

Aplicação dos métodos de integração

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1 Aplicação dos métodos de integração:

$$A = \int g(x, y) dA$$

$$A = 4 \int g(x, y) dx dy$$

$$f(x, y) = 0.2(x^2 - y^2)$$

$$\frac{df}{dx} = 0.4x \quad \frac{df}{dy} = -0.4y$$

$$g(x, y) = \sqrt{0.16x^2 + 0.16y^2 + 1}$$

$$A_1 = \int_0^{40} \int_0^{\sqrt{40^2 - x^2}} dy \, dx$$

$$\begin{cases} x = \rho R \cos(\theta) \\ y = \rho R \sin(\theta) \end{cases} \\ = \int_0^1 \int_0^{\frac{\pi}{2}} g(\rho R \cos \theta, \rho R \sin \theta) |J_1| d\rho d\theta$$

$$J_1 = \begin{vmatrix} R \cos \theta & -\rho R \sin \theta \\ R \sin \theta & \rho R \cos \theta \end{vmatrix} = \rho R^2 (\cos^2 \theta + \sin^2 \theta) = \rho R^2$$

$$A_1 = \int_0^1 \int_0^{\frac{\pi}{2}} g(x(\rho, \theta), y(\rho, \theta)) \rho R^2 \, d\theta d\rho =$$

$$\int_{-1}^1 \int_{-1}^1 g(x(\rho(s, t), \theta(s, t)), y(\rho(s, t), \theta(s, t))) \, \rho R^2 |J_2| \, ds \, dt$$

$$J_2 = \begin{vmatrix} \frac{1}{2} & 0 \\ 0 & \frac{\pi}{4} \end{vmatrix} = \frac{\pi}{8}$$

$$\rho = \frac{0+1}{2} + \frac{1-0}{2}s = \frac{1}{2} + \frac{s}{2}$$

$$\theta = \frac{0+\frac{\pi}{2}}{2} + \frac{\frac{\pi}{2}-0}{2}t = \frac{\pi}{4} + \frac{\pi}{4}t$$

$$s = -\sqrt{\frac{3}{5}}, 0, \sqrt{\frac{3}{5}} \text{ e } t = -\sqrt{\frac{3}{5}}, 0, \sqrt{\frac{3}{5}}$$

$$A = \int_{-1}^1 \int_{-1}^1 \hat{g}(s, t) \, ds dt = \int_{-1}^1 \int_{-1}^1 \sqrt{0.16x^2 + 0.16y^2 + 1} \, \rho R^2 \frac{\pi}{8} =$$

$$\sum \sum w_s w_t \hat{g}(s, t)$$