pulsar3

October 8, 2022

- 1 Pulsar Emission Data Analysis
- 2 All Imports that may or may not be needed and used for the notebook

```
[]: #currently including any and all Imports that maybe needed for the project.
     import pandas as pd
     import numpy as np
     import seaborn as sns
     import matplotlib.pyplot as plt
     %matplotlib inline
     from sklearn.model_selection import train_test_split
     from sklearn import linear_model
     from sklearn.metrics import r2_score, mean_squared_error
     from sklearn.linear_model import LogisticRegression, LinearRegression
     from sklearn.metrics import confusion_matrix, accuracy_score
     from sklearn.feature_selection import RFE
     import datetime as dt
     from sklearn.cluster import KMeans
     from sklearn.metrics import pairwise_distances
     from scipy.cluster.hierarchy import linkage, dendrogram, cut_tree
     from scipy.spatial.distance import pdist
     from sklearn.feature extraction.text import TfidfVectorizer
     import matplotlib.dates as mdates
     from scipy.stats import pearsonr
     from scipy import stats
     import statistics
     import math
     from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
     from statsmodels.tsa.stattools import acf, pacf
     from statsmodels.tsa.tsatools import lagmat
     from numpy import array
     from sklearn.model_selection import train_test_split
     from keras.models import Sequential
     from keras.layers import LSTM
     from keras.layers import Dense
     from keras.layers import Bidirectional
```

3 Section for extracting from a tar file.

Currently implemented for original TAR File structure.

```
[]: #This is also found in the main file under tarunzip.py
import tarfile
import os
import sys

#tar = tarfile.open("pulseTarFile.tar")
#tar.extractall('./Data')
#tar.close()
```

3.1 Beginning of Exploration

3.1.1 Examining the data

In this section we are determining the total integrity of the data to determine if further comprehensive data cleaning and uniforming processes are needed.

```
[]: colnames = ['Pulse Number', 'Brightness', 'Uncertainty']

pulsar = pd.read_csv("Data/J0835-4510.pulses", sep = ' ', header = None, names

→= colnames)
```

```
[]: pulsar.shape
```

[]: (1331, 3)

```
[]: pulsar.head(25)
```

```
[]:
         Pulse Number
                         Brightness
                                      Uncertainty
                           0.984043
                                         0.053831
     0
                      1
                      2
                           2.487928
                                         0.048796
     1
     2
                      3
                           1.690295
                                         0.025639
     3
                      4
                           1.196142
                                         0.039539
                      5
     4
                           1.979783
                                         0.041460
     5
                      6
                           2.297645
                                         0.054210
     6
                      7
                           2.322135
                                         0.043554
     7
                      8
                           2.289047
                                         0.049957
     8
                      9
                           2.442574
                                         0.025110
     9
                    10
                           2.136332
                                         0.022712
                                         0.037551
     10
                    11
                           1.976790
     11
                    12
                           2.445764
                                         0.047004
     12
                    13
                           1.937017
                                         0.028561
     13
                    14
                           2.315184
                                         0.045216
     14
                    15
                           2.584888
                                         0.040232
     15
                    16
                                         0.030372
                           1.581452
     16
                    17
                           1.849656
                                         0.024236
     17
                                         0.048330
                    18
                           2.529834
     18
                    19
                           2.894401
                                         0.066794
```

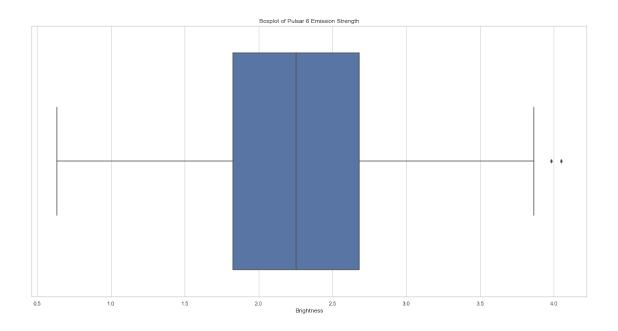
```
20
                   21
                          1.824490
                                       0.036531
     21
                   22
                         1.498133
                                       0.035557
     22
                   23
                          2.005834
                                       0.028621
     23
                   24
                          2.594836
                                       0.032925
     24
                   25
                          2.745045
                                       0.055348
    pulsar.describe()
                            Brightness
                                        Uncertainty
[]:
            Pulse Number
     count
             1331.000000
                          1331.000000
                                        1331.000000
     mean
              666.000000
                              2.248107
                                           0.039495
     std
              384.370915
                              0.591161
                                           0.013056
    min
                1.000000
                              0.633413
                                           0.012888
     25%
              333.500000
                              1.825375
                                           0.030223
     50%
              666.000000
                              2.255182
                                           0.037513
     75%
              998.500000
                              2.682259
                                           0.046771
                              4.050718
     max
             1331.000000
                                           0.098902
[]: nullBoolBrightness = pd.isnull(pulsar["Brightness"])
     pulsar[nullBoolBrightness]
[]: Empty DataFrame
     Columns: [Pulse Number, Brightness, Uncertainty]
     Index: []
[]: pulsar["Brightness"].describe()
[]: count
              1331.000000
     mean
                 2.248107
     std
                 0.591161
    min
                 0.633413
     25%
                 1.825375
     50%
                 2.255182
     75%
                 2.682259
                 4.050718
    max
     Name: Brightness, dtype: float64
[]: plt.figure(figsize=(20,10))
     sns.set_theme(style="whitegrid")
     ax = sns.boxplot(x=pulsar["Brightness"]).set_title("Boxplot of Pulsar 6")
      →Emission Strength")
```

0.059082

19

20

2.769474



```
[]: medianpulse6 = pulsar["Brightness"].median()
    print("Median of Pulsar6: ", medianpulse6)
    pulsar['Binary'] = np.where(pulsar['Brightness'] > medianpulse6, 1, 0)
```

Median of Pulsar6: 2.255182

[]: pulsar

Pulse Number	${ t Brightness}$	${\tt Uncertainty}$	Binary
1	0.984043	0.053831	0
2	2.487928	0.048796	1
3	1.690295	0.025639	0
4	1.196142	0.039539	0
5	1.979783	0.041460	0
•••	•••		
1327	1.842016	0.028216	0
1328	1.547695	0.024030	0
1329	2.797312	0.035090	1
1330	3.351977	0.052178	1
1331	3.115255	0.035134	1
	1 2 3 4 5 1327 1328 1329 1330	1 0.984043 2 2.487928 3 1.690295 4 1.196142 5 1.979783 1327 1.842016 1328 1.547695 1329 2.797312 1330 3.351977	1 0.984043 0.053831 2 2.487928 0.048796 3 1.690295 0.025639 4 1.196142 0.039539 5 1.979783 0.041460 1327 1.842016 0.028216 1328 1.547695 0.024030 1329 2.797312 0.035090 1330 3.351977 0.052178

[1331 rows x 4 columns]

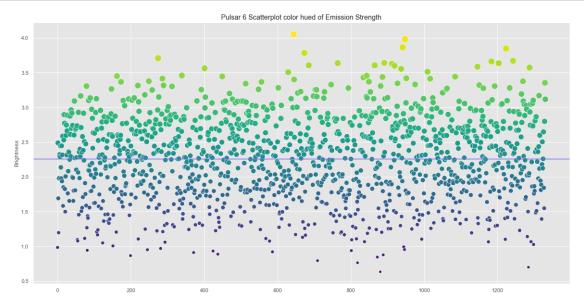
```
[]: plt.figure(figsize=(20,10))
    sns.set_style("darkgrid", {"axes.facecolor": ".75"})
    strength = pulsar.Brightness.values
    plt.style.use('ggplot')
```

```
ax = sns.scatterplot(data=pulsar["Brightness"], s= strength*50, c=strength, 

⇒cmap="viridis", marker="o").set_title('Pulsar 6 Scatterplot color hued of 

⇒Emission Strength')

ax= plt.axhline( y=2.255182, ls='-',c='mediumslateblue')
```

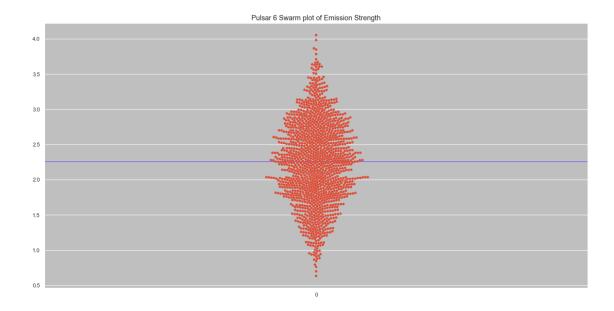


```
[]: print(len(pulsar[(pulsar.Brightness > 2.255182)]))
print(len(pulsar[(pulsar.Brightness < 2.255182)]))
```

665 665

```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar.Brightness.values
ax = plt.axhline( y=2.255182, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=pulsar["Brightness"], c="blue").set_title('Pulsar 6

→Swarm plot of Emission Strength')
```

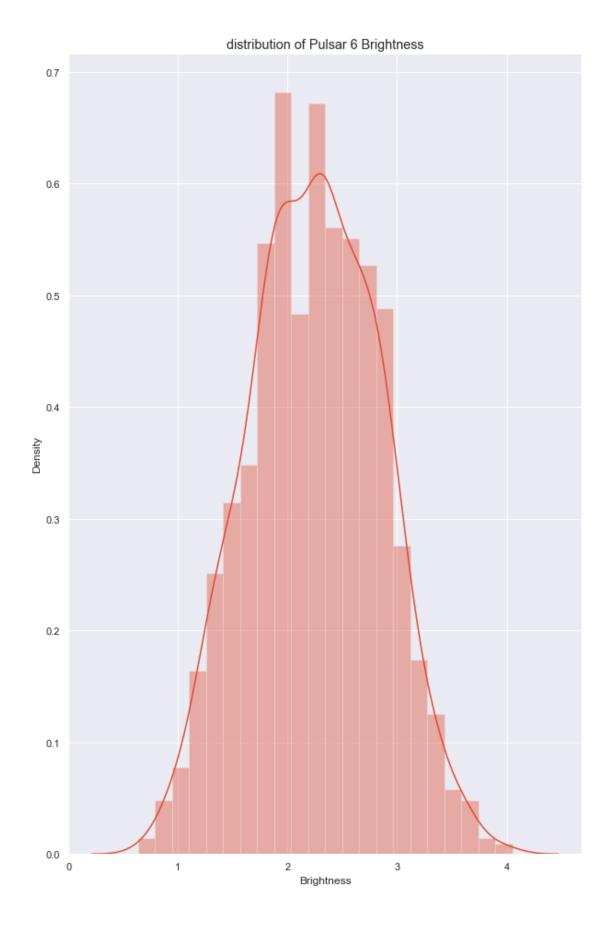


```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Brightness)
plt.title("distribution of Pulsar 6 Brightness")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 Brightness')



```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Binary)
plt.title("distribution of Pulsar 6 binary assignments")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 binary assignments')



3.2 Binary Classification

```
[]: X = pulsar[['Brightness', 'Uncertainty']]
     y = pulsar['Binary']
[]: X.head()
[]:
       Brightness Uncertainty
          0.984043
                      0.053831
     1
         2.487928
                      0.048796
         1.690295
     2
                      0.025639
     3
         1.196142
                      0.039539
     4
          1.979783
                      0.041460
[]: y.head()
[]: 0
     1
          1
     2
          0
     3
         0
     4
          0
     Name: Binary, dtype: int32
[]: from sklearn.model_selection import train_test_split
     X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: from sklearn.preprocessing import StandardScaler
     train_scaler = StandardScaler()
     X_train = train_scaler.fit_transform(X_train)
     test scaler = StandardScaler()
     X_test = test_scaler.fit_transform(X_test)
[]: model = LogisticRegression()
     model.fit(X_train, y_train)
[]: LogisticRegression()
[]: predictions = model.predict(X_test)
[]: from sklearn.metrics import confusion_matrix
```

```
cm = confusion_matrix(y_test, predictions)
     TN, FP, FN, TP = confusion_matrix(y_test, predictions).ravel()
     print('True Positive(TP) = ', TP)
     print('False Positive(FP) = ', FP)
     print('True Negative(TN) = ', TN)
     print('False Negative(FN) = ', FN)
    True Positive(TP) = 132
    False Positive(FP) = 0
    True Negative(TN) = 122
    False Negative(FN) = 13
[]: accuracy = (TP + TN) / (TP + FP + TN + FN)
    print("Accuracy of the model is ", accuracy)
    Accuracy of the model is 0.951310861423221
    3.3 Bidirectional LSTM Model
[]: brightness_list = list(pulsar['Brightness'])
     brightness_list[:10]
[]: [0.9840433,
     2.487928,
     1.690295,
     1.196142,
      1.979783,
     2.297645,
     2.322135,
     2.289047,
     2.442574,
     2.136332]
[]: def split_list(blist, steps):
        X, y = list(), list()
        for i in range(len(blist)):
             # find the end of this pattern
             end_ix = i + steps
             # check if we are beyond the sequence
             if end_ix > len(blist)-1:
             # gather input and output parts of the pattern
            list_x, list_y = blist[i:end_ix], blist[end_ix]
            X.append(list_x)
             y.append(list_y)
```

```
return array(X), array(y)
[]: X, y = split_list(brightness_list, 100)
    X = X.reshape((X.shape[0], X.shape[1], 1))
    X[:1]
[]: array([[[0.9840433],
             [2.487928],
            [1.690295],
            [1.196142],
            [1.979783],
            [2.297645],
            [2.322135],
            [2.289047],
            [2.442574],
            [2.136332],
            [1.97679],
            [2.445764],
            [1.937017],
            [2.315184],
            [2.584888],
            [1.581452],
            [1.849656],
             [2.529834],
            [2.894401],
            [2.769474],
            [1.82449],
            [1.498133],
            [2.005834],
            [2.594836],
            [2.745045],
            [2.312928],
            [2.661311],
            [2.885388],
            [1.761946],
            [2.081099],
            [2.36358],
            [2.35345],
            [1.652502],
            [2.248286],
            [2.874749],
            [2.610421],
            [2.294724],
            [2.961658],
            [2.696347],
            [2.917047],
             [1.996423],
```

- [2.739376],
- [1.986204],
- [1.653353],
- [1.800485],
- [2.600838],
- [3.090313],
- [2.271085],
- [1.805165],
- [2.681646],
- [2.696566],
- [2.101715],
- [2.278763],
- [2.734046],
- [1.096633],
- [1.077475],
- [2.062858],
- [2.92687],
- [1.454358],
- [2.356589],
- [1.98154],
- [2.399687],
- [2.292884],
- [3.16329],
- [2.709231],
- [1.506129],
- [2.353669],
- [1.554678],
- [2.579631],
- [1.70781],
- [2.381017],
- [2.914784],
- [2.236938],
- [2.507387],
- [1.114129],
- [1.90936],
- [1.752472],
- [2.473441],
- [1.586753],
- [3.304978],
- [1.267595],
- [0.9429132],
- [1.435816],
- [1.407151],
- [2.094246],
- [3.098825],
- [2.088198],
- [1.557415],

```
[2.167673],
          [3.134241],
          [1.791176],
          [2.026329],
          [1.796364],
          [2.971239],
          [2.195826],
          [2.841772],
          [2.411585],
          [2.63257],
          [1.859452],
          [1.621589]]])
[]: X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: model = Sequential()
    model.add(Bidirectional(LSTM(50, activation='relu'), input_shape=(100, 1)))
    model.add(Dense(8, activation='relu'))
    model.add(Dense(1, activation='sigmoid'))
    model.compile(loss='binary_crossentropy', optimizer='adam',_

→metrics=['accuracy'])
[]: history = model.fit(X_train, y_train, epochs=50, verbose=1, batch_size=10)
   Epoch 1/50
   99/99 [========== ] - 3s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 2/50
   99/99 [========== - - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 3/50
   99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 4/50
   0.0000e+00
   Epoch 5/50
   99/99 [========== - - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 6/50
   99/99 [========== - - 2s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 7/50
   99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 8/50
   0.0000e+00
```

```
Epoch 9/50
99/99 [=========== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 10/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 11/50
0.0000e+00
Epoch 12/50
99/99 [============= ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 13/50
99/99 [========= ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 14/50
99/99 [========== - - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 15/50
99/99 [============= ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 16/50
0.0000e+00
Epoch 17/50
99/99 [========= ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 18/50
0.0000e+00
Epoch 19/50
0.0000e+00
Epoch 20/50
0.0000e+00
Epoch 21/50
0.0000e+00
Epoch 22/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 23/50
0.0000e+00
Epoch 24/50
99/99 [========= ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
```

```
Epoch 25/50
99/99 [========== ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 26/50
99/99 [============= ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 27/50
0.0000e+00
Epoch 28/50
99/99 [========== ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 29/50
0.0000e+00
Epoch 30/50
99/99 [========== - - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 31/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 32/50
0.0000e+00
Epoch 33/50
99/99 [========= ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 34/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 35/50
0.0000e+00
Epoch 36/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 37/50
0.0000e+00
Epoch 38/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 39/50
99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
0.0000e+00
Epoch 40/50
99/99 [========= ] - 2s 20ms/step - loss: nan - accuracy:
0.0000e+00
```

```
99/99 [========== - - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 42/50
   99/99 [============= ] - 2s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 43/50
   0.0000e+00
   Epoch 44/50
   99/99 [============= ] - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 45/50
   99/99 [========= ] - 2s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 46/50
   99/99 [========== - - 2s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 47/50
                  ======== ] - 2s 21ms/step - loss: nan - accuracy:
   99/99 [======
   0.0000e+00
   Epoch 48/50
   0.0000e+00
   Epoch 49/50
   99/99 [============= ] - 2s 20ms/step - loss: nan - accuracy:
   0.0000e+00
   Epoch 50/50
   99/99 [============== ] - 2s 21ms/step - loss: nan - accuracy:
   0.0000e+00
[]: y_pred = model.predict(X_test, verbose=0)
   y_pred[:10]
[]: array([[nan],
         [nan],
         [nan],
         [nan],
         [nan],
         [nan],
         [nan],
         [nan],
         [nan],
         [nan]], dtype=float32)
[]: model.evaluate(X_test, y_test)
   8/8 [============ ] - Os 7ms/step - loss: nan - accuracy:
```

Epoch 41/50

0.0000e+00

[]: [nan, 0.0]

3.4 ML Evaluation.

3.4.1 Logistic Regression

This model appears to have gained some insight in the data and accurately defined a majority of the data. The accuracy of the model is >95% which indicates that it was able to determine a trend and apply it in a useful manner in the predictions during evaluation. Further, the confusion matrix further supports the high accuracy and likely usefulness of the model with only 3 false assignments. However, in analysis this is only to determine if there is a correlation between binary assignment and the emission strength x error in measurement. This doesn't aid us in our overall randomness determination, but it does determine that uncertainty has a role in the binary assignment and the overall trust of emission strength.

3.4.2 Bidirectional LSTM

This model is very error prone as the loss value is consistently at 60% or higher at every epoch during training and at exactly 63.07% in evaluation with a 0% accuracy this indicates that there is either a great error in the formation of the model, data used or trend being obtained. Alternatively it could indicate that there is no trend there to predict. Likely this indicates that the model is not valuable for any meaningful analysis.

4 Preliminary runs test

4.0.1 Math Logic

$$Z = \frac{R - \tilde{R}}{s_R}$$

$$\tilde{R} = \frac{2_{n1n2}}{n1 + n2} + 1$$

$$s_R^2 = \frac{2nn_2(2nn_2 - n_1 - n_2)}{(n_1 + n_2)^2(n_1 + n_2 - 1)}$$

link to resource: https://www.geeksforgeeks.org/runs-test-of-randomness-in-python/

 $Z_{\text{critical}} = 1.96$ s as the confidence interval level of 95% thus this is a 2 tailed test. If the probability as corrosponding to this confidence interval H_{null} will be rejected as it is not statistically significant as denoted by $|Z| > Z_{\text{critical}}$

There is also code attempting to change it from a z-score probability to a P-score for ease of understanding and clarity.

5 FUNCTION CODE FOR RUNS TEST

```
[]: binaryData1 = pulsar['Binary'].tolist()
print("pulsar6 original: ",binaryData1)
```

```
pulsar6 original: [0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1,
0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 1, 1,
1, 0, 1, 1, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 1, 1, 0, 1, 0, 1, 0, 1, 1, 0, 1,
0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 0, 0,
1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 0, 1,
0, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0,
1, 0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1,
0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1,
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```

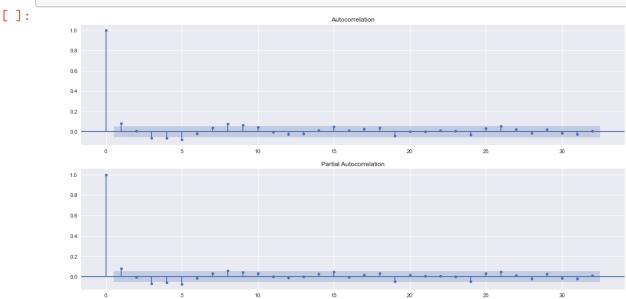
6 Below we begin autocorrelation and autocovariance analysis

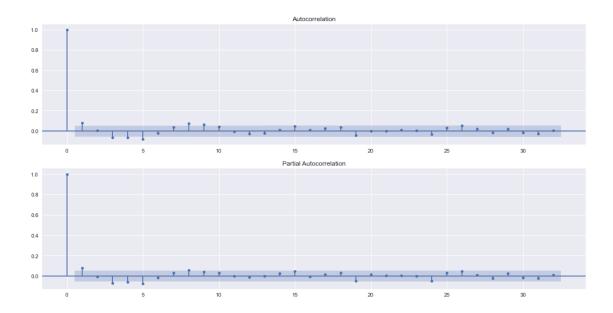
To get started with this I am playing around with guide from: https://towards datascience.com/a-step-by-step-guide-to-calculating-autocorrelation-and-partial-autocorrelation-8c4342b784e8

```
[]: plt.style.use("seaborn")
  plt.rcParams["figure.figsize"] = (18, 9)

fig, ax = plt.subplots(2,1)

plot_acf(pulsar['Brightness'], ax=ax[0])
  plot_pacf(pulsar['Brightness'], ax=ax[1], method="ols")
```





```
[]: acf(pulsar['Brightness'], nlags=10)
    FutureWarning: fft=True will become the default after the release of the 0.12
    release of statsmodels. To suppress this warning, explicitly set fft=False.
      warnings.warn(
[]: array([1.
                       0.08095517, 0.00412699, -0.06721578, -0.06554554,
           -0.07977771, -0.02053543, 0.03766276, 0.07611705, 0.06106126,
            0.04441705])
[]: acfpulsar = pd.DataFrame()
    for lag in range(0,11):
        acfpulsar[f"B_lag_{lag}"] = pulsar['Brightness'].shift(lag)
    acfpulsar
[]:
           B_lag_0
                                       B_lag_3
                                                 B_lag_4
                                                           B_lag_5
                                                                    B_lag_6 \
                    B_lag_1
                              B_lag_2
          0.984043
    0
                        NaN
                                  {\tt NaN}
                                           NaN
                                                     NaN
                                                              NaN
                                                                        NaN
    1
          2.487928
                   0.984043
                                  {\tt NaN}
                                           NaN
                                                     NaN
                                                              NaN
                                                                        NaN
    2
          1.690295
                   2.487928
                             0.984043
                                           NaN
                                                     NaN
                                                              NaN
                                                                        NaN
    3
          1.196142
                   1.690295
                             2.487928
                                      0.984043
                                                     NaN
                                                              NaN
                                                                        NaN
    4
          1.979783
                   1.196142
                             1.690295
                                      2.487928
                                               0.984043
                                                              NaN
                                                                        NaN
          1.842016
                   2.646750
                                                2.503202
    1326
                             2.258860
                                       2.123736
                                                          2.178636
                                                                   1.392491
    1327
          1.547695
                             2.646750
                                       2.258860
                                                          2.503202
                   1.842016
                                                2.123736
                                                                   2.178636
```

2.646750

2.258860

2.123736 2.503202

1328

2.797312 1.547695 1.842016

```
1329
     3.351977 2.797312 1.547695 1.842016 2.646750 2.258860 2.123736
1330 3.115255 3.351977
                         2.797312 1.547695 1.842016 2.646750 2.258860
      B_lag_7
                B_lag_8
                          B_lag_9 B_lag_10
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3
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4
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                          1.943447
                                    1.950708
1326
     1.886326
                1.810641
1327
     1.392491
               1.886326
                          1.810641
                                   1.943447
1328
     2.178636
              1.392491 1.886326
                                   1.810641
1329
     2.503202 2.178636 1.392491
                                    1.886326
1330 2.123736 2.503202 2.178636 1.392491
[1331 rows x 11 columns]
```

```
[]: acfpulsar.corr()["B_lag_0"].values
```

```
[]: array([1. , 0.0811623 , 0.00414645, -0.06751767, -0.06595236, -0.08029629, -0.02066581, 0.0379259 , 0.07664111, 0.06149054, 0.04473245])
```

- 6.0.1 Getting every 5th as per the auto correlation
- 6.0.2 Creating a new set of discrete 100 sets and examining them specifically
- 6.0.3 Further Random testing to move into extensive testing

Getting every 5th as per the auto correlation

```
[]: held5ths = pulsar[pulsar.index % 5 == 0] held5ths
```

[]:		Pulse	Number	Brightness	Uncertainty	Binary
	0		1	0.984043	0.053831	0
	5		6	2.297645	0.054210	1
	10		11	1.976790	0.037551	0
	15		16	1.581452	0.030372	0
	20		21	1.824490	0.036531	0
			•••	•••	•••	
	1310		1311	2.360064	0.034759	1
	1315		1316	2.596850	0.048041	1
	1320		1321	1.392491	0.030957	0
	1325		1326	2.646750	0.036691	1
	1330		1331	3.115255	0.035134	1

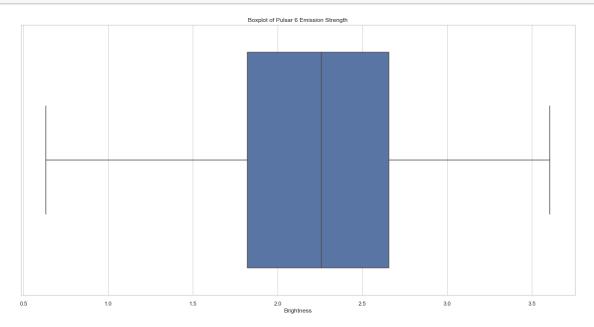
[267 rows x 4 columns]

```
[]: medianheld5ths = held5ths["Brightness"].median() medianheld5ths
```

[]: 2.256816

```
[]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=held5ths["Brightness"]).set_title("Boxplot of Pulsar 6

→Emission Strength")
```



```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = sns.scatterplot(data=held5ths["Brightness"], s= strength*50, c=strength,

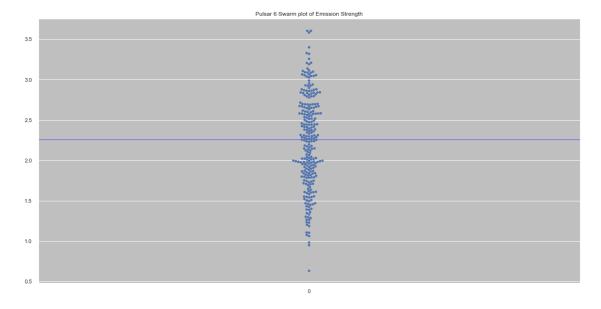
→cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color

→hued of Emission Strength')
ax = plt.axhline( y=2.256816, ls='-',c='mediumslateblue')
```



```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = plt.axhline( y=2.256816, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=held5ths["Brightness"], c="blue").set_title('Pulsar 6

→Swarm plot of Emission Strength')
```



```
[]: print(len(held5ths[(held5ths.Brightness > 2.256816)]))
print(len(held5ths[(held5ths.Brightness < 2.256816)]))
```

```
133133
```

```
Randomness testing
```

```
[]: pulsar.Binary
```

```
[]: 0
              0
     1
              1
     2
              0
     3
              0
     4
              0
              0
     1326
     1327
     1328
              1
     1329
              1
     1330
              1
```