

Homework #3: Selection and order statistics, heaps/heapsort
Due Date: Tuesday, 1 February 2000

Reading: Chapters 7, 10.

Recall that *exercises* are for you to work out on your own; *problems* are to be handed in.

Exercise 3-1. Do Exercise 10.1–2 on page 187 of CLR.

Exercise 3-2. Do Exercise 10.3–8 on page 192 of CLR.

Exercise 3-3. Do Exercise 7.2–5 on page 144 of CLR.

Exercise 3-4. Do Exercise 7.3–3 on page 147 of CLR.

Exercise 3-5. Do Exercise 7.4–2 on page 149 of CLR.

Problem 1. Weighted statistics [50 points].

For n distinct elements x_1, x_2, \dots, x_n with positive weights w_1, w_2, \dots, w_n such that $\sum_{i=1}^n w_i = W$, the **weighted 3-median** is the element x_k satisfying

$$\sum_{x_i < x_k} w_i \leq \frac{W}{3}$$

and

$$\sum_{x_i > x_k} w_i \leq \frac{2W}{3}.$$

- (a) Show how to compute the weighted 3-median of n elements in $O(n \lg n)$ worst-case time using sorting.
- (b) Show how to compute the weighted 3-median in $\Theta(n)$ worst-case time using a linear-time median algorithm such as SELECT from the text.

Problem 2. Do Exercise 7.5-5 on page 151 of CLR [10 points].

Problem 3. Do Problem 7-1 on page 152 of CLR [20 points].