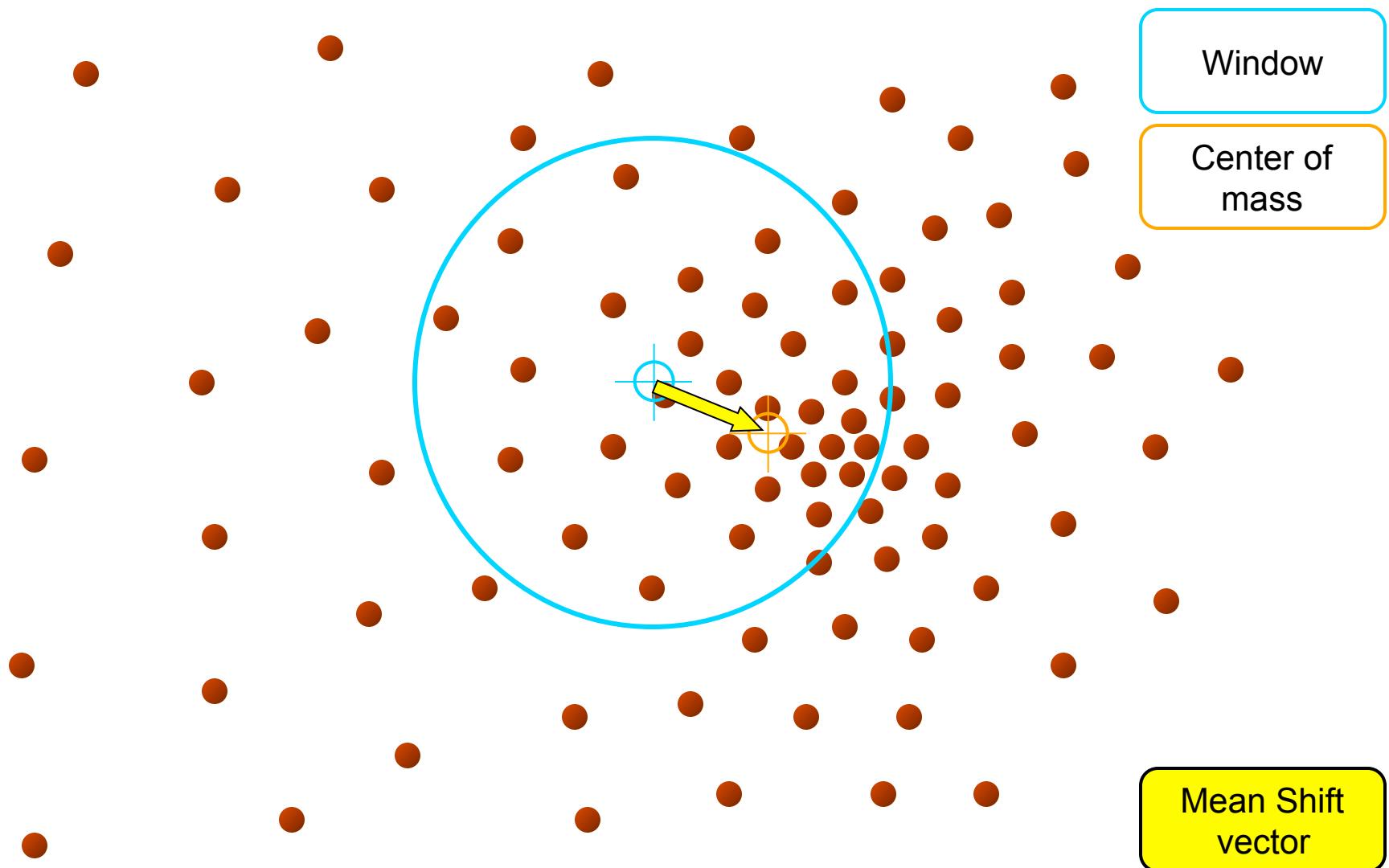
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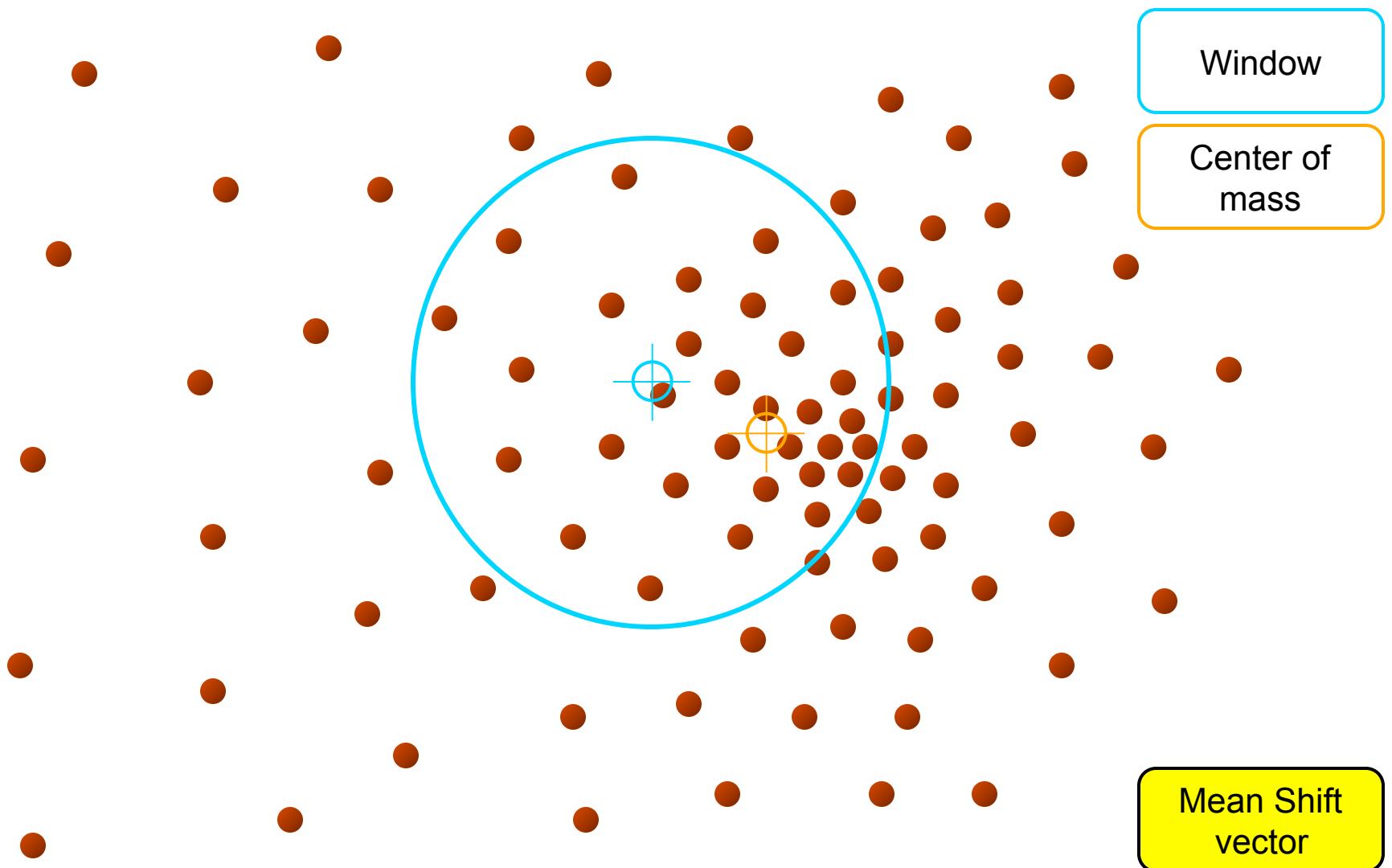


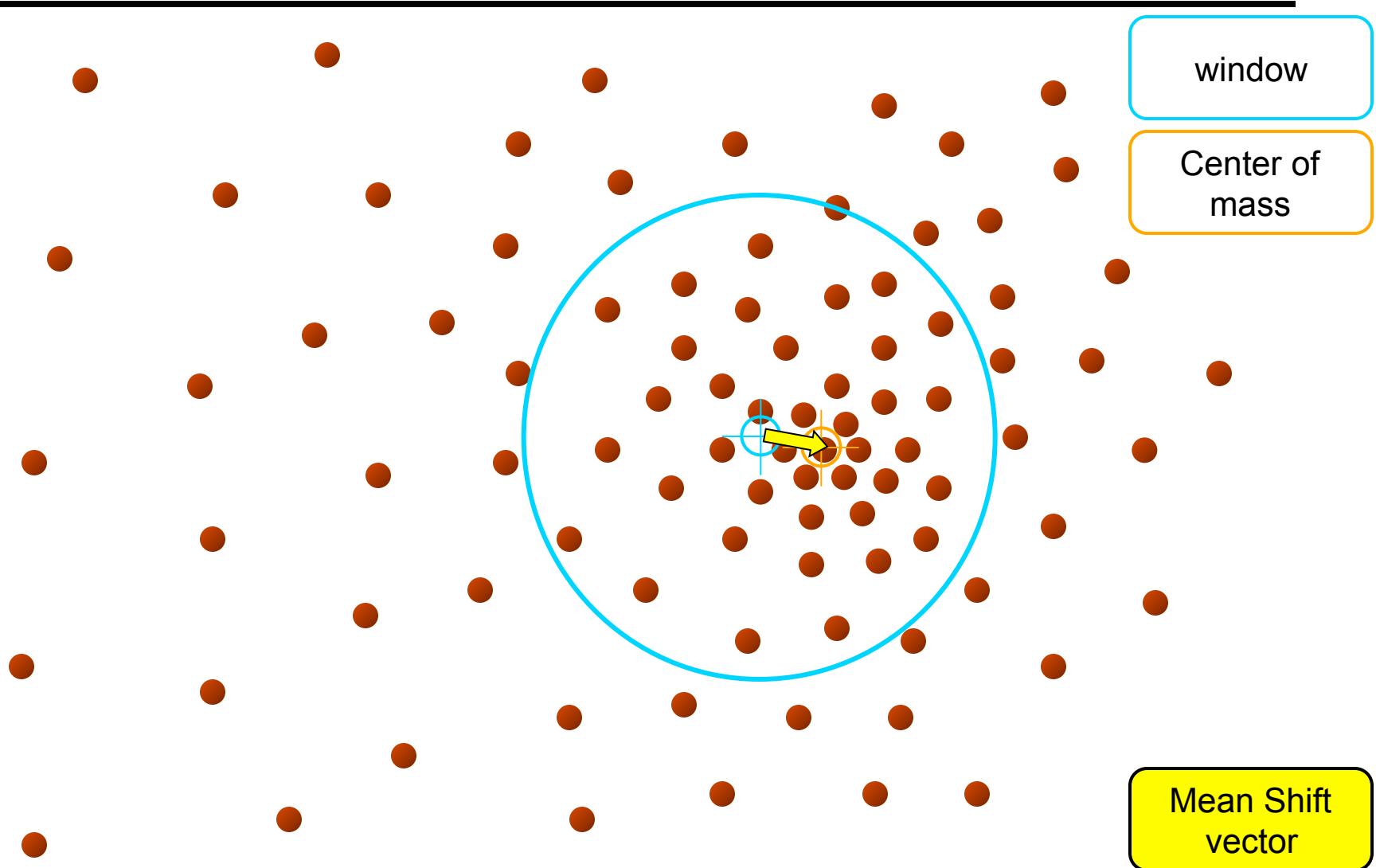


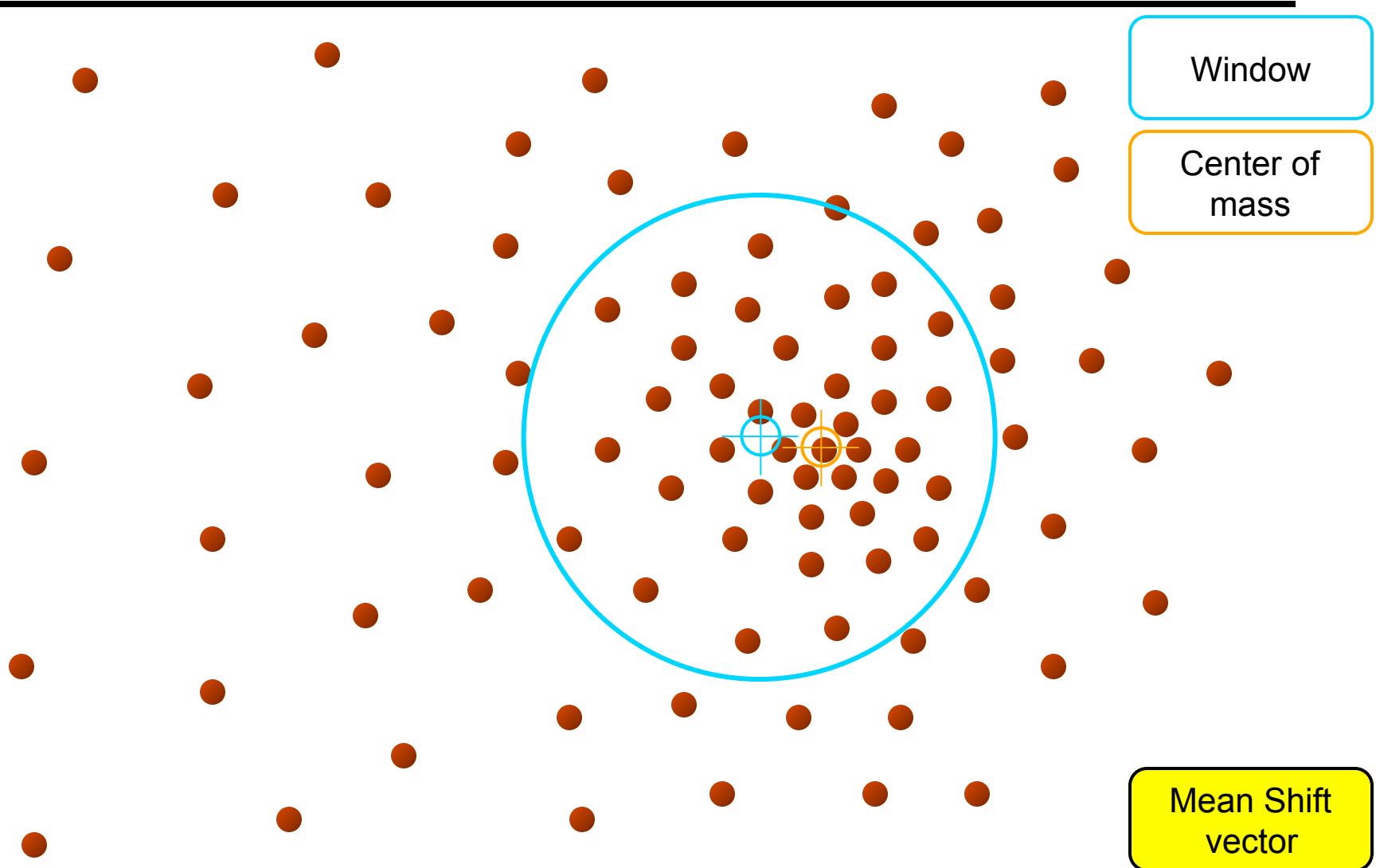
Mean shift

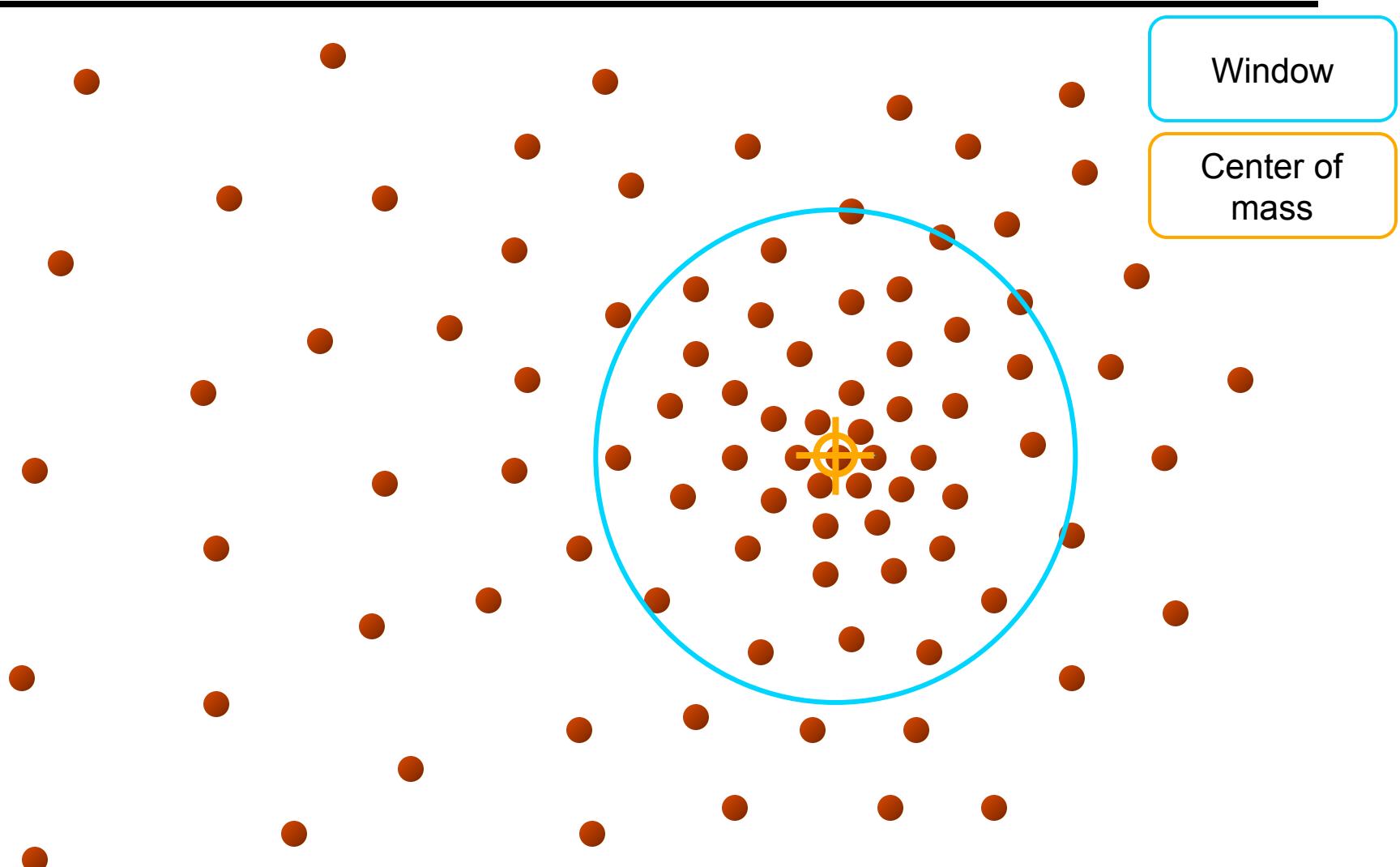


Mean shift

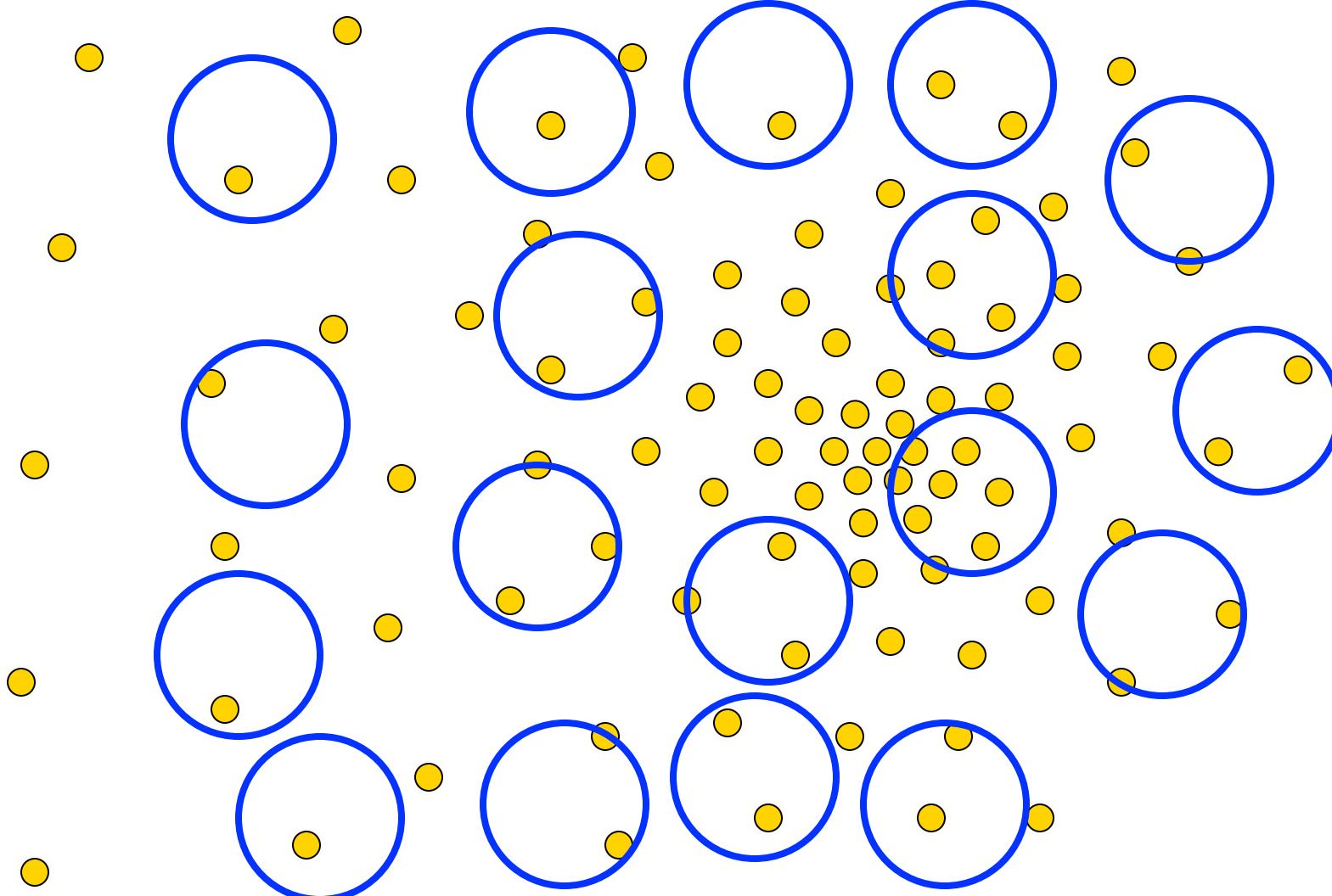








Real Modality Analysis

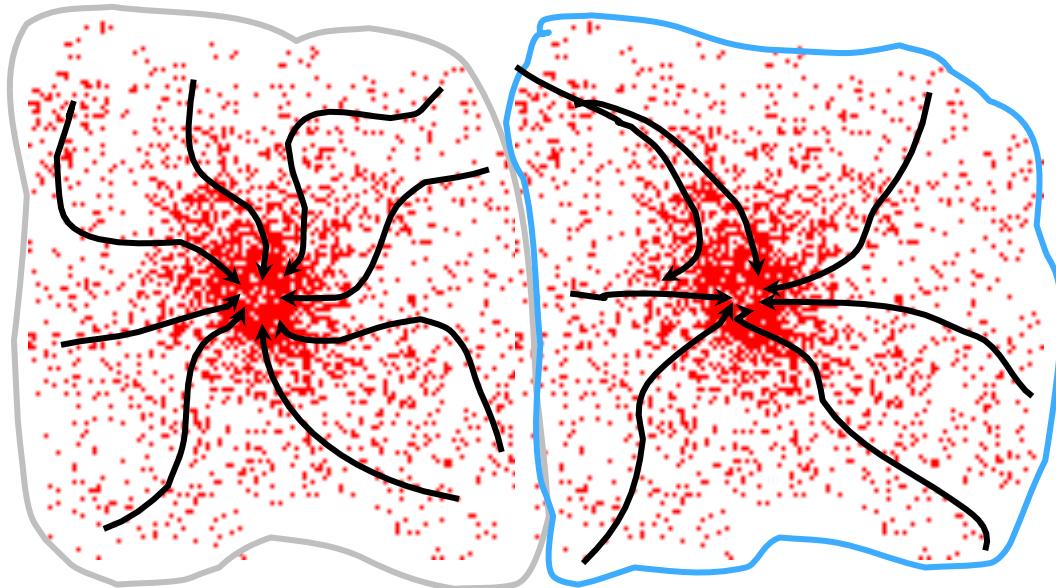


- Tessellate the space with windows

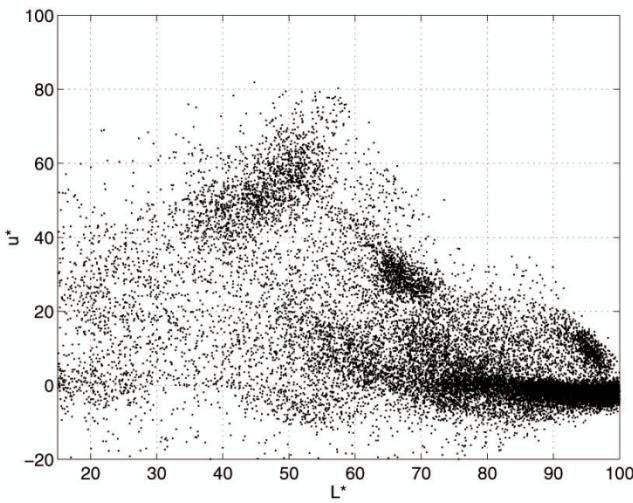
- Merge windows that end up near the same “peak” or model

Attraction basin

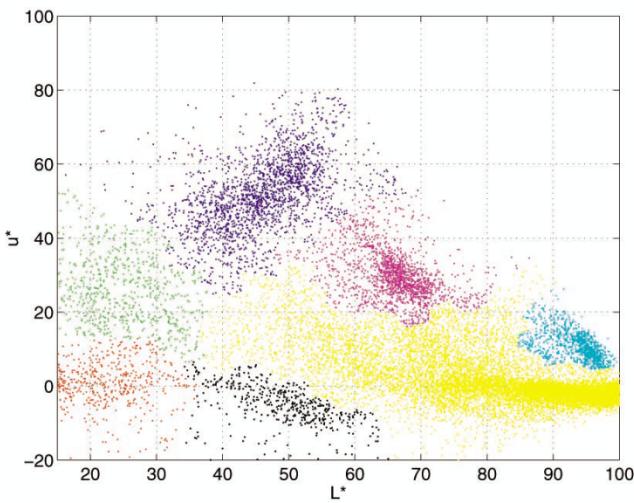
- **Attraction basin:** the region for which all trajectories lead to the same mode
- **Cluster:** all data points in the attraction basin of a mode



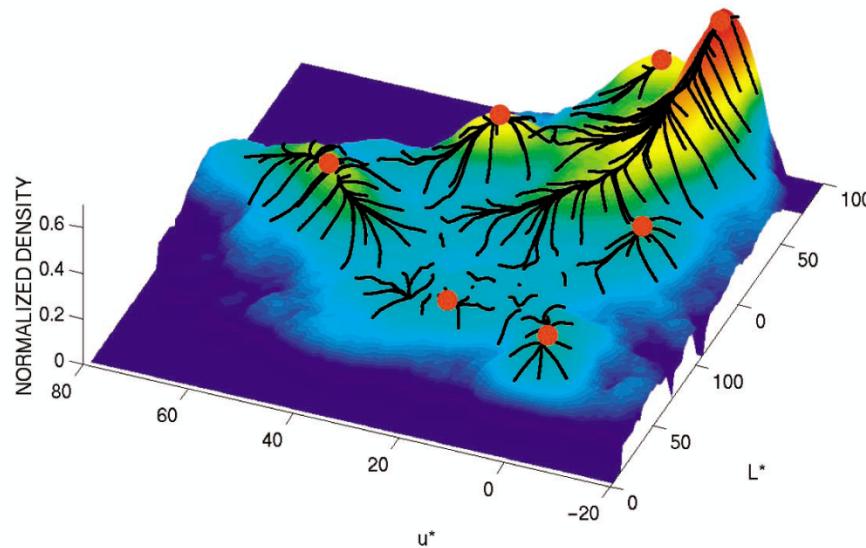
Attraction basin



(a)

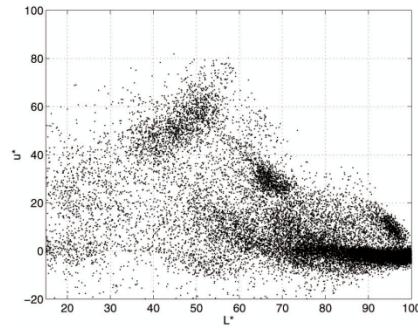


(b)

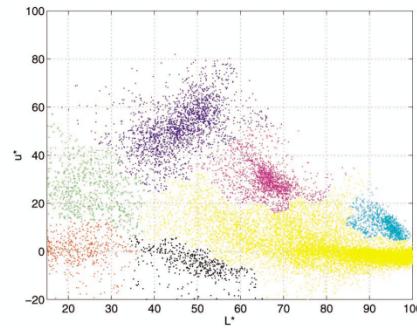


Segmentation by Mean Shift

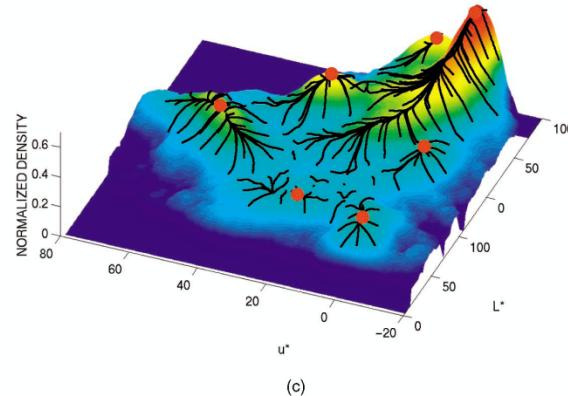
- Find features (color, gradients, texture, etc)
- Plot points in a joint feature-spatial space, e.g. (u, v, R, G, B)
- Initialize windows at individual pixel locations
- Perform mean shift for each window until convergence
- Merge windows that end up near the same “peak” or mode



(a)

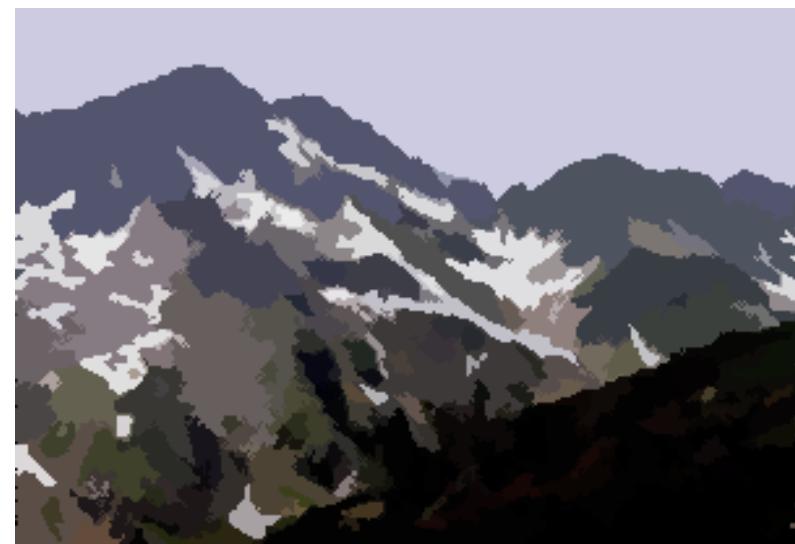


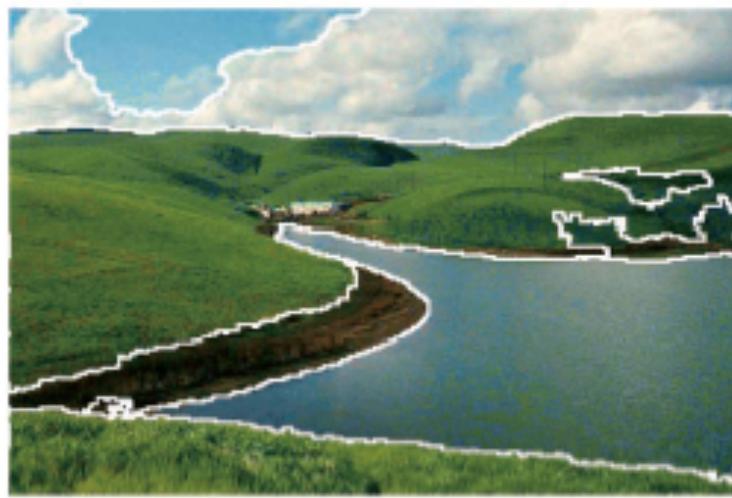
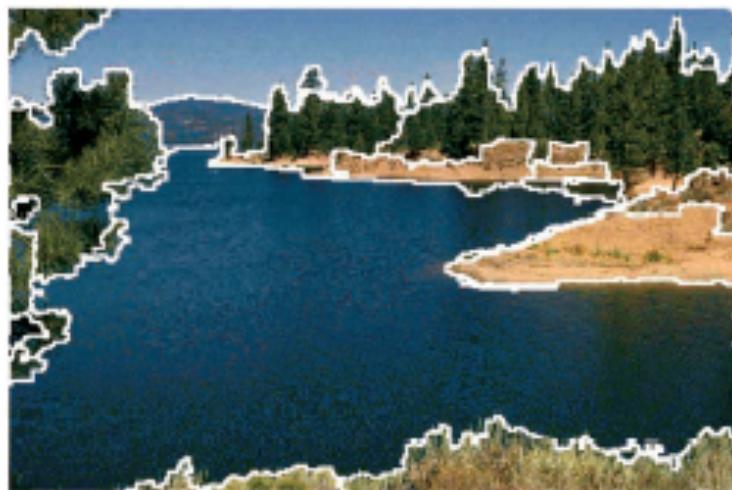
(b)



(c)

Mean shift segmentation results





Mean shift pros and cons

- Pros
 - Arbitrary shape of the clusters (not necessarily spherical as in kmeans)
 - Just a small number of parameters
 - Finds variable number of modes
 - Robust to outliers
- Cons
 - Output depends on window size
 - Computationally expensive
 - Does not scale well with dimension of feature space

Lecture 13

Segmentation and Scene understanding



- Introduction
- Mean-shift
- Graph-based segmentation
 - Normalized cut
 - Energy based
- Top-down segmentation

Graph-based segmentation

- Represent features and their relationships using a graph
- Cut the graph to get subgraphs with strong interior links and weaker exterior links
- Cuts correspond to segmentation boundaries

Images as graphs



- Node for every pixel
- Edge between every pair of pixels
- Each edge is weighted by the *affinity* or similarity of the two nodes

Measuring Affinity

Distance

$$aff(x, y) = \exp\left\{-\left(\frac{1}{2\sigma_d^2}\right)\left(\|x - y\|^2\right)\right\}$$

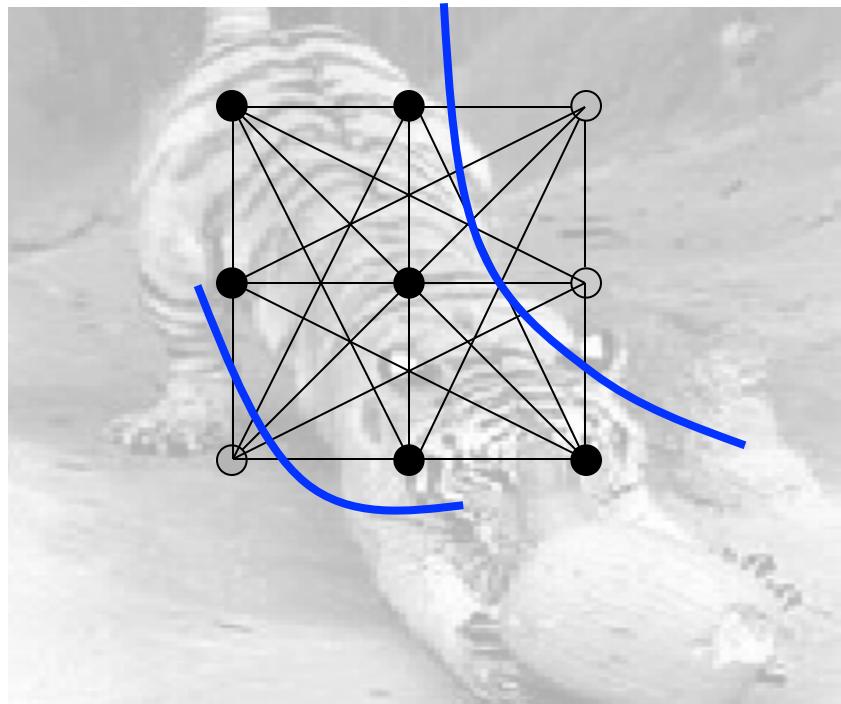
Intensity

$$aff(x, y) = \exp\left\{-\left(\frac{1}{2\sigma_i^2}\right)\left(\|I(x) - I(y)\|^2\right)\right\}$$

Color

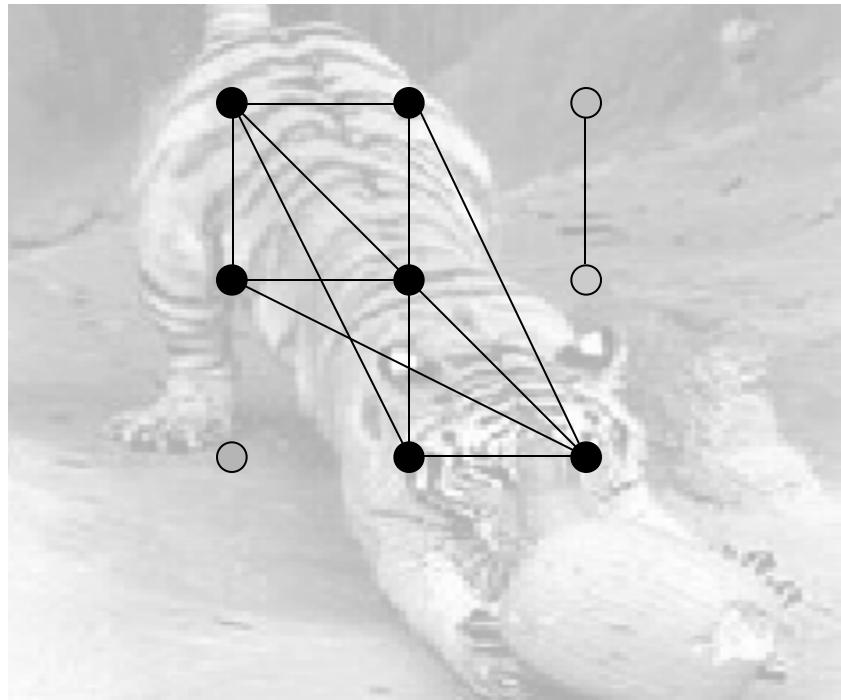
$$aff(x, y) = \exp\left\{-\left(\frac{1}{2\sigma_c^2}\right)\left(\|c(x) - c(y)\|^2\right)\right\}$$

Segmentation by graph partitioning



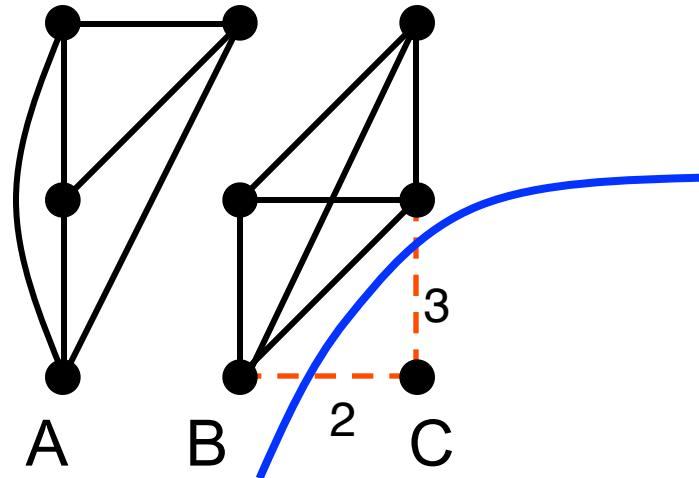
- Break Graph into sub-graphs
 - Break links (**cutting**) that have low affinity
 - similar pixels should be in the same sub-graphs
 - dissimilar pixels should be in different sub-graphs
- Sub-graphs represents different image segments

Segmentation by graph partitioning



- Break Graph into sub-graphs
 - Break links (*cutting*) that have low affinity
 - similar pixels should be in the same sub-graphs
 - dissimilar pixels should be in different sub-graphs
- Sub-graphs represents different image segments
- Graph-cut: technique to cut a graph optimally

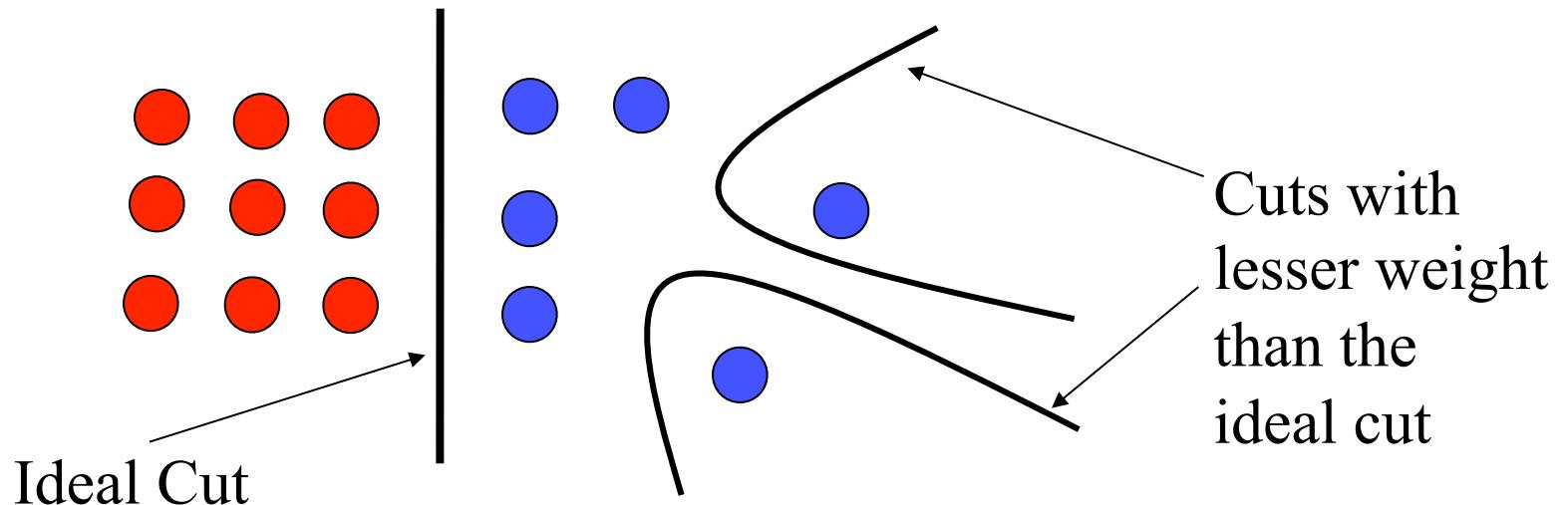
Segmentation by graph partitioning



- CUT: Set of edges whose removal makes a graph disconnected
- Cost of a cut: sum of weights of cut edges
- Example: Cost of the blue cut?

Minimum cut

- We can do segmentation by finding the *minimum cut* in a graph (i.e. cut associated with the min cost)
 - Efficient algorithms exist for doing this
- Drawback: minimum cut tends to cut off very small, isolated components



Normalized cut

J. Shi and J. Malik. Normalized cuts and image segmentation. PAMI 2000

IDEA: normalizing the cut by component size

The *normalized cut* cost is:

$$\frac{cut(A, B)}{assoc(A, V)} + \frac{cut(A, B)}{assoc(B, V)}$$

$assoc(A, V)$ = sum of weights of all edges in V that touch A

Normalized cut

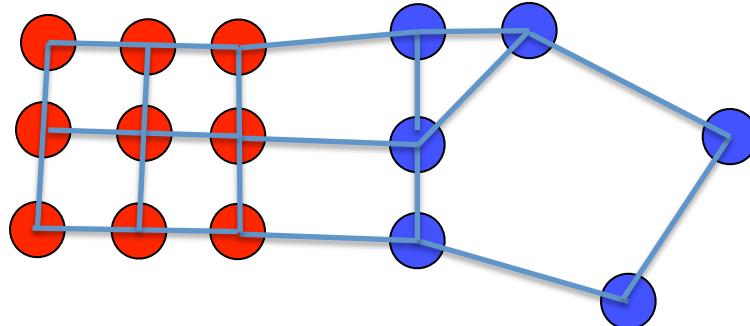
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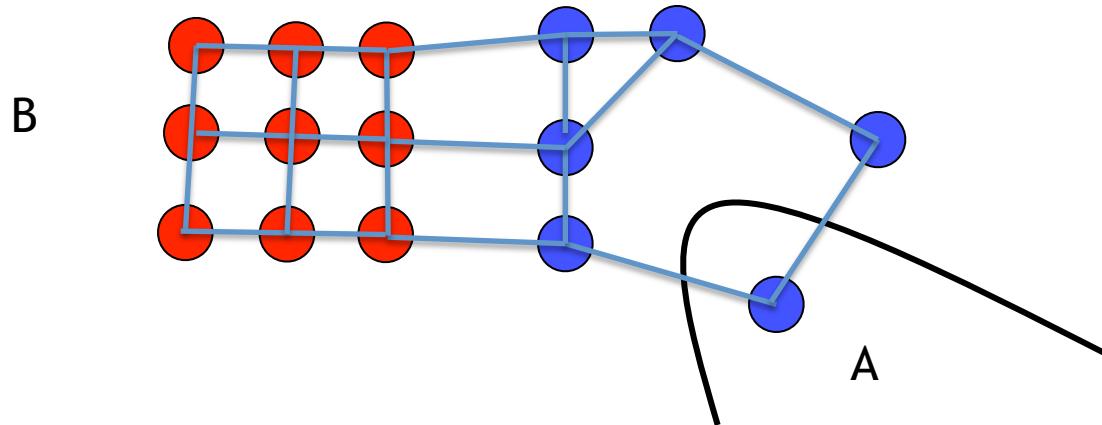
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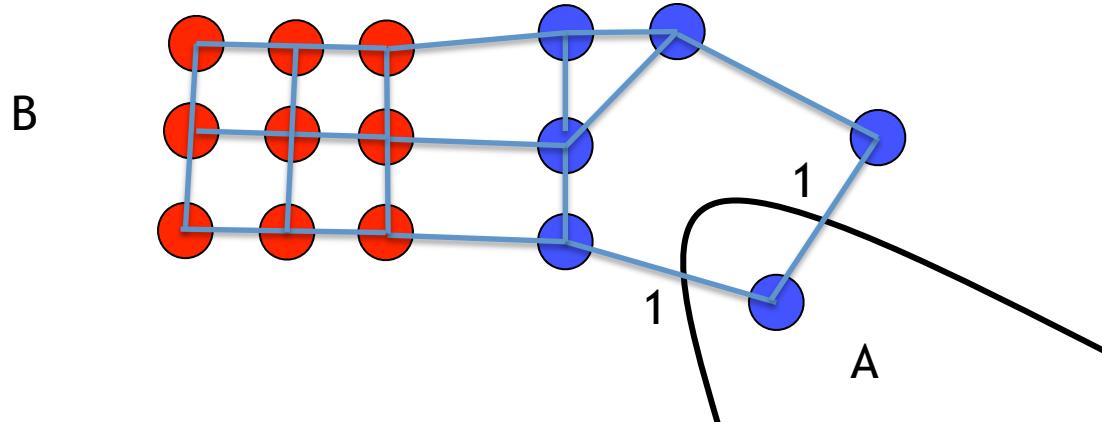
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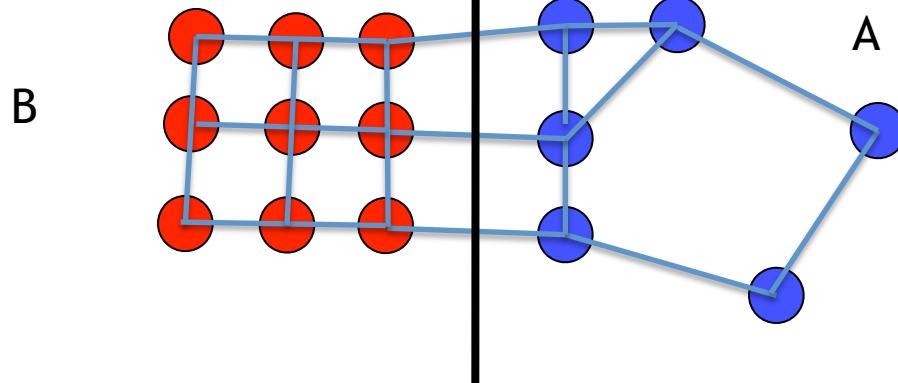
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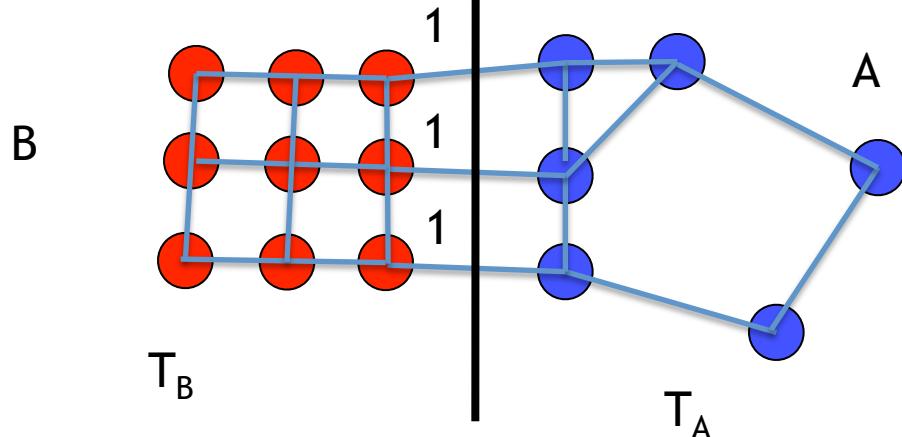
J. Shi and J. Malik. Normalized cuts and image segmentation. PAMI 2000

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Normalized Cuts

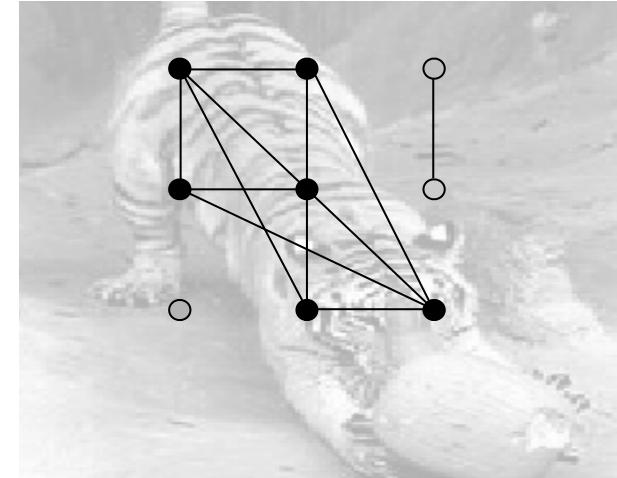
$$G = (V, E, W)$$

$$k = \frac{\sum_{x_i > 0} D_{i,i}}{\sum_i D_{i,i}}$$

$$b = \frac{k}{1 - k}$$

$$y = (1 + x) - b(1 - x)$$

$$y^T D 1 = 0 \text{ and } y^T D y = b 1^T D 1$$

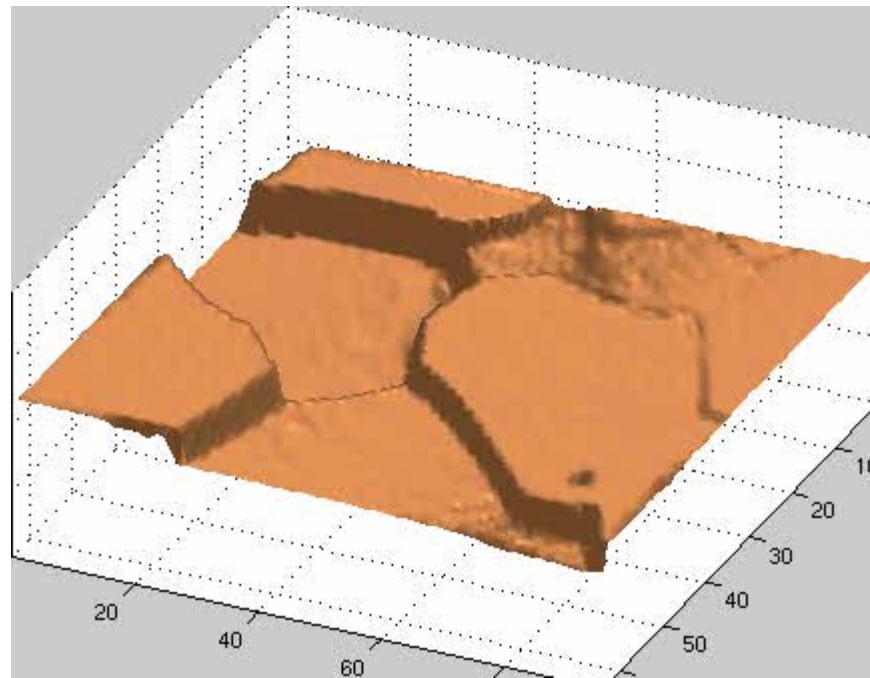


$$\min_x \text{ncut}(x, W, D) = \min_y \frac{y^T (W - D)y}{y^T D y}$$

$$y_i \in \{1, -b\}, \quad y^T D 1 = 0.$$

$$(D - W)y = \lambda D y$$

Interpretation as a Dynamical System



Treat the links as springs and shake the system

- elasticity proportional to cost
- vibration “modes” correspond to segments
 - can compute these by solving an eigenvector problem
 - http://www.cis.upenn.edu/~jshi/papers/pami_ncut.pdf

Color Image Segmentation

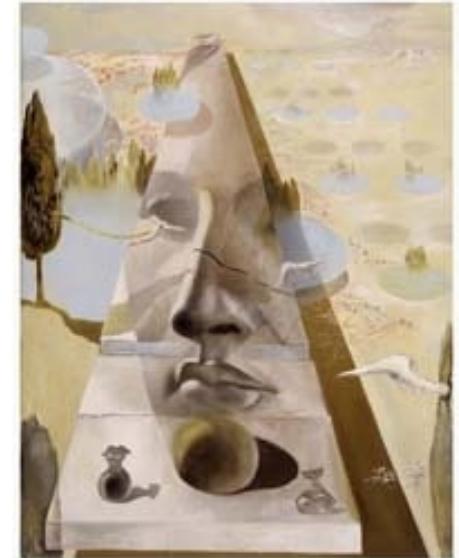


Normalized cuts: Pro and con

- Pros
 - Generic framework, can be used with many different features and affinity formulations
- Cons
 - High storage requirement and time complexity
 - Bias towards partitioning into equal segments

Lecture 13

Segmentation and Scene understanding



- Introduction
- Mean-shift
- Graph-based segmentation
 - Graph cut
 - Energy based
- Top-down segmentation

Binary segmentation as energy minimization

- Suppose we want to segment an image into foreground and background



User sketches out a few strokes on
foreground and background...

How do we classify the rest of the
pixels?

Courtesy of Noah Snavely

Binary segmentation as energy minimization

- Define a labeling L as an assignment of each pixel with a 0-1 label (background or foreground)
- Problem statement: find the labeling L that minimizes

$$E(L) = E_d(L) + \lambda E_s(L)$$

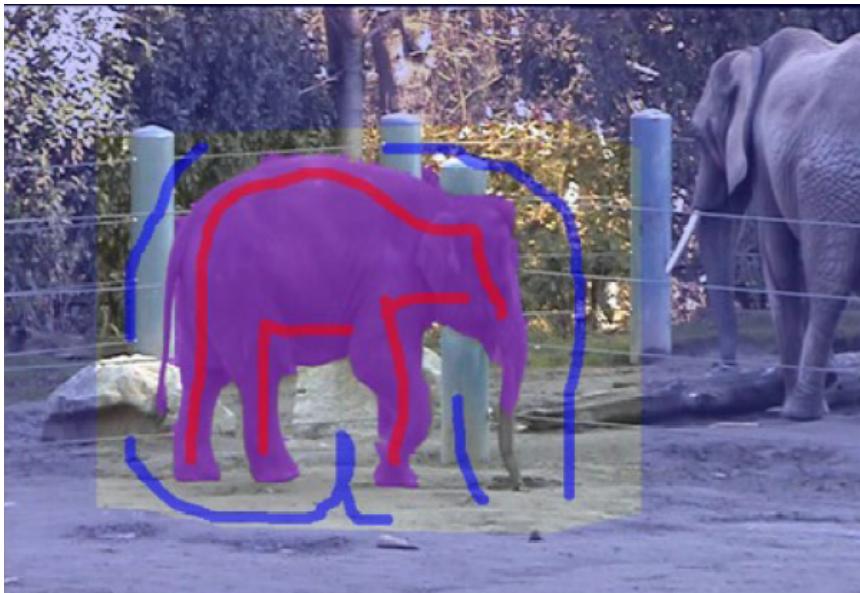


match cost smoothness cost

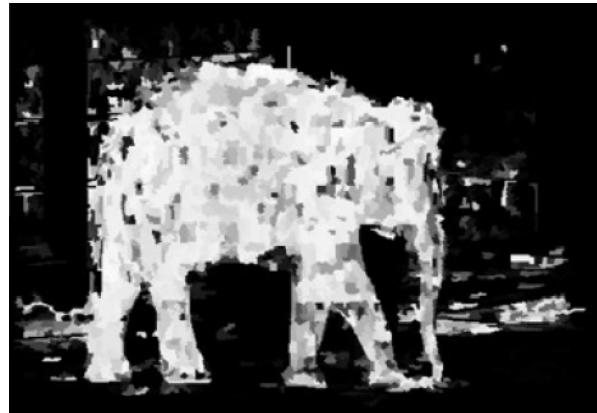
(“how similar is each pixel
to the foreground /
background?”)



$$E(L) = E_d(L) + \lambda E_s(L)$$



$$C'(x, y, 0)$$

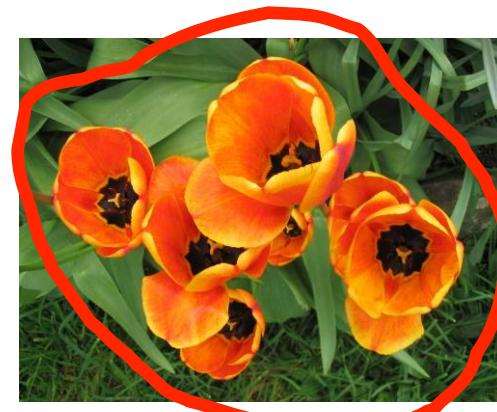


$$C'(x, y, 1)$$

Courtesy of Noah Snavely

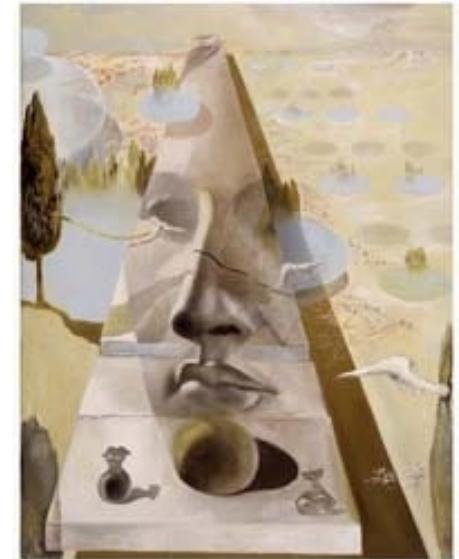
GrabCut

Grabcut [Rother et al., SIGGRAPH 2004]



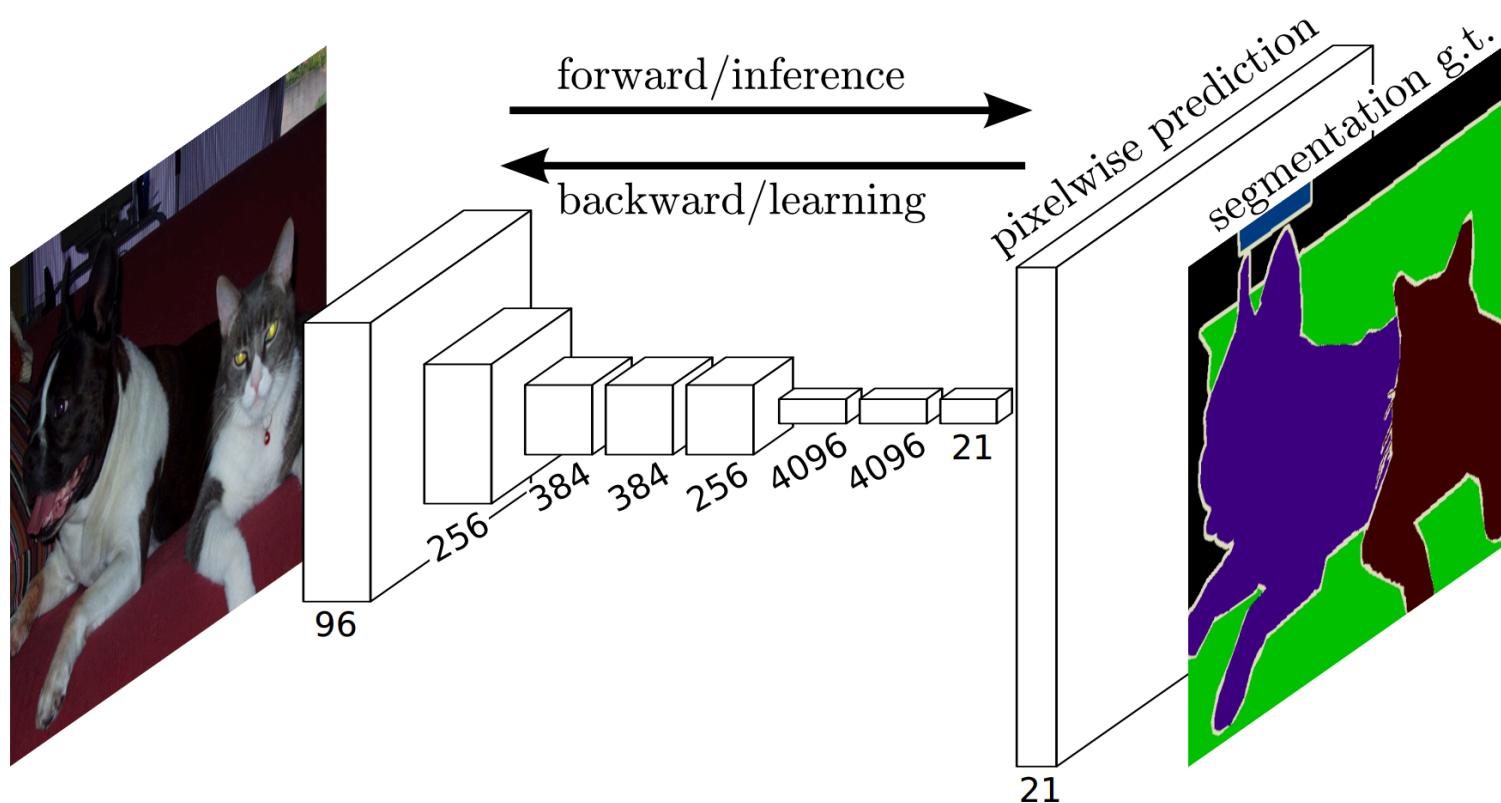
Lecture 13

Segmentation and Scene understanding



- Introduction
- Mean-shift
- Graph-based segmentation
- Top-down segmentation

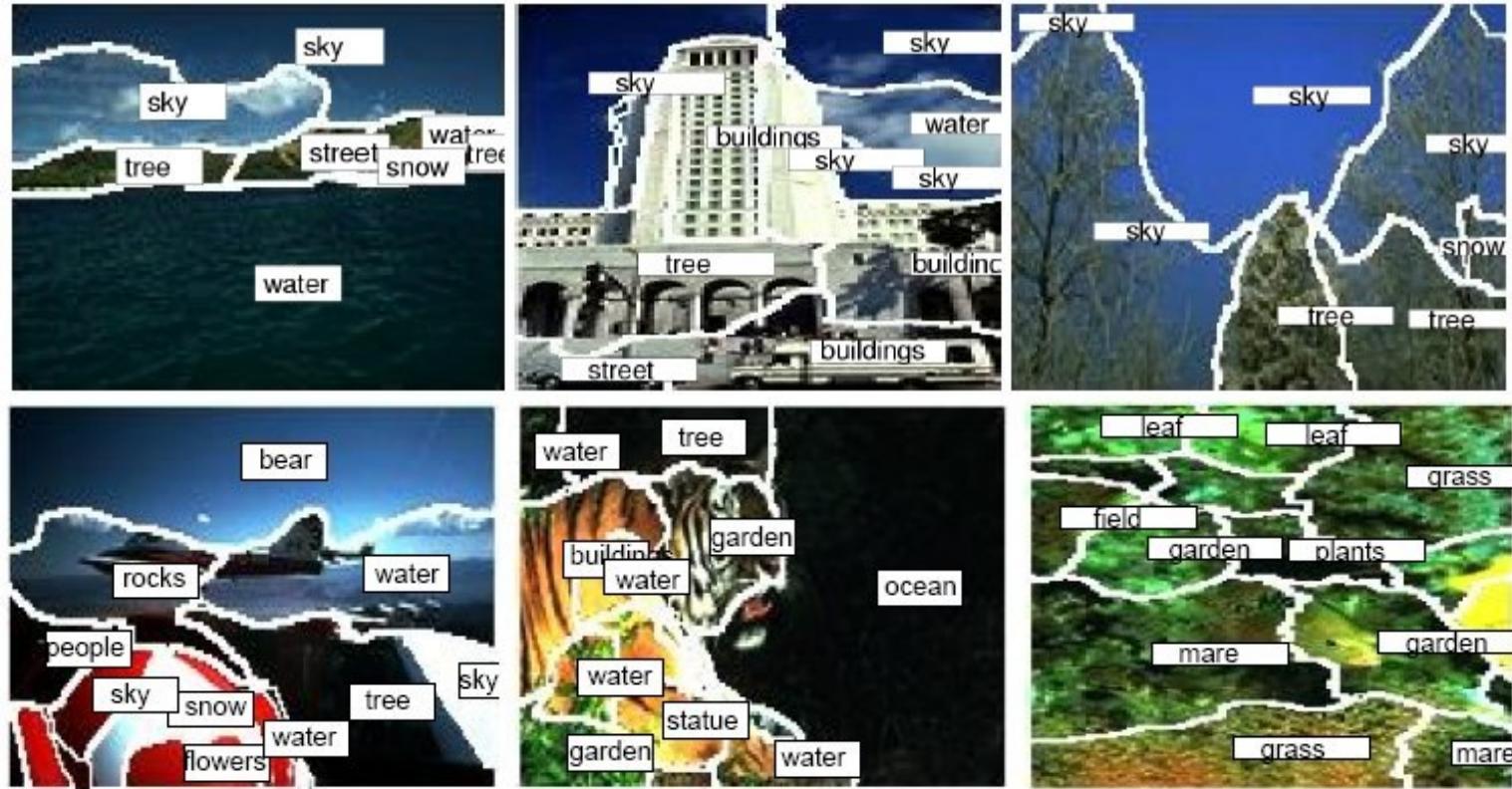
Semantic segmentation



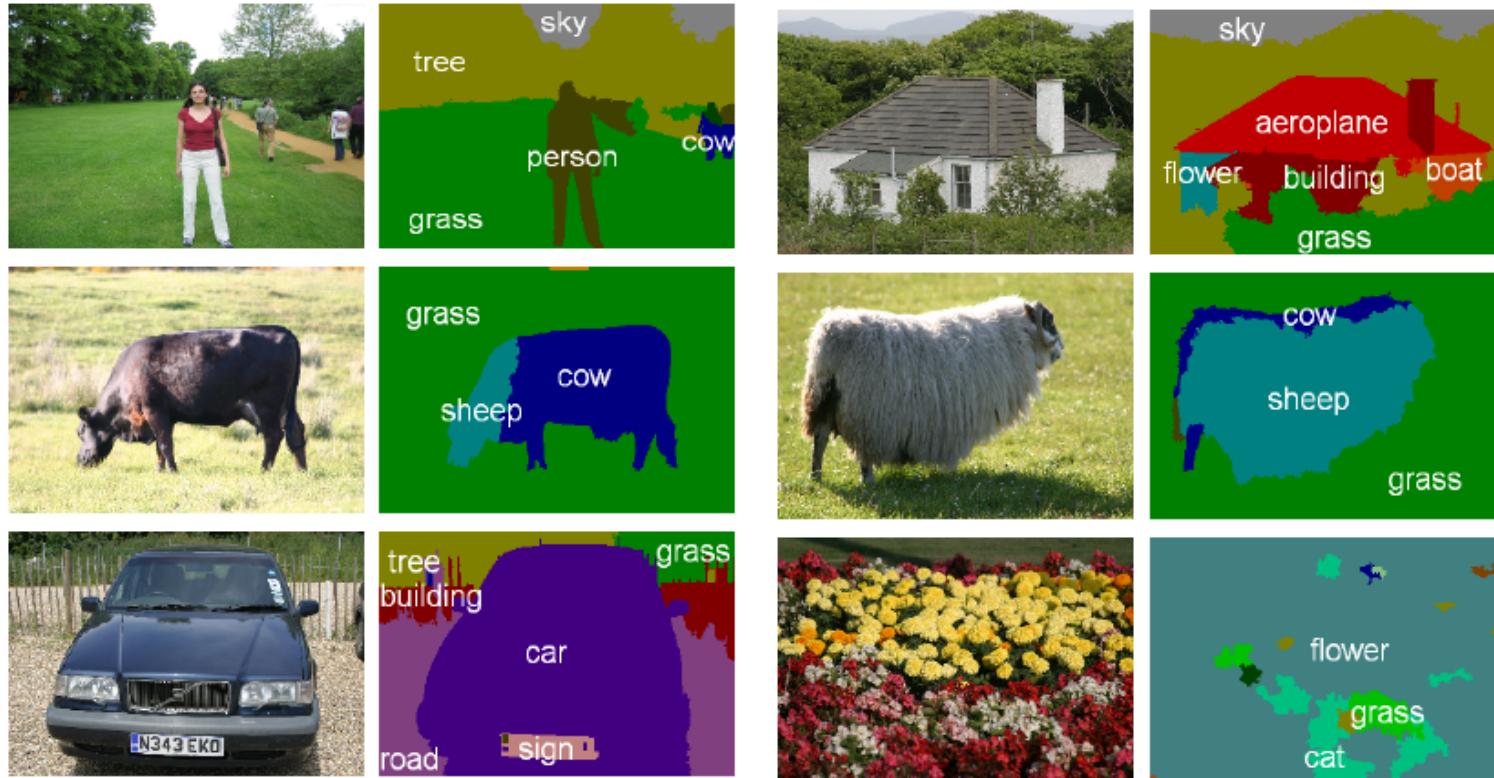
Long, Shelhamer, Darrel (Arxiv)

Semantic segmentation

Object Recognition as Machine Translation, Duygulu, Barnard, **de Freitas**, Forsyth, ECCV02



Semantic segmentation



Ladický, Russell, Kohli, Torr ICCV09