

Aktividade Derivadas - Douglas Horvath

1. $f(x) = (6x+1)(2x+4), x=1$

$$f'(x) = 6 \cdot (2x+4) + (6x+1) \cdot 2 \quad | \quad f'(1) = 24 \cdot (1) + 26 = 50 //$$

$$f'(x) = 12x + 24 + 12x + 2$$

$$f'(x) = 24x + 26 //$$

2. $x^2(6x-5)^3, x=1$

$$f'(x) = 2x(6x-5)^3 + x^2(3 \cdot (6x-5)^2 \cdot 6)$$

$$f'(1) = 2 + 18 = f'(1) = 20 //$$

3. $f(x) = \frac{5x-7}{x+1}, x=1$

$$f'(x) = \frac{5(x+1) - 1(5x-7)}{(x+1)^2}$$

$$f'(x) = \frac{5x+5 - 5x+7}{(x+1)^2}$$

$$f'(x) = \frac{12}{(x+1)^2} \quad | \quad f'(1) = \frac{12}{4} = 3 //$$

4. $f(x) = x^8 - \frac{4}{3}x^6 + 3x^3 + 7x - 2\sqrt{3}, x=1$

$$f'(x) = 8x^7 - 8x^5 + 9x^2 + 7$$

$$f'(1) = 8 - 8 + 9 + 7 = 16 //$$

5. $f(x) = \frac{-x^3 - 2x^2 + 5x + 8}{4x^5 - 9x + 5}, x=0$

$$f'(x) = \frac{(-3x^2 - 4x + 5) \cdot (4x^5 - 9x + 5) - (-x^3 - 2x^2 + 5x + 8) \cdot (20x^4 - 9)}{(4x^5 - 9x + 5)^2}$$

$$f'(0) = \frac{(5 \cdot 5) - (8 \cdot (-9))}{25} = \frac{25 + 72}{25} = \frac{97}{25}$$

$$6. p(x) = 3x^{10} \cdot (-x+4)^4, x=2$$

$$p'(x) = 30x^9(-x+4)^4 + (4(-x+4)^3 \cdot (-1)) \cdot 3x^{10}$$

$$p'(2) = 30 \cdot 2^9 \cdot (-2+4)^4 + (-4(-2+4)^3) \cdot 3 \cdot 2^{10}$$

$$p'(2) = 30 \cdot 512(5)^4 + (-4(5)^3) \cdot 3 \cdot 1024$$

$$p'(2) = 15360 \cdot 625 + (-4 \cdot 125) \cdot 3072$$

$$p'(2) = 9600000 + (-1536000)$$

$$p'(2) = 8064000 //$$

$$1 = x \cdot \frac{2 \cdot (2-x)^5}{(2-x)^5} \cdot x$$

$$1 = x \cdot \frac{1-x^2}{1+x}$$

$$1 = x \cdot \frac{1-x^2}{1+x} \Rightarrow 1+x = x(1-x^2) \Rightarrow 1+x = x - x^3 \Rightarrow x^3 + 2x + 1 = 0$$

$$0 = x^3 + 2x + 1 \Rightarrow x^3 + 2x + 1 = 0$$