pulsar6

November 4, 2022

- 1 Pulsar Emission Data Analysis
- 2 All Imports that may or may not be needed and used for the notebook

```
[]: #currently including any and all Imports that maybe needed for the project.
     import pandas as pd
     import numpy as np
     import seaborn as sns
     import matplotlib.pyplot as plt
     %matplotlib inline
     from sklearn.model selection import train test split
     from sklearn import linear_model
     from sklearn.metrics import r2_score, mean_squared_error
     from sklearn.linear_model import LogisticRegression, LinearRegression
     from sklearn.metrics import confusion_matrix, accuracy_score
     from sklearn.feature_selection import RFE
     import datetime as dt
     from sklearn.cluster import KMeans
     from sklearn.metrics import pairwise_distances
     from scipy.cluster.hierarchy import linkage, dendrogram, cut_tree
     from scipy.spatial.distance import pdist
     from sklearn.feature_extraction.text import TfidfVectorizer
     import matplotlib.dates as mdates
     from scipy.stats import pearsonr
     from scipy import stats
     import statistics
     import math
     from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
     from statsmodels.tsa.stattools import acf, pacf
     from statsmodels.tsa.tsatools import lagmat
     from numpy import array
     from sklearn.model_selection import train_test_split
     from keras.models import Sequential
     from keras.layers import LSTM
     from keras.layers import Dense
     from keras.layers import Bidirectional
```

```
from sklearn.datasets import load_iris
from sklearn import datasets, linear_model, metrics
from scipy.stats import binned_statistic
```

3 Section for extracting from a tar file.

Currently implemented for original TAR File structure.

```
[]: #This is also found in the main file under tarunzip.py
import tarfile
import os
import sys

#tar = tarfile.open("pulseTarFile.tar")
#tar.extractall('./Data')
#tar.close()
```

```
[]: #How to remove outlier data for these datasets.

#pulsar6npcleaned = pulsar6[(np.abs(stats.zscore(pulsar6["Brightness"])) <3)]

#pulsar6npcleaned
```

3.1 Beginning of Exploration

3.1.1 Examining the data

In this section we are determining the total integrity of the data to determine if further comprehensive data cleaning and uniforming processes are needed.

```
[]: colnames = ['Pulse Number', 'Brightness', 'Uncertainty']

pulsar = pd.read_csv("Data/J1644-4559.pulses", sep = ' ', header = None, names

→= colnames)
```

- []: pulsar.shape
- []: (698, 3)
- []: pulsar.head(25)

```
[]:
         Pulse Number
                        Brightness
                                     Uncertainty
     0
                           0.634671
                                         0.002761
     1
                     2
                           0.736945
                                         0.005207
     2
                     3
                           0.693834
                                         0.002706
     3
                     4
                           1.021866
                                         0.010184
     4
                     5
                           0.673845
                                         0.006236
     5
                     6
                           0.676883
                                         0.004763
                     7
     6
                           0.527039
                                         0.002422
     7
                     8
                           0.673417
                                         0.003174
     8
                     9
                           0.357076
                                         0.002848
                    10
                           0.661704
                                         0.005588
```

```
12
     11
                          0.494655
                                        0.003145
     12
                    13
                          0.804260
                                        0.005258
     13
                    14
                          0.513362
                                        0.005700
     14
                    15
                          0.477025
                                        0.002945
     15
                    16
                          0.399571
                                        0.004712
     16
                    17
                          0.188069
                                        0.002452
     17
                    18
                          0.748592
                                        0.005468
                    19
                          0.723437
                                        0.004548
     18
     19
                    20
                          0.960154
                                        0.006765
     20
                    21
                                        0.006011
                          0.707715
     21
                    22
                          1.074550
                                        0.006831
     22
                    23
                          0.961340
                                        0.006617
     23
                    24
                          0.754457
                                        0.004117
     24
                    25
                          0.773151
                                        0.004920
[]:
     pulsar.describe()
[]:
            Pulse Number
                           Brightness
                                        Uncertainty
                698.00000
                           698.000000
                                         698.000000
     count
     mean
                349.50000
                             0.654319
                                           0.004445
                                           0.001855
     std
                201.63953
                             0.163945
                             0.007642
                                           0.002129
     min
                  1.00000
     25%
                175.25000
                             0.555267
                                           0.003086
     50%
                349.50000
                             0.658295
                                           0.003951
     75%
                523.75000
                             0.753396
                                           0.005349
     max
                698.00000
                             1.159334
                                           0.016097
[]: nullBoolBrightness = pd.isnull(pulsar["Brightness"])
     pulsar[nullBoolBrightness]
[]: Empty DataFrame
     Columns: [Pulse Number, Brightness, Uncertainty]
     Index: []
[]: pulsar["Brightness"].describe()
[]: count
              698.000000
     mean
                 0.654319
     std
                 0.163945
     min
                 0.007642
     25%
                 0.555267
     50%
                 0.658295
     75%
                 0.753396
                 1.159334
     max
     Name: Brightness, dtype: float64
```

0.003835

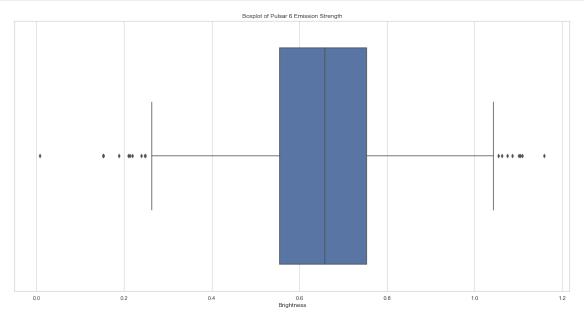
10

11

0.545564

```
[]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=pulsar["Brightness"]).set_title("Boxplot of Pulsar 6

→Emission Strength")
```



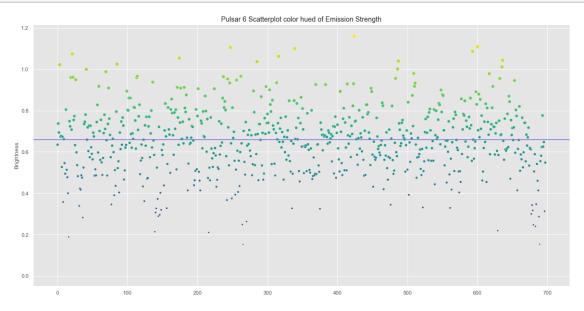
```
[]: medianpulse6 = pulsar["Brightness"].median()
print("Median of Pulsar6: ", medianpulse6)
pulsar['Binary'] = np.where(pulsar['Brightness'] > medianpulse6, 1, 0)
```

Median of Pulsar6: 0.65829515

[]: pulsar

[]:		Pulse	Number	Brightness	Uncertainty	Binary
	0		1	0.634671	0.002761	0
	1		2	0.736945	0.005207	1
	2		3	0.693834	0.002706	1
	3		4	1.021866	0.010184	1
	4		5	0.673845	0.006236	1
				•••	•••	
	693		694	0.776083	0.008928	1
	694		695	0.625382	0.006018	0
	695		696	0.647559	0.003765	0
	696		697	0.312449	0.002901	0
	697		698	0.548353	0.009056	0

[698 rows x 4 columns]

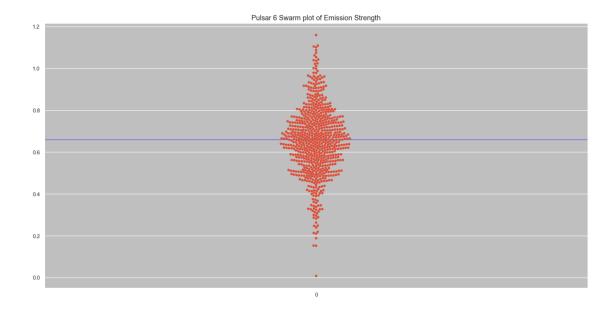


```
[]: print(len(pulsar[(pulsar.Brightness > 0.6589028)]))

print(len(pulsar[(pulsar.Brightness < 0.6589028)]))

348
350

[]: plt.figure(figsize=(20,10))
    sns.set_style("darkgrid", {"axes.facecolor": ".75"})
    strength = pulsar.Brightness.values
    ax = plt.axhline( y=0.65829515, ls='-',c='mediumslateblue')
    ax = sns.swarmplot(data=pulsar["Brightness"], c="blue").set_title('Pulsar 6⊔
    →Swarm plot of Emission Strength')
```

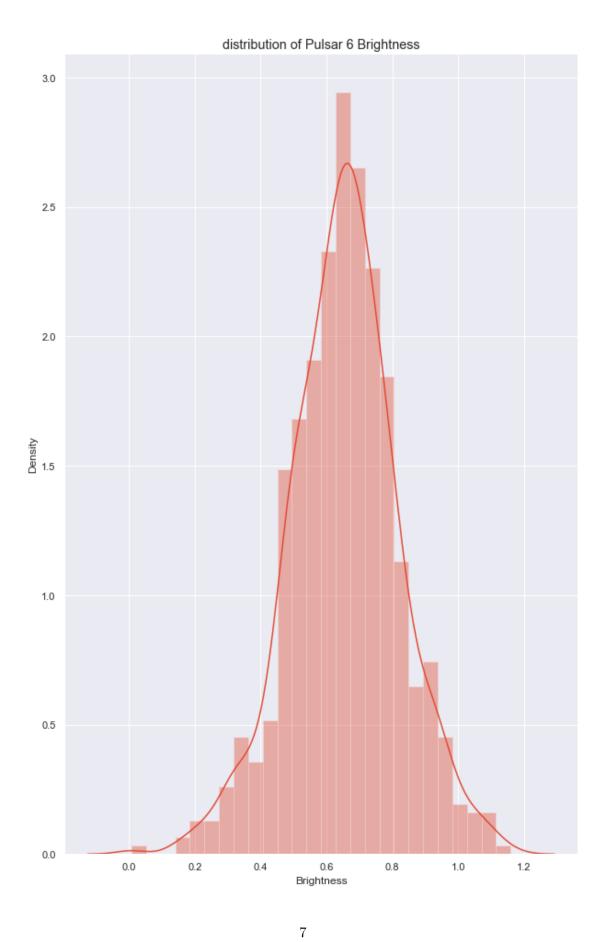


```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
          sns.distplot(pulsar.Brightness)
plt.title("distribution of Pulsar 6 Brightness")
```

C:\Users\tajki\anaconda3\lib\site-packages\seaborn\distributions.py:2619: FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 Brightness')



```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
        sns.distplot(pulsar.Binary)
plt.title("distribution of Pulsar 6 binary assignments")
```

C:\Users\tajki\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

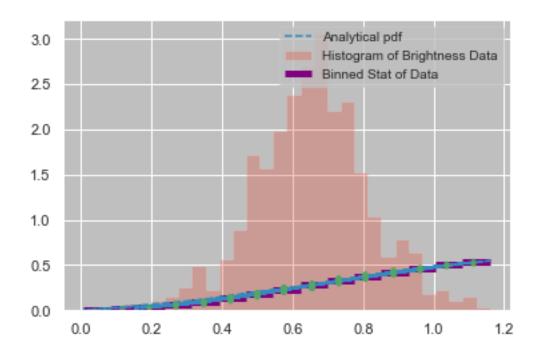
warnings.warn(msg, FutureWarning)

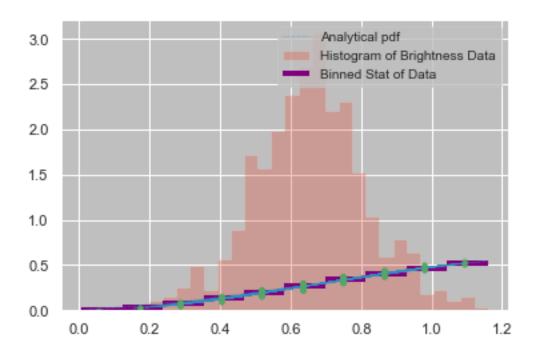
[]: Text(0.5, 1.0, 'distribution of Pulsar 6 binary assignments')



4 Rolling Medians, Rolling Means, Binned Medians and Binned Mean analysis.

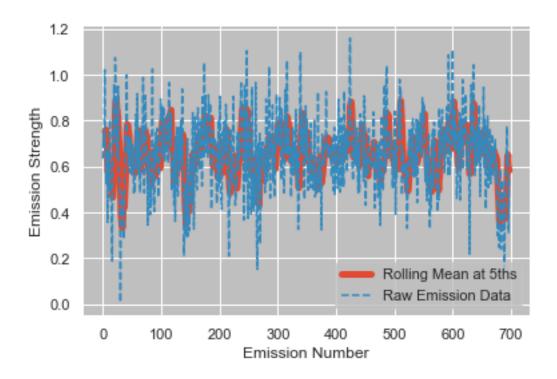
```
[]: data = pulsar["Brightness"]
     data
[]: 0
            0.634671
            0.736945
     1
     2
            0.693834
     3
            1.021866
            0.673845
              •••
            0.776083
     693
     694
            0.625382
     695
            0.647559
     696
            0.312449
     697
            0.548353
     Name: Brightness, Length: 698, dtype: float64
[ ]: dataPDF = stats.maxwell.pdf(data)
     bin_means, bin_edges, binnumber = stats.binned_statistic(data, dataPDF,
             statistic='mean', bins=15)
     bin_width = (bin_edges[1] - bin_edges[0])
     bin_centers = bin_edges[1:] - bin_width/2
     plt.figure()
     plt.hist(data, bins=30, density=True, histtype='stepfilled', alpha=0.3,
      →label='Histogram of Brightness Data')
     plt.plot(data, dataPDF, '--', label = "Analytical pdf")
     plt.hlines(bin_means, bin_edges[:-1], bin_edges[1:], colors='purple', lw=5,__
      →label='Binned Stat of Data')
     plt.plot((binnumber - 0.5) * bin_width, dataPDF, 'g.', alpha=0.5)
     plt.legend(fontsize=10)
     plt.show()
```

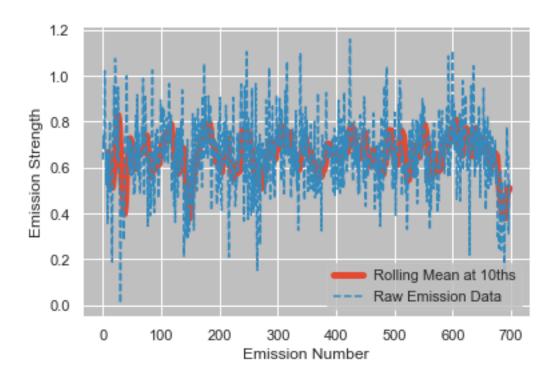


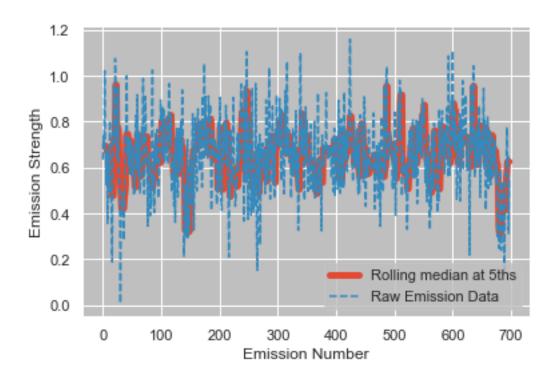


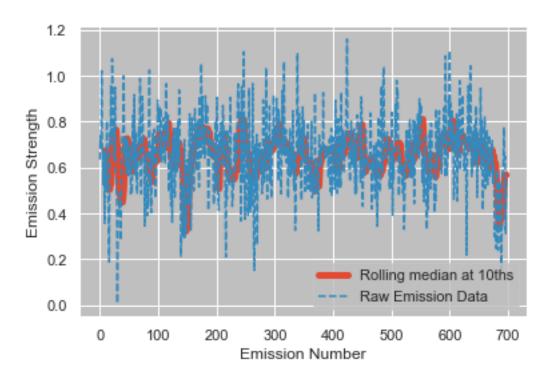
```
[]: pulsar['RollingMeanEmissions5ths'] = pulsar["Brightness"].rolling(5).mean()

plt.plot(pulsar['RollingMeanEmissions5ths'], label="Rolling Mean at 5ths", lw=5)
  plt.plot(pulsar['Brightness'], label= "Raw Emission Data", linestyle='--')
  plt.legend()
  plt.ylabel('Emission Strength')
  plt.xlabel('Emission Number')
  plt.show()
```









[]:	pulsar.he	ad(25)					
[]:	Pulse	Number	Brightness	Uncertainty	Binary	RollingMeanEmissions5ths	\
	0	1	0.634671	0.002761	0	NaN	
	1	2	0.736945	0.005207	1	NaN	
	2	3	0.693834	0.002706	1	NaN	
	3	4	1.021866	0.010184	1	NaN	
	4	5	0.673845	0.006236	1	0.752232	
	5	6	0.676883	0.004763	1	0.760675	
	6	7	0.527039	0.002422	0	0.718693	
	7	8	0.673417	0.003174	1	0.714610	
	8	9	0.357076	0.002848	0	0.581652	
	9	10	0.661704	0.005588	1	0.579224	
	10	11	0.545564	0.003835	0	0.552960	
	11	12	0.494655	0.003145	0	0.546483	
	12	13	0.804260	0.005258	1	0.572651	
	13	14	0.513362	0.005700	0	0.603909	
	14	15	0.477025	0.002945	0	0.566973	
	15	16	0.399571	0.004712	0	0.537775	
	16	17	0.188069	0.002452	0	0.476457	
	17	18	0.748592	0.005468	1	0.465324	
	18	19	0.723437	0.004548	1	0.507339	
	19	20	0.960154	0.006765	1	0.603965	
	20	21	0.707715	0.006011	1	0.665593	

```
21
               22
                                    0.006831
                                                                          0.842890
                      1.074550
                                                     1
22
               23
                                    0.006617
                                                     1
                                                                          0.885439
                      0.961340
23
               24
                                                     1
                      0.754457
                                    0.004117
                                                                          0.891643
24
                                                     1
               25
                      0.773151
                                    0.004920
                                                                          0.854242
    RollingMeanEmissions10ths
                                  RollingMedianEmissions5ths
0
                            NaN
                                                           NaN
1
                            NaN
                                                           NaN
2
                            NaN
                                                           NaN
3
                            NaN
                                                           NaN
                            NaN
4
                                                      0.693834
                            NaN
5
                                                      0.693834
6
                            NaN
                                                      0.676883
7
                            NaN
                                                      0.673845
8
                            NaN
                                                      0.673417
9
                       0.665728
                                                      0.661704
10
                       0.656817
                                                      0.545564
11
                       0.632588
                                                      0.545564
12
                       0.643631
                                                      0.545564
13
                       0.592780
                                                      0.545564
14
                       0.573098
                                                      0.513362
15
                       0.545367
                                                      0.494655
16
                       0.511470
                                                      0.477025
17
                       0.518988
                                                      0.477025
18
                       0.555624
                                                      0.477025
19
                       0.585469
                                                      0.723437
20
                       0.601684
                                                      0.723437
21
                       0.659673
                                                      0.748592
22
                                                      0.960154
                       0.675381
23
                       0.699491
                                                      0.960154
24
                       0.729103
                                                      0.773151
    RollingMedianEmissions10ths
0
                               NaN
                               NaN
1
2
                               NaN
3
                               NaN
4
                               NaN
5
                               NaN
6
                               NaN
7
                               NaN
8
                               NaN
9
                         0.673631
10
                         0.673631
11
                         0.667561
12
                         0.667561
13
                         0.603634
```

```
14
                         0.536301
15
                         0.520201
16
                         0.504008
                        0.504008
17
18
                         0.529463
19
                         0.529463
20
                         0.610538
21
                         0.715576
22
                         0.715576
23
                         0.736015
                         0.751524
24
```

5 Kalman Filter to go here

```
[]:
    5.1 Binary Classification
[]: X = pulsar[['Brightness', 'Uncertainty']]
     y = pulsar['Binary']
[]: X.head()
[]:
       Brightness Uncertainty
         0.634671
                       0.002761
     1
         0.736945
                       0.005207
     2
         0.693834
                       0.002706
     3
         1.021866
                       0.010184
         0.673845
     4
                       0.006236
[]: y.head()
[]: 0
         0
     1
          1
     2
     3
          1
          1
    Name: Binary, dtype: int32
[]: from sklearn.model_selection import train_test_split
     X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: from sklearn.preprocessing import StandardScaler
     train_scaler = StandardScaler()
     X_train = train_scaler.fit_transform(X_train)
```

```
test_scaler = StandardScaler()
    X_test = test_scaler.fit_transform(X_test)
[]: model = LogisticRegression()
    model.fit(X_train, y_train)
[]: LogisticRegression()
[]: predictions = model.predict(X_test)
[]: from sklearn.metrics import confusion_matrix
    cm = confusion_matrix(y_test, predictions)
    TN, FP, FN, TP = confusion_matrix(y_test, predictions).ravel()
    print('True Positive(TP) = ', TP)
    print('False Positive(FP) = ', FP)
    print('True Negative(TN) = ', TN)
    print('False Negative(FN) = ', FN)
    True Positive(TP) = 67
    False Positive(FP) = 0
    True Negative(TN) = 71
    False Negative(FN) = 2
[]: accuracy = (TP + TN) / (TP + FP + TN + FN)
    print("Accuracy of the model is ", accuracy)
    Accuracy of the model is 0.9857142857142858
    5.2 Bidirectional LSTM Model
[]: # making a list with the brightness and uncertainty values
    values_list = pulsar[['Brightness', 'Uncertainty']].values.tolist()
    values_list[:10]
[]: [[0.6346714, 0.002760888],
      [0.7369454, 0.005207055],
      [0.6938341, 0.0027059],
      [1.021866, 0.01018372],
      [0.6738453, 0.006235539],
      [0.6768825, 0.004762893],
      [0.5270392, 0.002422239],
      [0.6734173, 0.003174072],
```

```
[0.3570756, 0.00284815],
     [0.6617037, 0.005587867]]
[]: from sklearn import preprocessing
    # normalizing the values
    values list = preprocessing.normalize(values list)
[]: # function for spliting list in a format we can use in the model
    def split_list(blist, steps):
        X, y = list(), list()
        for i in range(len(blist)):
           end_ix = i + steps
           if end_ix > len(blist)-1:
               break
           list_x, list_y = blist[i:end_ix], blist[end_ix][0]
           X.append(list_x)
           y.append(list_y)
        return array(X), array(y)
[]: # splitting the list
    X, y = split_list(values_list, 100)
    # reshaping the list to feed the model
    X = X.reshape((X.shape[0], X.shape[1], 2))
[]: # splitting the list into train and test sets
    X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: # setting the parameters for the lstm model and compiling it
    model = Sequential()
    model.add(Bidirectional(LSTM(50, activation='relu'), input_shape=(100, 2)))
    model.add(Dense(25, activation='relu'))
    model.add(Dense(12, activation='relu'))
    model.add(Dense(6, activation='relu'))
    model.add(Dense(1, activation='sigmoid'))
    model.compile(loss='binary_crossentropy', optimizer='adam', __
     →metrics=['accuracy'])
[]: # training the model
    history = model.fit(X_train, y_train, epochs=50, verbose=1,_
     →batch_size=(int(X_train.shape[0]/50)))
   Epoch 1/50
   0.0000e+00
   Epoch 2/50
```

```
accuracy: 0.0000e+00
Epoch 3/50
0.0000e+00
Epoch 4/50
0.0000e+00
Epoch 5/50
0.0000e+00
Epoch 6/50
0.0000e+00
Epoch 7/50
0.0000e+00
Epoch 8/50
0.0000e+00
Epoch 9/50
0.0000e+00
Epoch 10/50
0.0000e+00
Epoch 11/50
0.0000e+00
Epoch 12/50
0.0000e+00
Epoch 13/50
0.0000e+00
Epoch 14/50
0.0000e+00
Epoch 15/50
0.0000e+00
Epoch 16/50
0.0000e+00
Epoch 17/50
0.0000e+00
Epoch 18/50
```

```
0.0000e+00
Epoch 19/50
0.0000e+00
Epoch 20/50
0.0000e+00
Epoch 21/50
0.0000e+00
Epoch 22/50
0.0000e+00
Epoch 23/50
0.0000e+00
Epoch 24/50
0.0000e+00
Epoch 25/50
0.0000e+00
Epoch 26/50
0.0000e+00
Epoch 27/50
0.0000e+00
Epoch 28/50
0.0000e+00
Epoch 29/50
0.0000e+00
Epoch 30/50
0.0000e+00
Epoch 31/50
0.0000e+00
Epoch 32/50
0.0000e+00
Epoch 33/50
0.0000e+00
Epoch 34/50
```

```
0.0000e+00
Epoch 35/50
0.0000e+00
Epoch 36/50
0.0000e+00
Epoch 37/50
0.0000e+00
Epoch 38/50
0.0000e+00
Epoch 39/50
0.0000e+00
Epoch 40/50
0.0000e+00
Epoch 41/50
0.0000e+00
Epoch 42/50
0.0000e+00
Epoch 43/50
0.0000e+00
Epoch 44/50
0.0000e+00
Epoch 45/50
0.0000e+00
Epoch 46/50
0.0000e+00
Epoch 47/50
0.0000e+00
Epoch 48/50
0.0000e+00
Epoch 49/50
0.0000e+00
Epoch 50/50
```

0.0000e+00

```
[]: # predicting the y/brightness values for the test set
    y_pred = model.predict(X_test, verbose=0)
    y_pred[:10]
[]: array([[0.99742967],
          [0.9974283],
          [0.99742913],
          [0.9974295],
          [0.99742895],
          [0.9974301],
          [0.99742985],
          [0.99742836],
          [0.9974307],
          [0.99742925]], dtype=float32)
[]: # evaluating the model
    model.evaluate(X_test, y_test)
   0.0000e+00
[]: [0.0027466383762657642, 0.0]
```

[]: [0:002/400000/0200/042, 0:0]

5.3 ML Evaluation.

5.3.1 Logistic Regression

Rewards no significant results for this type of analysis and is dropped for a LSTM attempt

5.3.2 Bidirectional LSTM

Loss is low so the model is performing well. But the accuracy is low therefore unable to obtain trend and therefore not rewarding any information. This means we cannot predict any of the values with confidence.

6 Preliminary runs test

6.0.1 Math Logic

$$Z = \frac{R - \tilde{R}}{s_R}$$

$$\tilde{R} = \frac{2n_1n_2}{n_1 + n_2} + 1$$

$$s_R^2 = \frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1 + n_2)^2(n_1 + n_2 - 1)}$$

link to resource: https://www.geeksforgeeks.org/runs-test-of-randomness-in-python/

 $Z_{\text{critical}} = 1.96$ s as the confidence interval level of 95% thus this is a 2 tailed test. If the probability as corrosponding to this confidence interval H_{null} will be rejected as it is not statistically significant as denoted by $|Z| > Z_{\text{critical}}$

There is also code attempting to change it from a z-score probability to a P-score for ease of understanding and clarity.

7 FUNCTION CODE FOR RUNS TEST

```
[]: binaryData1 = pulsar['Binary'].tolist()
print("pulsar6 original: ",binaryData1)
```

```
pulsar6 original: [0, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1,
1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0,
1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1,
1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1,
1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1,
0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1,
1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1,
1, 1, 1, 1, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1,
1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0,
1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1,
0, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1,
0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1,
0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1,
1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0,
0, 0, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1,
0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1,
1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0,
0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1,
0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1,
1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1,
1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1,
0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0,
0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0,
1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0,
0, 0, 1, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 1,
0, 0, 0]
```

8 Below we begin autocorrelation and autocovariance analysis

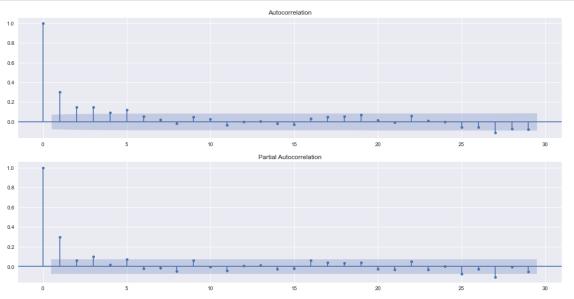
To get started with this I am playing around with guide from: https://towardsdatascience.com/a-step-by-step-guide-to-calculating-autocorrelation-and-partial-autocorrelation-8c4342b784e8

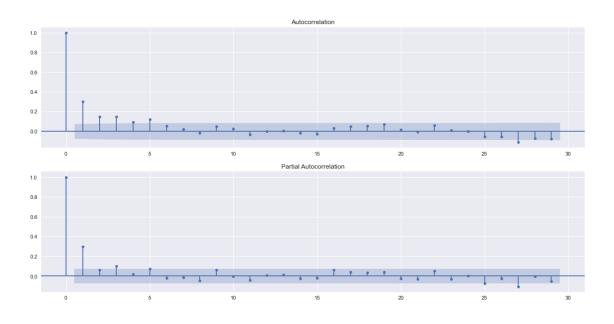
```
[]: plt.style.use("seaborn")
plt.rcParams["figure.figsize"] = (18, 9)

fig, ax = plt.subplots(2,1)

plot_acf(pulsar['Brightness'], ax=ax[0])
plot_pacf(pulsar['Brightness'], ax=ax[1], method="ols")
```

[]:





```
[]: acf(pulsar['Brightness'], nlags=10)
```

```
C:\Users\tajki\anaconda3\lib\site-packages\statsmodels\tsa\stattools.py:667:
    FutureWarning: fft=True will become the default after the release of the 0.12
    release of statsmodels. To suppress this warning, explicitly set fft=False.
      warnings.warn(
[]: array([1.
                         0.29929122,
                                       0.14656878, 0.14948301,
                                                                 0.09384681,
                          0.05493324, 0.02160374, -0.01711482,
             0.11707783.
             0.02563995])
[]: acfpulsar = pd.DataFrame()
     for lag in range(0,11):
         acfpulsar[f"B_lag_{lag}"] = pulsar['Brightness'].shift(lag)
     acfpulsar
[]:
                                         B_lag_3
                                                   B_lag_4
                                                             B_lag_5
                                                                       B_lag_6 \
           B_lag_0
                     B_lag_1
                               B_lag_2
          0.634671
                         NaN
                                             NaN
                                                                 NaN
                                                                           NaN
     0
                                   NaN
                                                       {\tt NaN}
     1
          0.736945
                    0.634671
                                             NaN
                                                       NaN
                                                                 NaN
                                                                           NaN
                                   NaN
     2
         0.693834
                    0.736945
                              0.634671
                                             NaN
                                                       NaN
                                                                 NaN
                                                                           NaN
     3
                              0.736945
                                        0.634671
          1.021866
                    0.693834
                                                       NaN
                                                                 NaN
                                                                           NaN
          0.673845
                    1.021866
                              0.693834 0.736945
                                                                 NaN
                                                                           NaN
                                                  0.634671
     . .
     693 0.776083
                                                  0.152886
                    0.623757
                              0.581248 0.555266
                                                            0.286132
                                                                      0.413354
     694 0.625382
                    0.776083
                              0.623757 0.581248
                                                  0.555266
                                                            0.152886
                                                                      0.286132
     695 0.647559
                    0.625382 0.776083 0.623757
                                                  0.581248
                                                            0.555266
                                                                      0.152886
     696 0.312449
                    0.647559
                              0.625382
                                        0.776083
                                                  0.623757
                                                            0.581248
                                                                      0.555266
     697 0.548353
                    0.312449
                              0.647559
                                        0.625382
                                                  0.776083
                                                            0.623757
                                                                      0.581248
                     B_lag_8
                               B_lag_9
           B_lag_7
                                        B_lag_10
     0
               NaN
                         {\tt NaN}
                                   NaN
                                             NaN
     1
               NaN
                         NaN
                                   NaN
                                             NaN
     2
                                             NaN
               NaN
                         {\tt NaN}
                                   NaN
     3
                                             NaN
               NaN
                         NaN
                                   NaN
     4
               NaN
                         NaN
                                   NaN
                                             NaN
        0.460095
                    0.541486
                              0.346502 0.239302
     693
     694 0.413354
                    0.460095
                              0.541486 0.346502
     695 0.286132
                    0.413354
                              0.460095
                                        0.541486
     696 0.152886 0.286132
                             0.413354 0.460095
     697 0.555266 0.152886 0.286132 0.413354
     [698 rows x 11 columns]
[]: acfpulsar.corr()["B_lag_0"].values
[]: array([1.
                          0.29938402, 0.14710414, 0.15003691, 0.09455452,
```

0.11800036,

0.05537751, 0.02179885, -0.01724535, 0.04863954,

0.02621294])

- 8.0.1 Getting every 5th as per the auto correlation
- 8.0.2 Creating a new set of discrete 100 sets and examining them specifically
- 8.0.3 Further Random testing to move into extensive testing

Getting every 5th as per the auto correlation

```
[]: held5ths = pulsar[pulsar.index % 5 == 0] held5ths
```

[]:	Pulse Number	${ t Brightness}$	${\tt Uncertainty}$	Binary	RollingMeanEmissions5ths	\
0	1	0.634671	0.002761	0	NaN	
5	6	0.676883	0.004763	1	0.760675	
10	11	0.545564	0.003835	0	0.552960	
15	16	0.399571	0.004712	0	0.537775	
20	21	0.707715	0.006011	1	0.665593	
	•••	•••				
675	676	0.618826	0.002507	0	0.634092	
680	681	0.246916	0.004276	0	0.363455	
685	686	0.541486	0.003149	0	0.444185	
690	691	0.555266	0.003657	0	0.373547	
695	696	0.647559	0.003765	0	0.650806	

	RollingMeanEmissions10ths	${\tt Rolling Median Emissions 5 ths}$	\
0	NaN	NaN	
5	NaN	0.693834	
10	0.656817	0.545564	
15	0.545367	0.494655	
20	0.601684	0.723437	
			
675	0.648694	0.630414	
680	0.498773	0.316197	
685	0.403820	0.505084	
690	0.408866	0.413354	
695	0.512176	0.625382	

${\tt Rolling Median Emissions 10 ths}$

0	NaN
5	NaN
10	0.673631
15	0.520201
20	0.610538
• •	•••
675	0.650434
680	0.572860
685	0.344559

```
690 0.436725
695 0.568257
```

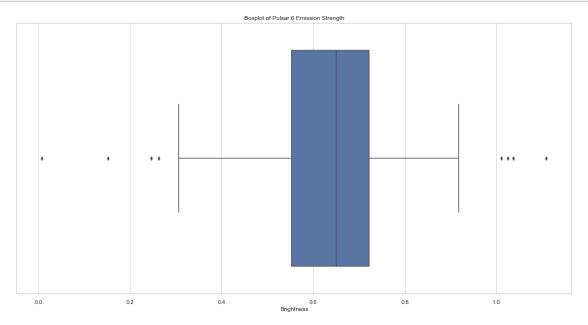
[140 rows x 8 columns]

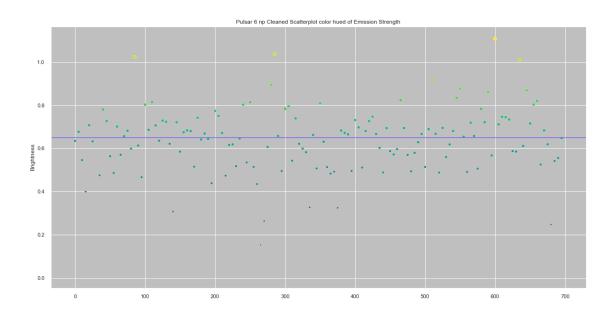
```
[]: medianheld5ths = held5ths["Brightness"].median() medianheld5ths
```

[]: 0.6508051

```
[]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=held5ths["Brightness"]).set_title("Boxplot of Pulsar 6

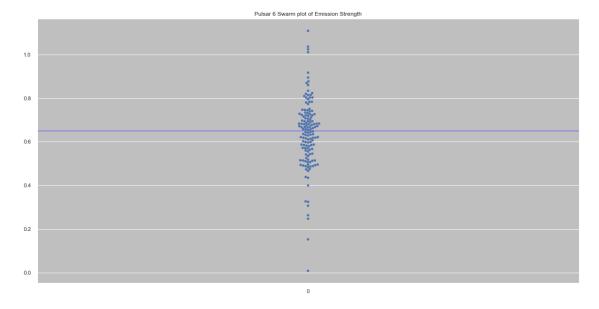
→Emission Strength")
```





```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = plt.axhline( y=0.6508051, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=held5ths["Brightness"], c="blue").set_title('Pulsar 6

→Swarm plot of Emission Strength')
```



```
[]: print(len(held5ths[(held5ths.Brightness > 0.6508051)]))
print(len(held5ths[(held5ths.Brightness < 0.6508051)]))
```

```
70
70
```

```
Randomness testing
```

```
[]: pulsar.Binary
```

```
[]: 0
             0
     1
             1
     2
             1
     3
             1
     4
             1
     693
     694
             0
     695
             0
     696
             0
     697
             0
```