pulsar2

October 8, 2022

- 1 Pulsar Emission Data Analysis
- 2 All Imports that may or may not be needed and used for the notebook

```
[]: #currently including any and all Imports that maybe needed for the project.
     import pandas as pd
     import numpy as np
     import seaborn as sns
     import matplotlib.pyplot as plt
     %matplotlib inline
     from sklearn.model_selection import train_test_split
     from sklearn import linear_model
     from sklearn.metrics import r2_score, mean_squared_error
     from sklearn.linear_model import LogisticRegression, LinearRegression
     from sklearn.metrics import confusion_matrix, accuracy_score
     from sklearn.feature_selection import RFE
     import datetime as dt
     from sklearn.cluster import KMeans
     from sklearn.metrics import pairwise_distances
     from scipy.cluster.hierarchy import linkage, dendrogram, cut_tree
     from scipy.spatial.distance import pdist
     from sklearn.feature extraction.text import TfidfVectorizer
     import matplotlib.dates as mdates
     from scipy.stats import pearsonr
     from scipy import stats
     import statistics
     import math
     from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
     from statsmodels.tsa.stattools import acf, pacf
     from statsmodels.tsa.tsatools import lagmat
     from numpy import array
     from sklearn.model_selection import train_test_split
     from keras.models import Sequential
     from keras.layers import LSTM
     from keras.layers import Dense
     from keras.layers import Bidirectional
```

3 Section for extracting from a tar file.

Currently implemented for original TAR File structure.

```
[]: #This is also found in the main file under tarunzip.py
import tarfile
import os
import sys

#tar = tarfile.open("pulseTarFile.tar")
#tar.extractall('./Data')
#tar.close()
```

3.1 Beginning of Exploration

3.1.1 Examining the data

In this section we are determining the total integrity of the data to determine if further comprehensive data cleaning and uniforming processes are needed.

```
[]: colnames = ['Pulse Number', 'Brightness', 'Uncertainty']

pulsar = pd.read_csv("Data/J0953+0755.pulses", sep = ' ', header = None, names

→= colnames)
```

- []: pulsar.shape
- []: (14329, 3)
- []: pulsar.head(25)

```
[]:
         Pulse Number
                         Brightness
                                      Uncertainty
                           0.334330
                                         0.015570
     0
                      1
                      2
                          -0.098659
     1
                                         0.014051
     2
                      3
                                         0.011901
                           0.123514
     3
                      4
                           0.443923
                                         0.014365
                      5
     4
                                         0.057785
                           1.590446
     5
                      6
                           1.233848
                                         0.018692
     6
                     7
                           0.857876
                                         0.022208
     7
                     8
                           0.254255
                                         0.018185
     8
                     9
                           0.292077
                                         0.021672
     9
                    10
                           0.439929
                                         0.046293
                    11
                                         0.036243
     10
                           0.824310
     11
                    12
                           1.443460
                                         0.088372
     12
                    13
                           0.127981
                                         0.018070
     13
                    14
                           0.327896
                                         0.012362
     14
                    15
                           2.473663
                                         0.099205
     15
                    16
                           0.683800
                                         0.049683
     16
                    17
                           0.744937
                                         0.033909
     17
                           0.628764
                                         0.032342
                    18
     18
                    19
                           5.077294
                                         0.093078
```

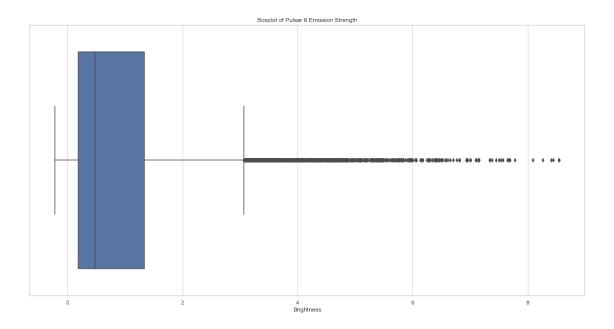
```
20
                   21
                         1.006799
                                       0.029068
     21
                   22
                         4.359872
                                       0.091381
     22
                   23
                         1.576034
                                       0.030928
     23
                   24
                         1.218368
                                       0.067754
     24
                   25
                         1.377933
                                       0.036103
    pulsar.describe()
[]:
            Pulse Number
                            Brightness
                                          Uncertainty
     count
            14329.000000
                          14329.000000
                                         14329.000000
     mean
             7165.000000
                               0.994458
                                             0.034561
     std
             4136.570339
                               1.211127
                                             0.029641
    min
                1.000000
                              -0.219110
                                             0.010120
     25%
             3583.000000
                              0.184157
                                             0.014351
     50%
             7165.000000
                              0.481894
                                             0.021999
     75%
            10747.000000
                               1.337406
                                             0.043380
            14329.000000
                               8.552022
                                             0.242041
     max
[]: nullBoolBrightness = pd.isnull(pulsar["Brightness"])
     pulsar[nullBoolBrightness]
[]: Empty DataFrame
     Columns: [Pulse Number, Brightness, Uncertainty]
     Index: []
[]: pulsar["Brightness"].describe()
[]: count
              14329.000000
     mean
                  0.994458
     std
                  1.211127
    min
                 -0.219110
     25%
                  0.184157
     50%
                  0.481894
     75%
                  1.337406
                  8.552022
    max
     Name: Brightness, dtype: float64
[]: plt.figure(figsize=(20,10))
     sns.set_theme(style="whitegrid")
     ax = sns.boxplot(x=pulsar["Brightness"]).set_title("Boxplot of Pulsar 6")
      →Emission Strength")
```

0.025086

19

20

0.554981



```
[]: medianpulse6 = pulsar["Brightness"].median()
    print("Median of Pulsar6: ", medianpulse6)
    pulsar['Binary'] = np.where(pulsar['Brightness'] > medianpulse6, 1, 0)
```

Median of Pulsar6: 0.4818942

[]: pulsar

[]:		Pulse	Number	Brightness	Uncertainty	Binary
	0		1	0.334330	0.015570	0
	1		2	-0.098659	0.014051	0
	2		3	0.123514	0.011901	0
	3		4	0.443923	0.014365	0
	4		5	1.590446	0.057785	1
	•••		•••	•••	•••	
	14324		14325	4.876881	0.097181	1
	14325		14326	2.074136	0.080444	1
	14326		14327	0.585504	0.026204	1
	14327		14328	0.360930	0.035051	0
	14328		14329	8.409811	0.120164	1

[14329 rows x 4 columns]

```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar.Brightness.values
plt.style.use('ggplot')
```

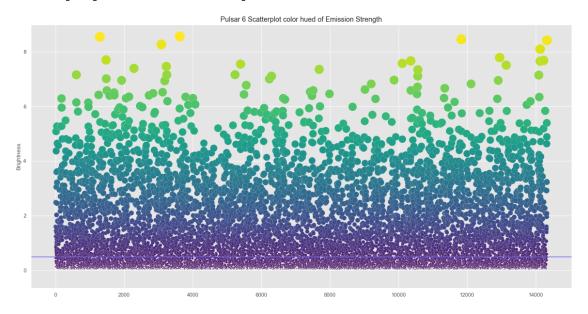
```
ax = sns.scatterplot(data=pulsar["Brightness"], s= strength*50, c=strength, 

⇒cmap="viridis", marker="o").set_title('Pulsar 6 Scatterplot color hued of 

⇒Emission Strength')

ax= plt.axhline( y=0.4818942, ls='-',c='mediumslateblue')
```

c:\Users\oxlay\anaconda3\lib\site-packages\matplotlib\collections.py:1003:
RuntimeWarning: invalid value encountered in sqrt
scale = np.sqrt(self._sizes) * dpi / 72.0 * self._factor



```
[]: print(len(pulsar[(pulsar.Brightness > 0.4818942)]))
print(len(pulsar[(pulsar.Brightness < 0.4818942)]))</pre>
```

7164 7164

```
[]: #plt.figure(figsize=(20,10))
    #sns.set_style("darkgrid", {"axes.facecolor": ".75"})
    #strength = pulsar.Brightness.values
    #ax = plt.axhline( y=0.4818942, ls='-',c='mediumslateblue')
    #ax = sns.swarmplot(data=pulsar["Brightness"], c="blue").set_title('Pulsar 6
    →Swarm plot of Emission Strength')
```

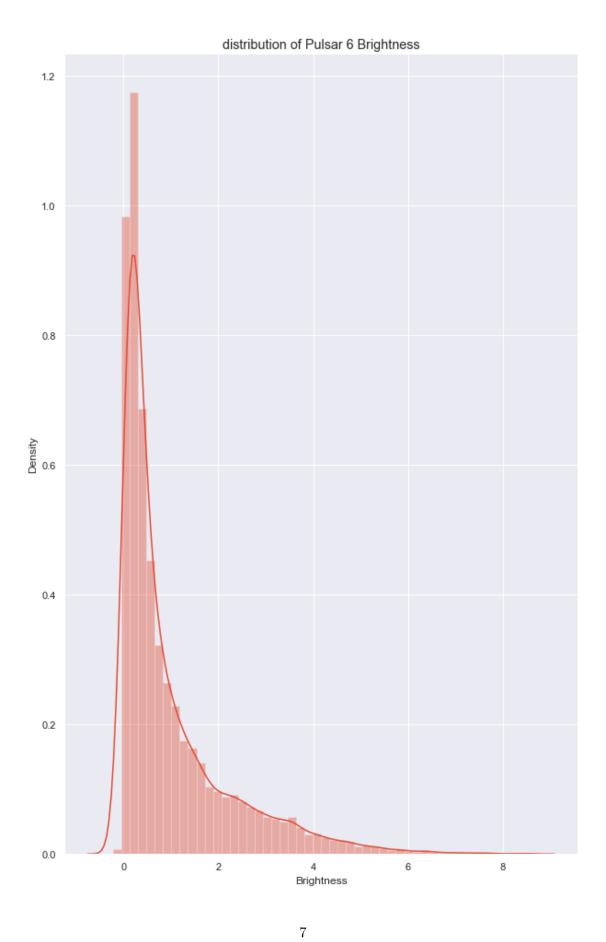
```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Brightness)
plt.title("distribution of Pulsar 6 Brightness")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a

future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 Brightness')

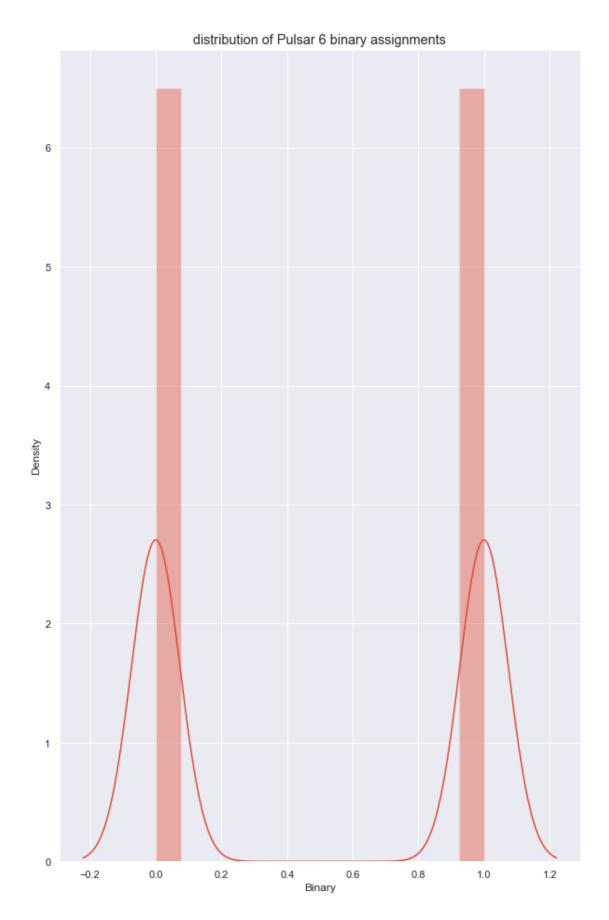


```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Binary)
plt.title("distribution of Pulsar 6 binary assignments")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 binary assignments')



3.2 Binary Classification

```
[]: X = pulsar[['Brightness', 'Uncertainty']]
     y = pulsar['Binary']
[]: X.head()
[]:
       Brightness Uncertainty
         0.334330
                      0.015570
        -0.098659
                      0.014051
     1
         0.123514
     2
                      0.011901
     3
         0.443923
                      0.014365
     4
          1.590446
                      0.057785
[]: y.head()
[]: 0
         0
     1
     2
          0
     3
         0
     4
          1
     Name: Binary, dtype: int32
[]: from sklearn.model_selection import train_test_split
     X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: from sklearn.preprocessing import StandardScaler
     train_scaler = StandardScaler()
     X_train = train_scaler.fit_transform(X_train)
     test_scaler = StandardScaler()
     X_test = test_scaler.fit_transform(X_test)
[]: model = LogisticRegression()
     model.fit(X_train, y_train)
[]: LogisticRegression()
[]: predictions = model.predict(X_test)
[]: from sklearn.metrics import confusion_matrix
```

```
cm = confusion_matrix(y_test, predictions)
     TN, FP, FN, TP = confusion_matrix(y_test, predictions).ravel()
     print('True Positive(TP) = ', TP)
     print('False Positive(FP) = ', FP)
     print('True Negative(TN) = ', TN)
     print('False Negative(FN) = ', FN)
    True Positive(TP) = 1420
    False Positive(FP) = 8
    True Negative(TN) = 1428
    False Negative(FN) = 10
[]: accuracy = (TP + TN) / (TP + FP + TN + FN)
    print("Accuracy of the model is ", accuracy)
    Accuracy of the model is 0.9937194696441033
    3.3 Bidirectional LSTM Model
[]: brightness_list = list(pulsar['Brightness'])
     brightness_list[:10]
[]: [0.3343305,
     -0.09865925,
     0.1235136,
     0.4439226,
      1.590446,
      1.233848,
     0.8578762,
     0.2542552,
     0.2920765,
     0.4399285]
[]: def split_list(blist, steps):
        X, y = list(), list()
        for i in range(len(blist)):
             # find the end of this pattern
             end_ix = i + steps
             # check if we are beyond the sequence
             if end_ix > len(blist)-1:
             # gather input and output parts of the pattern
            list_x, list_y = blist[i:end_ix], blist[end_ix]
            X.append(list_x)
             y.append(list_y)
```

```
return array(X), array(y)
[]: X, y = split_list(brightness_list, 100)
     X = X.reshape((X.shape[0], X.shape[1], 1))
     X[:1]
[]: array([[[ 0.3343305],
             [-0.09865925],
             [ 0.1235136 ],
             [ 0.4439226 ],
             [ 1.590446 ],
             [ 1.233848 ],
             [ 0.8578762 ],
             [ 0.2542552 ],
             [ 0.2920765 ],
             [ 0.4399285 ],
             [ 0.8243096 ],
             [ 1.44346
                         ],
             [ 0.127981
                        ],
             [ 0.327896 ],
             [ 2.473663 ],
             [ 0.6838004 ],
             [ 0.7449372 ],
             [ 0.6287637 ],
             [5.077294],
             [ 0.5549809 ],
             [ 1.006799 ],
             [ 4.359872
             [ 1.576034
             [ 1.218368
             [ 1.377933
                        ],
             [ 0.930978
                        ],
             [ 3.043829
             [ 1.546754 ],
             [ 1.121343 ],
             [ 0.2231065 ],
             [ 1.046509 ],
             [3.591599],
             [ 0.2794989 ],
             [ 2.020426 ],
             [ 0.1834685 ],
             [ 0.1728863 ],
             [ 0.08091074],
             [ 0.482004 ],
             [ 0.4997924 ],
             [ 0.1020256 ],
             [ 0.1811799 ],
```

```
[ 0.0734898 ],
[ 0.1686549 ],
[ 0.1140138 ],
[ 0.2534638 ],
[ 2.445954 ],
[ 5.267987
           ],
[ 3.209211 ],
[ 3.61146
            ],
[ 0.4521517 ],
[ 0.3187844 ],
[ 0.1093535 ],
[ 0.349598 ],
[ 1.801916 ],
[ 4.641071 ],
[ 0.9302299 ],
[ 0.2540756 ],
[ 0.1235713 ],
[ 0.07940372],
[ 0.6344433 ],
            ],
[ 1.77306
[ 1.09541
            ],
[ 0.7851931 ],
[ 1.048576 ],
[ 0.4031171 ],
[ 0.06401307],
[ 0.5247178 ],
[ 1.18829
            ],
[0.9450719],
[ 0.1678216 ],
[ 1.293165 ],
[ 0.7533471 ],
[ 0.2794956 ],
[ 0.32502
            ],
[ 0.337905 ],
[ 0.2770691 ],
[ 0.1680058 ],
[ 0.3047891 ],
[ 0.1164062 ],
[ 0.1846148 ],
[ 0.4561068 ],
[ 0.0423768 ],
[ 0.541339 ],
[ 0.2756999 ],
[ 0.2174998 ],
[ 1.347416 ],
[ 4.561518
           ],
[ 1.020322 ],
```

```
[ 0.288448 ],
           [ 0.1711328 ],
           [ 0.524166 ],
           [ 1.066911 ],
           [ 0.1387746 ],
           [ 0.07770184],
           [ 0.7084595 ],
           [ 0.7501087 ],
           [ 0.1608082 ],
           [ 0.5056017 ],
           [ 1.310186 ],
           [ 0.1655302 ]]])
[]: X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: model = Sequential()
    model.add(Bidirectional(LSTM(50, activation='relu'), input_shape=(100, 1)))
    model.add(Dense(8, activation='relu'))
    model.add(Dense(1, activation='sigmoid'))
    model.compile(loss='binary_crossentropy', optimizer='adam',_

→metrics=['accuracy'])
[]: history = model.fit(X_train, y_train, epochs=1, verbose=1, batch_size=10)
   accuracy: 0.0000e+00
[]: y_pred = model.predict(X_test, verbose=0)
    y_pred[:10]
[]: array([[0.92071056],
          [0.9388161],
          [0.89009047],
          [0.97404736],
          [0.9535792],
          [0.9790253],
          [0.97632176],
          [0.9037658],
          [0.94391733],
          [0.96781904]], dtype=float32)
[]: model.evaluate(X_test, y_test)
   accuracy: 0.0000e+00
[]: [-0.07192137837409973, 0.0]
```

3.4 ML Evaluation.

3.4.1 Logistic Regression

This model appears to have gained some insight in the data and accurately defined a majority of the data. The accuracy of the model is >95% which indicates that it was able to determine a trend and apply it in a useful manner in the predictions during evaluation. Further, the confusion matrix further supports the high accuracy and likely usefulness of the model with only 3 false assignments. However, in analysis this is only to determine if there is a correlation between binary assignment and the emission strength x error in measurement. This doesn't aid us in our overall randomness determination, but it does determine that uncertainty has a role in the binary assignment and the overall trust of emission strength.

3.4.2 Bidirectional LSTM

This model is very error prone as the loss value is consistently at 60% or higher at every epoch during training and at exactly 63.07% in evaluation with a 0% accuracy this indicates that there is either a great error in the formation of the model, data used or trend being obtained. Alternatively it could indicate that there is no trend there to predict. Likely this indicates that the model is not valuable for any meaningful analysis.

4 Preliminary runs test

4.0.1 Math Logic

$$Z = \frac{R - \tilde{R}}{s_R}$$

$$\tilde{R} = \frac{2n1n2}{n1 + n2} + 1$$

$$s_R^2 = \frac{2nn2}{(n1+n2)^2(n1+n2-1)}$$

link to resource: https://www.geeksforgeeks.org/runs-test-of-randomness-in-python/

 $Z_{\text{critical}} = 1.96$ \$ as the confidence interval level of 95% thus this is a 2 tailed test. If the probability as corrosponding to this confidence interval H_{null} will be rejected as it is not statistically significant as denoted by $|Z| > Z_{\text{critical}}$

There is also code attempting to change it from a z-score probability to a P-score for ease of understanding and clarity.

5 FUNCTION CODE FOR RUNS TEST

```
[]: binaryData1 = pulsar['Binary'].tolist()
print("pulsar6 original: ",binaryData1)
```

pulsar6 original: [0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 1, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 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```

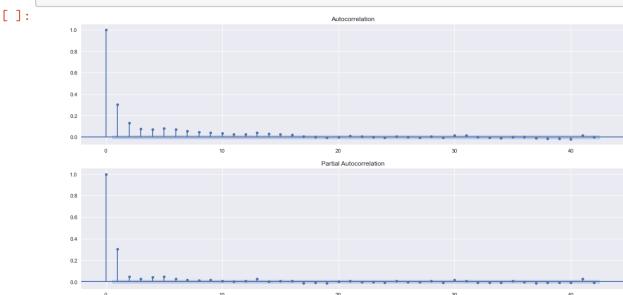
6 Below we begin autocorrelation and autocovariance analysis

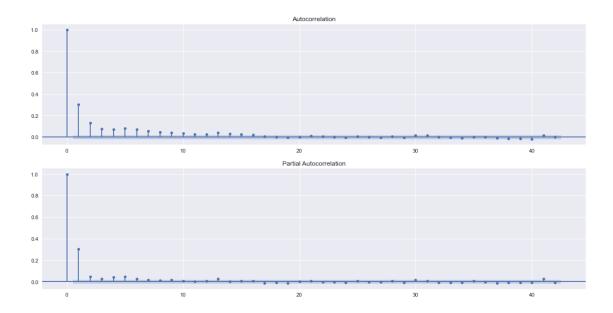
To get started with this I am playing around with guide from: https://towardsdatascience.com/a-step-by-step-guide-to-calculating-autocorrelation-and-partial-autocorrelation-8c4342b784e8

```
[]: plt.style.use("seaborn")
  plt.rcParams["figure.figsize"] = (18, 9)

fig, ax = plt.subplots(2,1)

plot_acf(pulsar['Brightness'], ax=ax[0])
  plot_pacf(pulsar['Brightness'], ax=ax[1], method="ols")
```





```
[]: acf(pulsar['Brightness'], nlags=10)
   FutureWarning: fft=True will become the default after the release of the 0.12
   release of statsmodels. To suppress this warning, explicitly set fft=False.
     warnings.warn(
[]: array([1.
                    , 0.30152047, 0.13254511, 0.07716124, 0.07364129,
          0.08096058, 0.07046427, 0.05556536, 0.0436438, 0.04277081,
          0.03660132])
[]: acfpulsar = pd.DataFrame()
    for lag in range(0,11):
        acfpulsar[f"B_lag_{lag}"] = pulsar['Brightness'].shift(lag)
    acfpulsar
[]:
           B_lag_0
                                                B_lag_4
                                                                   B_lag_6 \
                     B_lag_1
                              B_lag_2
                                       B_lag_3
                                                         B_lag_5
          0.334330
                                                                      NaN
    0
                        NaN
                                  NaN
                                           NaN
                                                    NaN
                                                             NaN
    1
          -0.098659
                   0.334330
                                           NaN
                                                    NaN
                                                             NaN
                                                                      NaN
                                  NaN
    2
          0.123514 -0.098659
                             0.334330
                                           NaN
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    3
          0.443923 0.123514 -0.098659
                                      0.334330
                                                    NaN
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```

1.590446 0.443923 0.123514 -0.098659

4.876881 5.386421 3.224787

2.074136 4.876881 5.386421

14326 0.585504 2.074136 4.876881 5.386421

4

14324

14325

1.953645

3.224787

0.334330

4.624813

1.953645

3.224787

NaN

0.225158

4.624813

1.953645

NaN

1.502603

0.225158

4.624813

```
14327
      0.360930 0.585504 2.074136 4.876881
                                               5.386421 3.224787
                                                                    1.953645
14328 8.409811
                 0.360930
                           0.585504
                                     2.074136
                                               4.876881 5.386421
                                                                    3.224787
        B_lag_7
                  B_lag_8
                            B_lag_9
                                     B_lag_10
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                                NaN
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                                          NaN
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14324
      1.389349
                 1.592995
                           2.913151
                                     0.181665
14325
      1.502603
                 1.389349
                           1.592995
                                     2.913151
                1.502603
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      0.225158
                           1.389349
                                    1.592995
14327
      4.624813 0.225158
                           1.502603 1.389349
14328 1.953645 4.624813
                           0.225158
                                    1.502603
[14329 rows x 11 columns]
```

```
[]: acfpulsar.corr()["B_lag_0"].values
```

```
[]: array([1.
                      , 0.30191886, 0.13272532, 0.07726788, 0.07374568,
            0.08110522, 0.07062283, 0.0556971 , 0.04374889, 0.04288793,
           0.0367024])
```

- 6.0.1 Getting every 5th as per the auto correlation
- 6.0.2Creating a new set of discrete 100 sets and examining them specifically
- 6.0.3 Further Random testing to move into extensive testing

Getting every 5th as per the auto correlation

```
[]: held5ths = pulsar[pulsar.index % 5 == 0]
     held5ths
```

[]:		Pulse	Number	${ t Brightness}$	Uncertainty	Binary
	0		1	0.334330	0.015570	0
	5		6	1.233848	0.018692	1
	10		11	0.824310	0.036243	1
	15		16	0.683800	0.049683	1
	20		21	1.006799	0.029068	1
				•••		
	14305		14306	0.081548	0.011737	0
	14310		14311	0.060433	0.011708	0
	14315		14316	2.913151	0.089312	1
	14320		14321	4.624813	0.095899	1
	14325		14326	2.074136	0.080444	1

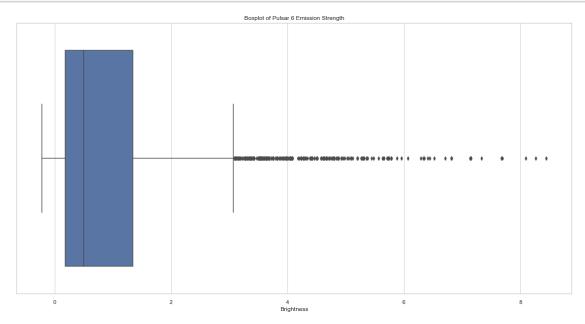
[2866 rows x 4 columns]

```
[]: medianheld5ths = held5ths["Brightness"].median() medianheld5ths
```

[]: 0.49492415

```
[]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=held5ths["Brightness"]).set_title("Boxplot of Pulsar 6

→Emission Strength")
```

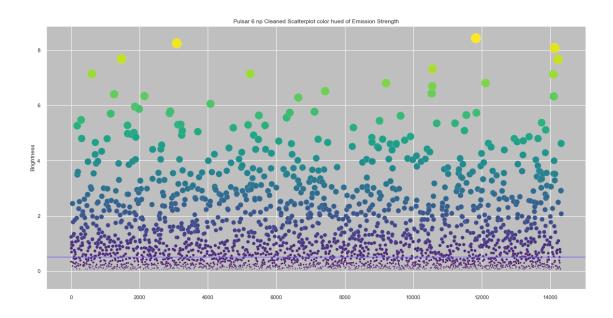


```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = sns.scatterplot(data=held5ths["Brightness"], s= strength*50, c=strength,

→cmap="viridis", marker="o").set_title('Pulsar 6 np Cleaned Scatterplot color

→hued of Emission Strength')
ax = plt.axhline( y=0.49492415, ls='-',c='mediumslateblue')
```

c:\Users\oxlay\anaconda3\lib\site-packages\matplotlib\collections.py:1003:
RuntimeWarning: invalid value encountered in sqrt
 scale = np.sqrt(self._sizes) * dpi / 72.0 * self._factor



```
[]: #plt.figure(figsize=(20,10))
    #sns.set_style("darkgrid", {"axes.facecolor": ".75"})
    #strength = held5ths.Brightness.values
    #ax = plt.axhline( y=0.49492415, ls='-',c='mediumslateblue')
    #ax = sns.swarmplot(data=held5ths["Brightness"], c="blue").set_title('Pulsar 6

→Swarm plot of Emission Strength')
```

```
[ ]: print(len(held5ths[(held5ths.Brightness > 0.49492415)]))
print(len(held5ths[(held5ths.Brightness < 0.49492415)]))</pre>
```

1433

1433

Randomness testing

```
[]: np.savetxt(r'every5thbinarypulsar2.txt', held5ths.Binary, fmt='%d', u

delimiter='')

np.savetxt(r'allpulsar2.txt', pulsar.Binary, fmt='%d', delimiter='')
```

[]: pulsar.Binary

```
[]: 0 0
1 0
2 0
3 0
4 1
...
14324 1
14325 1
```

14326 1 14327 0 14328 1

Name: Binary, Length: 14329, dtype: int32