Report

November 3, 2022

```
[]: #currently including any and all Imports that maybe needed for the project.
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
```

1 Importing all CSVs

2 Key for Outcome Column

Absolute = value of 1.0 (Positive) Error = Value of -1.0 - P-values are never negative therefore indicates an error Random = P-values match the random proof Non-Random = P-values match the non-random proof

3 All Emissions

```
[]: AllofAll = pulsar1_all
     pulsar2_all = pulsar2_all.set_axis(['Test Name', 'P-Value', 'Outcome2'], axis =__
      \rightarrow 1, inplace= False)
     pulsar3_all = pulsar3_all.set_axis(['Test Name', 'P-Value', 'Outcome3'], axis =__
      \rightarrow 1, inplace= False)
     pulsar4_all = pulsar4_all.set_axis(['Test Name', 'P-Value', 'Outcome4'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar5_all = pulsar5_all.set_axis(['Test Name', 'P-Value', 'Outcome5'], axis =__
      \rightarrow 1, inplace= False)
     pulsar6_all = pulsar6_all.set_axis(['Test Name', 'P-Value', 'Outcome6'], axis =__
      \hookrightarrow 1, inplace= False)
     AllofAll['Outcome2'] = pulsar2_all['Outcome2'].values
     AllofAll['Outcome3'] = pulsar3_all['Outcome3'].values
     AllofAll['Outcome4'] = ''
     AllofAll['Outcome5'] = pulsar5_all['Outcome5'].values
     AllofAll['Outcome6'] = pulsar6_all['Outcome6'].values
     pulse4 = np.array(pulsar4_all['Outcome4'].values)
     AllofAll['Outcome4'] = pd.Series(pulse4)
     AllofAll = AllofAll.drop(columns='P-Value')
     AllofAll
```

```
[]:
                                           Test Name
                                                                     Outcome2 \
                                                          Outcome
     0
                           Frequency Test (Monobit)
                                                         Absolute
                                                                       Random
     1
                      Frequency Test within a Block
                                                      Non-Random Non-Random
     2
                                            Run Test
                                                      Non-Random Non-Random
     3
                     Longest Run of Ones in a Block
                                                           Random Non-Random
                                                                       Random
     4
                            Binary Matrix Rank Test
                                                           Random
     5
         Discrete Fourier Transform (Spectral) Test
                                                           Random Non-Random
     6
             Non-Overlapping Template Matching Test
                                                      Non-Random
                                                                  Non-Random
     7
                 Overlapping Template Matching Test
                                                      Non-Random
                                                                  Non-Random
     8
                Maurer's Universal Statistical Test
                                                            Error
                                                                        Error
     9
                              Linear Complexity Test
                                                           Random
                                                                       Random
     10
                                       Serial Test A
                                                      Non-Random
                                                                   Non-Random
     11
                                       Serial Test B
                                                      Non-Random
                                                                       Random
     12
                            Approximate Entropy Test
                                                      Non-Random
                                                                   Non-Random
     13
                     Cumulative Sums (Forward) Test
                                                           Random
                                                                       Random
     14
                     Cumulative Sums (Reverse) Test
                                                                       Random
                                                           Random
     15
                    Random Excursions Test State -4
                                                           Random
                                                                       Random
                    Random Excursions Test State -3
                                                                   Non-Random
     16
                                                           Random
     17
                    Random Excursions Test State -2
                                                           Random
                                                                   Non-Random
     18
                    Random Excursions Test State -1
                                                           Random
                                                                       Random
     19
                    Random Excursions Test State +1
                                                           Random
                                                                       Random
     20
                    Random Excursions Test State +2
                                                           Random
                                                                       Random
     21
                    Random Excursions Test State +3
                                                           Random
                                                                       Random
     22
                    Random Excursions Test State +4
                                                           Random
                                                                       Random
```

23	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	-9	Random	${\tt Random}$
24	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-8	Random	${\tt Random}$
25	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-7	Random	${\tt Random}$
26	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-6	Random	${\tt Random}$
27	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-5	Random	${\tt Random}$
28	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-4	Random	${\tt Random}$
29	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-3	Random	${\tt Random}$
30	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-2	Random	${\tt Random}$
31	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	-1	Random	${\tt Random}$
32	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+1	Random	${\tt Random}$
33	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+2	Random	${\tt Random}$
34	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+3	Random	${\tt Random}$
35	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+4	Random	${\tt Random}$
36	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+5	Random	${\tt Random}$
37	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+6	Random	${\tt Random}$
38	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+7	Random	${\tt Random}$
39	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+8	Random	${\tt Random}$
40	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+9	Random	${\tt Random}$

	Outcome3	Outcome4	Outcome5	Outcome6
0	Random	Random	Random	Absolute
1	Random	Non-Random	Random	Random
2	Random	Non-Random	Non-Random	Non-Random
3	Random	Non-Random	Random	Non-Random
4	Random	Random	Random	Error
5	Random	Random	Random	Random
6	Random	Random	Random	Random
7	Random	Random	Random	Error
8	Error	Error	Error	Error
9	Random	Random	Random	Error
10	Random	Non-Random	Random	Random
11	Random	Non-Random	Random	Random
12	Random	Non-Random	Random	Absolute
13	Random	Non-Random	Random	Random
14	Random	Non-Random	Random	Random
15	Random	Random	Non-Random	Random
16	Random	Random	Random	Random
17	Random	Random	Random	Random
18	Random	Random	Random	Random
19	Random	Random	Random	Random
20	Random	Random	Random	Random
21	Random	Random	Random	Random
22	Random	Random	Random	Non-Random
23	Random	Random	Random	Random
24	Random	Random	Random	Random
25	Random	Random	Random	Random
26	Random	Random	Random	Random

Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Absolute	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
	Random	Random NaN	Random NaN Random Random NaN Random Random NaN Absolute Random NaN Random

4 Every 5th

```
[]: Allof5th = pulsar1_5th
     pulsar2_5th = pulsar2_5th.set_axis(['Test Name', 'P-Value', 'Outcome2'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar3_5th = pulsar3_5th.set_axis(['Test Name', 'P-Value', 'Outcome3'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar4_5th = pulsar4_5th.set_axis(['Test Name', 'P-Value', 'Outcome4'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar5_5th = pulsar5_5th.set_axis(['Test Name', 'P-Value', 'Outcome5'], axis =__
      \hookrightarrow1, inplace= False)
     pulsar6 5th = pulsar6 5th.set axis(['Test Name', 'P-Value', 'Outcome6'], axis = []
      \hookrightarrow 1, inplace= False)
     Allof5th['Outcome2'] = ''
     Allof5th['Outcome3'] = ''
     Allof5th['Outcome4'] = ''
     Allof5th['Outcome5'] = ''
     Allof5th['Outcome6'] = ''
     pulse2 = np.array(pulsar2_5th['Outcome2'].values)
     Allof5th['Outcome2'] = pd.Series(pulse2)
     pulse3 = np.array(pulsar3_5th['Outcome3'].values)
     Allof5th['Outcome3'] = pd.Series(pulse3)
     pulse4 = np.array(pulsar4_5th['Outcome4'].values)
     Allof5th['Outcome4'] = pd.Series(pulse4)
     pulse5 = np.array(pulsar5_5th['Outcome5'].values)
     Allof5th['Outcome5'] = pd.Series(pulse5)
     pulse6 = np.array(pulsar6_5th['Outcome6'].values)
     Allof5th['Outcome6'] = pd.Series(pulse6)
     Allof5th = Allof5th.drop(columns='P-Value')
     Allof5th
```

r 3			m . N		0 . 0	
[]:			Test Name	Outcome	Outcome2	\
0			Test (Monobit)	Random	Random	
1		Frequency lest	within a Block	Random	Random	
2		I t D f (Run Test	Random	Random	
3		Longest Run of		Random	Random	
4	D	•	atrix Rank Test	Random	Random	
5		ourier Transform	_	Random	Random	
6		erlapping Template	_	Random	Random	
7		erlapping Template	_	Random	Random	
8	Maui	rer's Universal S		Error	Error	
9		Linear	Complexity Test	Random	Random	
10			Serial Test A	Random	Random	
11			Serial Test B	Random	Random	
12			te Entropy Test	Non-Random	Non-Random	
13		Cumulative Sums		Random	Random	
14		Cumulative Sums		Random	Random	
15		Random Excursion		Random	Random	
16		Random Excursion		Random	Random	
17		Random Excursion		Random	Random	
18		Random Excursion		Random	Random	
19		Random Excursion		Random	Non-Random	
20		Random Excursion		Non-Random	Non-Random	
21		Random Excursion		Non-Random	Random	
22		Random Excursion		Random	Random	
23		Exursions Varian		Random	Random	
24		Exursions Varian		Random	Random	
25		Exursions Varian		Random	Random	
26		Exursions Varian		Non-Random	Random	
27		Exursions Varian		Non-Random	Random	
28		Exursions Varian		Non-Random	Random	
29		Exursions Varian		Non-Random	Random	
30		Exursions Varian		Random	Random	
31	Random	Exursions Varian	t Test State +9	Random	Random	
	Outcome3	Outcome4 Out	come5 Outcome6			
0	Random		andom Random			
1	Random		andom Random			
2	Random		andom Random			
3	Random		andom Random			
4	Error		Error Error			
5	Non-Random		andom Random			
6	Random		olute Random			
7	Error		Error Error			
8	Error		Error Error			
9	Error		Error Error			
10	Random		andom Random			
11	Random	Non-Random Ra	andom Random			

12	Absolute	Absolute	Absolute	Absolute
13	Random	Non-Random	Random	Random
14	Random	Non-Random	Random	Random
15	Random	Random	Random	Random
16	Random	Random	Random	Random
17	Random	Random	Random	Random
18	Random	Random	Random	Random
19	Random	Non-Random	Random	Random
20	Random	Non-Random	Random	Random
21	Random	Non-Random	Random	Random
22	Random	Non-Random	Random	Random
23	Random	Random	Random	Random
24	Random	Non-Random	Random	Random
25	Random	Non-Random	Random	Random
26	Random	Non-Random	Random	Random
27	Random	Random	Random	Random
28	Random	Random	Random	Random
29	Random	Random	Random	Random
30	Random	Random	Random	Random
31	Random	Random	Random	Random

5 Edge Case Pulsar analysis

```
[]: pulsar4_10th = pulsar4_10th.drop(columns='P-Value')
pulsar4_10th
```

Outcome	Test Name]:	[]
Random	Frequency Test (Monobit)	0	
Random	Frequency Test within a Block	1	
Non-Random	Run Test	2	
Random	Longest Run of Ones in a Block	3	
Error	Binary Matrix Rank Test	4	
Random	Discrete Fourier Transform (Spectral) Test	5	
Absolute	Non-Overlapping Template Matching Test	6	
Error	Overlapping Template Matching Test	7	
Error	Maurer's Universal Statistical Test	8	
Error	Linear Complexity Test	9	
Non-Random	Serial Test A	10	
Non-Random	Serial Test B	11	
Absolute	Approximate Entropy Test	12	
Random	Cumulative Sums (Forward) Test	13	
Random	Cumulative Sums (Reverse) Test	14	
Random	Random Excursions Test State -4	15	
Random	Random Excursions Test State -3	16	
Random	Random Excursions Test State -2	17	
Random	Random Excursions Test State -1	18	

19		Random Exc	cursions	Test	${\tt State}$	+1	Random
20		Random Exc	cursions	Test	${\tt State}$	+2	Random
21		Random Exc	cursions	Test	${\tt State}$	+3	Random
22		Random Exc	cursions	Test	${\tt State}$	+4	Random
23	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-3	Random
24	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-2	Random
25	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-1	Random
26	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+1	Absolute
27	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+2	Random
28	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+3	Random
29	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+4	Random
30	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+5	Random
31	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+6	Random
32	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+7	Random
33	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+8	Random
34	Random	Exursions	Variant	Test	State	+9	Random

6 Looking at Pulsars with RandTest Lib

True

[]: R	andTestResults	8	
[]:	RandTestAll	RandTest5ths	RandTestElse
0	True	True	Null
1	True	True	Null
2	True	True	Null
3	True	True	True
4	True	True	Null

Null

6.1 Analysis of RandTest Results

True

5

The RandTest suite uses an algorithm called "exponentially-decaying moment prediction" to determine the net deviation between predicted and actual elements in sequences. It evaluated whether or not a sequence of numbers are random or not.

It has a stated accuracy of 99.85% for non random sequences and 96.82% for random sequences. This means the test will typically sustain a high degree of accuracy especially at a 0.05 cut off. But does falter at meeting the cyber security standard of 0.01. This means we will use this in conjunction with the overall statement from the NIST suite on the specific tests as extra evidence to prove or disprove randomness.

In the case above we can clearly see that RandTest labels all binary sequences as random with no prediction this means we can confidently say with 96% certainty of this truth, this meets most standards of prediction. But fails to meet the industry standard of 99% accuracy with cybersecurity.

7 Important results from NIST

The first five tests are interpreted as the most important.

1. The Frequency (Monobit) Test is the first test in the NIST suite, and the remainder of the tests are dependent upon this test retaining the null hypothesis. The test determines the closeness of the fraction of 1's to 1/2. For the test to pass, the number of 1's and 0's in the sequence should be similar.

For the datasets containing every observation, the binary sequence has been created based on the median of the dataset, so by the nature of median (the middle value), the number of 0's and 1's will be equal (or different by 1 in the case of an odd number of observations), hence running the test on these sequences will return a p-value of 1 (or very close to 1 for odd number of observations), providing strong evidence to retain the null hypothesis, the expected outcome.

Of more interest is the same test on the datasets of every 5th observation (pulsars 1, 2, 3, 4,5, 6) and the test on every 10th observation (pulsar 4), where there isn't the same guarantee of an equal amount of 0's and 1's. Analysing the results of each test, every number sequence passes. The lowest p-value observed is 0.096872 for pulsar 1 for every 5th observation, however it is still well above the 0.01 significance level. Now that each dataset has passed this test, further testing can be undertaken.

2. The next test, Frequency Test within a Block, applies a similar logic to the previous test, but instead tests the proportion of 1's in a bit block of length M, expecting the frequency of 1's to be close to M/2 for the test to pass.

For the datasets with every observation, pulsars 1,2 and 4 fail this test (extremely small p-values). On the other hand, pulsars 3 and 6 provide extremely strong evidence (high p-value) that the fraction of 1's with the M length bit blocks is close to 1/2. While pulsar 5 has provides moderate evidence, p-value = 0.0398, just over the alpha of 0.01, that there is an equal proportion of 1's and 0's.

Looking to the datasets with every 5th observation, pulsars 1,2,3,5 and 6 pass with fairly strong evidence, while pulsar 4 fails. Then for pulsar 4 with every 10th observation it just passes with a p-value of 0.0216.

3. The Runs Test focuses on the number of runs in a sequence, where a run is the number of identical bits in a row. E.g., a run of length 25 is a sequence of 25 zeroes (or ones) in a row. The test determines if the number of runs is as would be expected in a random sequence.

For datasets containing every observation, pulsar 1,2,4,5 and 6 fail to pass this test, while pulsar 3 passes.

For the datasets on every 5th observation, there is a large shift in the number of sequences that pass, pulsar 1, 2, 3, 5 and 6 all pass, while only pulsar 4 fails. For every 10th observation on pulsar 4 the test also fails.

4. The Test for the Longest Run of Ones in a Block provides a similar approach as the previous Runs Test; however, it instead focuses on the longest run of ones within M-bit blocks and compares it with what would be expected of a random sequence.

For the datasets containing all observations, pulsar 1, 3 and 5 passes pulsar 2, 4 and 6 fails.

When we look at the datasets containing every 5th observation, all six pulsars pass. In addition, the test on every 10th observation of pulsar 4 also passes.

5. The fifth test is the Binary Matric Rank Test, this test breaks the binary sequence down into 32x32 matrices. Then it tests for linear dependence within the matrices. Given the nature

of this test, the datasets need to be quite large for the test to be able to run, some of the datasets, especially those with every 5th or 10th observation may not have had enough data to run. If this situation occurs, the test will return a p-value of -1, which is an indicator that the test was unable to run, based on too little data.

For pulsars with every observation included pulsars 1, 2, 3, 4 and 5 pass and pulsar 6 doesn't have enough data to run (hence p-value = -1).

For the datasets containing every 5th observation, 1 and 2 pass while pulsars 3, 4, 5 and 6 can't run due to too little data.

7.1 Summary Table of these 5 important tests per test

7.1.1 Pulsar 1 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Fail
Runs Test	Fail
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	Pass
Total	3/5

7.1.2 Pulsar 1 5ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	Pass
Total	5/5

7.1.3 Pulsar 2 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Fail
Runs Test	Fail
Logest Run of Ones in a Block	Fail
Binary Matrix Rank Test	Pass
Total	2/5

7.1.4 Pulsar 2 5ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	Pass
Total	5/5

7.1.5 Pulsar 3 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	Pass
Total	5/5

7.1.6 Pulsar 3 5ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	N/A
Total	4/5

7.1.7 Pulsar 4 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Fail
Runs Test	Fail
Logest Run of Ones in a Block	Fail
Binary Matrix Rank Test	Pass
Total	2/5

7.1.8 Pulsar 4 5ths

Test	Result
Frequency Test (Monobit)	Pass

Test	Result
Frequencey Test within a Block	Fail
Runs Test	Fail
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	N/A
Total	2/5

7.1.9 Pulsar 4 10ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Fail
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	N/A
Total	3/5

7.1.10 Pulsar 5 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Fail
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	Pass
Total	4/5

7.1.11 Pulsar 5 5ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	N/A
Total	4/5

7.1.12 Pulsar 6 ALL

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass

Result
Fail
Fail
N/A
2/5

7.1.13 Pulsar 6 5ths

Test	Result
Frequency Test (Monobit)	Pass
Frequencey Test within a Block	Pass
Runs Test	Pass
Logest Run of Ones in a Block	Pass
Binary Matrix Rank Test	N/A
Total	4/5

8 Final Summary of Data

We can see here that the majority of the tests passed the first 2 most crucial tests except for Pulsar 4 which immediately disqualifies it from further evaluation. The same expectation can be said for the Pulsar binary datasets that do fail the Runs Test. However, Pulsar 5 is seen as a bit of an exception due to the fact that it is the only pulsar that fails the Runs test but none of the other tests outside of the Random Excursions test at state -4. We pass 5 as random due to the sheer weighting of all the other evidence stacked against the runs test, this strongly indicates that the pulsar 5 should be more deeply investigate for a true determination.

We can come to the summary conclusion that for all emissions, only Pulsar 3 is truly random and Pulsar 5 is seen to be random pending further investigation.

For Auto-Correlated observations at every 5th we can determine that the random pulsars are all of them except for 4 so this means Pulsars 1,2,3,5,6 at every 5th emission is random.

At ACF 10th lags we find that the Pulsar 4 observations indeed become random, but due to the distance from the original emissions it is still seen as a non-random pulsar with some underlying structure uniforming it.

9 Appendix Individual Table Results

You can also find the individual results in the pulsarBinaryDataResults file. With each txt corresponding with each test and their P-values.

Note most P-values below were reformatted by the excel program to not be a decimal

9.1 Pulsar 1 All

[]: pulsar1_all

[]:		Test Name	P-Value	Outcome	\
	0	Frequency Test (Monobit)	1.000000e+00	Absolute	
	1	Frequency Test within a Block	9.050000e-08	Non-Random	
	2	Run Test	3.353164e-03	Non-Random	
	3	Longest Run of Ones in a Block	4.782901e-02	Random	
	4	Binary Matrix Rank Test	1.020085e-01	Random	
	5	Discrete Fourier Transform (Spectral) Test	5.765222e-01	Random	
	6	Non-Overlapping Template Matching Test	4.860000e-07	Non-Random	
	7	Overlapping Template Matching Test	5.365440e-04	Non-Random	
	8	Maurer's Universal Statistical Test	-1.000000e+00	Error	
	9	Linear Complexity Test	8.177284e-01	Random	
	10	Serial Test A	2.420000e-19	Non-Random	
	11	Serial Test B	1.600000e-06	Non-Random	
	12	Approximate Entropy Test	1.840000e-13	Non-Random	
	13	Cumulative Sums (Forward) Test	6.250000e-01	Random	
	14	Cumulative Sums (Reverse) Test	6.250000e-01	Random	
	15	Random Excursions Test State -4	1.210000e-01	Random	
	16	Random Excursions Test State -3	3.158609e-01	Random	
	17	Random Excursions Test State -2	3.590000e-01	Random	
	18	Random Excursions Test State -1	7.280000e-01	Random	
	19	Random Excursions Test State +1	2.730000e-01	Random	
	20	Random Excursions Test State +2	1.640000e-01	Random	
	21	Random Excursions Test State +3	3.070000e-01	Random	
	22	Random Excursions Test State +4	1.160000e-01	Random	
	23	Random Exursions Variant Test State -9	1.503674e-01	Random	
	24	Random Exursions Variant Test State -8	2.508288e-01	Random	
	25	Random Exursions Variant Test State -7	2.850494e-01	Random	
	26	Random Exursions Variant Test State -6	2.685964e-01	Random	
	27	Random Exursions Variant Test State -5	4.008621e-01	Random	
	28	Random Exursions Variant Test State -4	7.261831e-01	Random	
	29	Random Exursions Variant Test State -3	9.471395e-01	Random	
	30	Random Exursions Variant Test State -2	7.808785e-01	Random	
	31	Random Exursions Variant Test State -1	9.114677e-01	Random	
	32	Random Exursions Variant Test State +1	7.110000e-01	Random	
	33	Random Exursions Variant Test State +2	7.320000e-01	Random	
	34	Random Exursions Variant Test State +3	6.430000e-01	Random	
	35	Random Exursions Variant Test State +4	5.100000e-01	Random	
	36	Random Exursions Variant Test State +5	8.140000e-01	Random	
	37	Random Exursions Variant Test State +6	9.820000e-01	Random	
	38	Random Exursions Variant Test State +7	9.340000e-01	Random	
	39	Random Exursions Variant Test State +8	6.670000e-01	Random	
	40	Random Exursions Variant Test State +9	7.260000e-01	Random	

Outcome2 Outcome3 Outcome4 Outcome5 Outcome6

0	Random	Random	Random	Random	Absolute
1	Non-Random	Random	Non-Random	Random	Random
2	Non-Random	Random	Non-Random	Non-Random	Non-Random
3	Non-Random	Random	Non-Random	Random	Non-Random
4	Random	Random	Random	Random	Error
5	Non-Random	Random	Random	Random	Random
6	Non-Random	Random	Random	Random	Random
7	Non-Random	Random	Random	Random	Error
8	Error	Error	Error	Error	Error
9	Random	Random	Random	Random	Error
10	Non-Random	Random	Non-Random	Random	Random
11	Random	Random	Non-Random	Random	Random
12	Non-Random	Random	Non-Random	Random	Absolute
13	Random	Random	Non-Random	Random	Random
14	Random	Random	Non-Random	Random	Random
15	Random	Random	Random	Non-Random	Random
16	Non-Random	Random	Random	Random	Random
17	Non-Random	Random	Random	Random	Random
18	Random	Random	Random	Random	Random
19	Random	Random	Random	Random	Random
20	Random	Random	Random	Random	Random
21	Random	Random	Random	Random	Random
22	Random	Random	Random	Random	Non-Random
23	Random	Random	Random	Random	Random
24	Random	Random	Random	Random	Random
25	Random	Random	Random	Random	Random
26	Random	Random	Random	Random	Random
27	Random	Random	Random	Random	Random
28	Random	Random	Random	Random	Random
29	Random	Random	Random	Random	Random
30	Random	Random	Random	Random	Random
31	Random	Random	Random	Random	Random
32	Random	Random	Random	Random	Random
33	Random	Random	NaN	Random	Random
34	Random	Random	NaN	Random	Random
35	Random	Random	NaN	Absolute	Random
36	Random	Random	NaN	Random	Random
37	${\tt Random}$	Random	NaN	Random	Random
38	${\tt Random}$	Random	NaN	Random	Random
39	Random	Random	NaN	Random	Random
40	Random	Random	NaN	Random	Random

9.2 Pulsar 1 5ths

[]: pulsar1_5th

```
[]:
                                             Test Name
                                                         P-Value
                                                                      Outcome
     0
                            Frequency Test (Monobit)
                                                        0.096872
                                                                       Random
     1
                       Frequency Test within a Block
                                                        0.273011
                                                                       Random
     2
                                                        0.295998
                                                                       Random
                                             Run Test
     3
                                                                       Random
                      Longest Run of Ones in a Block
                                                        0.143727
     4
                             Binary Matrix Rank Test
                                                                       Random
                                                        0.858290
     5
         Discrete Fourier Transform (Spectral) Test
                                                         0.453695
                                                                       Random
     6
             Non-Overlapping Template Matching Test
                                                        0.424735
                                                                       Random
     7
                  Overlapping Template Matching Test
                                                        0.418207
                                                                       Random
                                                       -1.000000
     8
                 Maurer's Universal Statistical Test
                                                                        Error
     9
                               Linear Complexity Test
                                                        0.757153
                                                                       Random
                                        Serial Test A
     10
                                                        0.148533
                                                                       Random
                                        Serial Test B
     11
                                                        0.445237
                                                                       Random
                             Approximate Entropy Test
     12
                                                        0.000145
                                                                   Non-Random
     13
                      Cumulative Sums (Forward) Test
                                                         0.072222
                                                                       Random
     14
                      Cumulative Sums (Reverse) Test
                                                        0.193743
                                                                       Random
     15
                     Random Excursions Test State -4
                                                        0.997903
                                                                       Random
     16
                     Random Excursions Test State -3
                                                                       Random
                                                        0.995330
     17
                     Random Excursions Test State -2
                                                        0.984748
                                                                       Random
     18
                     Random Excursions Test State -1
                                                        0.849145
                                                                       Random
                     Random Excursions Test State +1
                                                        0.156236
                                                                       Random
     19
     20
                     Random Excursions Test State +2
                                                                   Non-Random
                                                        0.000354
     21
                     Random Excursions Test State +3
                                                        0.000475
                                                                   Non-Random
     22
                     Random Excursions Test State +4
                                                                       Random
                                                        0.369569
     23
             Random Exursions Variant Test State +1
                                                                       Random
                                                        0.317311
     24
             Random Exursions Variant Test State +2
                                                        0.386476
                                                                       Random
     25
             Random Exursions Variant Test State +3
                                                                       Random
                                                        0.013906
     26
             Random Exursions Variant Test State +4
                                                        0.000670
                                                                   Non-Random
     27
             Random Exursions Variant Test State +5
                                                                   Non-Random
                                                         0.007661
     28
             Random Exursions Variant Test State +6
                                                         0.000526
                                                                   Non-Random
     29
             Random Exursions Variant Test State +7
                                                        0.002282
                                                                   Non-Random
             Random Exursions Variant Test State +8
     30
                                                        0.038867
                                                                       Random
     31
             Random Exursions Variant Test State +9
                                                        0.015293
                                                                       Random
           Outcome2
                        Outcome3
                                     Outcome4
                                                Outcome5
                                                          Outcome6
     0
                                                             Random
             Random
                          Random
                                       Random
                                                  Random
     1
             Random
                                                             Random
                          Random
                                   Non-Random
                                                  Random
     2
             Random
                          Random
                                   Non-Random
                                                  Random
                                                             Random
     3
             Random
                                       Random
                                                  Random
                                                             Random
                          Random
     4
             Random
                                        Error
                                                              Error
                           Error
                                                   Error
     5
             Random
                      Non-Random
                                       Random
                                                  Random
                                                             Random
     6
             Random
                                                             Random
                          Random
                                     Absolute
                                                Absolute
     7
             Random
                                        Error
                                                   Error
                                                              Error
                           Error
     8
              Error
                           Error
                                        Error
                                                   Error
                                                              Error
     9
             Random
                           Error
                                        Error
                                                   Error
                                                              Error
     10
             Random
                          Random
                                   Non-Random
                                                  Random
                                                             Random
     11
             Random
                          Random
                                   Non-Random
                                                  Random
                                                             Random
```

12	Non-Random	Absolute	Absolute	Absolute	Absolute
13	Random	Random	Non-Random	Random	Random
14	Random	Random	Non-Random	Random	Random
15	Random	Random	Random	Random	Random
16	Random	Random	Random	Random	Random
17	Random	Random	Random	Random	Random
18	Random	Random	Random	Random	Random
19	Non-Random	Random	Non-Random	Random	Random
20	Non-Random	Random	Non-Random	Random	Random
21	Random	Random	Non-Random	Random	Random
22	Random	Random	Non-Random	Random	Random
23	Random	Random	Random	Random	Random
24	Random	Random	Non-Random	Random	Random
25	Random	Random	Non-Random	Random	Random
26	Random	Random	Non-Random	Random	Random
27	Random	Random	Random	Random	Random
28	Random	Random	Random	Random	Random
29	Random	Random	Random	Random	Random
30	Random	Random	Random	Random	Random
31	Random	Random	Random	Random	Random

9.3 Pulsar 2 All

[]: pulsar2_all

г 1.	Test Name	P-Value	Outcome2
[]:	2 2 2 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3		
0	Frequency Test (Monobit)	9.933346e-01	Random
1	Frequency Test within a Block	9.910000e-12	Non-Random
2	Run Test	3.200000e-94	Non-Random
3	Longest Run of Ones in a Block	3.810000e-36	Non-Random
4	Binary Matrix Rank Test	2.570000e-01	Random
5	Discrete Fourier Transform (Spectral) Test	6.140000e-05	Non-Random
6	Non-Overlapping Template Matching Test	3.830000e-26	Non-Random
7	Overlapping Template Matching Test	4.630000e-13	Non-Random
8	Maurer's Universal Statistical Test	-1.000000e+00	Error
9	Linear Complexity Test	5.807496e-01	Random
10	Serial Test A	2.350000e-17	Non-Random
11	Serial Test B	9.520000e-01	Random
12	Approximate Entropy Test	8.310000e-34	Non-Random
13	Cumulative Sums (Forward) Test	5.600000e-01	Random
14	Cumulative Sums (Reverse) Test	5.530000e-01	Random
15	Random Excursions Test State -4	2.050000e-01	Random
16	Random Excursions Test State -3	7.680000e-03	Non-Random
17	Random Excursions Test State -2	1.610000e-03	Non-Random
18	Random Excursions Test State -1	1.780000e-02	Random
19	Random Excursions Test State +1	3.980000e-01	Random
20	Random Excursions Test State +2	4.020000e-01	Random

```
21
               Random Excursions Test State +3
                                                  1.520000e-01
                                                                    Random
22
               Random Excursions Test State +4
                                                  4.760000e-01
                                                                    Random
23
        Random Exursions Variant Test State -9
                                                  8.054226e-01
                                                                    Random
24
        Random Exursions Variant Test State -8
                                                  8.514120e-01
                                                                    Random
25
        Random Exursions Variant Test State -7
                                                                    Random
                                                  9.198637e-01
        Random Exursions Variant Test State -6
26
                                                  9.651054e-01
                                                                    Random
27
        Random Exursions Variant Test State -5
                                                                    Random
                                                  9.037602e-01
        Random Exursions Variant Test State -4
28
                                                  6.808479e-01
                                                                    Random
29
        Random Exursions Variant Test State -3
                                                                    Random
                                                  5.164123e-01
30
        Random Exursions Variant Test State -2
                                                                    Random
                                                  3.147768e-01
31
        Random Exursions Variant Test State -1
                                                  1.467931e-01
                                                                    Random
32
        Random Exursions Variant Test State +1
                                                  3.100000e-01
                                                                    Random
33
        Random Exursions Variant Test State +2
                                                  7.060000e-01
                                                                    Random
34
        Random Exursions Variant Test State +3
                                                  8.460000e-01
                                                                    Random
        Random Exursions Variant Test State +4
35
                                                  9.560000e-01
                                                                    Random
36
        Random Exursions Variant Test State +5
                                                  7.170000e-01
                                                                    Random
37
        Random Exursions Variant Test State +6
                                                                    Random
                                                  8.100000e-01
38
        Random Exursions Variant Test State +7
                                                  9.680000e-01
                                                                    Random
39
        Random Exursions Variant Test State +8
                                                  9.550000e-01
                                                                    Random
40
        Random Exursions Variant Test State +9
                                                  8.880000e-01
                                                                    Random
```

9.4 Pulsar 2 5ths

[]: pulsar2_5th

[]:	Test Name	P-Value	Outcome2
0	Frequency Test (Monobit)	0.736699	Random
1	Frequency Test within a Block	0.753000	Random
2	Run Test	0.018694	Random
3	Longest Run of Ones in a Block	0.092363	Random
4	Binary Matrix Rank Test	0.481248	Random
5	Discrete Fourier Transform (Spectral) Test	0.565809	Random
6	Non-Overlapping Template Matching Test	0.526000	Random
7	Overlapping Template Matching Test	0.248594	Random
8	Maurer's Universal Statistical Test	-1.000000	Error
9	Linear Complexity Test	0.543779	${\tt Random}$
10	Serial Test A	0.123000	Random
11	Serial Test B	0.224000	Random
12	Approximate Entropy Test	0.000025	Non-Random
13	Cumulative Sums (Forward) Test	0.604000	Random
14	Cumulative Sums (Reverse) Test	0.904000	Random
15	Random Excursions Test State -4	0.332000	Random
16	Random Excursions Test State -3	0.161000	Random
17	Random Excursions Test State -2	0.625000	Random
18	Random Excursions Test State -1	0.719000	Random
19	Random Excursions Test State +1	0.008430	Non-Random
20	Random Excursions Test State +2	0.000040	Non-Random

```
21
               Random Excursions Test State +3
                                                                 Random
                                                  0.152000
22
               Random Excursions Test State +4
                                                                 Random
                                                  0.383000
23
        Random Exursions Variant Test State -5
                                                  0.226919
                                                                 Random
24
        Random Exursions Variant Test State -4
                                                  0.237548
                                                                 Random
        Random Exursions Variant Test State -3
                                                                 Random
25
                                                  0.263552
26
        Random Exursions Variant Test State -2
                                                                 Random
                                                  0.193931
27
        Random Exursions Variant Test State -1
                                                                 Random
                                                  0.133614
28
        Random Exursions Variant Test State +1
                                                  0.261000
                                                                 Random
29
        Random Exursions Variant Test State +2
                                                                 Random
                                                  0.516000
30
        Random Exursions Variant Test State +3
                                                                 Random
                                                  0.576000
        Random Exursions Variant Test State +4
31
                                                  0.450000
                                                                 Random
32
        Random Exursions Variant Test State +5
                                                                 Random
                                                  0.739000
33
        Random Exursions Variant Test State +6
                                                  0.792000
                                                                 Random
34
        Random Exursions Variant Test State +7
                                                  0.533000
                                                                 Random
        Random Exursions Variant Test State +8
35
                                                  0.561000
                                                                 Random
36
        Random Exursions Variant Test State +9
                                                  0.649000
                                                                 Random
```

9.5 Pulsar 3 All

[]: pulsar3_all

```
[]:
                                            Test Name
                                                         P-Value Outcome3
                            Frequency Test (Monobit)
     0
                                                        0.978133
                                                                    Random
     1
                       Frequency Test within a Block
                                                        0.843000
                                                                    Random
     2
                                             Run Test
                                                        0.051600
                                                                    Random
     3
                      Longest Run of Ones in a Block
                                                        0.206000
                                                                    Random
     4
                             Binary Matrix Rank Test
                                                                    Random
                                                        0.694000
     5
         Discrete Fourier Transform (Spectral) Test
                                                        0.655000
                                                                    Random
     6
             Non-Overlapping Template Matching Test
                                                        0.771000
                                                                    Random
     7
                  Overlapping Template Matching Test
                                                        0.887000
                                                                    Random
                Maurer's Universal Statistical Test
     8
                                                       -1.000000
                                                                    Error
     9
                              Linear Complexity Test
                                                        0.320837
                                                                    Random
     10
                                        Serial Test A
                                                                    Random
                                                        0.876000
     11
                                        Serial Test B
                                                        0.553000
                                                                   Random
     12
                            Approximate Entropy Test
                                                        0.767000
                                                                   Random
                      Cumulative Sums (Forward) Test
     13
                                                                   Random
                                                        0.943000
     14
                      Cumulative Sums (Reverse) Test
                                                        0.926000
                                                                   Random
                     Random Excursions Test State -4
     15
                                                        0.339000
                                                                   Random
     16
                     Random Excursions Test State -3
                                                        0.590000
                                                                    Random
     17
                     Random Excursions Test State -2
                                                                    Random
                                                        0.573000
     18
                     Random Excursions Test State -1
                                                        0.590000
                                                                    Random
     19
                     Random Excursions Test State +1
                                                                    Random
                                                        0.491000
     20
                     Random Excursions Test State +2
                                                        0.565000
                                                                    Random
     21
                     Random Excursions Test State +3
                                                                    Random
                                                        0.448000
     22
                     Random Excursions Test State +4
                                                        0.643000
                                                                    Random
             Random Exursions Variant Test State -9
     23
                                                        0.215330
                                                                    Random
     24
             Random Exursions Variant Test State -8
                                                        0.180652
                                                                    Random
```

```
25
        Random Exursions Variant Test State -7
                                                  0.150421
                                                             Random
26
        Random Exursions Variant Test State -6
                                                  0.174968
                                                             Random
27
        Random Exursions Variant Test State -5
                                                  0.232254
                                                             Random
28
        Random Exursions Variant Test State -4
                                                  0.286278
                                                             Random
29
        Random Exursions Variant Test State -3
                                                  0.322716
                                                             Random
        Random Exursions Variant Test State -2
30
                                                  0.332797
                                                             Random
31
        Random Exursions Variant Test State -1
                                                             Random
                                                  0.541866
        Random Exursions Variant Test State +1
32
                                                  0.493000
                                                             Random
33
        Random Exursions Variant Test State +2
                                                  0.509000
                                                             Random
34
        Random Exursions Variant Test State +3
                                                             Random
                                                  0.759000
        Random Exursions Variant Test State +4
35
                                                  0.863000
                                                             Random
36
        Random Exursions Variant Test State +5
                                                  0.780000
                                                             Random
37
        Random Exursions Variant Test State +6
                                                  0.629000
                                                             Random
38
        Random Exursions Variant Test State +7
                                                  0.410000
                                                             Random
        Random Exursions Variant Test State +8
39
                                                  0.288000
                                                             Random
        Random Exursions Variant Test State +9
40
                                                  0.309000
                                                             Random
```

9.6 Pulsar 3 5ths

[]: pulsar3_5th

[]:		Test Name P-Value Outcome3
	0	Frequency Test (Monobit) 0.951201 Random
	1	Frequency Test within a Block 0.925000 Random
	2	Run Test 0.126000 Random
	3	Longest Run of Ones in a Block 0.957000 Random
	4	Binary Matrix Rank Test -1.000000 Error
	5	Discrete Fourier Transform (Spectral) Test 0.003660 Non-Random
	6	Non-Overlapping Template Matching Test 1.000000 Random
	7	Overlapping Template Matching Test -1.000000 Error
	8	Maurer's Universal Statistical Test -1.000000 Error
	9	Linear Complexity Test -1.000000 Error
	10	Serial Test A 0.499000 Random
	11	Serial Test B 0.499000 Random
	12	Approximate Entropy Test 1.000000 Absolute
	13	Cumulative Sums (Forward) Test 0.763000 Random
	14	Cumulative Sums (Reverse) Test 0.705000 Random
	15	Random Excursions Test State -4 0.886000 Random
	16	Random Excursions Test State -3 0.347000 Random
	17	Random Excursions Test State -2 0.735000 Random
	18	Random Excursions Test State -1 0.700000 Random
	19	Random Excursions Test State +1 0.659000 Random
	20	Random Excursions Test State +2 0.258000 Random
	21	Random Excursions Test State +3 0.018600 Random
	22	Random Excursions Test State +4 0.783000 Random
	23	Random Exursions Variant Test State -9 0.490920 Random
	24	Random Exursions Variant Test State -8 0.463355 Random

```
25
        Random Exursions Variant Test State -7
                                                  0.410205
                                                                 Random
26
        Random Exursions Variant Test State -6
                                                  0.413686
                                                                 Random
27
        Random Exursions Variant Test State -5
                                                  0.438578
                                                                 Random
        Random Exursions Variant Test State -4
28
                                                  0.406813
                                                                 Random
29
        Random Exursions Variant Test State -3
                                                  0.603332
                                                                 Random
        Random Exursions Variant Test State -2
30
                                                  0.765594
                                                                 Random
31
        Random Exursions Variant Test State -1
                                                                 Random
                                                  0.605577
        Random Exursions Variant Test State +1
32
                                                  0.699000
                                                                 Random
33
        Random Exursions Variant Test State +2
                                                  0.502000
                                                                 Random
34
        Random Exursions Variant Test State +3
                                                  0.326000
                                                                 Random
35
        Random Exursions Variant Test State +4
                                                  0.262000
                                                                 Random
        Random Exursions Variant Test State +5
36
                                                  0.263000
                                                                 Random
37
        Random Exursions Variant Test State +6
                                                  0.259000
                                                                 Random
38
                                             NaN
                                                       NaN
                                                                    NaN
39
                                             NaN
                                                       NaN
                                                                    NaN
40
                                             NaN
                                                       NaN
                                                                    NaN
```

9.7 Pulsar 4 All

[]: pulsar4_all

[]:		Test Name	P-Value	Outcome4
	0	Frequency Test (Monobit)	9.812939e-01	Random
	1	Frequency Test within a Block	3.910000e-53	Non-Random
	2	Run Test	3.420000e-21	Non-Random
	3	Longest Run of Ones in a Block	3.930000e-08	Non-Random
	4	Binary Matrix Rank Test	6.940000e-01	Random
	5	Discrete Fourier Transform (Spectral) Test	1.820000e-02	Random
	6	Non-Overlapping Template Matching Test	7.120000e-02	Random
	7	Overlapping Template Matching Test	2.960000e-01	Random
	8	Maurer's Universal Statistical Test	-1.000000e+00	Error
	9	Linear Complexity Test	4.620000e-01	Random
	10	Serial Test A	0.000000e+00	Non-Random
	11	Serial Test B	0.000000e+00	Non-Random
	12	Approximate Entropy Test	2.100000e-12	Non-Random
	13	Cumulative Sums (Forward) Test	1.040000e-09	Non-Random
	14	Cumulative Sums (Reverse) Test	8.930000e-10	Non-Random
	15	Random Excursions Test State -4	9.730000e-01	Random
	16	Random Excursions Test State -3	9.450000e-01	Random
	17	Random Excursions Test State -2	8.490000e-01	Random
	18	Random Excursions Test State -1	3.060000e-01	Random
	19	Random Excursions Test State +1	9.310000e-01	Random
	20	Random Excursions Test State +2	5.080000e-01	Random
	21	Random Excursions Test State +3	1.770000e-01	Random
	22	Random Excursions Test State +4	1.180000e-02	Random
	23	Random Exursions Variant Test State -1	5.637029e-01	Random
	24	Random Exursions Variant Test State +1	3.860000e-01	Random

```
25
        Random Exursions Variant Test State +2
                                                  6.170000e-01
                                                                     Random
26
        Random Exursions Variant Test State +3
                                                  6.990000e-01
                                                                     Random
27
        Random Exursions Variant Test State +4
                                                  8.270000e-01
                                                                     Random
28
        Random Exursions Variant Test State +5
                                                  8.470000e-01
                                                                     Random
29
        Random Exursions Variant Test State +6
                                                                     Random
                                                  7.280000e-01
30
        Random Exursions Variant Test State +7
                                                  8.100000e-01
                                                                     Random
31
        Random Exursions Variant Test State +8
                                                                     Random
                                                  8.810000e-01
        Random Exursions Variant Test State +9
32
                                                  8.340000e-01
                                                                     Random
```

9.8 Pulsar 4 5ths

[]: pulsar4_5th

```
[]:
                                                             P-Value
                                                                        Outcome4
                                            Test Name
     0
                            Frequency Test (Monobit)
                                                       8.339354e-01
                                                                          Random
     1
                       Frequency Test within a Block
                                                       3.340000e-03
                                                                      Non-Random
     2
                                             Run Test
                                                       3.350000e-03
                                                                      Non-Random
     3
                      Longest Run of Ones in a Block
                                                       4.350000e-01
                                                                          Random
     4
                             Binary Matrix Rank Test -1.000000e+00
                                                                           Error
                                                       3.120000e-01
     5
         Discrete Fourier Transform (Spectral) Test
                                                                          Random
             Non-Overlapping Template Matching Test
     6
                                                       1.000000e+00
                                                                        Absolute
     7
                 Overlapping Template Matching Test -1.000000e+00
                                                                           Error
     8
                Maurer's Universal Statistical Test -1.000000e+00
                                                                           Error
     9
                              Linear Complexity Test -1.000000e+00
                                                                           Error
     10
                                       Serial Test A
                                                       0.000000e+00
                                                                      Non-Random
     11
                                       Serial Test B
                                                       0.00000e+00
                                                                      Non-Random
     12
                            Approximate Entropy Test
                                                                        Absolute
                                                       1.000000e+00
     13
                      Cumulative Sums (Forward) Test
                                                       3.970000e-03
                                                                      Non-Random
     14
                      Cumulative Sums (Reverse) Test
                                                       7.880000e-03
                                                                      Non-Random
     15
                     Random Excursions Test State -4
                                                       9.980000e-01
                                                                          Random
                     Random Excursions Test State -3
     16
                                                       9.950000e-01
                                                                          Random
     17
                     Random Excursions Test State -2
                                                       9.850000e-01
                                                                          Random
                     Random Excursions Test State -1
     18
                                                       8.490000e-01
                                                                          Random
     19
                     Random Excursions Test State +1
                                                       6.840000e-03
                                                                      Non-Random
     20
                     Random Excursions Test State +2
                                                       2.980000e-04
                                                                      Non-Random
     21
                     Random Excursions Test State +3
                                                       3.550000e-04
                                                                      Non-Random
     22
                     Random Excursions Test State +4
                                                                      Non-Random
                                                       1.220000e-04
     23
             Random Exursions Variant Test State +1
                                                       1.240000e-02
                                                                          Random
     24
             Random Exursions Variant Test State +2
                                                       1.490000e-05
                                                                      Non-Random
     25
             Random Exursions Variant Test State +3
                                                       2.700000e-07
                                                                      Non-Random
     26
             Random Exursions Variant Test State +4
                                                       1.570000e-04
                                                                      Non-Random
     27
             Random Exursions Variant Test State +5
                                                       6.680000e-02
                                                                          Random
     28
             Random Exursions Variant Test State +6
                                                       1.320000e-01
                                                                          Random
     29
             Random Exursions Variant Test State +7
                                                       3.750000e-02
                                                                          Random
     30
             Random Exursions Variant Test State +8
                                                       5.280000e-02
                                                                          Random
             Random Exursions Variant Test State +9
     31
                                                       2.750000e-01
                                                                          Random
```

9.9 Pulsar 4 10ths

[]: pulsar4_10th

[]:		Test Name	Outcome
	0	Frequency Test (Monobit)	Random
	1	Frequency Test within a Block	Random
	2	Run Test	Non-Random
	3	Longest Run of Ones in a Block	Random
	4	Binary Matrix Rank Test	Error
	5	Discrete Fourier Transform (Spectral) Test	Random
	6	Non-Overlapping Template Matching Test	Absolute
	7	Overlapping Template Matching Test	Error
	8	Maurer's Universal Statistical Test	Error
	9	Linear Complexity Test	Error
	10	Serial Test A	Non-Random
	11	Serial Test B	Non-Random
	12	Approximate Entropy Test	Absolute
	13	Cumulative Sums (Forward) Test	Random
	14	Cumulative Sums (Reverse) Test	Random
	15	Random Excursions Test State -4	Random
	16	Random Excursions Test State -3	Random
	17	Random Excursions Test State -2	Random
	18	Random Excursions Test State -1	Random
	19	Random Excursions Test State +1	Random
	20	Random Excursions Test State +2	Random
	21	Random Excursions Test State +3	Random
	22	Random Excursions Test State +4	Random
	23	Random Exursions Variant Test State -3	Random
	24	Random Exursions Variant Test State -2	Random
	25	Random Exursions Variant Test State -1	Random
	26	Random Exursions Variant Test State +1	Absolute
	27	Random Exursions Variant Test State +2	Random
	28	Random Exursions Variant Test State +3	Random
	29	Random Exursions Variant Test State +4	Random
	30	Random Exursions Variant Test State +5	Random
	31	Random Exursions Variant Test State +6	Random
	32	Random Exursions Variant Test State +7	Random
	33	Random Exursions Variant Test State +8	Random
	34	Random Exursions Variant Test State +9	Random

9.10 Pulsar 5 All

[]: pulsar5_all

[]:	Test Name	P-Value	Outcome5
0	Frequency Test (Monobit)	0.977150	Random
1	Frequency Test within a Block	0.039800	Random

```
2
                                        Run Test
                                                   0.000020
                                                             Non-Random
3
                Longest Run of Ones in a Block
                                                                 Random
                                                   0.085500
4
                        Binary Matrix Rank Test
                                                   0.694000
                                                                 Random
5
    Discrete Fourier Transform (Spectral) Test
                                                   0.064800
                                                                 Random
        Non-Overlapping Template Matching Test
6
                                                   0.032300
                                                                 Random
7
            Overlapping Template Matching Test
                                                                 Random
                                                   0.296000
           Maurer's Universal Statistical Test -1.000000
8
                                                                  Error
9
                         Linear Complexity Test
                                                   0.029600
                                                                 Random
                                  Serial Test A
                                                   0.853000
                                                                 Random
10
                                  Serial Test B
                                                                 Random
11
                                                   0.963000
12
                       Approximate Entropy Test
                                                   0.956000
                                                                 Random
13
                Cumulative Sums (Forward) Test
                                                                 Random
                                                   0.761000
14
                 Cumulative Sums (Reverse) Test
                                                   0.761000
                                                                 Random
15
               Random Excursions Test State -4
                                                   0.000254
                                                             Non-Random
16
               Random Excursions Test State -3
                                                                 Random
                                                   0.019100
17
               Random Excursions Test State -2
                                                   0.162000
                                                                 Random
18
               Random Excursions Test State -1
                                                   0.067300
                                                                 Random
               Random Excursions Test State +1
19
                                                   0.941000
                                                                 Random
20
               Random Excursions Test State +2
                                                                 Random
                                                   0.951000
21
               Random Excursions Test State +3
                                                                 Random
                                                   0.155000
22
               Random Excursions Test State +4
                                                   0.027100
                                                                 Random
23
        Random Exursions Variant Test State -9
                                                   0.867859
                                                                 Random
24
        Random Exursions Variant Test State -8
                                                                 Random
                                                   0.790482
25
        Random Exursions Variant Test State -7
                                                   0.668588
                                                                 Random
26
        Random Exursions Variant Test State -6
                                                                 Random
                                                   0.569494
27
        Random Exursions Variant Test State -5
                                                   0.331137
                                                                 Random
        Random Exursions Variant Test State -4
28
                                                   0.194835
                                                                 Random
29
        Random Exursions Variant Test State -3
                                                                 Random
                                                   0.145052
30
        Random Exursions Variant Test State -2
                                                   0.092327
                                                                 Random
        Random Exursions Variant Test State -1
31
                                                   0.229949
                                                                 Random
32
        Random Exursions Variant Test State +1
                                                   0.170000
                                                                 Random
33
        Random Exursions Variant Test State +2
                                                   0.166000
                                                                 Random
34
        Random Exursions Variant Test State +3
                                                   0.645000
                                                                 Random
35
        Random Exursions Variant Test State +4
                                                   1.000000
                                                               Absolute
36
        Random Exursions Variant Test State +5
                                                                 Random
                                                   0.775000
37
        Random Exursions Variant Test State +6
                                                   0.642000
                                                                 Random
        Random Exursions Variant Test State +7
                                                                 Random
38
                                                   0.812000
39
        Random Exursions Variant Test State +8
                                                                 Random
                                                   0.965000
40
        Random Exursions Variant Test State +9
                                                   0.835000
                                                                 Random
```

9.11 Pulsar 5 5ths

1

Frequency Test within a Block

0.860000

Random

```
2
                                       Run Test
                                                  0.095800
                                                               Random
3
                Longest Run of Ones in a Block
                                                               Random
                                                  0.693000
4
                        Binary Matrix Rank Test -1.000000
                                                                Error
5
    Discrete Fourier Transform (Spectral) Test
                                                               Random
                                                  0.217000
6
        Non-Overlapping Template Matching Test
                                                  1.000000
                                                             Absolute
7
            Overlapping Template Matching Test -1.000000
                                                                Error
           Maurer's Universal Statistical Test -1.000000
8
                                                                Error
9
                         Linear Complexity Test -1.000000
                                                                Error
                                  Serial Test A
10
                                                  0.853000
                                                               Random
                                  Serial Test B
                                                               Random
11
                                                  0.932000
12
                       Approximate Entropy Test
                                                  1.000000
                                                             Absolute
13
                Cumulative Sums (Forward) Test
                                                  0.894000
                                                               Random
14
                Cumulative Sums (Reverse) Test
                                                  0.786000
                                                               Random
15
               Random Excursions Test State -4
                                                  0.728000
                                                               Random
               Random Excursions Test State -3
                                                  0.900000
16
                                                               Random
17
               Random Excursions Test State -2
                                                  0.755000
                                                               Random
18
               Random Excursions Test State -1
                                                               Random
                                                  0.968000
               Random Excursions Test State +1
19
                                                  0.383000
                                                               Random
20
               Random Excursions Test State +2
                                                  0.542000
                                                               Random
21
               Random Excursions Test State +3
                                                               Random
                                                  0.568000
22
               Random Excursions Test State +4
                                                  0.796000
                                                               Random
23
        Random Exursions Variant Test State -9
                                                  0.638822
                                                               Random
24
        Random Exursions Variant Test State -8
                                                               Random
                                                  8.415830
25
        Random Exursions Variant Test State -7
                                                  0.382103
                                                               Random
26
        Random Exursions Variant Test State -6
                                                               Random
                                                  0.500924
27
        Random Exursions Variant Test State -5
                                                  0.630192
                                                               Random
        Random Exursions Variant Test State -4
                                                  0.655119
28
                                                               Random
29
        Random Exursions Variant Test State -3
                                                  0.597154
                                                               Random
30
        Random Exursions Variant Test State -2
                                                  0.820090
                                                               Random
        Random Exursions Variant Test State -1
31
                                                  0.599426
                                                               Random
32
        Random Exursions Variant Test State +1
                                                  0.237000
                                                               Random
33
        Random Exursions Variant Test State +2
                                                  0.225000
                                                               Random
34
        Random Exursions Variant Test State +3
                                                  0.159000
                                                               Random
35
        Random Exursions Variant Test State +4
                                                  0.234000
                                                               Random
36
        Random Exursions Variant Test State +5
                                                               Random
                                                  0.294000
37
        Random Exursions Variant Test State +6
                                                  0.285000
                                                               Random
38
        Random Exursions Variant Test State +7
                                                               Random
                                                  0.382000
39
        Random Exursions Variant Test State +8
                                                               Random
                                                  0.416000
40
        Random Exursions Variant Test State +9
                                                  0.390000
                                                               Random
```

9.12 Pulsar 6 All

1

Frequency Test within a Block

0.836000

Random

```
2
                                        Run Test
                                                  0.000011
                                                             Non-Random
3
                Longest Run of Ones in a Block
                                                  0.000178
                                                             Non-Random
4
                        Binary Matrix Rank Test -1.000000
                                                                  Error
5
    Discrete Fourier Transform (Spectral) Test
                                                                 Random
                                                  0.218000
        Non-Overlapping Template Matching Test
6
                                                  0.087500
                                                                 Random
7
            Overlapping Template Matching Test -1.000000
                                                                  Error
           Maurer's Universal Statistical Test -1.000000
8
                                                                  Error
9
                         Linear Complexity Test -1.000000
                                                                  Error
                                  Serial Test A
                                                  0.356000
                                                                 Random
10
                                                                 Random
11
                                  Serial Test B
                                                  0.697000
12
                       Approximate Entropy Test
                                                  1.000000
                                                               Absolute
13
                Cumulative Sums (Forward) Test
                                                                 Random
                                                  0.679000
14
                 Cumulative Sums (Reverse) Test
                                                  0.679000
                                                                 Random
15
               Random Excursions Test State -4
                                                  0.196000
                                                                 Random
16
               Random Excursions Test State -3
                                                                 Random
                                                  0.398000
17
               Random Excursions Test State -2
                                                  0.760000
                                                                 Random
18
               Random Excursions Test State -1
                                                  0.845000
                                                                 Random
               Random Excursions Test State +1
19
                                                   0.272000
                                                                 Random
20
               Random Excursions Test State +2
                                                  0.135000
                                                                 Random
21
               Random Excursions Test State +3
                                                                 Random
                                                  0.076700
22
               Random Excursions Test State +4
                                                  0.002160
                                                             Non-Random
23
        Random Exursions Variant Test State -9
                                                  0.324324
                                                                 Random
24
        Random Exursions Variant Test State -8
                                                                 Random
                                                  0.338728
25
        Random Exursions Variant Test State -7
                                                  0.388747
                                                                 Random
26
        Random Exursions Variant Test State -6
                                                                 Random
                                                  0.449177
27
        Random Exursions Variant Test State -5
                                                  0.449063
                                                                 Random
                                                  0.366256
28
        Random Exursions Variant Test State -4
                                                                 Random
29
        Random Exursions Variant Test State -3
                                                                 Random
                                                  0.335979
30
        Random Exursions Variant Test State -2
                                                  0.407626
                                                                 Random
        Random Exursions Variant Test State -1
31
                                                                 Random
                                                  0.719918
32
        Random Exursions Variant Test State +1
                                                  0.720000
                                                                 Random
33
        Random Exursions Variant Test State +2
                                                                 Random
                                                  0.730000
34
        Random Exursions Variant Test State +3
                                                  0.364000
                                                                 Random
35
        Random Exursions Variant Test State +4
                                                  0.442000
                                                                 Random
36
        Random Exursions Variant Test State +5
                                                                 Random
                                                  0.605000
37
        Random Exursions Variant Test State +6
                                                  0.719000
                                                                 Random
38
        Random Exursions Variant Test State +7
                                                                 Random
                                                  0.947000
39
        Random Exursions Variant Test State +8
                                                                 Random
                                                  0.975000
40
        Random Exursions Variant Test State +9
                                                  0.908000
                                                                 Random
```

9.13 Pulsar 6 5ths

[]: pulsar6_5th []: Test Name P-Value Outcome6

Frequency Test (Monobit) 0.498962 Random
Frequency Test within a Block 0.596000 Random

2	Run Test 0.835000	Random
3	Longest Run of Ones in a Block 0.833000	Random
4	Binary Matrix Rank Test -1.000000	Error
5	Discrete Fourier Transform (Spectral) Test 0.698000	Random
6	Non-Overlapping Template Matching Test 1.000000	Random
7	Overlapping Template Matching Test -1.000000	Error
8	Maurer's Universal Statistical Test -1.000000	Error
9	Linear Complexity Test -1.000000	Error
10	Serial Test A 0.499000	Random
11	Serial Test B 0.098400	Random
12	Approximate Entropy Test 1.000000	Absolute
13	Cumulative Sums (Forward) Test 0.473000	Random
14	Cumulative Sums (Reverse) Test 0.849000	Random
15	Random Excursions Test State -4 0.431000	Random
16	Random Excursions Test State -3 0.494000	Random
17	Random Excursions Test State -2 0.221000	Random
18	Random Excursions Test State -1 0.149000	Random
19	Random Excursions Test State +1 0.570000	Random
20	Random Excursions Test State +2 0.801000	Random
21	Random Excursions Test State +3 0.924000	Random
22	Random Excursions Test State +4 0.963000	Random
23	Random Exursions Variant Test State -9 0.845815	Random
24	Random Exursions Variant Test State -8 0.944984	Random
25	Random Exursions Variant Test State -7 0.766848	Random
26	Random Exursions Variant Test State -6 0.808976	Random
27	Random Exursions Variant Test State -5 0.929013	Random
28	Random Exursions Variant Test State -4 0.613505	Random
29	Random Exursions Variant Test State -3 0.473289	Random
30	Random Exursions Variant Test State -2 0.643429	Random
31	Random Exursions Variant Test State -1 0.422678	Random
32	Random Exursions Variant Test State +1 0.109000	Random