# Report

### November 2, 2022

```
[]: #currently including any and all Imports that maybe needed for the project.
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
```

### 1 Importing all CSVs

## 2 Key for Outcome Column

Absolute = value of 1.0 (Positive) Error = Value of -1.0 - P-values are never negative therefore indicates an error Random = P-values match the random proof Non-Random = P-values match the non-random proof

#### 3 All Emissions

```
[]: AllofAll = pulsar1_all
     pulsar2_all = pulsar2_all.set_axis(['Test Name', 'P-Value', 'Outcome2'], axis =__
      \rightarrow 1, inplace= False)
     pulsar3_all = pulsar3_all.set_axis(['Test Name', 'P-Value', 'Outcome3'], axis =__
      \rightarrow 1, inplace= False)
     pulsar4_all = pulsar4_all.set_axis(['Test Name', 'P-Value', 'Outcome4'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar5_all = pulsar5_all.set_axis(['Test Name', 'P-Value', 'Outcome5'], axis =__
      \rightarrow 1, inplace= False)
     pulsar6_all = pulsar6_all.set_axis(['Test Name', 'P-Value', 'Outcome6'], axis =__
      \hookrightarrow 1, inplace= False)
     AllofAll['Outcome2'] = pulsar2_all['Outcome2'].values
     AllofAll['Outcome3'] = pulsar3_all['Outcome3'].values
     AllofAll['Outcome4'] = ''
     AllofAll['Outcome5'] = pulsar5_all['Outcome5'].values
     AllofAll['Outcome6'] = pulsar6_all['Outcome6'].values
     pulse4 = np.array(pulsar4_all['Outcome4'].values)
     AllofAll['Outcome4'] = pd.Series(pulse4)
     AllofAll = AllofAll.drop(columns='P-Value')
     AllofAll
```

```
[]:
                                           Test Name
                                                                     Outcome2 \
                                                          Outcome
     0
                           Frequency Test (Monobit)
                                                         Absolute
                                                                       Random
     1
                      Frequency Test within a Block
                                                      Non-Random Non-Random
     2
                                            Run Test
                                                      Non-Random Non-Random
     3
                     Longest Run of Ones in a Block
                                                           Random Non-Random
                                                                       Random
     4
                            Binary Matrix Rank Test
                                                           Random
     5
         Discrete Fourier Transform (Spectral) Test
                                                           Random Non-Random
     6
             Non-Overlapping Template Matching Test
                                                      Non-Random
                                                                  Non-Random
     7
                 Overlapping Template Matching Test
                                                      Non-Random
                                                                  Non-Random
     8
                Maurer's Universal Statistical Test
                                                            Error
                                                                        Error
     9
                              Linear Complexity Test
                                                           Random
                                                                       Random
     10
                                       Serial Test A
                                                      Non-Random
                                                                   Non-Random
     11
                                       Serial Test B
                                                      Non-Random
                                                                       Random
     12
                            Approximate Entropy Test
                                                      Non-Random
                                                                   Non-Random
     13
                     Cumulative Sums (Forward) Test
                                                           Random
                                                                       Random
     14
                     Cumulative Sums (Reverse) Test
                                                                       Random
                                                           Random
     15
                    Random Excursions Test State -4
                                                           Random
                                                                       Random
                    Random Excursions Test State -3
                                                                   Non-Random
     16
                                                           Random
     17
                    Random Excursions Test State -2
                                                           Random
                                                                   Non-Random
     18
                    Random Excursions Test State -1
                                                           Random
                                                                       Random
     19
                    Random Excursions Test State +1
                                                           Random
                                                                       Random
     20
                    Random Excursions Test State +2
                                                           Random
                                                                       Random
     21
                    Random Excursions Test State +3
                                                           Random
                                                                       Random
     22
                    Random Excursions Test State +4
                                                           Random
                                                                       Random
```

23	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	-9	Random	${\tt Random}$
24	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-8	Random	${\tt Random}$
25	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-7	Random	${\tt Random}$
26	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-6	Random	${\tt Random}$
27	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-5	Random	${\tt Random}$
28	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-4	Random	${\tt Random}$
29	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-3	Random	${\tt Random}$
30	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	-2	Random	${\tt Random}$
31	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	-1	Random	${\tt Random}$
32	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+1	Random	${\tt Random}$
33	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+2	Random	${\tt Random}$
34	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+3	Random	${\tt Random}$
35	${\tt Random}$	${\tt Exursions}$	Variant	Test	State	+4	Random	${\tt Random}$
36	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+5	Random	${\tt Random}$
37	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+6	Random	${\tt Random}$
38	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+7	Random	${\tt Random}$
39	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+8	Random	${\tt Random}$
40	${\tt Random}$	${\tt Exursions}$	${\tt Variant}$	Test	${\tt State}$	+9	Random	${\tt Random}$

	Outcome3	Outcome4	Outcome5	Outcome6
0	Random	Random	Random	Absolute
1	Random	Non-Random	Random	Random
2	Random	Non-Random	Non-Random	Non-Random
3	Random	Non-Random	Random	Non-Random
4	Random	Random	Random	Error
5	Random	Random	Random	Random
6	Random	Random	Random	Random
7	Random	Random	Random	Error
8	Error	Error	Error	Error
9	Random	Random	Random	Error
10	Random	Non-Random	Random	Random
11	Random	Non-Random	Random	Random
12	Random	Non-Random	Random	Absolute
13	Random	Non-Random	Random	Random
14	Random	Non-Random	Random	Random
15	Random	Random	Non-Random	Random
16	Random	Random	Random	Random
17	Random	Random	Random	Random
18	Random	Random	Random	Random
19	Random	Random	Random	Random
20	Random	Random	Random	Random
21	Random	Random	Random	Random
22	Random	Random	Random	Non-Random
23	Random	Random	Random	Random
24	Random	Random	Random	Random
25	Random	Random	Random	Random
26	Random	Random	Random	Random

Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	Random	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Absolute	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
Random	NaN	Random	Random
	Random	Random NaN	Random NaN Random Random NaN Random Random NaN Absolute Random NaN Random

### 4 Every 5th

```
[]: Allof5th = pulsar1_5th
     pulsar2_5th = pulsar2_5th.set_axis(['Test Name', 'P-Value', 'Outcome2'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar3_5th = pulsar3_5th.set_axis(['Test Name', 'P-Value', 'Outcome3'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar4_5th = pulsar4_5th.set_axis(['Test Name', 'P-Value', 'Outcome4'], axis =__
      \hookrightarrow 1, inplace= False)
     pulsar5_5th = pulsar5_5th.set_axis(['Test Name', 'P-Value', 'Outcome5'], axis =__
      \hookrightarrow1, inplace= False)
     pulsar6 5th = pulsar6 5th.set axis(['Test Name', 'P-Value', 'Outcome6'], axis = []
      \hookrightarrow 1, inplace= False)
     Allof5th['Outcome2'] = ''
     Allof5th['Outcome3'] = ''
     Allof5th['Outcome4'] = ''
     Allof5th['Outcome5'] = ''
     Allof5th['Outcome6'] = ''
     pulse2 = np.array(pulsar2_5th['Outcome2'].values)
     Allof5th['Outcome2'] = pd.Series(pulse2)
     pulse3 = np.array(pulsar3_5th['Outcome3'].values)
     Allof5th['Outcome3'] = pd.Series(pulse3)
     pulse4 = np.array(pulsar4_5th['Outcome4'].values)
     Allof5th['Outcome4'] = pd.Series(pulse4)
     pulse5 = np.array(pulsar5_5th['Outcome5'].values)
     Allof5th['Outcome5'] = pd.Series(pulse5)
     pulse6 = np.array(pulsar6_5th['Outcome6'].values)
     Allof5th['Outcome6'] = pd.Series(pulse6)
     Allof5th = Allof5th.drop(columns='P-Value')
     Allof5th
```

r 3			m . N	0 .	0 . 0	
[]:			Test Name	Outcome	Outcome2	\
0			Test (Monobit)	Random	Random	
1		Frequency lest	within a Block	Random	Random	
2		I t D f (	Run Test	Random	Random	
3		Longest Run of		Random	Random	
4	D	•	atrix Rank Test	Random	Random	
5		ourier Transform	_	Random	Random	
6		erlapping Template	_	Random	Random	
7		erlapping Template	_	Random	Random	
8	Maui	rer's Universal S		Error	Error	
9		Linear	Complexity Test	Random	Random	
10			Serial Test A	Random	Random	
11			Serial Test B	Random	Random	
12			te Entropy Test	Non-Random	Non-Random	
13		Cumulative Sums		Random	Random	
14		Cumulative Sums		Random	Random	
15		Random Excursion		Random	Random	
16		Random Excursion		Random	Random	
17		Random Excursion		Random	Random	
18		Random Excursion		Random	Random	
19		Random Excursion		Random	Non-Random	
20		Random Excursion		Non-Random	Non-Random	
21		Random Excursion		Non-Random	Random	
22		Random Excursion		Random	Random	
23		Exursions Varian		Random	Random	
24		Exursions Varian		Random	Random	
25		Exursions Varian		Random	Random	
26		Exursions Varian		Non-Random	Random	
27		Exursions Varian		Non-Random	Random	
28		Exursions Varian		Non-Random	Random	
29		Exursions Varian		Non-Random	Random	
30		Exursions Varian		Random	Random	
31	Random	Exursions Varian	t Test State +9	Random	Random	
	Outcome3	Outcome4 Out	come5 Outcome6			
0	Random		andom Random			
1	Random		andom Random			
2	Random		andom Random			
3	Random		andom Random			
4	Error		Error Error			
5	Non-Random		andom Random			
6	Random		olute Random			
7	Error		Error Error			
8	Error		Error Error			
9	Error		Error Error			
10	Random		andom Random			
11	Random	Non-Random Ra	andom Random			

12	Absolute	Absolute	Absolute	Absolute
13	Random	Non-Random	Random	Random
14	Random	Non-Random	Random	Random
15	Random	Random	Random	Random
16	Random	Random	Random	Random
17	Random	Random	Random	Random
18	Random	Random	Random	Random
19	Random	Non-Random	Random	Random
20	Random	Non-Random	Random	Random
21	Random	Non-Random	Random	Random
22	Random	Non-Random	Random	Random
23	Random	Random	Random	Random
24	Random	Non-Random	Random	Random
25	Random	Non-Random	Random	Random
26	Random	Non-Random	Random	Random
27	Random	Random	Random	Random
28	Random	Random	Random	Random
29	Random	Random	Random	Random
30	Random	Random	Random	Random
31	Random	Random	Random	Random

# 5 Edge Case Pulsar analysis

```
[]: pulsar4_10th = pulsar4_10th.drop(columns='P-Value')
pulsar4_10th
```

Outcome	Test Name	]:	[ ]
Random	Frequency Test (Monobit)	0	
Random	Frequency Test within a Block	1	
Non-Random	Run Test	2	
Random	Longest Run of Ones in a Block	3	
Error	Binary Matrix Rank Test	4	
Random	Discrete Fourier Transform (Spectral) Test	5	
Absolute	Non-Overlapping Template Matching Test	6	
Error	Overlapping Template Matching Test	7	
Error	Maurer's Universal Statistical Test	8	
Error	Linear Complexity Test	9	
Non-Random	Serial Test A	10	
Non-Random	Serial Test B	11	
Absolute	Approximate Entropy Test	12	
Random	Cumulative Sums (Forward) Test	13	
Random	Cumulative Sums (Reverse) Test	14	
Random	Random Excursions Test State -4	15	
Random	Random Excursions Test State -3	16	
Random	Random Excursions Test State -2	17	
Random	Random Excursions Test State -1	18	

19		Random Ex	cursions	Test	${\tt State}$	+1	Random
20		Random Ex	cursions	Test	${\tt State}$	+2	Random
21		Random Ex	cursions	Test	${\tt State}$	+3	Random
22		Random Ex	cursions	Test	${\tt State}$	+4	Random
23	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-3	Random
24	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-2	Random
25	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	-1	Random
26	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+1	Absolute
27	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+2	Random
28	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+3	Random
29	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+4	Random
30	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+5	Random
31	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+6	Random
32	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+7	Random
33	${\tt Random}$	Exursions	Variant	Test	${\tt State}$	+8	Random
34	Random	Exursions	Variant	Test	State	+9	Random

### 6 Looking at Pulsars with RandTest Lib

[ ]: RandTestResults
----------------------

[]:		RandTestAll	${\tt RandTest5ths}$	${\tt RandTestElse}$
	0	True	True	Null
	1	True	True	Null
	2	True	True	Null
	3	True	True	True
	4	True	True	Null
	5	True	True	Null

#### 6.1 Analysis of RandTest Results

The RandTest suite uses an algorithm called "exponentially-decaying moment prediction" to determine the net deviation between predicted and actual elements in sequences. It evaluated whether or not a sequence of numbers are random or not.

It has a stated accuracy of 99.85% for non random sequences and 96.82% for random sequences. This means the test will typically sustain a high degree of accuracy especially at a 0.05 cut off. But does falter at meeting the cyber security standard of 0.01. This means we will use this in conjunction with the overall statement from the NIST suite on the specific tests as extra evidence to prove or disprove randomness.

In the case above we can clearly see that RandTest labels all binary sequences as random with no prediction this means we can confidently say with 96% certainty of this truth, this meets most standards of prediction. But fails to meet the industry standard of 99% accuracy with cybersecurity.

### 7 Important results from NIST

The Frequency (Monobit) Test is the first test in the NIST suite, and the remainder of the tests are dependent upon this test retaining the null hypothesis. The test determines the closeness of the fraction of 1's to 1/2. For the test to pass, the number of 1's and 0's in the sequence should be similar.

For the datasets containing every observation, the binary sequence has been created based on the median of the dataset, so by the nature of median (the middle value), the number of 0's and 1's will be equal (or different by 1 in the case of an odd number of observations), hence running the test on these sequences will return a p-value of 1 (or very close to 1 for odd number of observations), providing strong evidence to retain the null hypothesis, the expected outcome.

Of more interest is the same test on the datasets of every 5th observations (pulsars 1, 2, 3, 4,5, 6) and the test on every 10th observation (pulsar 5), where there isn't the same guarantee of an equal amount of 0's and 1's. Analysing the results of each test, every number sequence passes. The lowest p-value observed is 0.096872 for pulsar 1 for every 5th observation, however it still well above the 0.01 significance level.

Now that each dataset has passed this test, further testing can be undertaken.

The next test, Frequency Test within a Block, applies a similar logic to the previous test, but instead tests the proportion of 1's in a bit block of length M, expecting the frequency of 1's to be close to M/2 for the test to pass.

For the datasets with every observation, pulsars 1,2 and 4 fail this test (extremely small p-values). On the other hand, pulsars 3 and 6 provide extremely strong evidence that the fraction of 1's with the M length bit blocks is close to 1/2. While, pulsar 5 has provides moderate evidence, p-value = 0.0398, just over the alpha of 0.01, that their is an equal proportion of 1's and 0's.

Looking to the datasets with every 5th observation, pulsars 1,2,3,5 and 6 pass with fairly strong evidence, while pulsar 4 fails. Then for pulsar 5 with every 10th observation it just passes with a p-value of 0.0216.

### 8 Final Summary of Data

### 9 Appendix Individual Table Results

You can also find the individual results in the pulsarBinaryDataResults file. With each txt corresponding with each test and their P-values.

## Note most P-values below were reformatted by the excel program to not be a decimal

#### 9.1 Pulsar 1 All

#### 

```
2
                                        Run Test
                                                  3.353164e-03
                                                                 Non-Random
3
                 Longest Run of Ones in a Block
                                                  4.782901e-02
                                                                     Random
4
                        Binary Matrix Rank Test
                                                   1.020085e-01
                                                                     Random
5
    Discrete Fourier Transform (Spectral) Test
                                                  5.765222e-01
                                                                     Random
6
        Non-Overlapping Template Matching Test
                                                  4.860000e-07
                                                                 Non-Random
            Overlapping Template Matching Test
7
                                                  5.365440e-04
                                                                 Non-Random
           Maurer's Universal Statistical Test -1.000000e+00
8
                                                                      Error
9
                         Linear Complexity Test
                                                  8.177284e-01
                                                                     Random
                                  Serial Test A
10
                                                  2.420000e-19
                                                                 Non-Random
11
                                  Serial Test B
                                                  1.600000e-06
                                                                 Non-Random
12
                       Approximate Entropy Test
                                                   1.840000e-13
                                                                 Non-Random
13
                 Cumulative Sums (Forward) Test
                                                  6.250000e-01
                                                                     Random
14
                 Cumulative Sums (Reverse) Test
                                                  6.250000e-01
                                                                     Random
15
                Random Excursions Test State -4
                                                  1.210000e-01
                                                                     Random
                Random Excursions Test State -3
16
                                                  3.158609e-01
                                                                     Random
17
                Random Excursions Test State -2
                                                  3.590000e-01
                                                                     Random
18
                Random Excursions Test State -1
                                                                     Random
                                                  7.280000e-01
19
                Random Excursions Test State +1
                                                   2.730000e-01
                                                                     Random
20
                Random Excursions Test State +2
                                                   1.640000e-01
                                                                     Random
21
                Random Excursions Test State +3
                                                                     Random
                                                  3.070000e-01
22
                Random Excursions Test State +4
                                                   1.160000e-01
                                                                     Random
23
        Random Exursions Variant Test State -9
                                                                     Random
                                                   1.503674e-01
24
        Random Exursions Variant Test State -8
                                                  2.508288e-01
                                                                     Random
25
        Random Exursions Variant Test State -7
                                                  2.850494e-01
                                                                     Random
26
        Random Exursions Variant Test State -6
                                                                     Random
                                                   2.685964e-01
27
        Random Exursions Variant Test State -5
                                                   4.008621e-01
                                                                     Random
        Random Exursions Variant Test State -4
28
                                                  7.261831e-01
                                                                     Random
29
        Random Exursions Variant Test State -3
                                                                     Random
                                                  9.471395e-01
                                                  7.808785e-01
30
        Random Exursions Variant Test State -2
                                                                     Random
31
        Random Exursions Variant Test State -1
                                                                     Random
                                                  9.114677e-01
32
        Random Exursions Variant Test State +1
                                                                     Random
                                                  7.110000e-01
33
        Random Exursions Variant Test State +2
                                                  7.320000e-01
                                                                     Random
34
        Random Exursions Variant Test State +3
                                                   6.430000e-01
                                                                     Random
35
        Random Exursions Variant Test State +4
                                                   5.100000e-01
                                                                     Random
36
        Random Exursions Variant Test State +5
                                                                     Random
                                                  8.140000e-01
37
        Random Exursions Variant Test State +6
                                                  9.820000e-01
                                                                     Random
38
        Random Exursions Variant Test State +7
                                                                     Random
                                                  9.340000e-01
39
        Random Exursions Variant Test State +8
                                                  6.670000e-01
                                                                     Random
40
        Random Exursions Variant Test State +9
                                                  7.260000e-01
                                                                     Random
      Outcome2 Outcome3
                            Outcome4
                                         Outcome5
                                                      Outcome6
0
        Random
                  Random
                              Random
                                           Random
                                                      Absolute
    Non-Random
                  Random
                          Non-Random
                                           Random
                                                        Random
1
2
    Non-Random
                  Random
                          Non-Random
                                       Non-Random
                                                   Non-Random
                          Non-Random
3
    Non-Random
                  Random
                                           Random
                                                   Non-Random
4
        Random
                  Random
                                           Random
                                                         Error
                              Random
5
    Non-Random
                  Random
                              Random
                                           Random
                                                        Random
```

6	Non-Random	Random	Random	Random	Random
7	Non-Random	Random	Random	Random	Error
8	Error	Error	Error	Error	Error
9	Random	Random	Random	Random	Error
10	Non-Random	Random	Non-Random	Random	Random
11	Random	Random	Non-Random	Random	Random
12	Non-Random	Random	Non-Random	Random	Absolute
13	Random	Random	Non-Random	Random	Random
14	Random	Random	Non-Random	Random	Random
15	Random	Random	Random	Non-Random	Random
16	Non-Random	Random	Random	Random	Random
17	Non-Random	Random	Random	Random	Random
18	Random	Random	Random	Random	Random
19	Random	Random	Random	Random	Random
20	Random	Random	Random	Random	Random
21	Random	Random	Random	Random	Random
22	Random	Random	Random	Random	Non-Random
23	Random	Random	Random	Random	Random
24	Random	Random	Random	Random	Random
25	Random	Random	Random	Random	Random
26	Random	Random	Random	Random	Random
27	Random	Random	Random	Random	Random
28	Random	Random	Random	Random	Random
29	Random	Random	Random	Random	Random
30	Random	Random	Random	Random	Random
31	Random	Random	Random	Random	Random
32	Random	Random	Random	Random	Random
33	Random	Random	NaN	Random	Random
34	Random	Random	NaN	Random	Random
35	Random	Random	NaN	Absolute	Random
36	Random	Random	NaN	Random	Random
37	Random	Random	NaN	Random	Random
38	Random	Random	NaN	Random	Random
39	Random	Random	NaN	Random	Random
40	Random	Random	NaN	Random	Random

### 9.2 Pulsar 1 5ths

### []: pulsar1\_5th

[]:	Test Name	P-Value	Outcome
0	Frequency Test (Monobit)	0.096872	Random
1	Frequency Test within a Block	0.273011	Random
2	Run Test	0.295998	Random
3	Longest Run of Ones in a Block	0.143727	Random
4	Binary Matrix Rank Test	0.858290	Random
5	Discrete Fourier Transform (Spectral) Test	0.453695	Random

```
6
        Non-Overlapping Template Matching Test
                                                  0.424735
                                                                 Random
7
            Overlapping Template Matching Test
                                                                 Random
                                                  0.418207
8
           Maurer's Universal Statistical Test
                                                 -1.000000
                                                                  Error
9
                         Linear Complexity Test
                                                  0.757153
                                                                 Random
10
                                  Serial Test A
                                                                 Random
                                                  0.148533
11
                                  Serial Test B
                                                  0.445237
                                                                 Random
12
                       Approximate Entropy Test
                                                             Non-Random
                                                  0.000145
                Cumulative Sums (Forward) Test
13
                                                  0.072222
                                                                 Random
                Cumulative Sums (Reverse) Test
                                                                 Random
14
                                                  0.193743
15
               Random Excursions Test State -4
                                                  0.997903
                                                                 Random
               Random Excursions Test State -3
                                                                 Random
16
                                                  0.995330
17
               Random Excursions Test State -2
                                                  0.984748
                                                                 Random
18
               Random Excursions Test State -1
                                                  0.849145
                                                                 Random
19
               Random Excursions Test State +1
                                                  0.156236
                                                                 Random
20
               Random Excursions Test State +2
                                                  0.000354
                                                             Non-Random
21
               Random Excursions Test State +3
                                                  0.000475
                                                             Non-Random
22
               Random Excursions Test State +4
                                                  0.369569
                                                                 Random
23
        Random Exursions Variant Test State +1
                                                                 Random
                                                  0.317311
24
        Random Exursions Variant Test State +2
                                                  0.386476
                                                                 Random
25
        Random Exursions Variant Test State +3
                                                                 Random
                                                  0.013906
26
        Random Exursions Variant Test State +4
                                                  0.000670
                                                             Non-Random
27
        Random Exursions Variant Test State +5
                                                             Non-Random
                                                  0.007661
28
        Random Exursions Variant Test State +6
                                                  0.000526
                                                             Non-Random
29
        Random Exursions Variant Test State +7
                                                             Non-Random
                                                  0.002282
30
        Random Exursions Variant Test State +8
                                                                 Random
                                                  0.038867
31
        Random Exursions Variant Test State +9
                                                  0.015293
                                                                 Random
```

#### 9.3 Pulsar 2 All

#### []: pulsar2\_all

```
[]:
                                            Test Name
                                                             P-Value
                                                                         Outcome2
     0
                            Frequency Test (Monobit)
                                                        9.933346e-01
                                                                           Random
     1
                       Frequency Test within a Block
                                                        9.910000e-12
                                                                      Non-Random
     2
                                             Run Test
                                                        3.200000e-94
                                                                      Non-Random
     3
                                                                      Non-Random
                      Longest Run of Ones in a Block
                                                        3.810000e-36
     4
                             Binary Matrix Rank Test
                                                        2.570000e-01
                                                                           Random
         Discrete Fourier Transform (Spectral) Test
     5
                                                        6.140000e-05
                                                                      Non-Random
             Non-Overlapping Template Matching Test
     6
                                                        3.830000e-26
                                                                      Non-Random
     7
                  Overlapping Template Matching Test
                                                        4.630000e-13
                                                                      Non-Random
     8
                Maurer's Universal Statistical Test
                                                      -1.000000e+00
                                                                            Error
     9
                              Linear Complexity Test
                                                                           Random
                                                        5.807496e-01
     10
                                        Serial Test A
                                                        2.350000e-17
                                                                      Non-Random
                                        Serial Test B
                                                        9.520000e-01
                                                                           Random
     11
     12
                            Approximate Entropy Test
                                                        8.310000e-34
                                                                      Non-Random
                      Cumulative Sums (Forward) Test
     13
                                                        5.600000e-01
                                                                           Random
                      Cumulative Sums (Reverse) Test
     14
                                                        5.530000e-01
                                                                           Random
```

```
15
               Random Excursions Test State -4
                                                  2.050000e-01
                                                                     Random
               Random Excursions Test State -3
16
                                                  7.680000e-03
                                                                 Non-Random
17
               Random Excursions Test State -2
                                                  1.610000e-03
                                                                 Non-Random
18
               Random Excursions Test State -1
                                                  1.780000e-02
                                                                     Random
19
               Random Excursions Test State +1
                                                                     Random
                                                  3.980000e-01
20
               Random Excursions Test State +2
                                                  4.020000e-01
                                                                     Random
21
               Random Excursions Test State +3
                                                                     Random
                                                  1.520000e-01
22
               Random Excursions Test State +4
                                                  4.760000e-01
                                                                     Random
23
        Random Exursions Variant Test State -9
                                                                     Random
                                                  8.054226e-01
24
        Random Exursions Variant Test State -8
                                                                     Random
                                                  8.514120e-01
25
        Random Exursions Variant Test State -7
                                                  9.198637e-01
                                                                     Random
26
        Random Exursions Variant Test State -6
                                                  9.651054e-01
                                                                     Random
27
        Random Exursions Variant Test State -5
                                                  9.037602e-01
                                                                     Random
28
        Random Exursions Variant Test State -4
                                                  6.808479e-01
                                                                     Random
29
        Random Exursions Variant Test State -3
                                                                     Random
                                                  5.164123e-01
30
        Random Exursions Variant Test State -2
                                                  3.147768e-01
                                                                     Random
31
        Random Exursions Variant Test State -1
                                                                     Random
                                                  1.467931e-01
32
        Random Exursions Variant Test State +1
                                                  3.100000e-01
                                                                     Random
33
        Random Exursions Variant Test State +2
                                                  7.060000e-01
                                                                     Random
34
        Random Exursions Variant Test State +3
                                                                     Random
                                                  8.460000e-01
35
        Random Exursions Variant Test State +4
                                                  9.560000e-01
                                                                     Random
36
        Random Exursions Variant Test State +5
                                                                     Random
                                                  7.170000e-01
37
        Random Exursions Variant Test State +6
                                                                     Random
                                                  8.100000e-01
        Random Exursions Variant Test State +7
38
                                                  9.680000e-01
                                                                     Random
39
        Random Exursions Variant Test State +8
                                                                     Random
                                                  9.550000e-01
40
        Random Exursions Variant Test State +9
                                                  8.880000e-01
                                                                     Random
```

#### 9.4 Pulsar 2 5ths

#### []: pulsar2\_5th

```
[]:
                                            Test Name
                                                         P-Value
                                                                      Outcome
     0
                            Frequency Test (Monobit)
                                                        0.736699
                                                                       Random
     1
                       Frequency Test within a Block
                                                        0.753000
                                                                       Random
     2
                                             Run Test
                                                        0.018694
                                                                       Random
     3
                                                                       Random
                      Longest Run of Ones in a Block
                                                        0.092363
     4
                             Binary Matrix Rank Test
                                                                       Random
                                                        0.481248
     5
         Discrete Fourier Transform (Spectral) Test
                                                        0.565809
                                                                       Random
     6
             Non-Overlapping Template Matching Test
                                                        0.526000
                                                                       Random
     7
                  Overlapping Template Matching Test
                                                                       Random
                                                        0.248594
     8
                 Maurer's Universal Statistical Test -1.000000
                                                                        Error
     9
                              Linear Complexity Test
                                                                       Random
                                                        0.543779
     10
                                        Serial Test A
                                                        0.123000
                                                                       Random
                                        Serial Test B
                                                                       Random
     11
                                                        0.224000
     12
                            Approximate Entropy Test
                                                        0.000025
                                                                   Non-Random
                      Cumulative Sums (Forward) Test
     13
                                                        0.604000
                                                                       Random
                      Cumulative Sums (Reverse) Test
     14
                                                        0.904000
                                                                       Random
```

```
15
               Random Excursions Test State -4
                                                  0.332000
                                                                 Random
16
               Random Excursions Test State -3
                                                                 Random
                                                  0.161000
17
               Random Excursions Test State -2
                                                  0.625000
                                                                 Random
18
               Random Excursions Test State -1
                                                  0.719000
                                                                 Random
               Random Excursions Test State +1
                                                             Non-Random
19
                                                  0.008430
20
               Random Excursions Test State +2
                                                             Non-Random
                                                  0.000040
21
               Random Excursions Test State +3
                                                                 Random
                                                  0.152000
22
               Random Excursions Test State +4
                                                  0.383000
                                                                 Random
23
        Random Exursions Variant Test State -5
                                                  0.226919
                                                                 Random
        Random Exursions Variant Test State -4
                                                                 Random
24
                                                  0.237548
        Random Exursions Variant Test State -3
25
                                                  0.263552
                                                                 Random
26
        Random Exursions Variant Test State -2
                                                                 Random
                                                  0.193931
27
        Random Exursions Variant Test State -1
                                                  0.133614
                                                                 Random
28
        Random Exursions Variant Test State +1
                                                  0.261000
                                                                 Random
29
        Random Exursions Variant Test State +2
                                                  0.516000
                                                                 Random
30
        Random Exursions Variant Test State +3
                                                  0.576000
                                                                 Random
31
        Random Exursions Variant Test State +4
                                                                 Random
                                                  0.450000
32
        Random Exursions Variant Test State +5
                                                  0.739000
                                                                 Random
33
        Random Exursions Variant Test State +6
                                                  0.792000
                                                                 Random
34
        Random Exursions Variant Test State +7
                                                                 Random
                                                  0.533000
35
        Random Exursions Variant Test State +8
                                                  0.561000
                                                                 Random
        Random Exursions Variant Test State +9
36
                                                  0.649000
                                                                 Random
```

#### 9.5 Pulsar 3 All

#### []: pulsar3\_all

```
[]:
                                            Test Name
                                                         P-Value Outcome3
     0
                            Frequency Test (Monobit)
                                                        0.978133
                                                                    Random
     1
                       Frequency Test within a Block
                                                        0.843000
                                                                    Random
     2
                                             Run Test
                                                        0.051600
                                                                    Random
                      Longest Run of Ones in a Block
     3
                                                        0.206000
                                                                    Random
     4
                             Binary Matrix Rank Test
                                                                    Random
                                                        0.694000
         Discrete Fourier Transform (Spectral) Test
     5
                                                        0.655000
                                                                    Random
     6
             Non-Overlapping Template Matching Test
                                                        0.771000
                                                                    Random
                  Overlapping Template Matching Test
     7
                                                                    Random
                                                        0.887000
     8
                 Maurer's Universal Statistical Test -1.000000
                                                                     Error
     9
                              Linear Complexity Test
                                                        0.320837
                                                                    Random
     10
                                        Serial Test A
                                                        0.876000
                                                                    Random
                                        Serial Test B
                                                        0.553000
                                                                    Random
     11
     12
                            Approximate Entropy Test
                                                        0.767000
                                                                    Random
     13
                      Cumulative Sums (Forward) Test
                                                        0.943000
                                                                    Random
     14
                      Cumulative Sums (Reverse) Test
                                                        0.926000
                                                                    Random
     15
                     Random Excursions Test State -4
                                                                    Random
                                                        0.339000
     16
                     Random Excursions Test State -3
                                                        0.590000
                                                                    Random
                     Random Excursions Test State -2
     17
                                                        0.573000
                                                                    Random
     18
                     Random Excursions Test State -1
                                                        0.590000
                                                                    Random
```

```
19
               Random Excursions Test State +1
                                                  0.491000
                                                              Random
20
               Random Excursions Test State +2
                                                              Random
                                                  0.565000
21
               Random Excursions Test State +3
                                                  0.448000
                                                              Random
22
               Random Excursions Test State +4
                                                  0.643000
                                                              Random
23
        Random Exursions Variant Test State -9
                                                              Random
                                                  0.215330
24
        Random Exursions Variant Test State -8
                                                  0.180652
                                                              Random
25
        Random Exursions Variant Test State -7
                                                              Random
                                                  0.150421
26
        Random Exursions Variant Test State -6
                                                  0.174968
                                                              Random
27
        Random Exursions Variant Test State -5
                                                  0.232254
                                                              Random
28
        Random Exursions Variant Test State -4
                                                              Random
                                                  0.286278
        Random Exursions Variant Test State -3
29
                                                  0.322716
                                                              Random
30
        Random Exursions Variant Test State -2
                                                  0.332797
                                                              Random
31
        Random Exursions Variant Test State -1
                                                  0.541866
                                                              Random
32
        Random Exursions Variant Test State +1
                                                  0.493000
                                                              Random
        Random Exursions Variant Test State +2
33
                                                  0.509000
                                                              Random
34
        Random Exursions Variant Test State +3
                                                  0.759000
                                                              Random
35
        Random Exursions Variant Test State +4
                                                              Random
                                                  0.863000
36
        Random Exursions Variant Test State +5
                                                  0.780000
                                                              Random
37
        Random Exursions Variant Test State +6
                                                  0.629000
                                                              Random
38
        Random Exursions Variant Test State +7
                                                              Random
                                                  0.410000
39
        Random Exursions Variant Test State +8
                                                  0.288000
                                                              Random
        Random Exursions Variant Test State +9
40
                                                  0.309000
                                                              Random
```

#### 9.6 Pulsar 3 5ths

#### []: pulsar3\_5th

```
[]:
                                            Test Name
                                                         P-Value
                                                                      Outcome
     0
                            Frequency Test (Monobit)
                                                                       Random
                                                        0.951201
     1
                       Frequency Test within a Block
                                                        0.925000
                                                                       Random
     2
                                             Run Test
                                                        0.126000
                                                                       Random
     3
                      Longest Run of Ones in a Block
                                                        0.957000
                                                                       Random
     4
                             Binary Matrix Rank Test -1.000000
                                                                        Error
                                                                  Non-Random
     5
         Discrete Fourier Transform (Spectral) Test
                                                        0.003660
     6
             Non-Overlapping Template Matching Test
                                                        1.000000
                                                                       Random
     7
                  Overlapping Template Matching Test -1.000000
                                                                        Error
     8
                 Maurer's Universal Statistical Test -1.000000
                                                                        Error
     9
                              Linear Complexity Test -1.000000
                                                                        Error
     10
                                        Serial Test A
                                                        0.499000
                                                                       Random
                                        Serial Test B
                                                                       Random
     11
                                                        0.499000
     12
                            Approximate Entropy Test
                                                        1.000000
                                                                     Absolute
     13
                      Cumulative Sums (Forward) Test
                                                                       Random
                                                        0.763000
     14
                      Cumulative Sums (Reverse) Test
                                                        0.705000
                                                                       Random
                                                                       Random
     15
                     Random Excursions Test State -4
                                                        0.886000
     16
                     Random Excursions Test State -3
                                                        0.347000
                                                                       Random
                     Random Excursions Test State -2
     17
                                                        0.735000
                                                                       Random
     18
                     Random Excursions Test State -1
                                                        0.700000
                                                                       Random
```

```
19
                Random Excursions Test State +1
                                                   0.659000
                                                                  Random
20
                Random Excursions Test State +2
                                                                  Random
                                                   0.258000
                Random Excursions Test State +3
21
                                                   0.018600
                                                                  Random
22
                Random Excursions Test State +4
                                                   0.783000
                                                                  Random
23
        Random Exursions Variant Test State -9
                                                                  Random
                                                   0.490920
24
        Random Exursions Variant Test State -8
                                                                 Random
                                                   0.463355
25
        Random Exursions Variant Test State -7
                                                   0.410205
                                                                 Random
26
        Random Exursions Variant Test State -6
                                                   0.413686
                                                                 Random
27
        Random Exursions Variant Test State -5
                                                                 Random
                                                   0.438578
28
        Random Exursions Variant Test State -4
                                                                 Random
                                                   0.406813
        Random Exursions Variant Test State -3
29
                                                   0.603332
                                                                 Random
30
        Random Exursions Variant Test State -2
                                                                  Random
                                                   0.765594
31
        Random Exursions Variant Test State -1
                                                   0.605577
                                                                 Random
32
        Random Exursions Variant Test State +1
                                                   0.699000
                                                                 Random
        Random Exursions Variant Test State +2
                                                   0.502000
33
                                                                 Random
34
        Random Exursions Variant Test State +3
                                                   0.326000
                                                                  Random
35
        Random Exursions Variant Test State +4
                                                                  Random
                                                   0.262000
36
        Random Exursions Variant Test State +5
                                                   0.263000
                                                                 Random
37
        Random Exursions Variant Test State +6
                                                   0.259000
                                                                  Random
38
                                             NaN
                                                        NaN
                                                                     NaN
39
                                             NaN
                                                        NaN
                                                                     NaN
40
                                             NaN
                                                        NaN
                                                                     NaN
```

#### 9.7 Pulsar 4 All

#### []: pulsar4\_all

```
[]:
                                            Test Name
                                                             P-Value
                                                                         Outcome4
     0
                            Frequency Test (Monobit)
                                                        9.812939e-01
                                                                           Random
     1
                       Frequency Test within a Block
                                                        3.910000e-53
                                                                       Non-Random
     2
                                             Run Test
                                                        3.420000e-21
                                                                       Non-Random
                      Longest Run of Ones in a Block
     3
                                                        3.930000e-08
                                                                       Non-Random
     4
                             Binary Matrix Rank Test
                                                                           Random
                                                        6.940000e-01
         Discrete Fourier Transform (Spectral) Test
     5
                                                        1.820000e-02
                                                                           Random
     6
             Non-Overlapping Template Matching Test
                                                        7.120000e-02
                                                                           Random
                  Overlapping Template Matching Test
     7
                                                                           Random
                                                        2.960000e-01
     8
                Maurer's Universal Statistical Test -1.000000e+00
                                                                            Error
     9
                              Linear Complexity Test
                                                        4.620000e-01
                                                                           Random
     10
                                        Serial Test A
                                                        0.000000e+00
                                                                       Non-Random
                                        Serial Test B
                                                                       Non-Random
     11
                                                        0.000000e+00
     12
                            Approximate Entropy Test
                                                        2.100000e-12
                                                                       Non-Random
     13
                      Cumulative Sums (Forward) Test
                                                        1.040000e-09
                                                                       Non-Random
     14
                      Cumulative Sums (Reverse) Test
                                                        8.930000e-10
                                                                       Non-Random
     15
                     Random Excursions Test State -4
                                                        9.730000e-01
                                                                           Random
     16
                     Random Excursions Test State -3
                                                        9.450000e-01
                                                                           Random
                     Random Excursions Test State -2
     17
                                                        8.490000e-01
                                                                           Random
     18
                     Random Excursions Test State -1
                                                        3.060000e-01
                                                                           Random
```

```
19
               Random Excursions Test State +1
                                                  9.310000e-01
                                                                     Random
20
               Random Excursions Test State +2
                                                  5.080000e-01
                                                                     Random
21
               Random Excursions Test State +3
                                                  1.770000e-01
                                                                     Random
22
               Random Excursions Test State +4
                                                  1.180000e-02
                                                                     Random
23
        Random Exursions Variant Test State -1
                                                                     Random
                                                  5.637029e-01
24
        Random Exursions Variant Test State +1
                                                  3.860000e-01
                                                                     Random
25
        Random Exursions Variant Test State +2
                                                                     Random
                                                  6.170000e-01
26
        Random Exursions Variant Test State +3
                                                  6.990000e-01
                                                                     Random
27
        Random Exursions Variant Test State +4
                                                                     Random
                                                  8.270000e-01
28
        Random Exursions Variant Test State +5
                                                                     Random
                                                  8.470000e-01
29
        Random Exursions Variant Test State +6
                                                  7.280000e-01
                                                                     Random
30
        Random Exursions Variant Test State +7
                                                  8.100000e-01
                                                                     Random
31
        Random Exursions Variant Test State +8
                                                  8.810000e-01
                                                                     Random
32
        Random Exursions Variant Test State +9
                                                  8.340000e-01
                                                                     Random
```

#### 9.8 Pulsar 4 5ths

#### []: pulsar4\_5th

```
[]:
                                                                         Outcome
                                            Test Name
                                                             P-Value
                                                       8.339354e-01
     0
                            Frequency Test (Monobit)
                                                                          Random
     1
                       Frequency Test within a Block
                                                        3.340000e-03
                                                                      Non-Random
     2
                                             Run Test
                                                        3.350000e-03
                                                                      Non-Random
     3
                      Longest Run of Ones in a Block
                                                       4.350000e-01
                                                                          Random
     4
                             Binary Matrix Rank Test -1.000000e+00
                                                                           Error
     5
         Discrete Fourier Transform (Spectral) Test
                                                        3.120000e-01
                                                                          Random
     6
             Non-Overlapping Template Matching Test
                                                        1.000000e+00
                                                                        Absolute
     7
                 Overlapping Template Matching Test -1.000000e+00
                                                                           Error
                Maurer's Universal Statistical Test -1.000000e+00
     8
                                                                           Error
     9
                              Linear Complexity Test -1.000000e+00
                                                                            Error
                                       Serial Test A
     10
                                                        0.000000e+00
                                                                      Non-Random
     11
                                       Serial Test B
                                                        0.000000e+00
                                                                      Non-Random
     12
                            Approximate Entropy Test
                                                                        Absolute
                                                        1.000000e+00
                      Cumulative Sums (Forward) Test
     13
                                                        3.970000e-03
                                                                      Non-Random
     14
                      Cumulative Sums (Reverse) Test
                                                        7.880000e-03
                                                                      Non-Random
                     Random Excursions Test State -4
                                                                          Random
     15
                                                        9.980000e-01
     16
                     Random Excursions Test State -3
                                                        9.950000e-01
                                                                          Random
     17
                     Random Excursions Test State -2
                                                        9.850000e-01
                                                                          Random
     18
                     Random Excursions Test State -1
                                                        8.490000e-01
                                                                          Random
     19
                     Random Excursions Test State +1
                                                        6.840000e-03
                                                                      Non-Random
     20
                     Random Excursions Test State +2
                                                        2.980000e-04
                                                                      Non-Random
                     Random Excursions Test State +3
     21
                                                        3.550000e-04
                                                                      Non-Random
     22
                     Random Excursions Test State +4
                                                        1.220000e-04
                                                                      Non-Random
             Random Exursions Variant Test State +1
     23
                                                        1.240000e-02
                                                                          Random
     24
             Random Exursions Variant Test State +2
                                                        1.490000e-05
                                                                      Non-Random
             Random Exursions Variant Test State +3
     25
                                                        2.700000e-07
                                                                      Non-Random
     26
             Random Exursions Variant Test State +4
                                                        1.570000e-04
                                                                      Non-Random
```

```
27
        Random Exursions Variant Test State +5
                                                  6.680000e-02
                                                                     Random
28
        Random Exursions Variant Test State +6
                                                  1.320000e-01
                                                                     Random
29
        Random Exursions Variant Test State +7
                                                  3.750000e-02
                                                                     Random
30
        Random Exursions Variant Test State +8
                                                  5.280000e-02
                                                                     Random
31
        Random Exursions Variant Test State +9
                                                  2.750000e-01
                                                                     Random
```

#### 9.9 Pulsar 4 10ths

#### []: pulsar4\_10th

```
[]:
                                            Test Name
                                                        P-Value
                                                                     Outcome
     0
                            Frequency Test (Monobit)
                                                        0.656501
                                                                       Random
     1
                       Frequency Test within a Block
                                                        0.021600
                                                                       Random
     2
                                             Run Test
                                                                  Non-Random
                                                        0.001920
     3
                      Longest Run of Ones in a Block
                                                        0.326000
                                                                      Random
                             Binary Matrix Rank Test -1.000000
     4
                                                                       Error
     5
         Discrete Fourier Transform (Spectral) Test
                                                        0.760000
                                                                      Random
     6
             Non-Overlapping Template Matching Test
                                                                    Absolute
                                                        1.000000
                  Overlapping Template Matching Test -1.000000
     7
                                                                       Error
     8
                Maurer's Universal Statistical Test -1.000000
                                                                       Error
                              Linear Complexity Test -1.000000
     9
                                                                       Error
                                        Serial Test A
     10
                                                        0.000000
                                                                  Non-Random
     11
                                        Serial Test B
                                                        0.000000
                                                                  Non-Random
     12
                            Approximate Entropy Test
                                                        1.000000
                                                                    Absolute
     13
                      Cumulative Sums (Forward) Test
                                                        0.023500
                                                                       Random
                      Cumulative Sums (Reverse) Test
     14
                                                        0.075900
                                                                      Random
     15
                     Random Excursions Test State -4
                                                        0.905000
                                                                      Random
                     Random Excursions Test State -3
     16
                                                        0.324000
                                                                      Random
     17
                     Random Excursions Test State -2
                                                                      Random
                                                        0.768000
     18
                     Random Excursions Test State -1
                                                        0.394000
                                                                      Random
                     Random Excursions Test State +1
     19
                                                        0.836000
                                                                      Random
     20
                     Random Excursions Test State +2
                                                        0.481000
                                                                      Random
     21
                     Random Excursions Test State +3
                                                                      Random
                                                        0.331000
     22
                     Random Excursions Test State +4
                                                        0.067000
                                                                      Random
     23
             Random Exursions Variant Test State -3
                                                        0.504501
                                                                      Random
     24
             Random Exursions Variant Test State -2
                                                        0.711923
                                                                      Random
     25
             Random Exursions Variant Test State -1
                                                                      Random
                                                        0.831170
     26
             Random Exursions Variant Test State +1
                                                        1.000000
                                                                    Absolute
     27
             Random Exursions Variant Test State +2
                                                        0.902000
                                                                       Random
     28
             Random Exursions Variant Test State +3
                                                                      Random
                                                        0.924000
     29
             Random Exursions Variant Test State +4
                                                        0.872000
                                                                       Random
                                                        0.570000
     30
             Random Exursions Variant Test State +5
                                                                       Random
     31
             Random Exursions Variant Test State +6
                                                        0.563000
                                                                      Random
             Random Exursions Variant Test State +7
     32
                                                                       Random
                                                        0.636000
     33
             Random Exursions Variant Test State +8
                                                        0.741000
                                                                       Random
             Random Exursions Variant Test State +9
     34
                                                        0.796000
                                                                      Random
```

# 9.10 Pulsar 5 All

# []: pulsar5\_all

[]:	Test Name	P-Value	Outcome5
0	Frequency Test (Monobit)	0.977150	Random
1	Frequency Test within a Block	0.039800	Random
2	Run Test	0.000020	Non-Random
3	Longest Run of Ones in a Block	0.085500	Random
4	Binary Matrix Rank Test	0.694000	Random
5	Discrete Fourier Transform (Spectral) Test	0.064800	Random
6	Non-Overlapping Template Matching Test	0.032300	Random
7	Overlapping Template Matching Test	0.296000	Random
8		-1.000000	Error
9	Linear Complexity Test	0.029600	Random
10	Serial Test A	0.853000	Random
11	Serial Test B	0.963000	Random
12	Approximate Entropy Test	0.956000	Random
13	Cumulative Sums (Forward) Test	0.761000	Random
14	Cumulative Sums (Reverse) Test	0.761000	Random
15	Random Excursions Test State -4	0.000254	Non-Random
16	Random Excursions Test State -3	0.019100	Random
17	Random Excursions Test State -2	0.162000	Random
18	Random Excursions Test State -1	0.067300	Random
19	Random Excursions Test State +1	0.941000	Random
20	Random Excursions Test State +2	0.951000	Random
21	Random Excursions Test State +3	0.155000	Random
22	Random Excursions Test State +4	0.027100	Random
23	Random Exursions Variant Test State -9	0.867859	Random
24	Random Exursions Variant Test State -8	0.790482	Random
25	Random Exursions Variant Test State -7	0.668588	Random
26	Random Exursions Variant Test State -6	0.569494	Random
27	Random Exursions Variant Test State -5	0.331137	Random
28	Random Exursions Variant Test State -4	0.194835	Random
29	Random Exursions Variant Test State -3	0.145052	Random
30	Random Exursions Variant Test State -2	0.092327	Random
31	Random Exursions Variant Test State -1		Random
32	Random Exursions Variant Test State +1	0.170000	Random
33	Random Exursions Variant Test State +2	0.166000	Random
34	Random Exursions Variant Test State +3	0.645000	Random
35	Random Exursions Variant Test State +4	1.000000	Absolute
36	Random Exursions Variant Test State +5	0.775000	Random
37	Random Exursions Variant Test State +6	0.642000	Random
38	Random Exursions Variant Test State +7	0.812000	Random
39	Random Exursions Variant Test State +8	0.965000	Random
40	Random Exursions Variant Test State +9	0.835000	Random

### 9.11 Pulsar 5 5ths

# []: pulsar5\_5th

[]:		Test Name	P-Value	Outcome
	0	Frequency Test (Monobit)	0.898120	Random
	1	Frequency Test within a Block	0.860000	Random
	2	Run Test	0.095800	Random
	3	Longest Run of Ones in a Block	0.693000	Random
	4	Binary Matrix Rank Test	-1.000000	Error
	5	Discrete Fourier Transform (Spectral) Test	0.217000	Random
	6	Non-Overlapping Template Matching Test	1.000000	Absolute
	7	Overlapping Template Matching Test	-1.000000	Error
	8	Maurer's Universal Statistical Test	-1.000000	Error
	9	Linear Complexity Test	-1.000000	Error
	10	Serial Test A	0.853000	Random
	11	Serial Test B	0.932000	Random
	12	Approximate Entropy Test	1.000000	Absolute
	13	Cumulative Sums (Forward) Test	0.894000	Random
	14	Cumulative Sums (Reverse) Test	0.786000	Random
	15	Random Excursions Test State -4	0.728000	Random
	16	Random Excursions Test State -3	0.900000	Random
	17	Random Excursions Test State -2	0.755000	Random
	18	Random Excursions Test State -1	0.968000	Random
	19	Random Excursions Test State +1	0.383000	Random
	20	Random Excursions Test State +2	0.542000	Random
	21	Random Excursions Test State +3	0.568000	Random
	22	Random Excursions Test State +4	0.796000	Random
	23	Random Exursions Variant Test State -9	0.638822	Random
	24	Random Exursions Variant Test State -8	8.415830	Random
	25	Random Exursions Variant Test State -7	0.382103	Random
	26	Random Exursions Variant Test State -6	0.500924	Random
	27	Random Exursions Variant Test State -5	0.630192	Random
	28	Random Exursions Variant Test State -4	0.655119	Random
	29	Random Exursions Variant Test State -3	0.597154	Random
	30	Random Exursions Variant Test State $-2$	0.820090	Random
	31	Random Exursions Variant Test State -1	0.599426	Random
	32	Random Exursions Variant Test State +1	0.237000	Random
	33	Random Exursions Variant Test State +2	0.225000	Random
	34	Random Exursions Variant Test State +3	0.159000	Random
	35	Random Exursions Variant Test State +4	0.234000	Random
	36	Random Exursions Variant Test State +5	0.294000	Random
	37	Random Exursions Variant Test State +6	0.285000	Random
	38	Random Exursions Variant Test State +7	0.382000	Random
	39	Random Exursions Variant Test State +8	0.416000	Random
	40	Random Exursions Variant Test State +9	0.390000	Random

### 9.12 Pulsar 6 All

# []: pulsar6\_all

[]:	Test Name	P-Value	Outcome6
0	Frequency Test (Monobit)	1.000000	Absolute
1	Frequency Test within a Block	0.836000	Random
2	Run Test	0.000011	Non-Random
3	Longest Run of Ones in a Block	0.000178	Non-Random
4	Binary Matrix Rank Test	-1.000000	Error
5	Discrete Fourier Transform (Spectral) Test	0.218000	Random
6	Non-Overlapping Template Matching Test	0.087500	Random
7	Overlapping Template Matching Test	-1.000000	Error
8	Maurer's Universal Statistical Test	-1.000000	Error
9	Linear Complexity Test	-1.000000	Error
10	Serial Test A	0.356000	Random
11	Serial Test B	0.697000	Random
12	Approximate Entropy Test	1.000000	Absolute
13	Cumulative Sums (Forward) Test	0.679000	Random
14	Cumulative Sums (Reverse) Test	0.679000	Random
15	Random Excursions Test State -4	0.196000	Random
16	Random Excursions Test State -3	0.398000	Random
17	Random Excursions Test State -2	0.760000	Random
18	Random Excursions Test State -1	0.845000	Random
19	Random Excursions Test State +1	0.272000	Random
20	Random Excursions Test State +2	0.135000	Random
21	Random Excursions Test State +3	0.076700	Random
22	Random Excursions Test State +4	0.002160	Non-Random
23	Random Exursions Variant Test State -9	0.324324	Random
24	Random Exursions Variant Test State -8	0.338728	Random
25	Random Exursions Variant Test State -7	0.388747	Random
26	Random Exursions Variant Test State -6	0.449177	Random
27	Random Exursions Variant Test State -5	0.449063	Random
28	Random Exursions Variant Test State -4	0.366256	Random
29	Random Exursions Variant Test State -3	0.335979	Random
30	Random Exursions Variant Test State -2	0.407626	Random
31	Random Exursions Variant Test State -1	0.719918	Random
32	Random Exursions Variant Test State +1	0.720000	Random
33	Random Exursions Variant Test State +2	0.730000	Random
34	Random Exursions Variant Test State +3	0.364000	Random
35	Random Exursions Variant Test State +4	0.442000	Random
36	Random Exursions Variant Test State +5	0.605000	Random
37	Random Exursions Variant Test State +6	0.719000	Random
38	Random Exursions Variant Test State +7	0.947000	Random
39	Random Exursions Variant Test State +8	0.975000	Random
40	Random Exursions Variant Test State +9	0.908000	Random

### 9.13 Pulsar 6 5ths

# []: pulsar6\_5th

[]:		Test Name	P-Value	Outcome
	0	Frequency Test (Monobit)	0.498962	Random
	1	Frequency Test within a Block	0.596000	Random
	2	Run Test	0.835000	Random
	3	Longest Run of Ones in a Block	0.833000	Random
	4	Binary Matrix Rank Test	-1.000000	Error
	5	Discrete Fourier Transform (Spectral) Test	0.698000	Random
	6	Non-Overlapping Template Matching Test	1.000000	Random
	7	Overlapping Template Matching Test	-1.000000	Error
	8	Maurer's Universal Statistical Test	-1.000000	Error
	9	Linear Complexity Test	-1.000000	Error
	10	Serial Test A	0.499000	Random
	11	Serial Test B	0.098400	Random
	12	Approximate Entropy Test	1.000000	Absolute
	13	Cumulative Sums (Forward) Test	0.473000	${\tt Random}$
	14	Cumulative Sums (Reverse) Test	0.849000	Random
	15	Random Excursions Test State -4	0.431000	Random
	16	Random Excursions Test State -3	0.494000	${\tt Random}$
	17	Random Excursions Test State -2	0.221000	${\tt Random}$
	18	Random Excursions Test State -1	0.149000	${\tt Random}$
	19	Random Excursions Test State +1	0.570000	Random
	20	Random Excursions Test State +2	0.801000	Random
	21	Random Excursions Test State +3	0.924000	Random
	22	Random Excursions Test State +4	0.963000	Random
	23	Random Exursions Variant Test State -9	0.845815	Random
	24	Random Exursions Variant Test State -8	0.944984	Random
	25	Random Exursions Variant Test State -7	0.766848	Random
	26	Random Exursions Variant Test State -6	0.808976	Random
	27	Random Exursions Variant Test State -5	0.929013	Random
	28	Random Exursions Variant Test State -4	0.613505	Random
	29	Random Exursions Variant Test State -3	0.473289	Random
	30	Random Exursions Variant Test State -2	0.643429	Random
	31	Random Exursions Variant Test State -1	0.422678	Random
	32	Random Exursions Variant Test State +1	0.109000	Random