

# pulsar6

August 25, 2022

## 1 Pulsar Emission Data Analysis

```
[ ]: #currently including any and all Imports that maybe needed for the project.
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
from sklearn.model_selection import train_test_split
from sklearn import linear_model
from sklearn.metrics import r2_score, mean_squared_error
from sklearn.linear_model import LogisticRegression, LinearRegression
from sklearn.metrics import confusion_matrix, accuracy_score
from sklearn.feature_selection import RFE
import datetime as dt
from sklearn.cluster import KMeans
from sklearn.metrics import pairwise_distances
from scipy.cluster.hierarchy import linkage, dendrogram, cut_tree
from scipy.spatial.distance import pdist
from sklearn.feature_extraction.text import TfidfVectorizer
import matplotlib.dates as mdates
from scipy.stats import pearsonr
from scipy import stats
import statistics
import math
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
from statsmodels.tsa.stattools import acf, pacf
from statsmodels.tsa.tsatools import lagmat
```

Section for extracting from a tar file.

Currently implemented for original TAR File structure.

```
[ ]: #This is also found in the main file under tarunzip.py
import tarfile
import os
import sys
```

```
#tar = tarfile.open("pulseTarFile.tar")
#tar.extractall('./Data')
#tar.close()
```

## 1.1 Beginning of Exploration

### 1.1.1 Examining the data

In this section we are determining the total integrity of the data to determine if further comprehensive data cleaning and uniforming processes are needed.

```
[ ]: colnames = ['Pulse Number', 'Brightness', 'Uncertainty']
pulsar6 = pd.read_csv("Data/J1644-4559.pulses", sep = ' ', header = None, names_
↳ colnames)
```

```
[ ]: pulsar6.shape
```

```
[ ]: (698, 3)
```

```
[ ]: pulsar6.head(25)
```

```
[ ]:
      Pulse Number  Brightness  Uncertainty
0                1    0.634671    0.002761
1                2    0.736945    0.005207
2                3    0.693834    0.002706
3                4    1.021866    0.010184
4                5    0.673845    0.006236
5                6    0.676883    0.004763
6                7    0.527039    0.002422
7                8    0.673417    0.003174
8                9    0.357076    0.002848
9               10    0.661704    0.005588
10              11    0.545564    0.003835
11              12    0.494655    0.003145
12              13    0.804260    0.005258
13              14    0.513362    0.005700
14              15    0.477025    0.002945
15              16    0.399571    0.004712
16              17    0.188069    0.002452
17              18    0.748592    0.005468
18              19    0.723437    0.004548
19              20    0.960154    0.006765
20              21    0.707715    0.006011
21              22    1.074550    0.006831
22              23    0.961340    0.006617
23              24    0.754457    0.004117
24              25    0.773151    0.004920
```

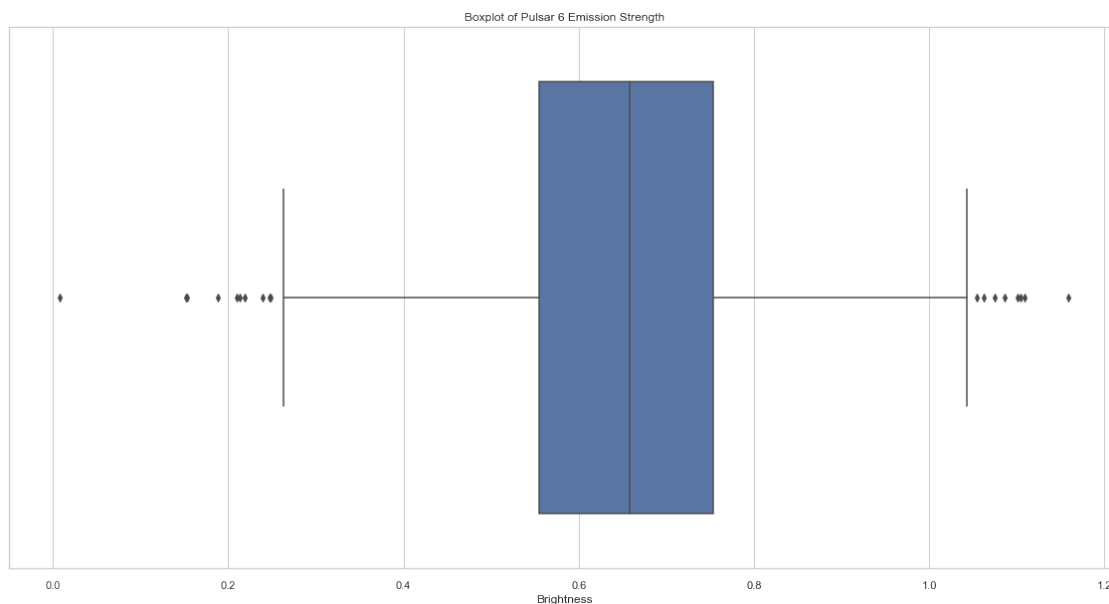
```
[ ]: pulsar6.describe()
```

```
[ ]:      Pulse Number  Brightness  Uncertainty
count      698.00000  698.000000   698.000000
mean       349.50000    0.654319    0.004445
std        201.63953    0.163945    0.001855
min         1.00000    0.007642    0.002129
25%        175.25000    0.555267    0.003086
50%        349.50000    0.658295    0.003951
75%        523.75000    0.753396    0.005349
max         698.00000    1.159334    0.016097
```

```
[ ]: pulsar6["Brightness"].describe()
```

```
[ ]: count      698.000000
mean          0.654319
std           0.163945
min           0.007642
25%           0.555267
50%           0.658295
75%           0.753396
max           1.159334
Name: Brightness, dtype: float64
```

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=pulsar6["Brightness"]).set_title("Boxplot of Pulsar 6_
↪Emission Strength")
```



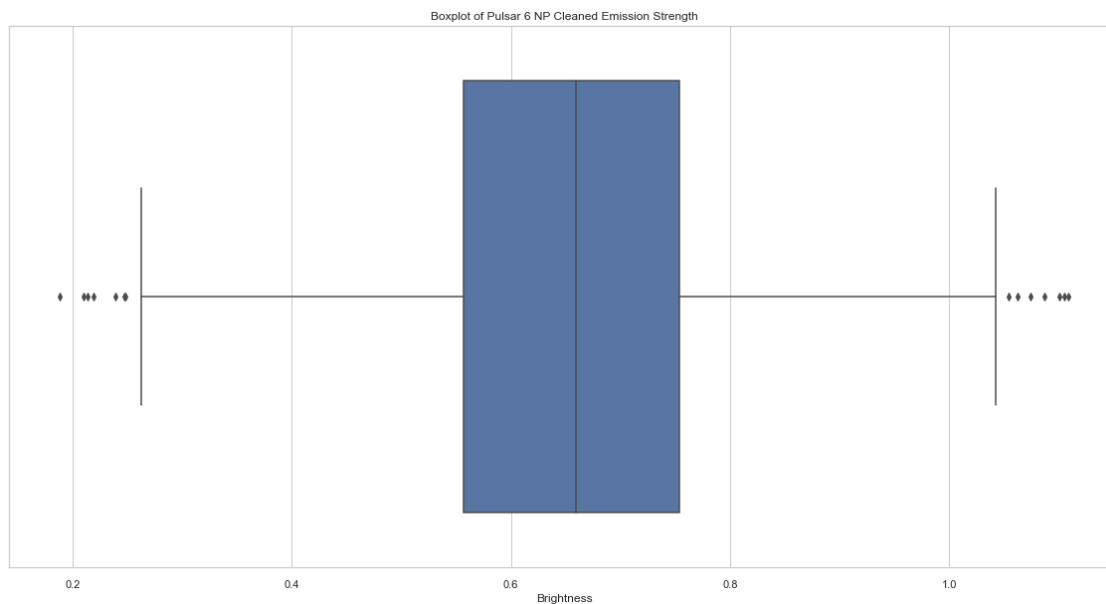
```
[ ]: #numpy method of outlier removal

pulsar6npcleaned = pulsar6[(np.abs(stats.zscore(pulsar6["Brightness"])) < 3)]
pulsar6npcleaned
```

```
[ ]:      Pulse Number  Brightness  Uncertainty
0           1      0.634671      0.002761
1           2      0.736945      0.005207
2           3      0.693834      0.002706
3           4      1.021866      0.010184
4           5      0.673845      0.006236
..          ...          ...          ...
693         694      0.776083      0.008928
694         695      0.625382      0.006018
695         696      0.647559      0.003765
696         697      0.312449      0.002901
697         698      0.548353      0.009056
```

[694 rows x 3 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=pulsar6npcleaned["Brightness"]).set_title("Boxplot of Pulsar_
→6 NP Cleaned Emission Strength")
```



```
[ ]: pulsar6npcleaned["Brightness"].describe()
```

```
[ ]: count      694.000000
      mean       0.655970
      std       0.159160
      min       0.188069
      25%       0.556461
      50%       0.658903
      75%       0.753396
      max       1.109122
      Name: Brightness, dtype: float64
```

```
[ ]: pulsar6npcleaned["Brightness"].median()
```

```
[ ]: 0.6589028
```

```
[ ]: medianpulse6 = pulsar6["Brightness"].median()
      print("Median of Pulsar6: ", medianpulse6)
      pulsar6['Binary'] = np.where(pulsar6['Brightness'] > medianpulse6, 1, 0)
```

```
Median of Pulsar6: 0.65829515
```

```
[ ]: pulsar6
```

```
[ ]:      Pulse Number  Brightness  Uncertainty  Binary
      0                1    0.634671    0.002761      0
      1                2    0.736945    0.005207      1
      2                3    0.693834    0.002706      1
      3                4    1.021866    0.010184      1
      4                5    0.673845    0.006236      1
      ..            ...         ...         ...      ...
      693            694    0.776083    0.008928      1
      694            695    0.625382    0.006018      0
      695            696    0.647559    0.003765      0
      696            697    0.312449    0.002901      0
      697            698    0.548353    0.009056      0
```

```
[698 rows x 4 columns]
```

```
[ ]: median = pulsar6npcleaned["Brightness"].median()
      print("Median of Pulsar6 np cleaned: ", median)
      pulsar6npcleaned['Binary'] = np.where(pulsar6npcleaned['Brightness'] > median, 1, 0)
```

```
Median of Pulsar6 np cleaned: 0.6589028
```

```
C:\Users\oxlay\AppData\Local\Temp\ipykernel_36516\1919336679.py:3:
```

```
SettingWithCopyWarning:
```

```
A value is trying to be set on a copy of a slice from a DataFrame.
```

Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: [https://pandas.pydata.org/pandas-docs/stable/user\\_guide/indexing.html#returning-a-view-versus-a-copy](https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

```
pulsar6npcleaned['Binary'] = np.where(pulsar6npcleaned['Brightness'] > median,
1, 0)
```

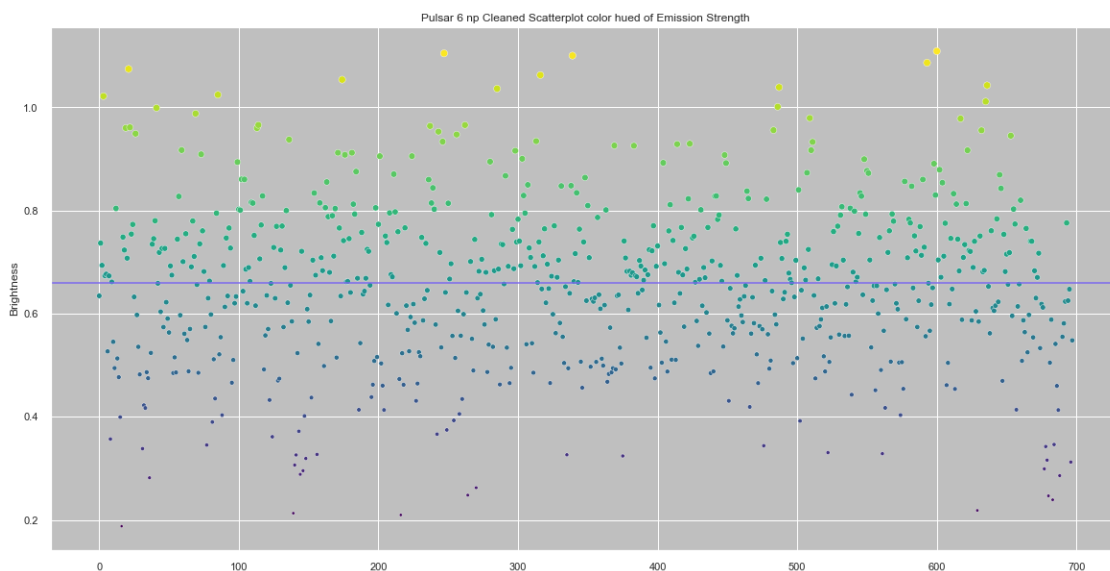
```
[ ]: pulsar6npcleaned
```

```
[ ]:
```

	Pulse Number	Brightness	Uncertainty	Binary
0	1	0.634671	0.002761	0
1	2	0.736945	0.005207	1
2	3	0.693834	0.002706	1
3	4	1.021866	0.010184	1
4	5	0.673845	0.006236	1
..	...	...	...	...
693	694	0.776083	0.008928	1
694	695	0.625382	0.006018	0
695	696	0.647559	0.003765	0
696	697	0.312449	0.002901	0
697	698	0.548353	0.009056	0

[694 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar6npcleaned.Brightness.values
ax = sns.scatterplot(data=pulsar6npcleaned["Brightness"], s= strength*50,
↪c=strength, cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned,
↪Scatterplot color hue of Emission Strength')
ax = plt.axhline( y=0.6589028, ls='-',c='mediumslateblue')
```

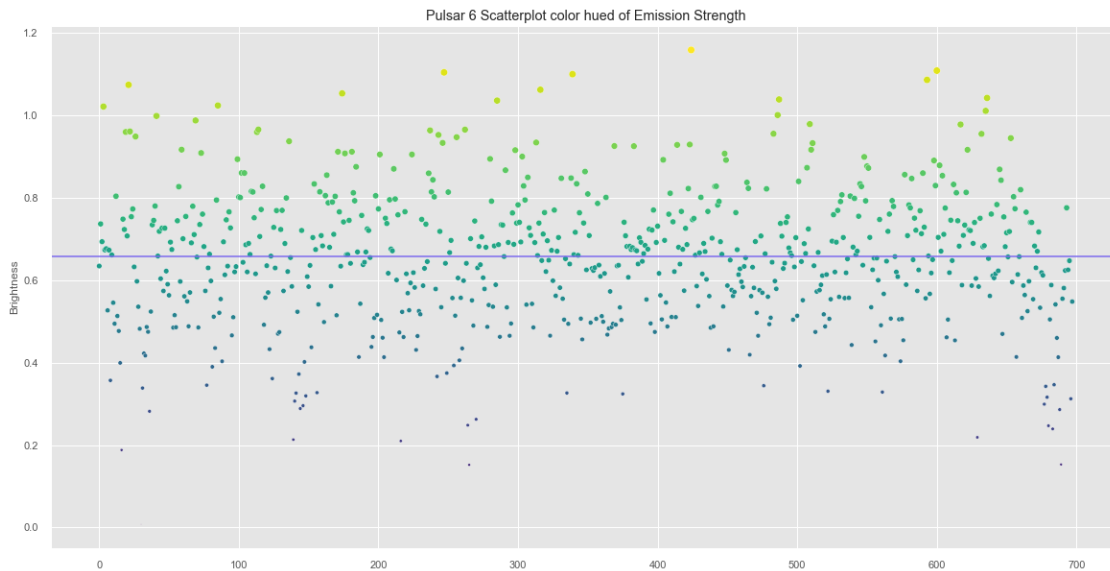


```
[ ]: print(len(pulsar6npcleaned[(pulsar6npcleaned.Brightness > 0.6589028)]))
      print(len(pulsar6npcleaned[(pulsar6npcleaned.Brightness < 0.6589028)]))
```

347

347

```
[ ]: plt.figure(figsize=(20,10))
      sns.set_style("darkgrid", {"axes.facecolor": ".75"})
      strength = pulsar6.Brightness.values
      plt.style.use('ggplot')
      ax = sns.scatterplot(data=pulsar6["Brightness"], s= strength*50, c=strength,
        ↪ cmap="viridis", marker="o").set_title('Pulsar 6 Scatterplot color hue of ↪
        ↪ Emission Strength')
      ax = plt.axhline( y=0.65829515, ls='-',c='mediumslateblue')
```



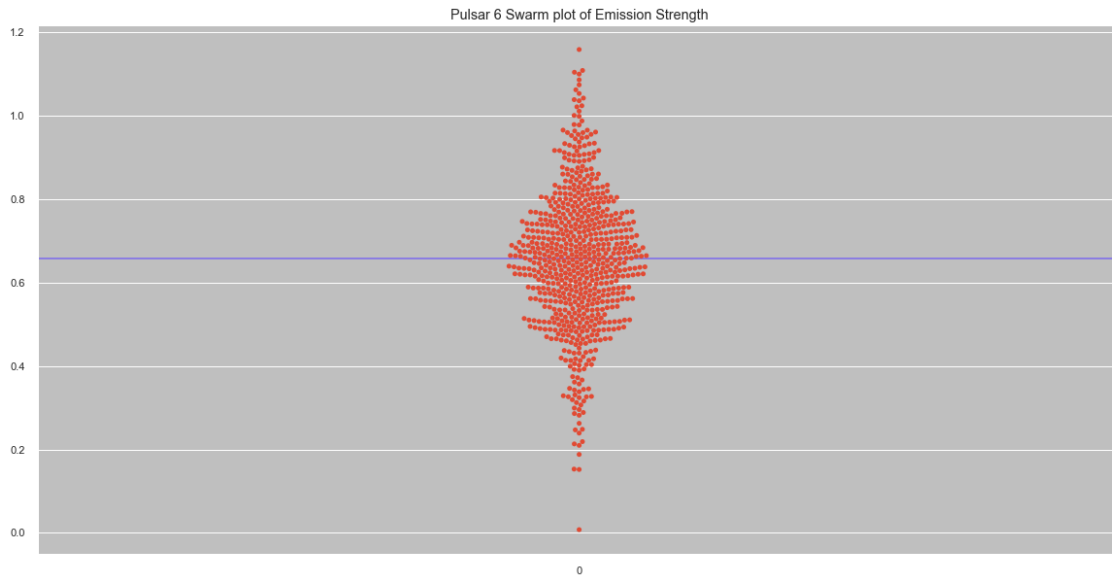
```
[ ]: print(len(pulsar6[(pulsar6.Brightness > 0.6589028)]))
      print(len(pulsar6[(pulsar6.Brightness < 0.6589028)]))
```

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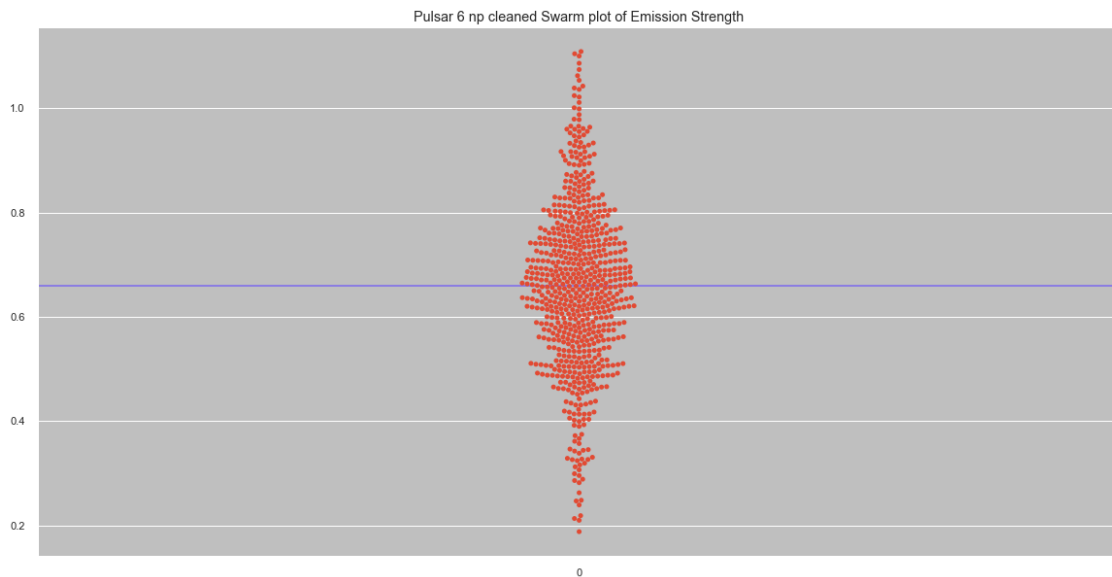
350

```
[ ]: plt.figure(figsize=(20,10))
      sns.set_style("darkgrid", {"axes.facecolor": ".75"})
      strength = pulsar6.Brightness.values
      ax = plt.axhline( y=0.65829515, ls='-',c='mediumslateblue')
```

```
ax = sns.swarmplot(data=pulsar6["Brightness"], c="blue").set_title('Pulsar 6_
↳Swarm plot of Emission Strength')
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar6npcleaned.Brightness.values
ax = sns.swarmplot(data=pulsar6npcleaned["Brightness"]).set_title('Pulsar 6 np_
↳cleaned Swarm plot of Emission Strength')
ax = plt.axhline( y=0.6589028, ls='-', c='mediumslateblue')
```



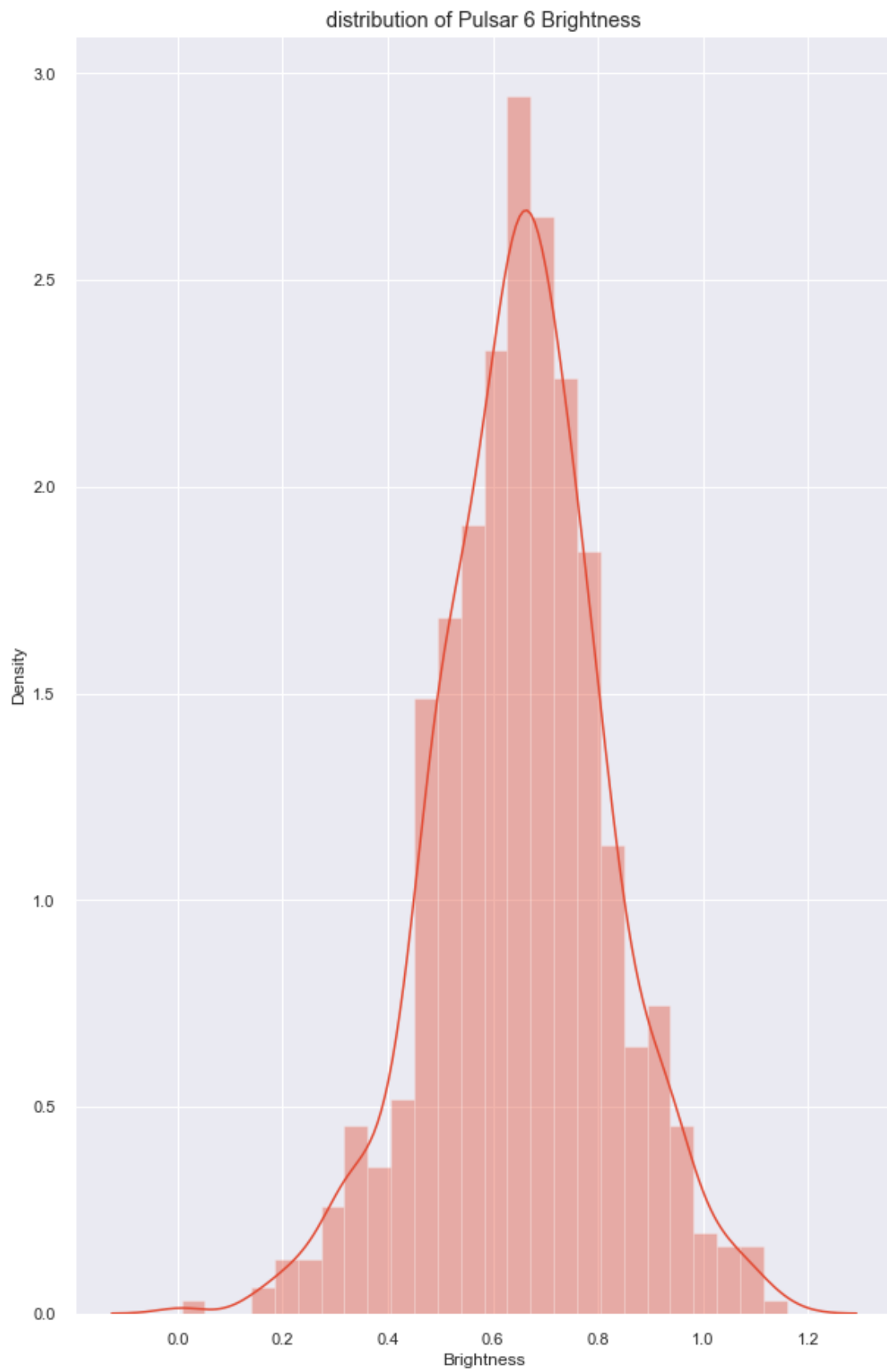


```
[ ]: plt.figure(figsize=(10, 16))
      with sns.axes_style('darkgrid'):
          sns.distplot(pulsar6.Brightness)
      plt.title("distribution of Pulsar 6 Brightness")
```

```
c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a
future version. Please adapt your code to use either `displot` (a figure-level
function with similar flexibility) or `histplot` (an axes-level function for
histograms).
```

```
warnings.warn(msg, FutureWarning)
```

```
[ ]: Text(0.5, 1.0, 'distribution of Pulsar 6 Brightness')
```

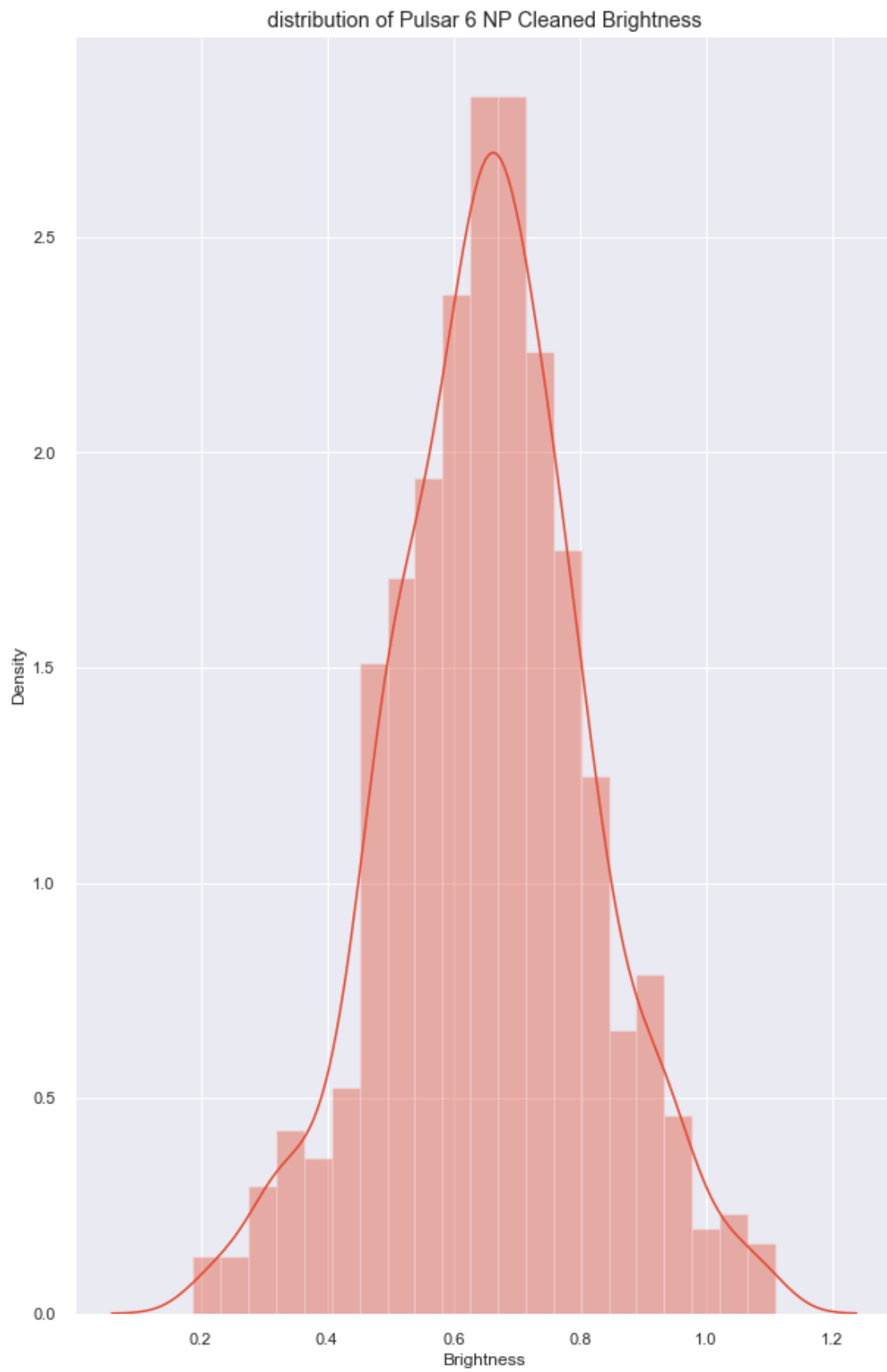


```
[ ]: plt.figure(figsize=(10, 16))
      with sns.axes_style('darkgrid'):
          sns.distplot(pulsar6npcleaned.Brightness)
      plt.title("distribution of Pulsar 6 NP Cleaned Brightness")
```

```
c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a
future version. Please adapt your code to use either `displot` (a figure-level
function with similar flexibility) or `histplot` (an axes-level function for
histograms).
```

```
warnings.warn(msg, FutureWarning)
```

```
[ ]: Text(0.5, 1.0, 'distribution of Pulsar 6 NP Cleaned Brightness')
```



```
[ ]: plt.figure(figsize=(10, 16))
      with sns.axes_style('darkgrid'):
          sns.distplot(pulsar6npcleaned.Binary)
      plt.title("distribution of Pulsar 6 NP Cleaned binary assignments")
```

```
c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a
future version. Please adapt your code to use either `displot` (a figure-level
function with similar flexibility) or `histplot` (an axes-level function for
histograms).
```

```
warnings.warn(msg, FutureWarning)
```

```
[ ]: Text(0.5, 1.0, 'distribution of Pulsar 6 NP Cleaned binary assignments')
```



```
[ ]: plt.figure(figsize=(10, 16))
      with sns.axes_style('darkgrid'):
          sns.distplot(pulsar6.Binary)
      plt.title("distribution of Pulsar 6 binary assignments")
```

```
c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a
future version. Please adapt your code to use either `displot` (a figure-level
function with similar flexibility) or `histplot` (an axes-level function for
histograms).
```

```
warnings.warn(msg, FutureWarning)
```

```
[ ]: Text(0.5, 1.0, 'distribution of Pulsar 6 binary assignments')
```





## 2 Preliminary runs test

### 2.0.1 Math Logic

$$Z = \frac{R - \tilde{R}}{s_R}$$

$$\tilde{R} = \frac{2n_1n_2}{n_1 + n_2} + 1$$

$$s_R^2 = \frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1 + n_2)^2(n_1 + n_2 - 1)}$$

link to resource: <https://www.geeksforgeeks.org/runs-test-of-randomness-in-python/>

\$ Z\_{\text{critical}} = 1.96 \$ as the confidence interval level of 95% thus this is a 2 tailed test. If the probability as corresponding to this confidence interval \$ H\_{\text{null}} \$ will be rejected as it is not statistically significant as denoted by \$ |Z| > Z\_{\text{critical}} \$

There is also code attempting to change it from a z-score probability to a P-score for ease of understanding and clarity.

## 3 FUNCTION CODE FOR RUNS TEST

```
[ ]: # MUST BE PASSED A LIST AND A INT/FLOAT

def runsTest(data, dataMedian):
    runs = 0
    above = 0
    below = 0

    for i in range(len(data)):
        if(data[i] >= dataMedian and data[i-1] < dataMedian) or (data[i] <
→dataMedian and data[i-1] >= dataMedian):
            runs += 1

        if(data[i] >= dataMedian):
            above += 1

        else:
            below += 1

    R = ((2*above*below)/(above+below))+1
```

```

    #sdevTemp = (2*above*below*(2*above*below-above-below))/
    ↳(((above+below)**2)*(above+below-1))
    #sdevTemp = (2*n1*n2*(2*n1*n2-n1-n2))/(((n1+n2)*2)*(n1+n2-1))
    Sdev = math.sqrt((2*above*below*(2*above*below-above-below))/
    ↳(((above+below)**2)*(above+below-1)))

    float(Sdev)
    float(R)
    float(runs)
    z = (runs-R)/Sdev
    return z

```

```

[ ]: binaryData1 = pulsar6['Binary'].tolist()
print("pulsar6 original: ",binaryData1)

binaryData1nooutlier = pulsar6npcleaned['Binary'].tolist()
print("\n pulsar6 original: ", binaryData1nooutlier)

```

```

pulsar6 original:  [0, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1,
1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0,
1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1,
1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1,
1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1,
0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1,
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1, 1, 1, 1, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1,
1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0,
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1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0,
0, 0, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1,
0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1,
1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0,
0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1,
0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1,
1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1,
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1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0,
0, 0, 1, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1,
1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0,
0, 0, 0]

```

```

pulsar6 original:  [0, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1,
1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0, 1,

```

```

0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1,
1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 1,
1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0,
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0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1,
1, 1, 1, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1,
1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1,
1, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0,
0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 1,
0, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1,
1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0,
0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0,
0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1,
1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1,
0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0,
0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1, 0, 0, 0,
0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1,
1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 0, 0,
0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0,
0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1,
1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 1,
1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 1,
0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1, 0, 1,
0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0]

```

```

[ ]: print("Brightness Median Test")
Zscore = abs(runsTest(binaryData1, medianpulse6))
Pval = stats.norm.sf(abs(Zscore))*2
print('Z Statistic is: ', Zscore)
print('P Value is : ', Pval)

if(Zscore >= 1.96):
    print('We reject the null Hypotheses as the Zscore greater than 1.96. Thus_
    ↳not statistically significant.')

if(Pval <= 0.05):
    print('We reject the null Hypotheses as the P-value is less than 0.05%._
    ↳Thus not statistically significant.')

print("Binary Median Test")
binarymedian1 = pulsar6["Binary"].median()

Zscore = abs(runsTest(binaryData1, binarymedian1))
Pval = stats.norm.sf(abs(Zscore))*2
print('Z Statistic is: ', Zscore)
print('P Value is : ', Pval)

```

```

if(Zscore >= 1.96):
    print('We reject the null Hypotheses as the Zscore greater than 1.96. Thus
    ↳not statistically significant.')

if(Pval <= 0.05):
    print('We reject the null Hypotheses as the P-value is less than 0.05%.
    ↳Thus not statistically significant.')

print("Removed outliers from dataset")
Zscore = abs(runsTest(binaryDataInooutlier, median))
Pval = stats.norm.sf(abs(Zscore))*2
print('Z Statistic is: ', Zscore)
print('P Value is : ', Pval)

if(Zscore >= 1.96):
    print('We reject the null Hypotheses as the Zscore greater than 1.96. Thus
    ↳not statistically significant.')

if(Pval <= 0.05):
    print('We reject the null Hypotheses as the P-value is less than 0.05%.
    ↳Thus not statistically significant.')

```

Brightness Median Test

Z Statistic is: 4.545328792576532

P Value is : 5.48495657884083e-06

We reject the null Hypotheses as the Zscore greater than 1.96. Thus not statistically significant.

We reject the null Hypotheses as the P-value is less than 0.05%. Thus not statistically significant.

Binary Median Test

Z Statistic is: 4.545328792576532

P Value is : 5.48495657884083e-06

We reject the null Hypotheses as the Zscore greater than 1.96. Thus not statistically significant.

We reject the null Hypotheses as the P-value is less than 0.05%. Thus not statistically significant.

Removed outliers from dataset

Z Statistic is: 4.558427804288349

P Value is : 5.153797471801667e-06

We reject the null Hypotheses as the Zscore greater than 1.96. Thus not statistically significant.

We reject the null Hypotheses as the P-value is less than 0.05%. Thus not statistically significant.

## 4 Analysis of the preliminary data analysis

We can see here through our printouts the value of both Z Statistic based on the above Runs Test of Randomness and the approximate correlative P-value.

If the conditional prints are not activated it means there is no statistical significance to reject the  $H_{null}$

**4.1 \$ H\_{\{null\}} \$ is where the numbers are randomly generated and sequenced**

**4.2 \$ H\_{\{alt\}} \$ is where the numbers are not randomly generated or sequenced**

Further testing can be done with more variety of datasets with pythonic libraries and R librariest such as NIST and Rrandtest (placeholders cant remember their names)

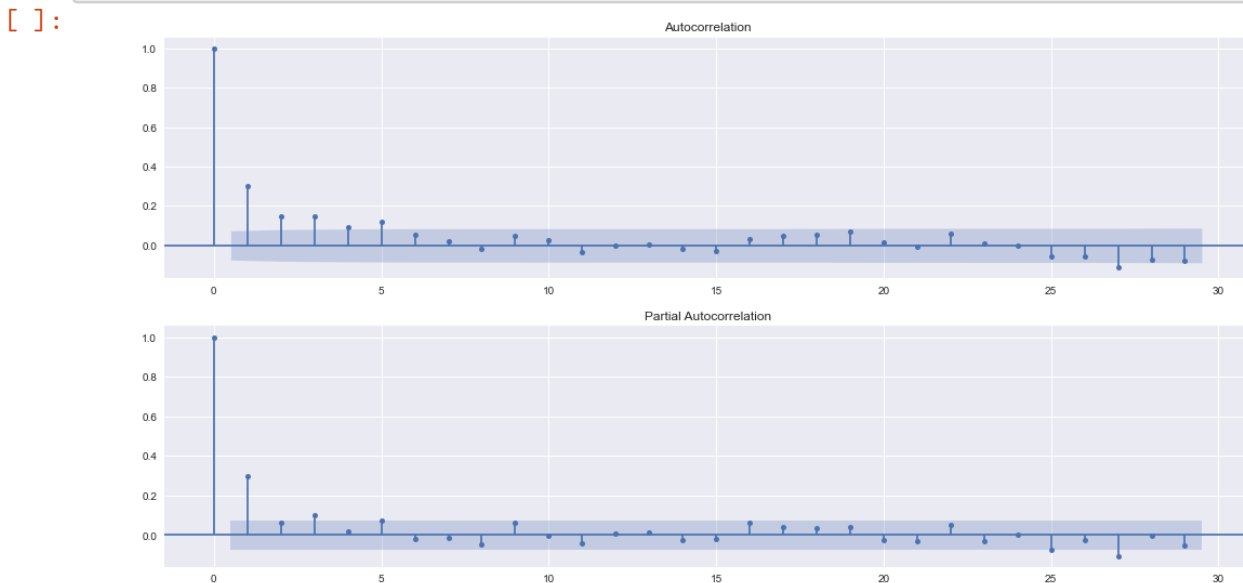
## 5 Below we begin autocorrelation and autocovariance analysis

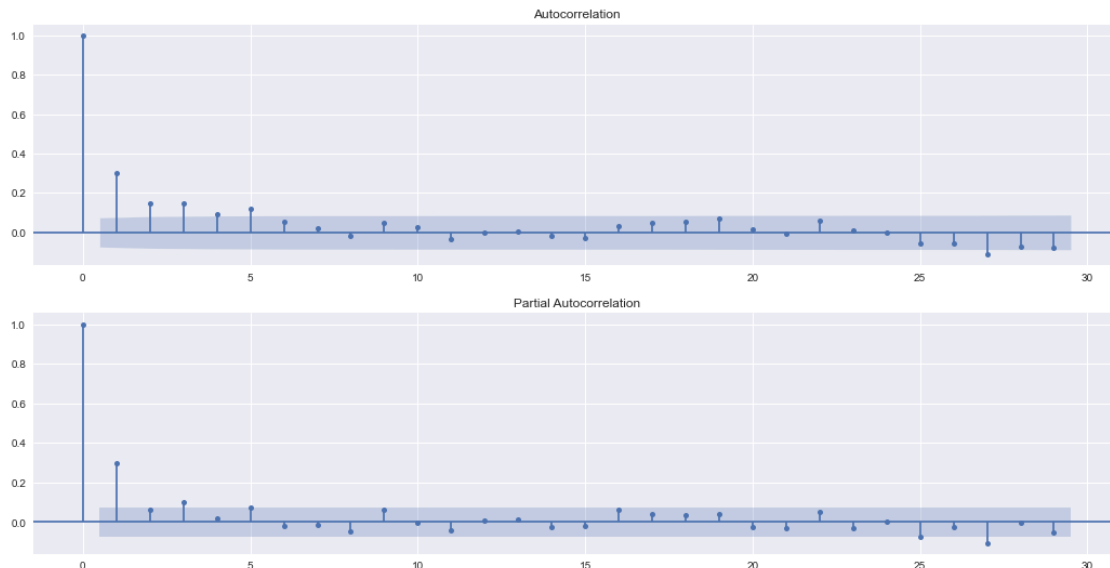
To get started with this I am playing around with guide from: <https://towardsdatascience.com/a-step-by-step-guide-to-calculating-autocorrelation-and-partial-autocorrelation-8c4342b784e8>

```
[ ]: plt.style.use("seaborn")
plt.rcParams["figure.figsize"] = (18, 9)

fig, ax = plt.subplots(2,1)

plot_acf(pulsar6['Brightness'], ax=ax[0])
plot_pacf(pulsar6['Brightness'], ax=ax[1], method="ols")
```





```
[ ]: acf(pulsar6['Brightness'], nlags=10)
```

```
c:\Users\oxlay\anaconda3\lib\site-packages\statsmodels\tsa\stattools.py:667:
FutureWarning: fft=True will become the default after the release of the 0.12
release of statsmodels. To suppress this warning, explicitly set fft=False.
warnings.warn(
```

```
[ ]: array([ 1.          ,  0.29929122,  0.14656878,  0.14948301,  0.09384681,
            0.11707783,  0.05493324,  0.02160374, -0.01711482,  0.04777   ,
            0.02563995])
```

```
[ ]: acfpulsar6 = pd.DataFrame()
for lag in range(0,11):
    acfpulsar6[f"B_lag_{lag}"] = pulsar6['Brightness'].shift(lag)
```

```
acfpulsar6
```

```
[ ]:
```

	B_lag_0	B_lag_1	B_lag_2	B_lag_3	B_lag_4	B_lag_5	B_lag_6	\
0	0.634671	NaN	NaN	NaN	NaN	NaN	NaN	
1	0.736945	0.634671	NaN	NaN	NaN	NaN	NaN	
2	0.693834	0.736945	0.634671	NaN	NaN	NaN	NaN	
3	1.021866	0.693834	0.736945	0.634671	NaN	NaN	NaN	
4	0.673845	1.021866	0.693834	0.736945	0.634671	NaN	NaN	
..	...	...	...	...	...	...	...	
693	0.776083	0.623757	0.581248	0.555266	0.152886	0.286132	0.413354	
694	0.625382	0.776083	0.623757	0.581248	0.555266	0.152886	0.286132	
695	0.647559	0.625382	0.776083	0.623757	0.581248	0.555266	0.152886	

```

696  0.312449  0.647559  0.625382  0.776083  0.623757  0.581248  0.555266
697  0.548353  0.312449  0.647559  0.625382  0.776083  0.623757  0.581248

```

```

      B_lag_7  B_lag_8  B_lag_9  B_lag_10
0         NaN         NaN         NaN         NaN
1         NaN         NaN         NaN         NaN
2         NaN         NaN         NaN         NaN
3         NaN         NaN         NaN         NaN
4         NaN         NaN         NaN         NaN
..         ...         ...         ...         ...
693  0.460095  0.541486  0.346502  0.239302
694  0.413354  0.460095  0.541486  0.346502
695  0.286132  0.413354  0.460095  0.541486
696  0.152886  0.286132  0.413354  0.460095
697  0.555266  0.152886  0.286132  0.413354

```

[698 rows x 11 columns]

```
[ ]: acfpulsar6.corr()["B_lag_0"].values
```

```
[ ]: array([ 1.          ,  0.29938402,  0.14710414,  0.15003691,  0.09455452,
            0.11800036,  0.05537751,  0.02179885, -0.01724535,  0.04863954,
            0.02621294])
```

### 5.0.1 Getting every 5th as per the auto correlation

### 5.0.2 Creating a new set of discrete 100 sets and examining them specifically

### 5.0.3 Further Random testing to move into extensive testing

#### Getting every 5th as per the auto correlation

```
[ ]: held5ths = pulsar6[pulsar6.index % 5 == 0]
      held5ths
```

```
[ ]:
      Pulse Number  Brightness  Uncertainty  Binary
0              1    0.634671    0.002761      0
5              6    0.676883    0.004763      1
10             11    0.545564    0.003835      0
15             16    0.399571    0.004712      0
20             21    0.707715    0.006011      1
..             ...         ...         ...
675            676    0.618826    0.002507      0
680            681    0.246916    0.004276      0
685            686    0.541486    0.003149      0
690            691    0.555266    0.003657      0
695            696    0.647559    0.003765      0

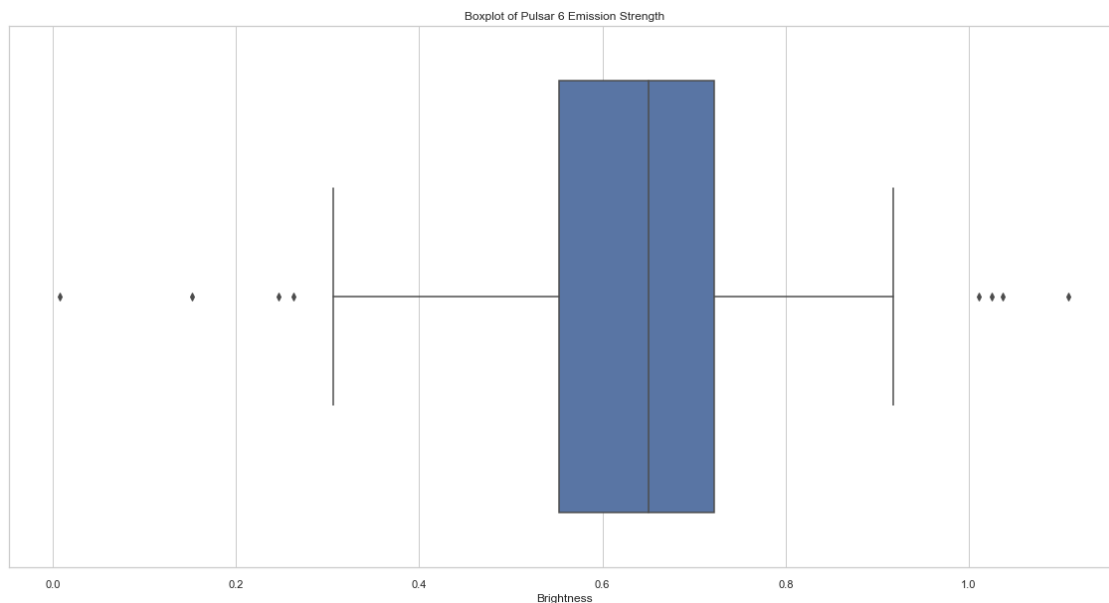
```

[140 rows x 4 columns]

```
[ ]: medianheld5ths = held5ths["Brightness"].median()
medianheld5ths
```

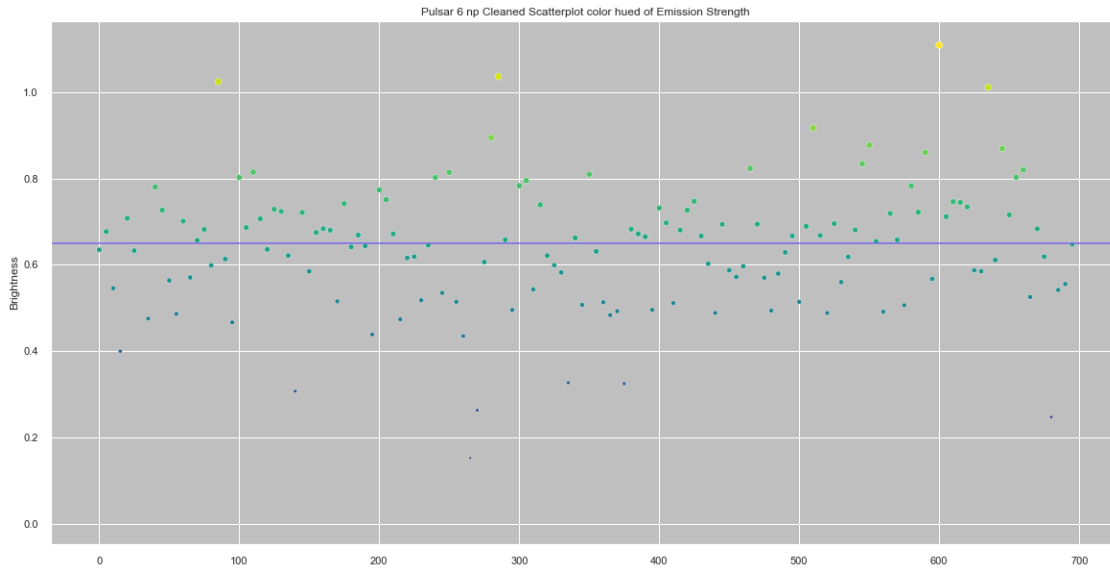
```
[ ]: 0.6508051
```

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=held5ths["Brightness"]).set_title("Boxplot of Pulsar 6_
↳Emission Strength")
```

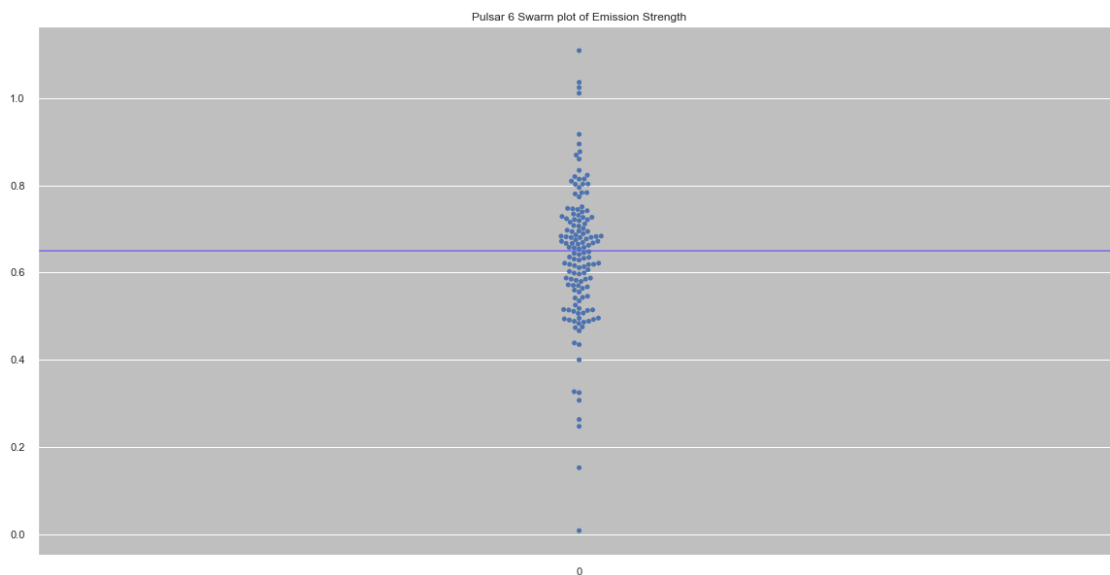


```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = sns.scatterplot(data=held5ths["Brightness"], s= strength*50, c=strength,
↳cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color_
↳hued of Emission Strength')
ax = plt.axhline( y=0.6508051, ls='-',c='mediumslateblue')
```





```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = plt.axhline( y=0.6508051, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=held5ths["Brightness"], c="blue").set_title('Pulsar 6_
↳Swarm plot of Emission Strength')
```



```
[ ]: print(len(held5ths[(held5ths.Brightness > 0.6508051)]))
print(len(held5ths[(held5ths.Brightness < 0.6508051)]))
```

70  
70

isolating every 100 rows into discrete sets.

```
[ ]: size = 100
N = int(len(pulsar6)/size)
pulsarsubframes = [pulsar6.iloc[i*size:(i+1)*size].copy() for i in range(N+1)]
#pulsarsubframes[-1]

frame1 = pulsarsubframes[0]
frame2 = pulsarsubframes[1]
frame3 = pulsarsubframes[2]
frame4 = pulsarsubframes[3]
frame5 = pulsarsubframes[4]
frame6 = pulsarsubframes[5]
frame7 = pulsarsubframes[6]

medianframe1 = frame1["Brightness"].median()
print("Median of Pulsar6: ", medianframe1)
frame1['Binary'] = np.where(frame1['Brightness'] > medianframe1, 1, 0)

medianframe2 = frame2["Brightness"].median()
print("Median of Pulsar6: ", medianframe2)
frame2['Binary'] = np.where(frame2['Brightness'] > medianframe2, 1, 0)

medianframe3 = frame3["Brightness"].median()
print("Median of Pulsar6: ", medianframe3)
frame3['Binary'] = np.where(frame3['Brightness'] > medianframe3, 1, 0)

medianframe4 = frame4["Brightness"].median()
print("Median of Pulsar6: ", medianframe4)
frame4['Binary'] = np.where(frame4['Brightness'] > medianframe4, 1, 0)

medianframe5 = frame5["Brightness"].median()
print("Median of Pulsar6: ", medianframe5)
frame5['Binary'] = np.where(frame5['Brightness'] > medianframe5, 1, 0)

medianframe6 = frame6["Brightness"].median()
print("Median of Pulsar6: ", medianframe6)
frame6['Binary'] = np.where(frame6['Brightness'] > medianframe6, 1, 0)

medianframe7 = frame7["Brightness"].median()
print("Median of Pulsar6: ", medianframe7)
frame7['Binary'] = np.where(frame7['Brightness'] > medianframe7, 1, 0)
```

Median of Pulsar6: 0.63457545  
Median of Pulsar6: 0.6688056  
Median of Pulsar6: 0.63955675

```

Median of Pulsar6:  0.66777675
Median of Pulsar6:  0.6605900499999999
Median of Pulsar6:  0.65585835
Median of Pulsar6:  0.6504474499999999

```

```
[ ]: framebinary = []
```

```
[ ]: print(frame1)

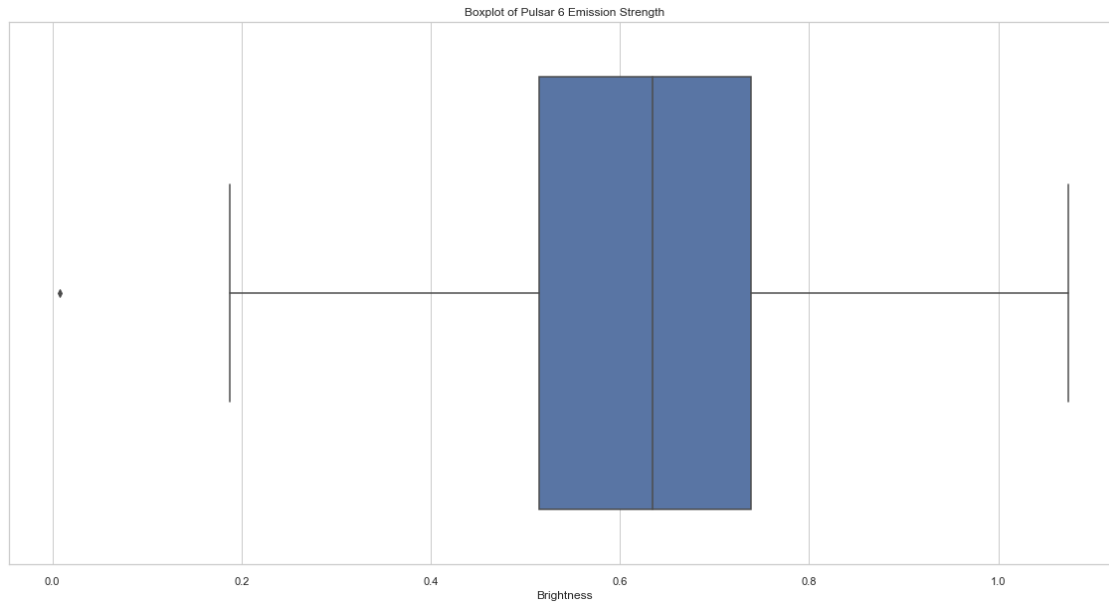
storeover1 = len(frame1[(frame1.Brightness > frame1["Brightness"].median())])
storeunder1 = len(frame1[(frame1.Brightness < frame1["Brightness"].median())])

if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

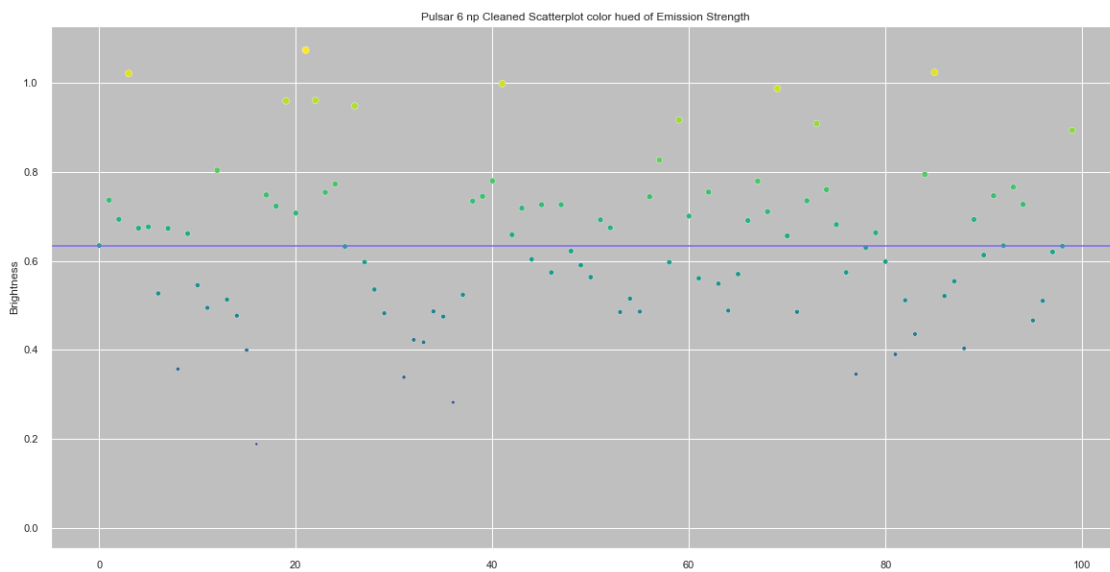
	Pulse Number	Brightness	Uncertainty	Binary
0	1	0.634671	0.002761	1
1	2	0.736945	0.005207	1
2	3	0.693834	0.002706	1
3	4	1.021866	0.010184	1
4	5	0.673845	0.006236	1
..	...	...	...	...
95	96	0.466249	0.002850	0
96	97	0.510350	0.003131	0
97	98	0.620342	0.004379	0
98	99	0.633366	0.005906	0
99	100	0.894052	0.008207	1

```
[100 rows x 4 columns]
```

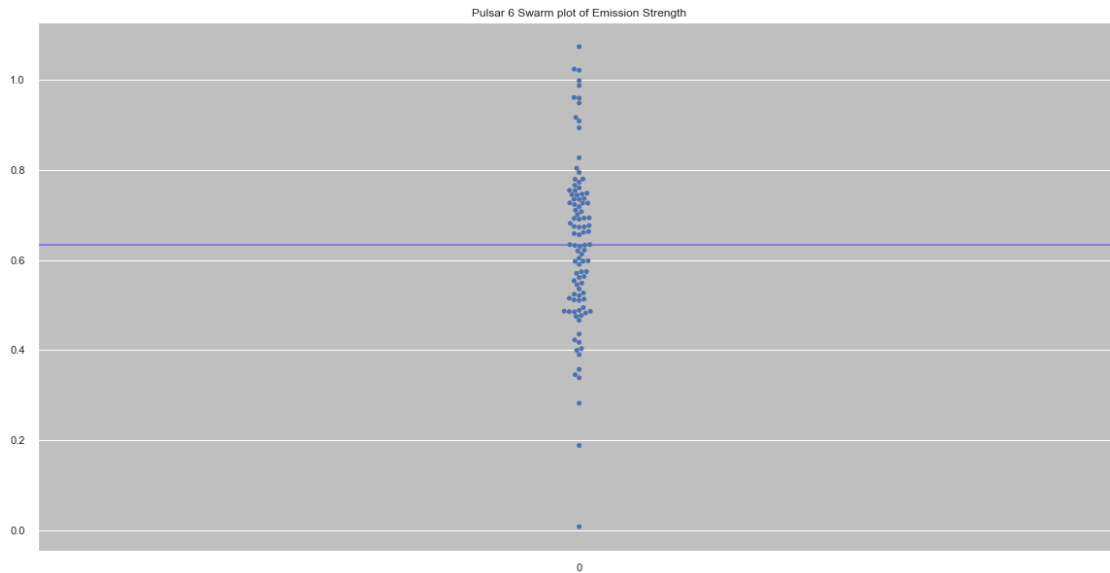
```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=frame1["Brightness"]).set_title("Boxplot of Pulsar 6_
↪Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame1.Brightness.values
ax = sns.scatterplot(data=frame1["Brightness"], s= strength*50, c=strength,
                    cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color
                    hue of Emission Strength')
ax = plt.axhline( y=0.63457545, ls='-',c='mediumslateblue')
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame1.Brightness.values
ax = plt.axhline( y=0.63457545, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=frame1["Brightness"], c="blue").set_title('Pulsar 6_
↳Swarm plot of Emission Strength')
```



```
[ ]: print(frame2)

storeover1 = len(frame2[(frame2.Brightness > frame2["Brightness"].median())])
storeunder1 = len(frame2[(frame2.Brightness < frame2["Brightness"].median())])

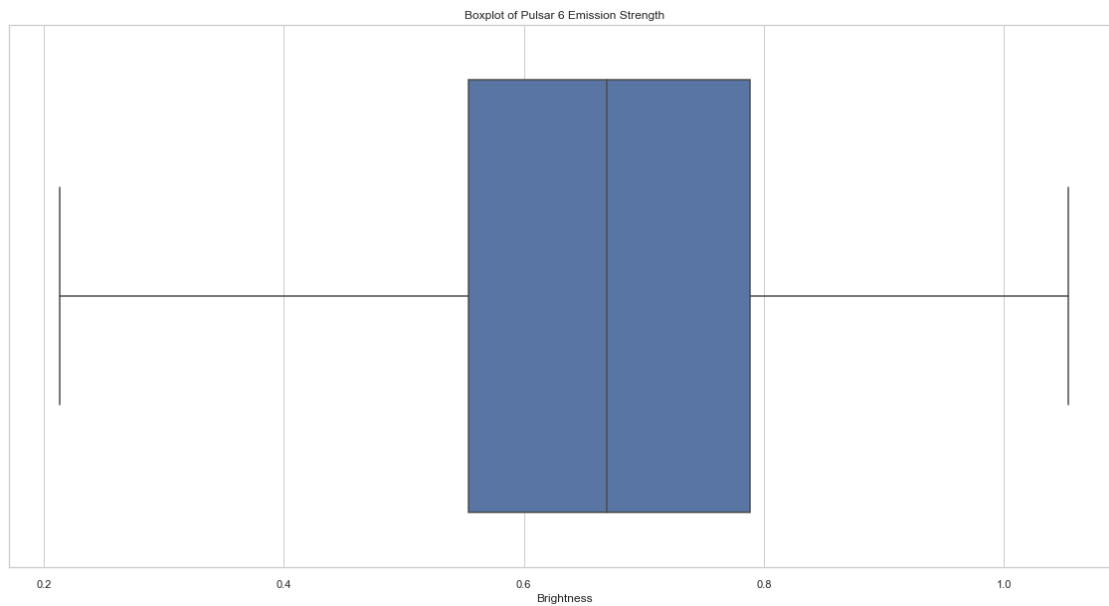
if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

	Pulse Number	Brightness	Uncertainty	Binary
100	101	0.802381	0.004107	1
101	102	0.800921	0.002385	1
102	103	0.860724	0.002700	1
103	104	0.643710	0.002618	0
104	105	0.860529	0.002837	1
..	...	...	...	...
195	196	0.438406	0.003504	0
196	197	0.462477	0.003358	0
197	198	0.508498	0.002759	0
198	199	0.805315	0.005269	1

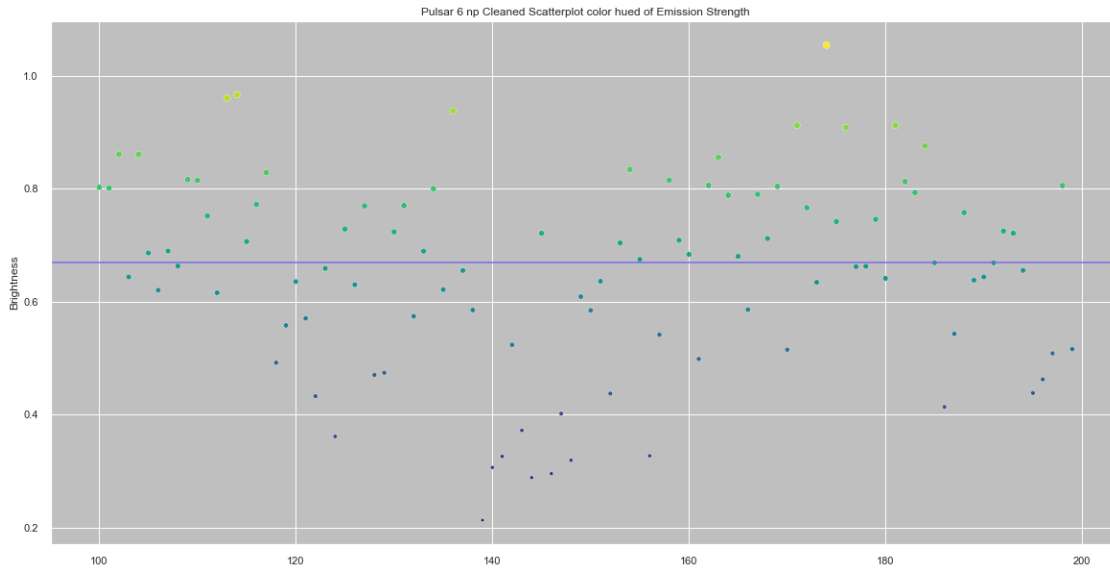
199                      200      0.516107      0.004522      0

[100 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=frame2["Brightness"]).set_title("Boxplot of Pulsar 6_
↳Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame2.Brightness.values
ax = sns.scatterplot(data=frame2["Brightness"], s= strength*50, c=strength,
↳cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color_
↳hued of Emission Strength')
ax = plt.axhline( y=0.6688056, ls='-',c='mediumslateblue')
```



```
[ ]: print(frame3)

storeover1 = len(frame3[(frame3.Brightness > frame3["Brightness"].median())])
storeunder1 = len(frame3[(frame3.Brightness < frame3["Brightness"].median())])

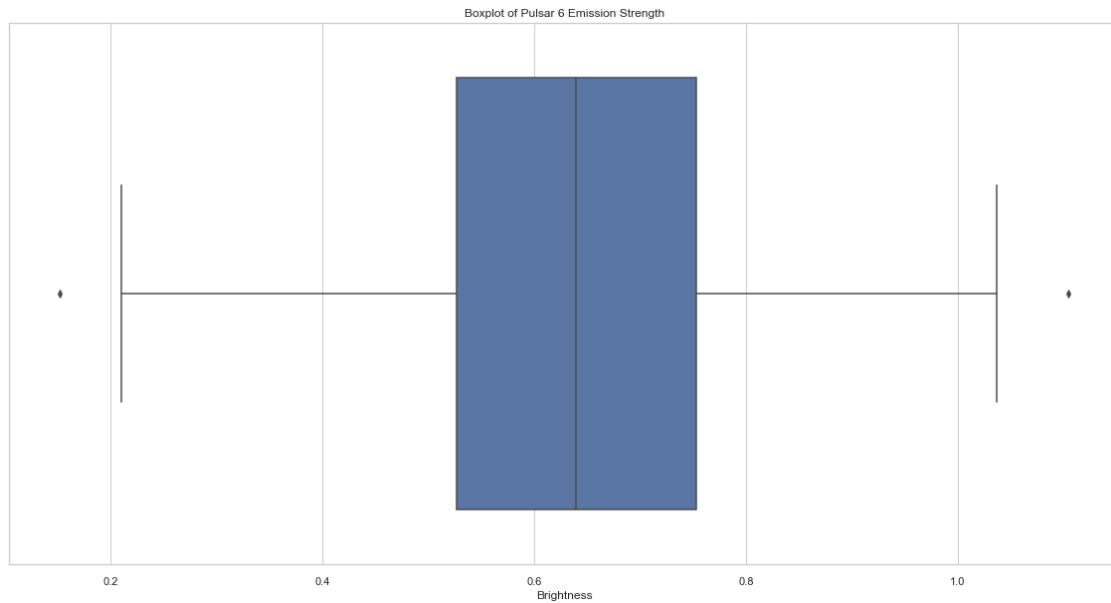
if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

	Pulse Number	Brightness	Uncertainty	Binary
200	201	0.773417	0.005146	1
201	202	0.905517	0.010704	1
202	203	0.503725	0.004764	0
203	204	0.460606	0.004345	0
204	205	0.413456	0.003170	0
..	...	...	...	...
295	296	0.495127	0.002502	0
296	297	0.763535	0.003293	1
297	298	0.687345	0.002819	1
298	299	0.915965	0.003761	1
299	300	0.739067	0.003667	1

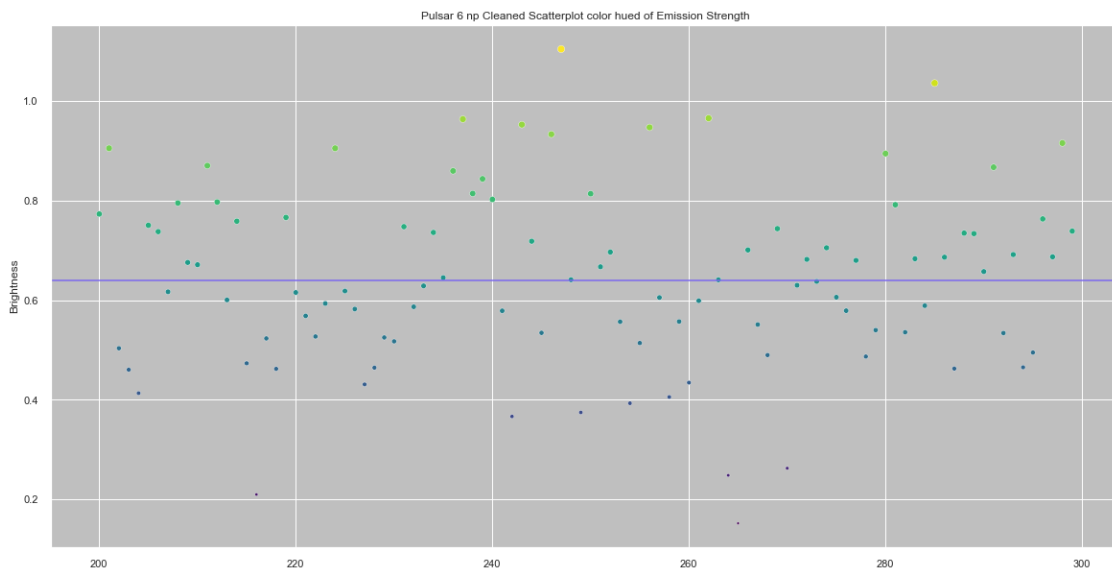
[100 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
```

```
ax = sns.boxplot(x=frame3["Brightness"]).set_title("Boxplot of Pulsar 6  
→Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame3.Brightness.values
ax = sns.scatterplot(data=frame3["Brightness"], s= strength*50, c=strength,
→cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color
→hued of Emission Strength')
ax = plt.axhline( y=0.63955675, ls='-',c='mediumslateblue')
```





```
[ ]: print(frame4)

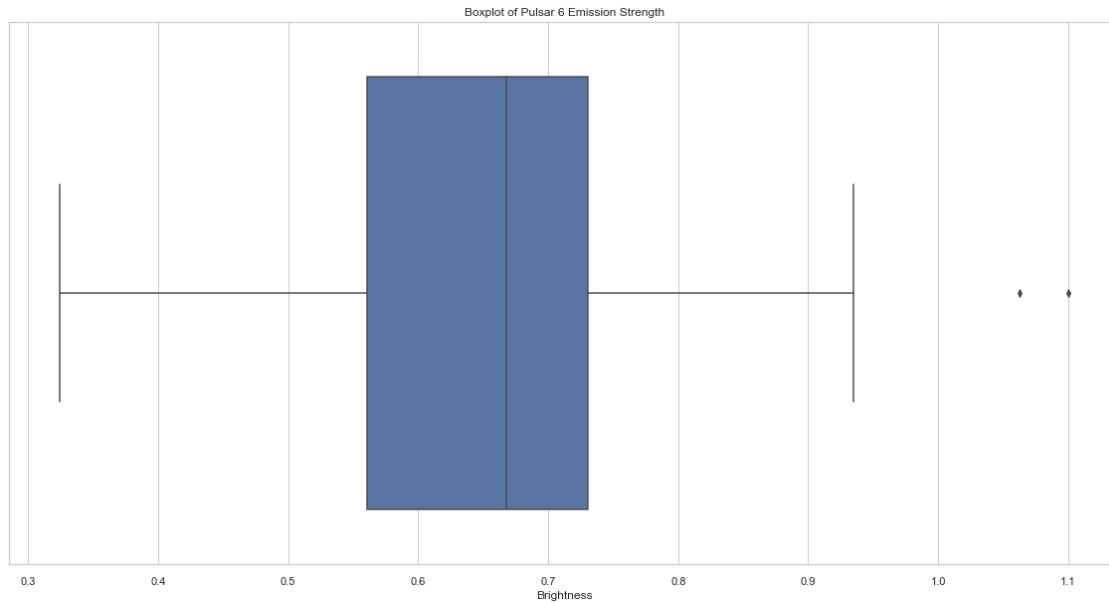
storeover1 = len(frame4[(frame4.Brightness > frame4["Brightness"].median())])
storeunder1 = len(frame4[(frame4.Brightness < frame4["Brightness"].median())])

if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

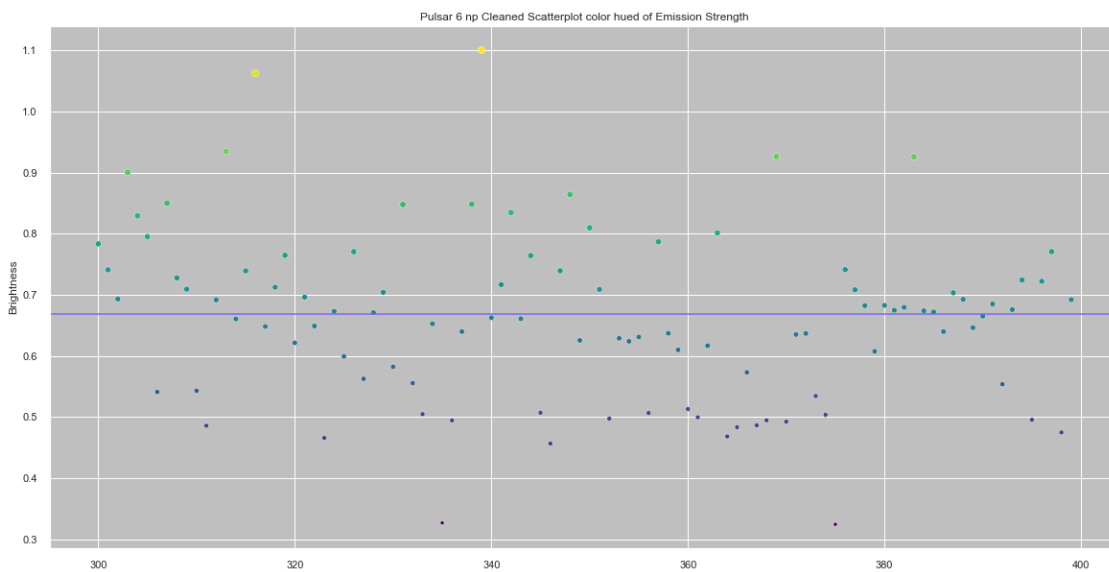
	Pulse Number	Brightness	Uncertainty	Binary
300	301	0.783253	0.003680	1
301	302	0.740742	0.007375	1
302	303	0.693110	0.002601	1
303	304	0.900445	0.003646	1
304	305	0.829165	0.002535	1
..	...	...	...	...
395	396	0.495397	0.003248	0
396	397	0.722009	0.008103	1
397	398	0.770565	0.008383	1
398	399	0.474685	0.004108	0
399	400	0.691962	0.004132	1

[100 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=frame4["Brightness"]).set_title("Boxplot of Pulsar 6_
↳Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame4.Brightness.values
ax = sns.scatterplot(data=frame4["Brightness"], s= strength*50, c=strength,
                    cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color
                    ↳hued of Emission Strength')
ax = plt.axhline( y=0.66777675, ls='-',c='mediumslateblue')
```



```
[ ]: print(frame5)

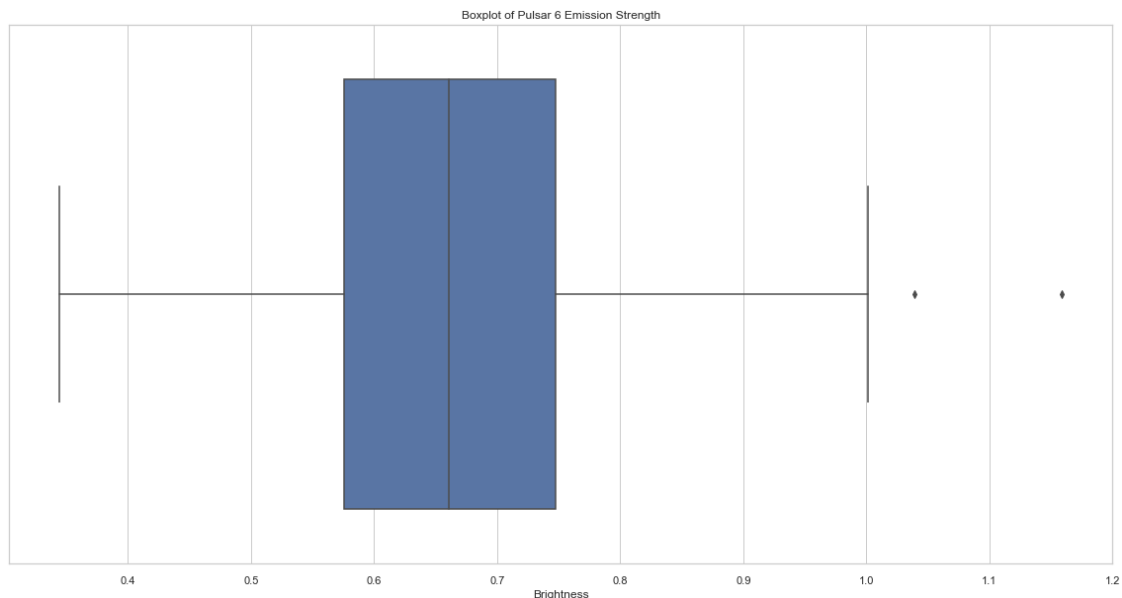
storeover1 = len(frame5[(frame5.Brightness > frame5["Brightness"].median())])
storeunder1 = len(frame5[(frame5.Brightness < frame5["Brightness"].median())])

if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

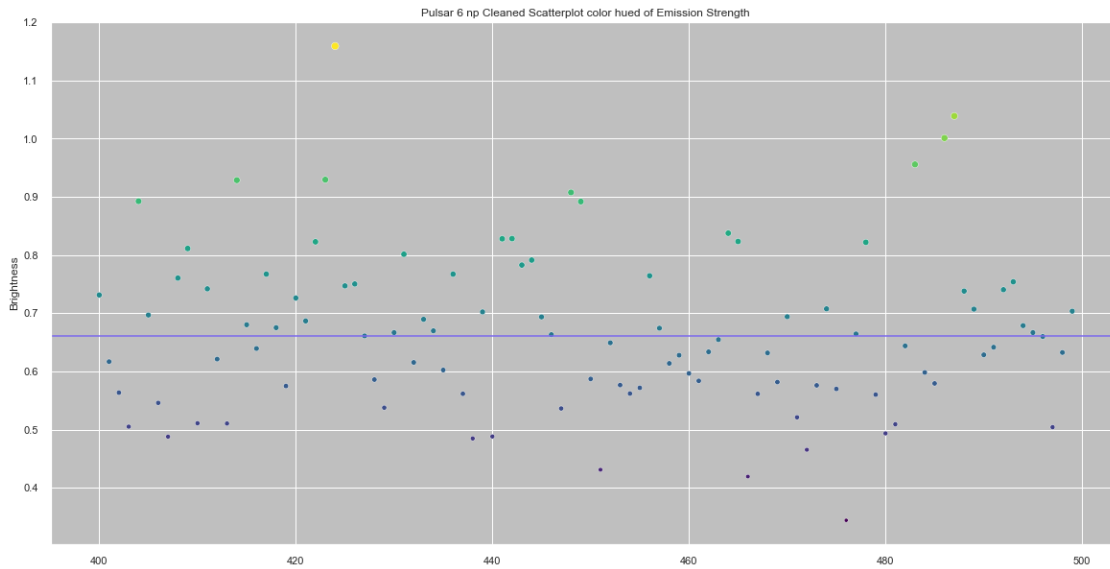
	Pulse Number	Brightness	Uncertainty	Binary
400	401	0.731438	0.002577	1
401	402	0.616883	0.002681	0
402	403	0.563571	0.002874	0
403	404	0.505136	0.002388	0
404	405	0.892605	0.007379	1
..	...	...	...	...
495	496	0.666784	0.005140	1
496	497	0.660054	0.005132	0
497	498	0.504216	0.003277	0
498	499	0.632565	0.005493	0
499	500	0.703630	0.005492	1

[100 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=frame5["Brightness"]).set_title("Boxplot of Pulsar 6_
↪Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame5.Brightness.values
ax = sns.scatterplot(data=frame5["Brightness"], s= strength*50, c=strength,
    cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color
    hue of Emission Strength')
ax = plt.axhline( y=0.6605900499999999, ls='-',c='mediumslateblue')
```



```
[ ]: print(frame6)

storeover1 = len(frame6[(frame6.Brightness > frame6["Brightness"].median())])
storeunder1 = len(frame6[(frame6.Brightness < frame6["Brightness"].median())])

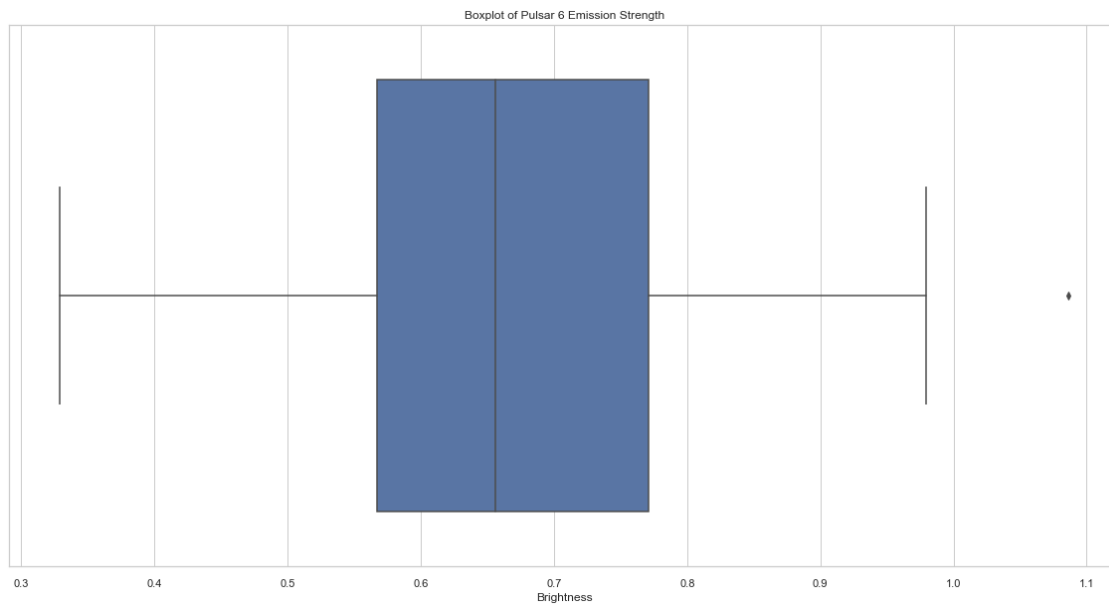
if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

	Pulse Number	Brightness	Uncertainty	Binary
500	501	0.513902	0.002946	0
501	502	0.840158	0.003412	1
502	503	0.392136	0.002529	0
503	504	0.645563	0.004307	0
504	505	0.551735	0.003081	0
..	...	...	...	...
595	596	0.567053	0.002552	0
596	597	0.617711	0.003246	0

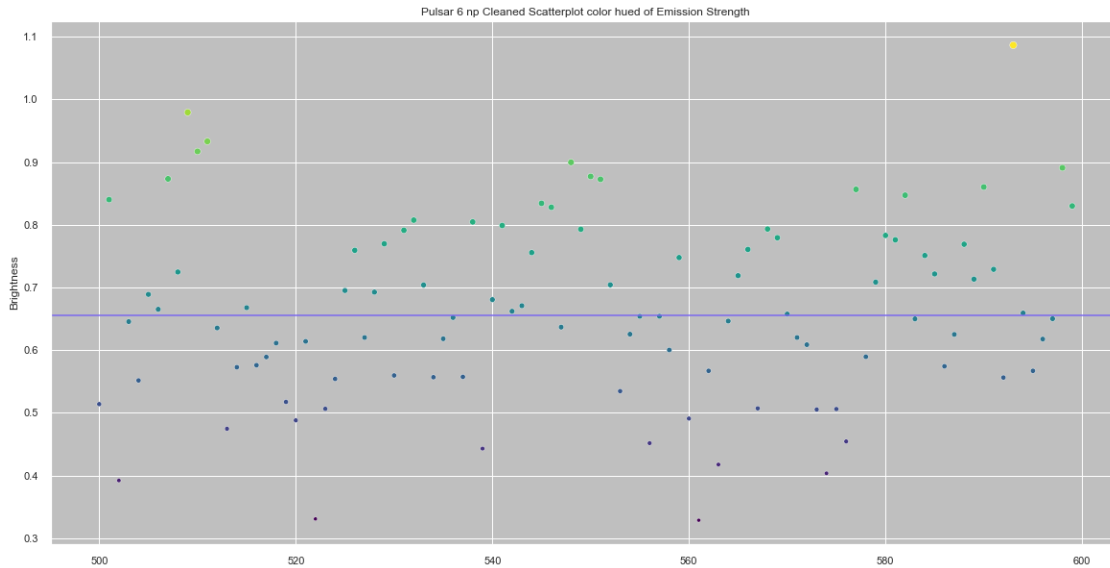
597	598	0.650200	0.002647	0
598	599	0.890907	0.004037	1
599	600	0.830011	0.003572	1

[100 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=frame6["Brightness"]).set_title("Boxplot of Pulsar 6_
↪Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame6.Brightness.values
ax = sns.scatterplot(data=frame6["Brightness"], s= strength*50, c=strength,
↪cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color_
↪hued of Emission Strength')
ax = plt.axhline( y=0.65585835, ls='-',c='mediumslateblue')
```



```
[ ]: print(frame7)

storeover1 = len(frame7[(frame7.Brightness > frame7["Brightness"].median())])
storeunder1 = len(frame7[(frame7.Brightness < frame7["Brightness"].median())])

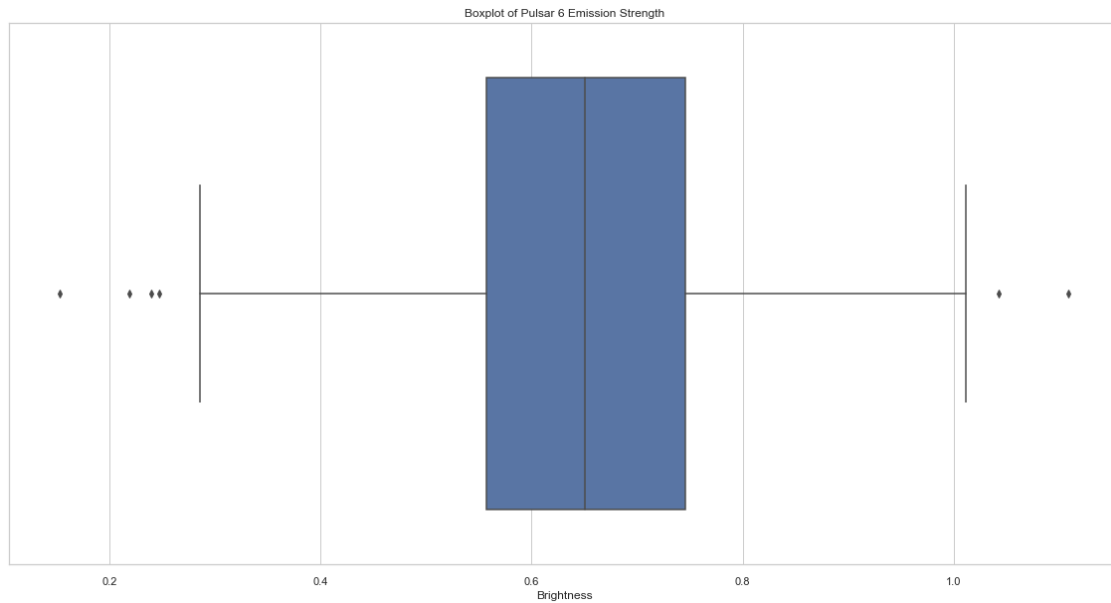
if (storeover1 > storeunder1):
    framebinary.append(1)
else:
    framebinary.append(0)
```

	Pulse Number	Brightness	Uncertainty	Binary
600	601	1.109122	0.003188	1
601	602	0.704272	0.002793	1
602	603	0.879200	0.003600	1
603	604	0.670774	0.002567	1
604	605	0.854064	0.005940	1
..	...	...	...	...
693	694	0.776083	0.008928	1
694	695	0.625382	0.006018	0
695	696	0.647559	0.003765	0
696	697	0.312449	0.002901	0
697	698	0.548353	0.009056	0

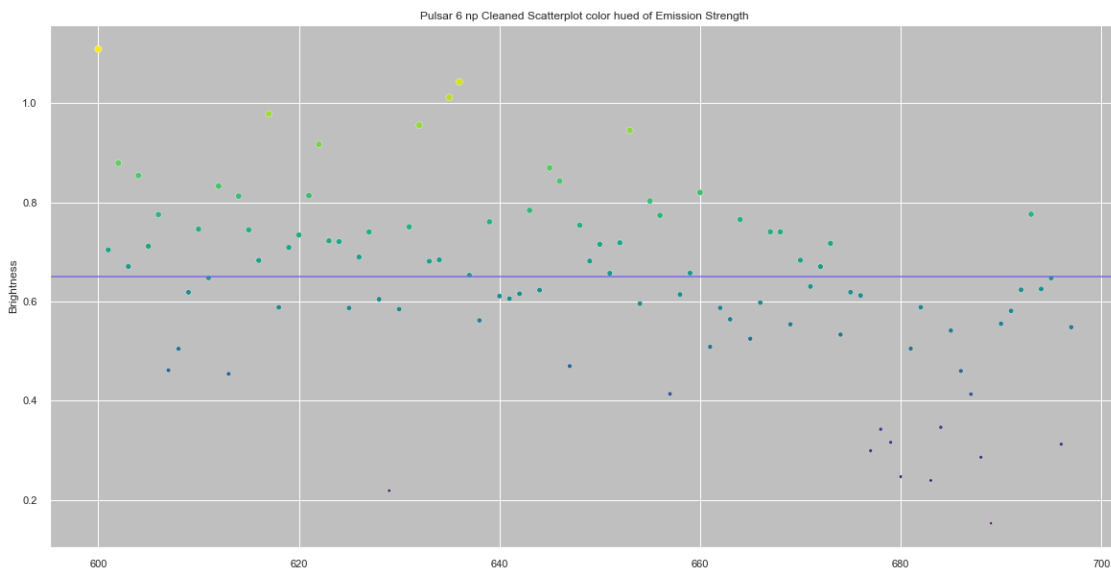
[98 rows x 4 columns]

```
[ ]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
```

```
ax = sns.boxplot(x=frame7["Brightness"]).set_title("Boxplot of Pulsar 6  
→Emission Strength")
```



```
[ ]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = frame7.Brightness.values
ax = sns.scatterplot(data=frame7["Brightness"], s= strength*50, c=strength,
→cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color
→hued of Emission Strength')
ax = plt.axhline( y=0.6504474499999999, ls='-',c='mediumslateblue')
```



```
[ ]: framebinary  
    #this didn't go to plan.
```

```
[ ]: [0, 0, 0, 0, 0, 0, 0]
```

### Randomness testing

```
[ ]:
```

```
[ ]:
```

```
[ ]:
```