pulsar6

October 8, 2022

- 1 Pulsar Emission Data Analysis
- 2 All Imports that may or may not be needed and used for the notebook

```
[]: #currently including any and all Imports that maybe needed for the project.
     import pandas as pd
     import numpy as np
     import seaborn as sns
     import matplotlib.pyplot as plt
     %matplotlib inline
     from sklearn.model_selection import train_test_split
     from sklearn import linear_model
     from sklearn.metrics import r2_score, mean_squared_error
     from sklearn.linear_model import LogisticRegression, LinearRegression
     from sklearn.metrics import confusion_matrix, accuracy_score
     from sklearn.feature_selection import RFE
     import datetime as dt
     from sklearn.cluster import KMeans
     from sklearn.metrics import pairwise_distances
     from scipy.cluster.hierarchy import linkage, dendrogram, cut_tree
     from scipy.spatial.distance import pdist
     from sklearn.feature extraction.text import TfidfVectorizer
     import matplotlib.dates as mdates
     from scipy.stats import pearsonr
     from scipy import stats
     import statistics
     import math
     from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
     from statsmodels.tsa.stattools import acf, pacf
     from statsmodels.tsa.tsatools import lagmat
     from numpy import array
     from sklearn.model_selection import train_test_split
     from keras.models import Sequential
     from keras.layers import LSTM
     from keras.layers import Dense
     from keras.layers import Bidirectional
```

3 Section for extracting from a tar file.

Currently implemented for original TAR File structure.

```
[]: #This is also found in the main file under tarunzip.py
import tarfile
import os
import sys

#tar = tarfile.open("pulseTarFile.tar")
#tar.extractall('./Data')
#tar.close()
```

```
[]: #How to remove outlier data for these datasets.
#pulsar6npcleaned = pulsar6[(np.abs(stats.zscore(pulsar6["Brightness"])) <3)]
#pulsar6npcleaned
```

3.1 Beginning of Exploration

3.1.1 Examining the data

In this section we are determining the total integrity of the data to determine if further comprehensive data cleaning and uniforming processes are needed.

```
[]: colnames = ['Pulse Number', 'Brightness', 'Uncertainty']

pulsar = pd.read_csv("Data/J1644-4559.pulses", sep = ' ', header = None, names⊔

⇒= colnames)
```

```
[]: pulsar.shape
```

[]: (698, 3)

```
[]: pulsar.head(25)
```

```
[]:
         Pulse Number
                         Brightness
                                      Uncertainty
                           0.634671
                                         0.002761
                      1
     1
                      2
                           0.736945
                                         0.005207
     2
                           0.693834
                      3
                                         0.002706
     3
                      4
                           1.021866
                                         0.010184
     4
                      5
                           0.673845
                                         0.006236
                                         0.004763
     5
                      6
                           0.676883
     6
                     7
                           0.527039
                                         0.002422
     7
                     8
                                         0.003174
                           0.673417
     8
                     9
                                         0.002848
                           0.357076
     9
                    10
                           0.661704
                                         0.005588
     10
                    11
                           0.545564
                                         0.003835
     11
                    12
                           0.494655
                                         0.003145
     12
                    13
                           0.804260
                                         0.005258
     13
                    14
                           0.513362
                                         0.005700
     14
                    15
                           0.477025
                                         0.002945
```

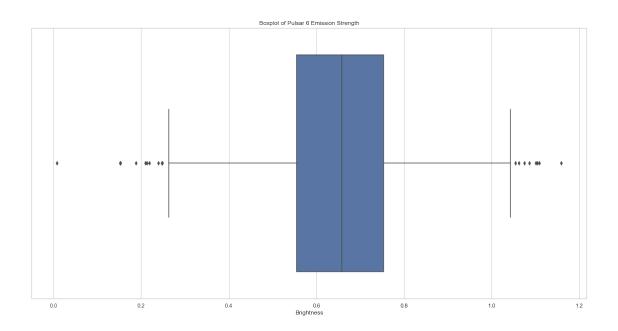
```
16
                   17
                          0.188069
                                       0.002452
     17
                   18
                          0.748592
                                       0.005468
     18
                   19
                          0.723437
                                       0.004548
     19
                   20
                          0.960154
                                       0.006765
     20
                   21
                          0.707715
                                       0.006011
     21
                   22
                          1.074550
                                       0.006831
     22
                   23
                          0.961340
                                       0.006617
     23
                   24
                          0.754457
                                       0.004117
     24
                   25
                          0.773151
                                       0.004920
    pulsar.describe()
[]:
            Pulse Number
                           Brightness
                                       Uncertainty
               698.00000
                           698.000000
                                        698.000000
     count
                             0.654319
     mean
               349.50000
                                           0.004445
     std
               201.63953
                             0.163945
                                          0.001855
     min
                 1.00000
                             0.007642
                                           0.002129
     25%
               175.25000
                             0.555267
                                          0.003086
     50%
                             0.658295
                                           0.003951
               349.50000
     75%
               523.75000
                             0.753396
                                           0.005349
               698.00000
                             1.159334
                                           0.016097
     max
[]: nullBoolBrightness = pd.isnull(pulsar["Brightness"])
     pulsar[nullBoolBrightness]
[]: Empty DataFrame
     Columns: [Pulse Number, Brightness, Uncertainty]
     Index: []
[]: pulsar["Brightness"].describe()
[]: count
              698.000000
     mean
                0.654319
     std
                0.163945
     min
                0.007642
     25%
                0.555267
     50%
                0.658295
     75%
                0.753396
                1.159334
     max
     Name: Brightness, dtype: float64
[]: plt.figure(figsize=(20,10))
     sns.set_theme(style="whitegrid")
     ax = sns.boxplot(x=pulsar["Brightness"]).set_title("Boxplot of Pulsar 6")
      →Emission Strength")
```

0.004712

0.399571

16

15



```
[]: medianpulse6 = pulsar["Brightness"].median()
print("Median of Pulsar6: ", medianpulse6)
pulsar['Binary'] = np.where(pulsar['Brightness'] > medianpulse6, 1, 0)
```

Median of Pulsar6: 0.65829515

[]: pulsar

[]:		Pulse	Number	Brightness	Uncertainty	Binary
	0		1	0.634671	0.002761	0
	1		2	0.736945	0.005207	1
	2		3	0.693834	0.002706	1
	3		4	1.021866	0.010184	1
	4		5	0.673845	0.006236	1
			•••	•••		
	693		694	0.776083	0.008928	1
	694		695	0.625382	0.006018	0
	695		696	0.647559	0.003765	0
	696		697	0.312449	0.002901	0
	697		698	0.548353	0.009056	0

[698 rows x 4 columns]

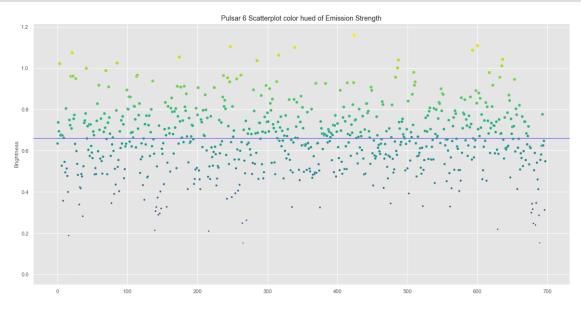
```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar.Brightness.values
plt.style.use('ggplot')
```

```
ax = sns.scatterplot(data=pulsar["Brightness"], s= strength*50, c=strength, 

⇒cmap="viridis", marker="o").set_title('Pulsar 6 Scatterplot color hued of 

⇒Emission Strength')

ax= plt.axhline( y=0.65829515, ls='-',c='mediumslateblue')
```

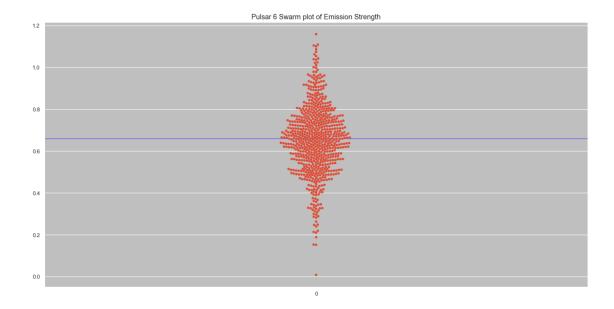


```
[]: print(len(pulsar[(pulsar.Brightness > 0.6589028)]))
print(len(pulsar[(pulsar.Brightness < 0.6589028)]))</pre>
```

348 350

```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = pulsar.Brightness.values
ax = plt.axhline( y=0.65829515, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=pulsar["Brightness"], c="blue").set_title('Pulsar 6

→Swarm plot of Emission Strength')
```

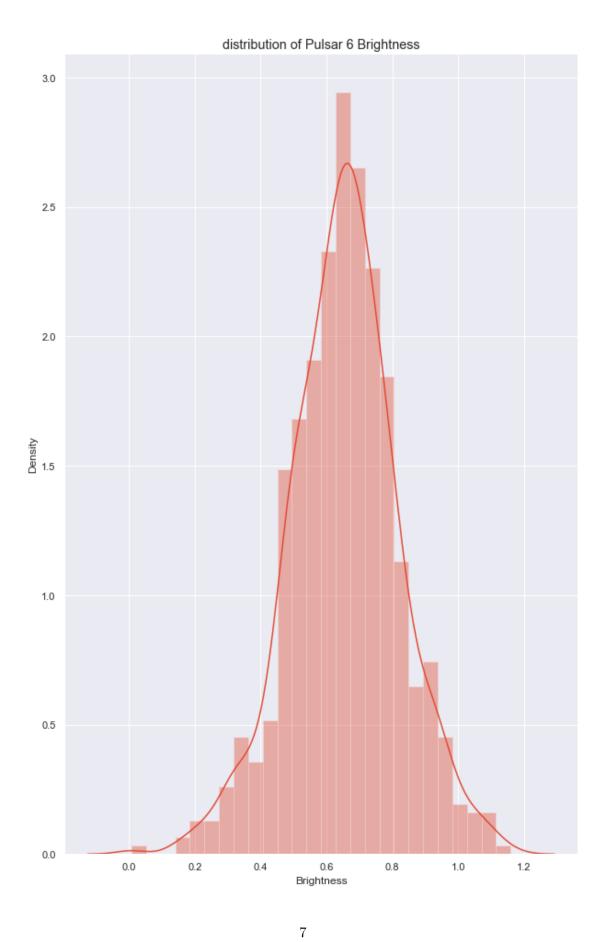


```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Brightness)
plt.title("distribution of Pulsar 6 Brightness")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619: FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 Brightness')



```
[]: plt.figure(figsize=(10, 16))
with sns.axes_style('darkgrid'):
    sns.distplot(pulsar.Binary)
plt.title("distribution of Pulsar 6 binary assignments")
```

c:\Users\oxlay\anaconda3\lib\site-packages\seaborn\distributions.py:2619:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

[]: Text(0.5, 1.0, 'distribution of Pulsar 6 binary assignments')



3.2 Binary Classification

```
[]: X = pulsar[['Brightness', 'Uncertainty']]
     y = pulsar['Binary']
[]: X.head()
[]:
       Brightness Uncertainty
          0.634671
                      0.002761
     1
         0.736945
                      0.005207
     2
         0.693834
                      0.002706
     3
         1.021866
                      0.010184
     4
         0.673845
                      0.006236
[]: y.head()
[]: 0
     1
     2
          1
     3
          1
     4
          1
     Name: Binary, dtype: int32
[]: from sklearn.model_selection import train_test_split
     X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: from sklearn.preprocessing import StandardScaler
     train_scaler = StandardScaler()
     X_train = train_scaler.fit_transform(X_train)
     test_scaler = StandardScaler()
     X_test = test_scaler.fit_transform(X_test)
[]: model = LogisticRegression()
     model.fit(X_train, y_train)
[]: LogisticRegression()
[]: predictions = model.predict(X_test)
[]: from sklearn.metrics import confusion_matrix
```

```
cm = confusion_matrix(y_test, predictions)
     TN, FP, FN, TP = confusion_matrix(y_test, predictions).ravel()
     print('True Positive(TP) = ', TP)
     print('False Positive(FP) = ', FP)
     print('True Negative(TN) = ', TN)
     print('False Negative(FN) = ', FN)
    True Positive(TP) = 68
    False Positive(FP) = 3
    True Negative(TN) = 69
    False Negative(FN) = 0
[]: accuracy = (TP + TN) / (TP + FP + TN + FN)
    print("Accuracy of the model is ", accuracy)
    Accuracy of the model is 0.9785714285714285
    3.3 Bidirectional LSTM Model
[]: brightness_list = list(pulsar['Brightness'])
     brightness_list[:10]
[]: [0.6346714,
     0.7369454,
     0.6938341,
     1.021866,
     0.6738453,
     0.6768825,
     0.5270392,
     0.6734173,
     0.3570756,
     0.6617037]
[]: def split_list(blist, steps):
        X, y = list(), list()
        for i in range(len(blist)):
             # find the end of this pattern
             end_ix = i + steps
             # check if we are beyond the sequence
             if end_ix > len(blist)-1:
             # gather input and output parts of the pattern
            list_x, list_y = blist[i:end_ix], blist[end_ix]
            X.append(list_x)
             y.append(list_y)
```

```
return array(X), array(y)
[]: X, y = split_list(brightness_list, 100)
    X = X.reshape((X.shape[0], X.shape[1], 1))
    X[:1]
[]: array([[[0.6346714],
             [0.7369454],
             [0.6938341],
             [1.021866],
             [0.6738453],
             [0.6768825],
             [0.5270392],
             [0.6734173],
             [0.3570756],
             [0.6617037],
             [0.5455637],
             [0.4946546],
             [0.8042599],
             [0.5133624],
             [0.4770252],
             [0.3995709],
             [0.1880686],
             [0.7485923],
             [0.723437],
             [0.960154],
             [0.7077145],
             [1.07455
                       ],
             [0.9613396],
             [0.7544566],
             [0.7731512],
             [0.6326247],
             [0.9491536],
             [0.5976236],
             [0.5358455],
             [0.4823253],
             [0.00764172],
             [0.3384609],
             [0.4226295],
             [0.4172967],
             [0.4866613],
             [0.474994],
             [0.2820107],
             [0.5241109],
             [0.7348035],
             [0.7454862],
             [0.7803042],
```

```
[0.9990716],
```

- [0.6589876],
- [0.7188401],
- [0.6039976],
- [0.7266428],
- -
- [0.5741913],
- [0.7266481],
- [0.6223379],
- [0.5905332],
- [0.5636434],
- [0.6927038],
- [0.6748244],
- [0.4850771],
- [0.5154094],
- [0.4861331],
- [0.7445553],
- [0.8274334],
- [0.5971083],
- [0.9172228],
- [0.7009897],
- [0.5611873],
- [0.0011070]
- [0.755055],
- [0.548961],
- [0.4883782],
- [0.5705138],
- [0.6909211],
- [0.7797759],
- [0.7110825],
- [0.9880999],
- [0.6565107],
- [0.0000107]
- [0.4854965],
- [0.7354586],
- [0.9091333],
- [0.7606739],
- [0.6818882],
- [0.5743544],
- [0.3454394],
- [0.0101001]
- [0.6301639],
- [0.6635159],
- [0.5985485],
- [0.3900236],
- [0.5116962],
- [0.4355926],
- [0.7949124],
- [1.0245],
- [0.5212468],
- [0.5545024],

```
[0.4035],
       [0.6934347],
       [0.6132591],
       [0.7468123],
       [0.6344795],
       [0.7662029],
       [0.7272725],
       [0.4662485],
       [0.5103499],
       [0.6203424],
       [0.6333662],
       [0.8940519]]])
[]: X_train, X_test, y_train, y_test = train_test_split(X, y , test_size=0.20)
[]: model = Sequential()
  model.add(Bidirectional(LSTM(50, activation='relu'), input_shape=(100, 1)))
  model.add(Dense(8, activation='relu'))
  model.add(Dense(1, activation='sigmoid'))
  model.compile(loss='binary_crossentropy', optimizer='adam',_
   →metrics=['accuracy'])
[]: history = model.fit(X_train, y_train, epochs=200, verbose=1, batch_size=10)
  Epoch 1/200
  0.0000e+00
  Epoch 2/200
  0.0000e+00
  Epoch 3/200
  48/48 [=======
              ========= ] - 1s 20ms/step - loss: 0.6435 - accuracy:
  0.0000e+00
  Epoch 4/200
  0.0000e+00
  Epoch 5/200
  0.0000e+00
  Epoch 6/200
  0.0000e+00
  Epoch 7/200
  0.0000e+00
  Epoch 8/200
  0.0000e+00
```

```
Epoch 9/200
0.0000e+00
Epoch 10/200
0.0000e+00
Epoch 11/200
0.0000e+00
Epoch 12/200
0.0000e+00
Epoch 13/200
0.0000e+00
Epoch 14/200
0.0000e+00
Epoch 15/200
0.0000e+00
Epoch 16/200
0.0000e+00
Epoch 17/200
0.0000e+00
Epoch 18/200
0.0000e+00
Epoch 19/200
0.0000e+00
Epoch 20/200
0.0000e+00
Epoch 21/200
0.0000e+00
Epoch 22/200
0.0000e+00
Epoch 23/200
0.0000e+00
Epoch 24/200
0.0000e+00
```

```
Epoch 25/200
0.0000e+00
Epoch 26/200
0.0000e+00
Epoch 27/200
0.0000e+00
Epoch 28/200
0.0000e+00
Epoch 29/200
0.0000e+00
Epoch 30/200
0.0000e+00
Epoch 31/200
0.0000e+00
Epoch 32/200
0.0000e+00
Epoch 33/200
0.0000e+00
Epoch 34/200
0.0000e+00
Epoch 35/200
0.0000e+00
Epoch 36/200
0.0000e+00
Epoch 37/200
0.0000e+00
Epoch 38/200
0.0000e+00
Epoch 39/200
0.0000e+00
Epoch 40/200
0.0000e+00
```

```
Epoch 41/200
0.0000e+00
Epoch 42/200
0.0000e+00
Epoch 43/200
0.0000e+00
Epoch 44/200
0.0000e+00
Epoch 45/200
0.0000e+00
Epoch 46/200
0.0000e+00
Epoch 47/200
0.0000e+00
Epoch 48/200
0.0000e+00
Epoch 49/200
0.0000e+00
Epoch 50/200
0.0000e+00
Epoch 51/200
0.0000e+00
Epoch 52/200
0.0000e+00
Epoch 53/200
0.0000e+00
Epoch 54/200
0.0000e+00
Epoch 55/200
0.0000e+00
Epoch 56/200
0.0000e+00
```

```
Epoch 57/200
0.0000e+00
Epoch 58/200
0.0000e+00
Epoch 59/200
0.0000e+00
Epoch 60/200
0.0000e+00
Epoch 61/200
0.0000e+00
Epoch 62/200
0.0000e+00
Epoch 63/200
0.0000e+00
Epoch 64/200
0.0000e+00
Epoch 65/200
0.0000e+00
Epoch 66/200
0.0000e+00
Epoch 67/200
0.0000e+00
Epoch 68/200
0.0000e+00
Epoch 69/200
0.0000e+00
Epoch 70/200
0.0000e+00
Epoch 71/200
0.0000e+00
Epoch 72/200
0.0000e+00
```

```
Epoch 73/200
0.0000e+00
Epoch 74/200
0.0000e+00
Epoch 75/200
0.0000e+00
Epoch 76/200
0.0000e+00
Epoch 77/200
0.0000e+00
Epoch 78/200
0.0000e+00
Epoch 79/200
0.0000e+00
Epoch 80/200
0.0000e+00
Epoch 81/200
0.0000e+00
Epoch 82/200
0.0000e+00
Epoch 83/200
0.0000e+00
Epoch 84/200
0.0000e+00
Epoch 85/200
0.0000e+00
Epoch 86/200
0.0000e+00
Epoch 87/200
0.0000e+00
Epoch 88/200
0.0000e+00
```

```
Epoch 89/200
0.0000e+00
Epoch 90/200
0.0000e+00
Epoch 91/200
0.0000e+00
Epoch 92/200
0.0000e+00
Epoch 93/200
0.0000e+00
Epoch 94/200
0.0000e+00
Epoch 95/200
0.0000e+00
Epoch 96/200
0.0000e+00
Epoch 97/200
0.0000e+00
Epoch 98/200
0.0000e+00
Epoch 99/200
0.0000e+00
Epoch 100/200
0.0000e+00
Epoch 101/200
0.0000e+00
Epoch 102/200
0.0000e+00
Epoch 103/200
0.0000e+00
Epoch 104/200
0.0000e+00
```

```
Epoch 105/200
0.0000e+00
Epoch 106/200
0.0000e+00
Epoch 107/200
0.0000e+00
Epoch 108/200
0.0000e+00
Epoch 109/200
0.0000e+00
Epoch 110/200
0.0000e+00
Epoch 111/200
0.0000e+00
Epoch 112/200
0.0000e+00
Epoch 113/200
48/48 [============= ] - 1s 21ms/step - loss: 10.3085 -
accuracy: 0.0000e+00
Epoch 114/200
0.0000e+00
Epoch 115/200
0.0000e+00
Epoch 116/200
0.0000e+00
Epoch 117/200
0.0000e+00
Epoch 118/200
0.0000e+00
Epoch 119/200
0.0000e+00
Epoch 120/200
0.0000e+00
```

```
Epoch 121/200
0.0000e+00
Epoch 122/200
0.0000e+00
Epoch 123/200
0.0000e+00
Epoch 124/200
0.0000e+00
Epoch 125/200
0.0000e+00
Epoch 126/200
0.0000e+00
Epoch 127/200
0.0000e+00
Epoch 128/200
0.0000e+00
Epoch 129/200
0.0000e+00
Epoch 130/200
0.0000e+00
Epoch 131/200
0.0000e+00
Epoch 132/200
0.0000e+00
Epoch 133/200
0.0000e+00
Epoch 134/200
0.0000e+00
Epoch 135/200
0.0000e+00
Epoch 136/200
0.0000e+00
```

```
Epoch 137/200
0.0000e+00
Epoch 138/200
0.0000e+00
Epoch 139/200
0.0000e+00
Epoch 140/200
0.0000e+00
Epoch 141/200
0.0000e+00
Epoch 142/200
0.0000e+00
Epoch 143/200
0.0000e+00
Epoch 144/200
0.0000e+00
Epoch 145/200
0.0000e+00
Epoch 146/200
0.0000e+00
Epoch 147/200
0.0000e+00
Epoch 148/200
0.0000e+00
Epoch 149/200
0.0000e+00
Epoch 150/200
0.0000e+00
Epoch 151/200
0.0000e+00
Epoch 152/200
0.0000e+00
```

```
Epoch 153/200
0.0000e+00
Epoch 154/200
0.0000e+00
Epoch 155/200
0.0000e+00
Epoch 156/200
0.0000e+00
Epoch 157/200
0.0000e+00
Epoch 158/200
0.0000e+00
Epoch 159/200
0.0000e+00
Epoch 160/200
0.0000e+00
Epoch 161/200
0.0000e+00
Epoch 162/200
0.0000e+00
Epoch 163/200
0.0000e+00
Epoch 164/200
0.0000e+00
Epoch 165/200
0.0000e+00
Epoch 166/200
0.0000e+00
Epoch 167/200
0.0000e+00
Epoch 168/200
0.0000e+00
```

```
Epoch 169/200
0.0000e+00
Epoch 170/200
0.0000e+00
Epoch 171/200
0.0000e+00
Epoch 172/200
0.0000e+00
Epoch 173/200
0.0000e+00
Epoch 174/200
0.0000e+00
Epoch 175/200
0.0000e+00
Epoch 176/200
0.0000e+00
Epoch 177/200
0.0000e+00
Epoch 178/200
0.0000e+00
Epoch 179/200
0.0000e+00
Epoch 180/200
0.0000e+00
Epoch 181/200
0.0000e+00
Epoch 182/200
0.0000e+00
Epoch 183/200
0.0000e+00
Epoch 184/200
0.0000e+00
```

```
Epoch 185/200
0.0000e+00
Epoch 186/200
0.0000e+00
Epoch 187/200
0.0000e+00
Epoch 188/200
0.0000e+00
Epoch 189/200
0.0000e+00
Epoch 190/200
0.0000e+00
Epoch 191/200
0.0000e+00
Epoch 192/200
0.0000e+00
Epoch 193/200
0.0000e+00
Epoch 194/200
0.0000e+00
Epoch 195/200
0.0000e+00
Epoch 196/200
0.0000e+00
Epoch 197/200
0.0000e+00
Epoch 198/200
0.0000e+00
Epoch 199/200
0.0000e+00
Epoch 200/200
0.0000e+00
```

```
[]:|y_pred = model.predict(X_test, verbose=0)
    y_pred[:10]
[]: array([[0.8022064],
         [0.70461446],
         [0.66105044],
         [0.6896631],
         [0.68478507],
         [0.7015957],
         [0.6640747],
         [0.50144947],
         [0.63427603],
         [0.72587335]], dtype=float32)
[]: model.evaluate(X_test, y_test)
   0.0000e+00
[]: [0.6307459473609924, 0.0]
```

3.4 ML Evaluation.

3.4.1 Logistic Regression

This model appears to have gained some insight in the data and accurately defined a majority of the data. The accuracy of the model is >95% which indicates that it was able to determine a trend and apply it in a useful manner in the predictions during evaluation. Further, the confusion matrix further supports the high accuracy and likely usefulness of the model with only 3 false assignments. However, in analysis this is only to determine if there is a correlation between binary assignment and the emission strength x error in measurement. This doesn't aid us in our overall randomness determination, but it does determine that uncertainty has a role in the binary assignment and the overall trust of emission strength.

3.4.2 Bidirectional LSTM

This model is very error prone as the loss value is consistently at 60% or higher at every epoch during training and at exactly 63.07% in evaluation with a 0% accuracy this indicates that there is either a great error in the formation of the model, data used or trend being obtained. Alternatively it could indicate that there is no trend there to predict. Likely this indicates that the model is not valuable for any meaningful analysis.

4 Preliminary runs test

4.0.1 Math Logic

$$Z = \frac{R - \tilde{R}}{s_R}$$

$$\tilde{R} = \frac{2n1n2}{n1 + n2} + 1$$

$$s_R^2 = \frac{2nn2(2n1n2 - n1 - n2)}{(n1 + n2)^2(n1 + n2 - 1)}$$

link to resource: https://www.geeksforgeeks.org/runs-test-of-randomness-in-python/

 $Z_{\text{critical}} = 1.96$ s as the confidence interval level of 95% thus this is a 2 tailed test. If the probability as corrosponding to this confidence interval H_{null} will be rejected as it is not statistically significant as denoted by $|Z| > Z_{\text{critical}}$

There is also code attempting to change it from a z-score probability to a P-score for ease of understanding and clarity.

5 FUNCTION CODE FOR RUNS TEST

```
[]: binaryData1 = pulsar['Binary'].tolist()
print("pulsar6 original: ",binaryData1)
```

```
pulsar6 original: [0, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1,
1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0,
1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1,
1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1,
1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1,
0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1,
1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1,
1, 1, 1, 1, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1,
1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0,
1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1,
0, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1,
0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1,
0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1,
1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0,
0, 0, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1,
0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1,
1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0,
0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1,
0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1,
1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1,
1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1,
0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0,
0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0,
1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0,
0, 0, 1, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 1,
0, 0, 0]
```

6 Below we begin autocorrelation and autocovariance analysis

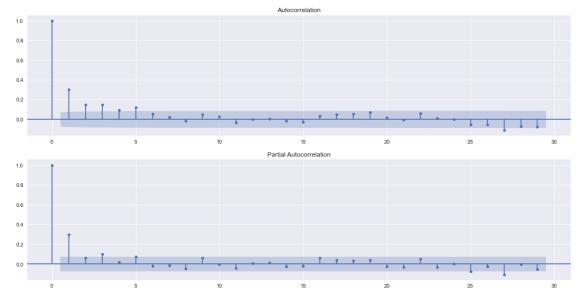
To get started with this I am playing around with guide from: https://towards datascience.com/a-step-by-step-guide-to-calculating-autocorrelation-and-partial-autocorrelation-8c4342b784e8

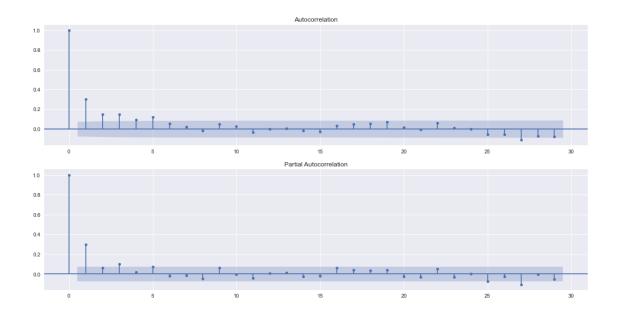
```
[]: plt.style.use("seaborn")
  plt.rcParams["figure.figsize"] = (18, 9)

fig, ax = plt.subplots(2,1)

plot_acf(pulsar['Brightness'], ax=ax[0])
  plot_pacf(pulsar['Brightness'], ax=ax[1], method="ols")
```

[]:





```
[]: acf(pulsar['Brightness'], nlags=10)
    c:\Users\oxlay\anaconda3\lib\site-packages\statsmodels\tsa\stattools.py:667:
    FutureWarning: fft=True will become the default after the release of the 0.12
    release of statsmodels. To suppress this warning, explicitly set fft=False.
      warnings.warn(
[]: array([1.
                          0.29929122,
                                        0.14656878, 0.14948301,
                                                                   0.09384681,
                                        0.02160374, -0.01711482,
             0.11707783,
                           0.05493324,
                                                                   0.04777
             0.02563995])
[]: acfpulsar = pd.DataFrame()
     for lag in range(0,11):
         acfpulsar[f"B_lag_{lag}"] = pulsar['Brightness'].shift(lag)
     acfpulsar
[]:
                                                                         B_lag_6 \
           B_lag_0
                     B_lag_1
                                B_lag_2
                                          B_lag_3
                                                     B_lag_4
                                                               B_lag_5
     0
          0.634671
                         NaN
                                    NaN
                                              NaN
                                                         NaN
                                                                   NaN
                                                                              NaN
     1
          0.736945
                    0.634671
                                    NaN
                                              NaN
                                                         NaN
                                                                   NaN
                                                                              NaN
     2
          0.693834
                    0.736945
                               0.634671
                                              NaN
                                                         NaN
                                                                   NaN
                                                                              NaN
     3
          1.021866
                    0.693834
                               0.736945
                                         0.634671
                                                         NaN
                                                                   NaN
                                                                              NaN
     4
          0.673845
                    1.021866
                               0.693834
                                         0.736945
                                                    0.634671
                                                                   NaN
                                                                              NaN
                               0.581248
     693
         0.776083
                    0.623757
                                         0.555266
                                                    0.152886
                                                              0.286132
                                                                        0.413354
     694
          0.625382
                    0.776083
                               0.623757
                                         0.581248
                                                    0.555266
                                                              0.152886
                                                                        0.286132
          0.647559
                                                    0.581248
     695
                    0.625382
                               0.776083
                                         0.623757
                                                              0.555266
                                                                        0.152886
     696
         0.312449
                    0.647559
                               0.625382
                                         0.776083
                                                    0.623757
                                                              0.581248
                                                                        0.555266
     697
          0.548353
                    0.312449
                               0.647559
                                         0.625382
                                                    0.776083
                                                              0.623757
                                                                        0.581248
           B_lag_7
                     B_lag_8
                                B_lag_9
                                         B_lag_10
     0
               NaN
                          NaN
                                    NaN
                                              NaN
                         NaN
                                              NaN
     1
               NaN
                                    NaN
     2
               NaN
                         NaN
                                    NaN
                                              NaN
     3
               NaN
                         NaN
                                    NaN
                                              NaN
     4
               NaN
                         NaN
                                    NaN
                                              NaN
     693
         0.460095
                    0.541486
                               0.346502 0.239302
     694
         0.413354
                    0.460095
                               0.541486
                                         0.346502
     695
          0.286132
                               0.460095
                    0.413354
                                         0.541486
     696
          0.152886
                    0.286132
                               0.413354
                                         0.460095
                               0.286132
     697
          0.555266
                    0.152886
                                         0.413354
     [698 rows x 11 columns]
```

```
[]: acfpulsar.corr()["B_lag_0"].values
                         0.29938402, 0.14710414, 0.15003691, 0.09455452,
[]: array([1.
            0.11800036,
                          0.05537751, 0.02179885, -0.01724535, 0.04863954,
            0.02621294])
    6.0.1 Getting every 5th as per the auto correlation
    6.0.2 Creating a new set of discrete 100 sets and examining them specifically
    6.0.3 Further Random testing to move into extensive testing
    Getting every 5th as per the auto correlation
[]: held5ths = pulsar[pulsar.index % 5 == 0]
     held5ths
[]:
         Pulse Number
                       Brightness
                                    Uncertainty Binary
                                                      0
     0
                     1
                          0.634671
                                       0.002761
     5
                     6
                          0.676883
                                       0.004763
                                                      1
     10
                    11
                          0.545564
                                       0.003835
                                                      0
```

```
0
15
                16
                       0.399571
                                     0.004712
20
                21
                       0.707715
                                     0.006011
                                                      1
. .
675
               676
                       0.618826
                                     0.002507
                                                      0
                                                      0
680
               681
                       0.246916
                                     0.004276
                                                      0
685
               686
                       0.541486
                                     0.003149
690
               691
                       0.555266
                                     0.003657
                                                      0
695
               696
                       0.647559
                                     0.003765
                                                      0
```

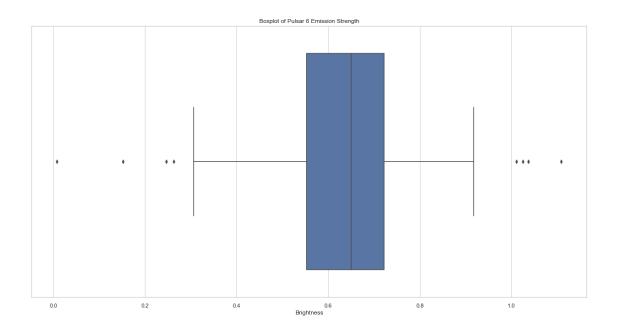
[140 rows x 4 columns]

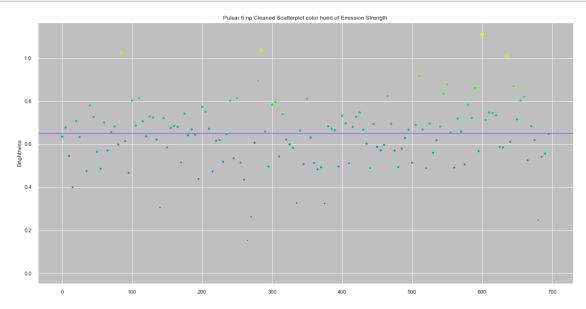
```
[ ]: medianheld5ths = held5ths["Brightness"].median()
medianheld5ths
```

[]: 0.6508051

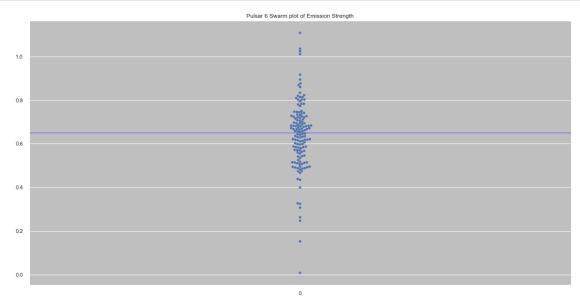
```
[]: plt.figure(figsize=(20,10))
sns.set_theme(style="whitegrid")
ax = sns.boxplot(x=held5ths["Brightness"]).set_title("Boxplot of Pulsar 6

→Emission Strength")
```





```
[]: plt.figure(figsize=(20,10))
sns.set_style("darkgrid", {"axes.facecolor": ".75"})
strength = held5ths.Brightness.values
ax = plt.axhline( y=0.6508051, ls='-',c='mediumslateblue')
ax = sns.swarmplot(data=held5ths["Brightness"], c="blue").set_title('Pulsar 6⊔
→Swarm plot of Emission Strength')
```



```
[]: print(len(held5ths[(held5ths.Brightness > 0.6508051)]))
print(len(held5ths[(held5ths.Brightness < 0.6508051)]))</pre>
```

70 70

Randomness testing

```
[]: np.savetxt(r'every5thbinarypulsar6.txt', held5ths.Binary, fmt='%d', u

delimiter='')

np.savetxt(r'allpulsar6.txt', pulsar.Binary, fmt='%d', delimiter='')
```

[]: pulsar.Binary

```
[]: 0 0
1 1
2 1
3 1
4 1
...
693 1
694 0
```

```
695 0
696 0
697 0
```

Name: Binary, Length: 698, dtype: int32