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I- $((F \to (F \to F)) \to (F \to F)) \to F$

$X \to X$ (R1)

$X \to V$ (R2)

$V \to F$ (R3)

F = "Sei, lá!"

II- $((F \to F) \to ((F \to F) \to F)) \to F$

$X \to X$ (R1)

$V \to X$ (R3)

$X = ((F \to F) \to F)$

$X \to X$ (R1)

$V \to F$ (R3)

$F \to F$

$X \to X$ (R1)

V = "Sim, claro!".

tilibra

(2-) $(C \to A) \to (C \to (A \to A))$

[1] $A \to ((A \to A) \to A)$, $p = A$, $q = (A \to A)$, usando H1.
[2] $(A \to ((A \to A) \to A)) \to ((A \to (A \to A)) \to (A \to A))$, $p = A$, $q = (A \to A)$ e $r = A$, usando H2.
[3] $((A \to (A \to A)) \to (A \to A))$, M.P. linhas 1 e 2.
[4] $A \to (A \to A)$, $p = A$, $q = A$, usando H1.
[5] $(A \to A)$ M.P. linhas 3 e 4.
[6] $(A \to A) \to (C \to (A \to A))$, $p = (A \to A)$, $q = C$, usando H1.
[7] $(C \to (A \to A))$, M.P. linhas 5 e 6.
[8] $(C \to (A \to A)) \to ((C \to A) \to (C \to (A \to A)))$, $p = (C \to (A \to A))$, $q = (C \to A)$, usando H1.
[9] $(C \to A) \to (C \to (A \to A))$, M.P. linhas 7 e 8.

(3) a) $((A \to B) \to C) \Rightarrow (B \to C)$

[1] $(A \to B) \to C$, início.
[2] $B \to ((A \to B) \to C)$, R2 linha 1.
[3] $(B \to (A \to B)) \to (B \to C)$, usando dist na linha 2.
[4] $B \to (A \to B)$, $p = B$, $q = A$, usando H1.
[5] $(B \to C)$, M.P. linhas 3 e 4. ∎

b) $((B \to C) \to D) \Rightarrow ((A \to (B \to C)) \to D)$

tilibra

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41. $(A \to (B \to C)) \Rightarrow ((A \wedge B) \to C)$

[1] $A \to (B \to C)$, início.
[2] $(A \wedge B) \to (A \to (B \to C))$, R2 linha 1.
[3] $((A \wedge B) \to A) \to ((A \wedge B) \to (B \to C))$, dist linha 2.
[4] $(A \wedge B) \to A$, $p = A$, $q = B$, usando H3.
[5] $(A \wedge B) \to (B \to C)$, M.P. linhas 3 e 4.
[6] $((A \wedge B) \to B) \to ((A \wedge B) \to C)$, dist linha 5
[7] $(A \wedge B) \to B$, $p = A$, $q = B$, usando H4.
[8] $(A \wedge B) \to C$, M.P. linhas 6 e 7. ∎

tilibra

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Declaro não trocar informações da prova com colegas e nem pesquisar na internet.

José Douglas Gondim Soares.