CS 231A Computer Vision (Spring 2016) Problem Set 0

Due Date: April 4th 2016 11:59pm

This is a short tutorial on how to use MATLAB and a review of some small linear algebra ideas. The point of this assignment is to get you used to manipulating matrices and images in MATLAB

Make sure you use a ".m" file to write your matlab script and use the publish functionality in MATLAB to print your code and results. Please suppress all unnecessary results with semicolons.

NOTE: This problem set is not representative of future problem sets in terms of length or difficulty, but the logistics will be similar (submission, Piazza, etc).

You will find the future problem sets to be more difficult than this one. This problem set is simply to ensure you have a sufficient understanding of the basic prerequisites for this class.

Submit your published results to Gradescope. Feel free to ask any questions to the class Piazza forum (but use a private post if you have code or specifics to discuss).

1 Piazza Poll (10 points)

Please register on the class Piazza forum and answer the poll about your class background.

2 Basic Matrix/Vector Manipulation (10 points)

In MATLAB, please calculate the following. Given matrix M and vectors a,b,c such that

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 0 & 2 & 2 \end{bmatrix}, a = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}, b = \begin{bmatrix} -1 \\ 2 \\ 5 \end{bmatrix}, c = \begin{bmatrix} 0 \\ 2 \\ 3 \\ 2 \end{bmatrix}$$

- (a) Define Matrix M and Vectors a,b,c in Matlab
- (b) Find the dot product of vectors a and b (i.e. $a^{\top}b$). Save this value as aDotb.
- (c) Find the element-wise product of a and b $[a_1b_1, a_2b_2, a_3b_3]^T$.
- (d) Find $(a^{\top}b)Ma$.
- (e) Without using a loop, multiply each row of M element-wise by a. (Hint: The function repmat() may come in handy).
- (f) Without using a loop, sort all of the values of M in increasing order and plot them.

3 Basic Image Manipulations (20 points)

- (a) Read in the images, image1.jpg and image2.jpg, as color images.
- (b) Convert the images to double precision and rescale them to stretch from minimum value 0 to maximum value 1.
- (c) Add the images together and re-normalize them to have minimum value 0 and maximum value 1. Display this image.
- (d) Create a new image such that the left half of the image is the left half of image1 and the right half of the image is the right half of image2.
- (e) Using a for loop, create a new image such that every odd numbered row is the corresponding row from image1 and the every even row is the corresponding row from image2. (Hint: Remember that indices start at 1 and not 0 in MATLAB).
- (f) Accomplish the same task as part e without using a for-loop (the functions reshape and repmat may be helpful here).
- (g) Convert the result from part f to a grayscale image. Display the grayscale image with a title.

4 Singular Value Decomposition (20 points)

- (a) Read in image1 as a grayscale image. Take the singular value decomposition of the image.
- (b) Recall from the discussion section that the best rank n approximation of a matrix is $\sum_{i=1}^{i=n} u_i \sigma_i v_i^{\mathsf{T}}$, where u_i , σ_i , and v_i are the ith left singular vector, singular value, and right singular vector respectively. Save and display the best rank 1 approximation of the (grayscale) image1.
- (c) Save and display the best rank 20 approximation of the (grayscale) image1.