EXERCÍCIOS - LISTA II

Calcule as seguintes integrais.

1)
$$I = \int (3x + 1)^{20} dx$$

 $3x + 1 = t$ $I = \frac{1}{3} \int_{-\infty}^{20} t^{20} dt - \Delta I = \frac{1}{3} \int_{-\infty}^{20} t^{20} dt$
 $3dx = 3t$
 $3dx =$

$$5x-1 = t$$
 $J = \frac{1}{5} \left(-\frac{1}{5} + -4 \right) I = \frac{1}{5} \frac{1}{16} - 4$
 $I = \frac{1}{80} t^{16}$
 $dx = \frac{1}{5} dt$
 $I = \frac{1}{80} (5x-1)^{16} + C$

3)
$$I = \int \frac{3}{(2x - 3)^{10}} dx$$

$$2x - 3 = t I = \frac{1}{2} \begin{cases} \frac{3}{t^{10}} dt & -6 & I = \frac{3}{2} \int t^{-10} dt \\ 2dx = dt & \\ dx = \frac{1}{2} dt & I = \frac{3}{2} \left(\frac{t^{3}}{-3} \right) - 6 & I = -\frac{3}{18} \frac{1}{t^{9}} - 6 & I = -\frac{1}{6(2x - 5)^{9}} + C \end{cases}$$

4) I =
$$\int \frac{1}{\sqrt{5+x}} dx$$

$$S+x=t \qquad I=\int \frac{1}{\sqrt{t}} dt - s \qquad I=\int \frac{t^2}{2} dt - s \qquad I=\frac{t^2}{2}$$

$$dx=dt \qquad I=2\sqrt{t}-s \qquad I=2\sqrt{s}+x+C \qquad V$$

$$5) I = \int \frac{x}{\sqrt{x^2 + 1}} dx$$

$$x^{2}+1=t$$

$$2\times d\times = d+$$

$$d\times = \frac{1}{2}d+$$

$$\int_{-\infty}^{\infty} \frac{1}{2}d+$$

6)
$$I = \int \frac{x^2}{\sqrt{5x^3 + 1}} dx$$

$$5x^{3} + J = t$$

$$15x^{2} dx = dt$$

$$15x^{2} dx = dt$$

$$1 = \frac{1}{15} \int \frac{x^{2}}{x^{2}} dt - \Delta I = \frac{1}{15} \int \frac{1}{15} dt$$

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7)
$$I = \int (2x + 1) \sqrt{x^2 + x - 3} dx$$

$$\frac{2}{x+x-3} = t$$

$$2x+1 dx = dt$$

$$dx = \frac{1}{2x+1} dt$$

$$T = \frac{2}{3} t^{\frac{3}{2}} \Rightarrow T = \frac{2}{3} \sqrt{(x^2+x-5)^3} + C$$

8)
$$I = \int \frac{2x^2 + 1}{\sqrt{2x^3 + 3x + 1}} dx$$

$$2x^{3} + 3x + 1 = t \qquad I = \begin{cases} (2x^{2} + 1) & \text{if } t = 1 \\ 6x^{2} + 3 & \text{if } t = 1 \end{cases}$$

$$6x^{2} + 3 & \text{if } t = 1 \end{cases}$$

$$4x = \frac{1}{6x^{2} + 3} \qquad I = \frac{1}{3} \left(\frac{1}{15} d + - 1 \right) = \frac{1}{3} \left(\frac{1}{2} d + - 1 \right) = \frac{1}{3} \frac{1}{2} d + \frac{1}{3}$$

$$1 = \frac{1}{3} \left(\frac{1}{2x^{3} + 3x + 1} \right) + C \qquad V$$

9)
$$I = \int \frac{1}{(x - a)^4} dx$$

$$X-a = t$$

$$dx = dt$$

$$T = \begin{cases} \frac{1}{4} dt & -b \\ \frac{1}{3} dt & -b \end{cases} = \begin{cases} \frac{1}{3} dt & -b \\ \frac{1}{3} dt & -b \end{cases} = \frac{1}{3} \frac{1}{3}$$

10) I =
$$\int \frac{(4x - 2)^2}{(2x - 1)^5} dx$$

$$2 \times -1 = t$$
 $J = \frac{1}{2} \left(\frac{2^2 (2 \times -1)^2 d \times -4}{(2 \times -1)^5} \right) = \frac{1}{2} \left(\frac{4 + 2^2}{t^5} \right) dt$

$$dx = \frac{1}{2}dt \qquad I = \frac{4}{2} \left(\frac{1}{2}dt - A I = 2 \int_{-2}^{-3} dt - A I = 2 \int_{-2}^{-3} dt \right)$$

$$\overline{I} = -\frac{1}{+^2} - \overline{D} = -\frac{1}{(2x-1)^2} + C \qquad \forall$$

11)
$$I = \int \frac{1}{(2x - 5)^2 \sqrt{2x - 5}} dx$$

$$2x-5=t I=\frac{1}{2}\left(\frac{1}{t^{2}t'^{2}}dt-n I=\frac{1}{2}\left(\frac{t^{-\frac{5}{2}}}{t^{2}d^{2}}dt-n J=\frac{1}{2}\left(\frac{t^{-\frac{5}{2}}}{t^{-\frac{3}{2}}}\right)\right)$$

$$dx = \frac{1}{2}dt$$
 $I = \frac{1}{2}\left[-\frac{2}{3}(2x-5)^{-3/2}\right]$ -0 $J = -\frac{1}{3}\sqrt{(2x-5)^3}$

$$T = -\frac{1}{3\sqrt{(2x-5)^3}} + C$$

13)
$$x = \int \frac{\sqrt[9]{(4x+2)^7}}{8x+4} dx$$

$$J = \int \frac{\sqrt[3]{(4x+2)^{\frac{1}{7}}}}{2(4x+2)^{\frac{1}{7}}} dx - b \quad J = \frac{1}{2\cdot 4} \int \frac{\sqrt[3]{t^{\frac{1}{7}}}}{t} dt - b \quad J = \frac{1}{8} \int t^{\frac{1}{7}} t^{\frac{1}{7}} dt$$

$$4x + 2 = t \qquad J = \frac{1}{8} \int t^{\frac{2}{7}} dt - b \quad J = \frac{1}{8} \int t^{\frac{1}{7}} dt - b \quad J = \frac{1}{8} \int t^{\frac{1}{7}} dt$$

$$4x = dt$$

$$4x = \frac{1}{4} dt \qquad J = \frac{5}{56} \int (4x+2)^{\frac{1}{7}} + C \quad V$$

14)
$$I = \int (\frac{x^2 - 1}{x + 1})^5 dx$$

$$J = \int (\frac{(x - 1)(x + 1)}{x + 1})^5 dx - D \quad J = \int (\frac{(x - 1)^5}{x + 1})^5 dx$$

$$x - 1 = t \qquad J = \int t^{\frac{5}{2}} dt - D \quad J = \frac{t^{\frac{7}{2}}}{\frac{7}{2}} - D \quad J = \frac{2}{7} \sqrt{t^{\frac{1}{2}}}$$

$$dx = dt$$

$$I = \frac{2}{7} \sqrt{(x - 1)^{\frac{1}{7}}} + C \qquad V$$

15)
$$I = \int_{-\infty}^{\infty} \frac{\sqrt{\left(4 - \frac{3}{x^2}\right)^3}}{x^3} dx$$

$$4 - \frac{3}{x^{2}} = t$$

$$J = \frac{1}{6} \int \frac{x^{3} \sqrt{t^{3}}}{x^{3}} dt - D \quad J = \frac{1}{6} \int \frac{t^{3/2}}{t^{3/2}} dt - D \quad J = \frac{1}{6} \int \frac{t^{5/2}}{t^{5/2}} dt$$

$$4 - 3x^{-2} = t$$

$$5 - 3 dx = dt$$

$$4 - 3x^{-2} = t$$

$$6x^{-3} dx = dt$$

$$4x = \frac{x^{3}}{t^{3}} dt$$

16)
$$I = \int \frac{1}{x^2} \sqrt{\left(\frac{1}{x} + b\right)^2} dx$$

$$\frac{1}{x} + b = t$$

$$\int \frac{x^{2}}{x^{2}} \left(t \right)^{2} dt - b \quad I = - \left[t^{\frac{3}{3}} dt \right]$$

$$\int \frac{1}{x^{2}} dx = dt$$

17)
$$I = \int \frac{1}{\sqrt[3]{\pi^2 \left(1 - 2\sqrt[3]{\pi}\right)}} dx$$

$$1 \cdot 2\sqrt[3]{x} = t \qquad dx = -\frac{3\sqrt[3]{x^2}}{2} dt$$

$$1 - 2x^{\frac{1}{3}} = t$$

$$-\frac{2}{3}x^{\frac{3}{3}} dx = dt \qquad I = -\frac{3}{2} \int_{\sqrt[3]{x^2}} \frac{1}{t} dt - x \qquad I = -\frac{3}{2} \int_{\sqrt[3]{x^2}} \frac{1}{t} dt$$

$$-\frac{2}{3\sqrt[3]{x^2}} dx = dt \qquad I = -\frac{3}{2} \int_{\sqrt[3]{x^2}} \frac{1}{t} dt - x \qquad I = -\frac{3}{2} \int_{\sqrt[3]{x^2}} \frac{1}{t} dt$$

18)
$$I = \int_{e}^{x} e^{-\frac{x}{a}} dx$$

$$-\frac{x}{a} = t$$

$$-\frac{1}{a} dx = dt$$

$$dx = -a dt$$

$$J = -a e^{-\frac{x}{a}} + C$$

$$V$$

19)
$$I = \int \frac{e^{3x-4}}{e^{x+2}} dx$$

$$I = \int e^{3x-4} e^{-(x+2)} dx - I = \int e^{3x-4-x-2} dx$$

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$$I = \int e^{3x-4} dx$$

$$I = \int e^{3x-4-x-2} dx$$

$$I = \int$$

$$20) I = \int \frac{x \cdot e^{x^2 + x}}{e^{x+1}} dx$$

 $dx = \frac{1}{3}dt$

 $dx = \frac{1}{2}df$

$$T = \begin{cases} x \cdot e^{x^2 + x} & -(x+1) \\ 0 & x \end{cases}$$

$$T = \begin{cases} x \cdot e^{x^2 + x} - x - 1 \\ 0 & x \end{cases}$$

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$$T = \begin{cases} x \cdot e^{x^2 + x} - x -$$

21)
$$I = \int a^{4x} \cdot \ln a \, dx$$

$$4x = t$$

$$J = \frac{1}{4} \ln a \int_{0}^{a} dt - s \quad J = \frac{1}{4} \ln a \frac{d}{ds}$$

$$\ln a$$

$$\partial x = \frac{1}{4} dt$$
 $I = \frac{1}{4} a^{4x} + c$

$$22) I = \int \sin \frac{x}{2} dx$$

$$\frac{x}{2} = t$$

$$\frac{1}{2} dx = dt$$

$$I = 2 \int san(t)dt - b I = -2 os(t)$$

$$\pm = -2\cos\left(\frac{\kappa}{2}\right) + C$$

23)
$$I = \int (x + 1) \cdot sen(x^2 + 2x) dx$$

$$x^{2} + 2x = t$$

$$I = \frac{1}{2} \int \frac{(x+1) \operatorname{sen}(+)}{x+1} dt$$

$$2x + 2 dx = dt$$

$$2x + 2 dx = dt$$

$$dx = \frac{1}{2} dt \qquad J = \frac{1}{2} \int sen(t) dt - n dt = \frac{1}{2} cs(t)$$

$$J = -\frac{1}{2} \cos(x^2 + 2x) + C$$

$$24) I = \int x \cdot \sin \frac{6x^4 - 2x^2}{x^2} dx$$

$$J = \int x \cdot sen(x^2(6x^2-2)) dx - A \quad J = \int x \cdot sen(6x^2-2) dx$$

$$6x^{2}-2=t$$

$$1=\frac{1}{12}\int \frac{\times sen(+)}{\times} dt - D \qquad J=\frac{1}{12}\int sen(+) dt$$

$$12\times dx=dt$$

$$dx = \frac{1}{12}dt$$
 $I = -\frac{1}{12}cos(6x^2-2)+C$ V

25) I =
$$\int tg(2x). \cos(2x) dx$$

$$2x = t$$
 $t = \frac{1}{2} \left\{ \frac{\text{Sen}(t)}{\text{Os}(t)} \cdot \text{Os}(t) dt \right\}$ $t = \frac{1}{2} \left\{ \frac{\text{Sen}(t)}{\text{Os}(t)} dt \right\}$

$$0x = \frac{1}{2}dt$$
 $T = \frac{1}{2}\cos(t) - b$ $T = -\frac{1}{2}\cos(2x) + c$

26)
$$I = \int e^{x} \cdot \cos(e^{x} - 1) dx$$

$$e^{\times} - 1 = t$$

$$= \int \frac{e^{\times} \cos(t)}{e^{\times}} dt - u \quad T = \int \cos(t) dt$$

$$= \int \frac{e^{\times} \cos(t)}{e^{\times}} dt - u \quad T = \int \cos(t) dt$$

$$dx = \frac{1}{e^x}dt$$
 $J = Sen(t) - I$ $J = Sen(e^x - 1) + C$ $\sqrt{e^x}$

27)
$$I = \int sen(2x). cos(2x) dx$$

$$Sen(2x) = t$$

$$J = \frac{1}{2} \int \frac{t \cos(2x)}{\cos(2x)} dt - n \quad J = \frac{1}{2} \int t dt$$

$$2\cos(2x) dx = dt$$

$$dx = \frac{1}{2} \int \frac{t}{2} - n \quad J = \frac{1}{2} \int \frac{t}{2} dt$$

$$I = \frac{1}{2} \int \frac{t}{2} - n \quad J = \frac{1}{2} \int \frac{t}{2} dt$$

28)
$$I = \int \cos(3x) \cdot \sin(3x) dx$$

$$5en(3x) = t$$
 $J = \frac{1}{3} \int \frac{as(3x)}{as(3x)} t dt - b I = \frac{1}{3} \int t dt$
 $3es(3x) dx = dt$
 $J = \frac{1}{3} \int \frac{as(3x)}{as(3x)} t dt - b I = \frac{1}{3} \int t dt$
 $J = \frac{1}{3} \int \frac{t^2}{as(3x)} t dt - b I = \frac{1}{3} \int t dt dt$
 $J = \frac{1}{3} \int \frac{t^2}{as(3x)} t dt - b I = \frac{1}{3} \int t dt dt$

29)
$$I = \int tg \times dx$$

$$I = \int \frac{d}{dx} dx \rightarrow I = \int \frac{dx}{dx} dx \rightarrow I$$

$$COS(X) = t$$

$$-SCN(X) dx = dt$$

$$J = -\int \frac{d}{dx} dx \rightarrow I = -\int \frac{1}{t} dt$$

$$dx = -\frac{1}{t} dt$$

$$J = -\ln|t| - a$$

$$I = -\ln|\cos(x)| + C$$

$$30) = \int \cot x \, dx$$

$$I = \int \cot g(x) dx - 0 \quad I = \int \frac{\cos(x)}{\sin(x)} dx$$

$$S(x) = t$$

$$O(x) = t$$

$$O(x) = t$$

$$I = \begin{cases} O(x) & t = t \\ T = t \end{cases}$$

$$I = \begin{cases} O(x) & t = t \\ T = t \end{cases}$$

$$I = \begin{cases} O(x) & t = t \\ T = t \end{cases}$$

$$I = \begin{cases} O(x) & t = t \\ T = t \end{cases}$$

31)
$$I = \int tg(2a + x) dx$$

$$2a+x-t$$
 $J=\int \frac{Sen(t)}{cos(t)} dt$

$$cos(t) = u$$
 $I = - \int \frac{sen(t)}{u} du - v = - \int \frac{1}{u} du$
- $sen(t) dt = du$

$$du = -\frac{1}{2} du$$
 $I = -\ln|u| - N$ $I = -\ln|\cos(4)| - N$ $I = -\ln|\cos(2\alpha + x)| + C$ V

32) I =
$$\int a \cdot \cot g(ax + b) dx$$

$$ax+b=t \qquad J=a \left(\cot_{\beta}(t) dt - b \right) \qquad J=\int_{Sen(t)} dt$$

$$adx=dt \qquad J=\int_{Sen(t)} du - b \qquad J=\int_{U} du$$

$$sen(t)=u \qquad J=\ln|sen(t)|$$

$$dt=du \qquad J=\ln|sen(ax+b)|+C \qquad V$$

33)
$$I = \int \frac{\sin x}{\cos^3 x} dx$$

$$\cos(x) = t$$

$$- \sec(x) dx = dt$$

$$\int_{-\infty}^{-\infty} \frac{dt}{dt} dt - \rho = \int_{-\infty}^{-\infty} \frac{1}{t^3} dt - \rho = \int_{-\infty}^{-\infty} \frac{1}{t^3} dt$$

$$dx = -\frac{1}{2}dt$$

$$dx = -\left[\frac{t^{-2}}{-2}\right] - \Delta I = \frac{1}{2t^{2}} - \Delta I = \frac{1}{2\cos^{2}(x)} + C$$

34)
$$I = \int \frac{1}{x \cdot \ln x} dx$$

$$\int_{X} dx = dt$$

35)
$$I = \int \frac{\ln^2 x}{x} dx$$

$$\int_{X} dx = dt$$

36)
$$I = \int \frac{\ln(2x - 4)}{x - 2} dx$$

$$Zx-4=t$$

$$Zdx=dt$$

$$Zdx=dt$$

$$D(+)=u$$

$$Z(x-2)=t$$

$$(x-2)=\frac{1}{2}$$

$$J=\frac{1}{2}\int \frac{\ln(t)}{t}dt$$

$$J=\frac{1}{2}\int \frac{\ln(t)}{t}dt$$

$$J=\int u du$$

$$I = \frac{1}{2} \left(\int_{0}^{2} (2x - 4x) + C \right)$$

37)
$$I = \int \frac{\ln^2(ax + 1)}{ax + 1} dx$$

$$\lim_{x \to a} (ax + 1) = t$$

$$\lim_{x \to a} \int \frac{1}{a} \left(\frac{1}{ax + 1} \right) dx$$

$$\lim_{x \to a} \int \frac{1}{a} \left(\frac{1}{ax + 1} \right) dx$$

$$\lim_{x \to a} \int \frac{1}{ax + 1} dx dx$$

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38)
$$I = \int \frac{\operatorname{arctg} x}{1 + x^2} \, \mathrm{d}x$$

$$f(x) = cic + g(x)$$

$$x = \frac{1}{g(f(x))}$$

$$\frac{1}{2} \int \frac{dx}{dx} dx = dt$$

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39)
$$I = \int \frac{\operatorname{arccotg} x}{1 + x^2} dx$$

$$f(x) = \operatorname{alc}(\operatorname{otg}(x))$$

$$x = \operatorname{otg}(f(x))$$

$$1 = -\operatorname{osc}(f(x)) f(x)$$

$$1 + \operatorname{cot}_{2}^{2}f(x) = \operatorname{cosc}(f(x))$$

$$1 + x^{2} = \operatorname{cosc}(f(x))$$

$$1 + x^{2} = \operatorname{cosc}(f(x))$$

$$\frac{\partial \mathcal{L}(x)}{\partial x} = t$$

$$\frac{1}{1+x^2} dx = dt$$

$$\frac{1}{2} dx = -(1+x^2)dt$$

$$40) I = \int \frac{\arcsin x}{\sqrt{1-x^2}} dx$$

0x = xd+

$$f(x) = \operatorname{dic} \operatorname{sen}(x) \qquad \operatorname{sen}^2 f(x) + \operatorname{os}^2 f(x) = 1 \qquad \operatorname{le}(x) = \frac{1}{\sqrt{1-x^2}}$$

$$x = \operatorname{sen}(x) \qquad \operatorname{os}^2 f(x) = 1 - \operatorname{sen}^2 f(x)$$

$$1 = \operatorname{os}(x) f(x) \qquad \operatorname{os}(x) = \sqrt{1-\operatorname{sen}^2 f(x)}$$

$$f(x) = \frac{1}{\operatorname{cos}(x)} \qquad \operatorname{cos}(x) = \sqrt{1-x^2}$$

$$\operatorname{cos}(x) = \frac{1}{\operatorname{cos}(x)} \qquad \operatorname{cos}(x) = \frac{1}{\operatorname{cos}(x)} = \frac{1}{\operatorname{cos}(x)}$$

$$\frac{1}{\sqrt{1-x^2}} dx = dt$$

$$41) I = \int \frac{1}{x + x \cdot \ln^2 x} dx$$

$$\int_{X} \int_{X} \int_{X$$

$$f(x) = \operatorname{dic} \operatorname{tg}(x) \qquad \underbrace{\operatorname{sen}^2 f(x) + \operatorname{cos}^2 f(x)}_{x^2 + 1} = \underbrace{\frac{1}{x^2 + 1}}_{x^2 + 1}$$

$$x = \operatorname{tg}(f(x)) \qquad \operatorname{cos}^2 f(x) \qquad \operatorname{cos}^2 f(x)$$

$$1 = \operatorname{sec}^2(f(x)) f(x) \qquad \operatorname{tg}^2 f(x) + 1 = \operatorname{sec}^2 f(x)$$

$$f'(x) = \underbrace{\frac{1}{x^2 + 1}}_{x^2 + 1} = \operatorname{sec}^2 f(x)$$

$$x^2 + 1 = \operatorname{sec}^2 f(x)$$

42) I =
$$\int \sqrt{x} \cdot \sin(x \sqrt{x}) dx$$

$$x = t$$

$$x^{1}x^{2} = t$$

$$x^{2}x^{2} = t$$

$$x^{3}x^{2} = t$$

$$x^{3}x^{3} = t$$

$$x^{3}x^{2} = t$$

$$x^{3}x^{3} =$$

43) I =
$$\int \sqrt{x} \cdot e^{2x \sqrt{x}} dx$$

$$2x \sqrt{x} = t \qquad dx = \frac{1}{3\sqrt{x}} dt$$

$$2x x^{\frac{1}{2}} = t \qquad T = \frac{1}{3} \int \sqrt{x} e^{t} dt - \Delta T = \frac{1}{3} \int e^{t} dt$$

$$\frac{1}{2} e^{t} dx = dt$$

$$T = \frac{1}{3} e^{t} - \Delta T = \frac{1}{3} e^{t} + C$$

44)
$$I = \int \frac{\sqrt{x}}{(a + x \sqrt{x})^2} dx$$

$$d + x\sqrt{x} = t$$

$$d + x^{2} = t$$

$$d + x^{3} = t$$

$$J = \frac{2}{3} \int \frac{1}{\sqrt{x}} dt - x \quad J = \frac{2}{3} \int \frac{1}{t^{2}} dt$$

$$J = \frac{2}{3} \int \frac{1}{\sqrt{x}} dt - x \quad J = \frac{2}{3} \int \frac{1}{t^{2}} dt$$

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$$J = \frac{2}{3} \int \frac{1}{\sqrt{x}} dt - x \quad J = \frac{2}{3} \int \frac{1}{t^{2}} dt - x$$

$$45) I = \int \sqrt{x} . \sqrt{1 + x \sqrt{x}} dx$$

$$1 + x\sqrt{x} = t \qquad J = \frac{2}{3} \int \sqrt{x} \sqrt{t} dt - \Delta J = \frac{2}{3} \left(t^{\frac{1}{2}} dt - \Delta J \right) = \frac{2}{3} \left(t^{\frac{3}{2}} dt - \Delta J$$

$$46) I = \int \frac{x}{\sqrt{1-x^4}} dx$$

$$x^{2} = t$$

$$Z \times dx = d +$$

$$T = \frac{1}{2} \int \frac{X}{X\sqrt{1-t^{2}}} dt - \mu \quad T = \frac{1}{2} \int \frac{1}{\sqrt{1-t^{2}}} dt$$

$$f(x) = arc sen(x) \qquad sen^2 f(x) + os^2 f(x) = 1$$

$$x = sen f(x) \qquad os^2 f(x) = 1 - sen^2 f(x)$$

$$1 = os f(x) f(x) \qquad os f(x) = \sqrt{1 - sen^2 f(x)}$$

$$f(x) = \frac{1}{\cos f(x)} \qquad cos f(x) = \sqrt{1 - x^2}$$

$$J = \frac{1}{2} \int \frac{1}{\sqrt{1-\frac{2}{1}}} dt - u \qquad J = \frac{1}{2} a(csen(t) - u) \qquad J = \frac{1}{2} a(csen(x^2) + c)$$

$$47) I = \int \frac{a}{\sqrt{a^2 - x^2}} dx$$

$$I = \int \frac{\alpha}{\sqrt{\alpha^2 \left(1 - \left(\frac{x}{\alpha}\right)^2\right)^2}} dx - b \qquad I = \int \frac{\alpha}{\alpha \sqrt{1 - \left(\frac{x}{\alpha}\right)^2}} dx$$

$$\frac{x}{a} = t - s \frac{1}{a} dx = dt - b dx = adt$$

$$\overline{J} = \alpha \int_{\sqrt{1-t^2}} dt + \Delta T = \alpha exc sen(t)$$

$$I = a. eicsen(\frac{X}{a}) + C$$

48)
$$I = \int x(x + 1)^{10} dx$$

$$-\frac{1}{2} \times = \pm -1$$

$$I = \frac{1}{2} + \frac{1}{2} - \frac{1}{2} + \frac{1}{2} = \frac{1}{2} (\times + 1) - \frac{1}{2} (\times + 1) + C$$

49)
$$I = \int x^2 (x - 2)^4 dx$$

$$\int 4x = dt$$
 $I = \int (1+2)^2 t^4 dt = \int (1+2)^2 t^4 dt$

$$5 \times -2 = t$$
 $T = \begin{cases} t^2 + 4t + 4 \end{cases} f^7 + 5 = \int t^6 + 4t^5 + 4t^7 dt$

$$I = \frac{1}{7}t^{\frac{1}{7}} + \frac{4}{6}t^{\frac{1}{7}} + \frac{4}{5}t^{\frac{1}{7}} - A \qquad I = \frac{1}{7}(x-2)^{\frac{1}{7}} + \frac{2}{5}(x-2)^{\frac{1}{7}} + \frac{4}{5}(x-2)^{\frac{1}{7}} + C \qquad V$$

$$50) I = \int \frac{x^3}{\sqrt{1+x^2}} dx$$

$$J + x^{2} = t$$

$$Z \times dx = dt$$

$$dx = \frac{1}{2} dt$$

$$J = \frac{1}{2} (t - 1) + \frac{1}{2} dt - b$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} dt$$

$$I = \frac{1}{2} \left(\frac{1}{2} - \frac{1}{$$

$$51) \quad r = \int_0^\infty \frac{x^2}{\sqrt{1+x}} dx$$

$$\int \sqrt{1+x} = t$$

$$(1+x)^{1/2} = t$$

$$\int (1+x)^{1/2} dx = dt$$

$$\int (1+x)^{-1/2} dx = dt$$

$$\int (1+x)^{-1/$$

52)
$$I = \int x^3 \sqrt{1 - x^2} dx$$

$$J = -\frac{1}{2} \int \frac{x^{3} \int t}{x} dt - \lambda t = -\frac{1}{2} \int x^{2} \int t dt - \lambda t = -\frac{1}{2} \int (1-t) \int t dt$$

$$dx = -\frac{1}{2} \int t^{2} - t t^{2} dt - \lambda t = -\frac{1}{2} \int t^{2} - t^{2} dt - \lambda t = -\frac{1}{2} \int t^$$

53)
$$I = \int x^5 \sqrt{1 - x^2} dx$$

$$I = -\frac{1}{2} \int \frac{x^{5} \sqrt{t}}{x} dt - 0 \quad I = -\frac{1}{2} \int x^{4} \int t dt$$

$$-2x dx = dt$$

$$dx = -\frac{1}{2} dt \qquad J = -\frac{1}{2} \int (1-t)^{2} t^{1/2} dt - 0 \quad I = -\frac{1}{2} \int (1-2t+t^{2}) t^{1/2} dt$$

$$-D \quad I - t = x^{2}$$

$$x^{4} = (1-t)^{2}$$

$$I = -\frac{1}{2} \int \frac{t^{1/2}}{3} - 2 \cdot \frac{3}{5} \int t^{5/2} dt - 0 \quad I = -\frac{1}{2} \int \frac{t^{3/2}}{3/2} - 2 \cdot \frac{t^{5/2}}{5/2} + \frac{t^{3/2}}{7/2}$$

$$I = -\frac{1}{2} \int \frac{2}{3} \int t^{3/2} - 2 \cdot \frac{2}{5} \int t^{5/2} dt - 0 \quad I = -\frac{1}{2} \int \frac{t^{3/2}}{3/2} - 2 \cdot \frac{t^{5/2}}{5/2} + \frac{t^{3/2}}{7/2}$$

$$I = -\frac{1}{2} \int \frac{2}{3} \int t^{3/2} - 2 \cdot \frac{2}{5} \int t^{5/2} dt - 0 \quad I = -\frac{1}{2} \int (1-x^{2})^{3/2} + C \int t^{3/2} dt - C \int t^{3/2} dt$$

54)
$$I = \int x^5 (x^3 + 1)^{\frac{2}{3}} dx$$

$$\int_{3x^{2}} dx = dt$$

55)
$$I = \int x^7 \sqrt{x^4 + 2} dx$$

56)
$$I = \int x^{3} \sqrt{2x^{2} + 4} dx$$

$$\int 2x^{2} + 4 = t \qquad I = \frac{1}{4} \int \frac{x^{3} \sqrt{t}}{x} dt - b \qquad I = \frac{1}{4} \int x^{2} \sqrt{t} dt$$

$$dx = \frac{1}{4x} dt \qquad I = \frac{1}{4} \int \frac{t - 4}{2} \sqrt{t} dt - b \qquad I = \frac{1}{8} \int (t - 4) t^{1/2} dt$$

$$dx = \frac{1}{4x} dt \qquad I = \frac{1}{4} \int \frac{t - 4}{2} \sqrt{t} dt - b \qquad I = \frac{1}{8} \int \frac{t - 4}{2} \sqrt{t} dt$$

$$2x^{2} + 4 = t \qquad I = \frac{1}{8} \int \frac{t}{5} \sqrt{t^{3}} - 4t^{1/2} dt - b \qquad I = \frac{1}{8} \int \frac{t - 4}{5} - 4t^{1/2} dt$$

$$x^{2} = \frac{t - 4}{2} \qquad I = \frac{1}{8} \int \frac{2}{5} \sqrt{t^{5}} - \frac{8}{3} \sqrt{t^{3}} - b \qquad J = \frac{1}{2} \sqrt{t^{5}} - \frac{1}{3} \sqrt{t^{3}}$$

$$I = \frac{1}{20} \sqrt{(2x^{2} + 4)^{5}} - \frac{1}{3} \sqrt{(2x^{2} + 4)^{3}} + C$$

$$57) \qquad I = \int x^{3} \sqrt{3x^{2} - 6} dx$$

$$-3x^{2} - 6 = t \qquad I = \frac{1}{4} \left(\frac{x^{3} \sqrt{t}}{3} dt + b \right) \qquad I = \frac{1}{4} \left(\frac{x^{2} \sqrt{t}}{3} dt + dt \right)$$

58)
$$I = \int \frac{1}{1 + \sqrt{x}} dx$$

$$\int_{1+\sqrt{x}}^{1+\sqrt{x}} dx = t \quad t = 2 \int_{1+\sqrt{x}}^{1+\sqrt{x}} dt - t \quad t = 2 \int_{1+\sqrt{x}}^{1$$

$$59) I = \int \frac{\sqrt{x}}{1 + \sqrt{x}} dx$$

$$\int_{-1}^{2} \frac{1}{\sqrt{x}} = t$$

60)
$$I = \int \frac{\sqrt[3]{x}}{(2 + x\sqrt[3]{x})^2} dx$$

$$2 + x \sqrt[3]{x} = t$$

$$2 + x \sqrt[3]{3} = t$$

$$4 \times \sqrt[3]{3} = t$$

$$2 + x \sqrt[3]{x} = t$$

$$2 + x x \sqrt[3]{3} = t$$

$$2 + x \sqrt[3]{3} = t$$

$$2 + x \sqrt[3]{3} = t$$

$$1 = \frac{3}{4} \int \frac{3 \sqrt{x}}{3 \sqrt{x}} (t)^{2} dt$$

$$1 = \frac{3}{4} \int \frac{1}{t} dt - x \int 1 = \frac{3}{4} \int t^{-2} dt$$

$$\frac{4}{3} \times \frac{3}{4} dx = dt$$

$$1 = \frac{3}{4} \int \frac{1}{t^{-1}} dt - x \int 1 = \frac{3}{4} \int t^{-2} dt$$

$$1 = \frac{3}{4} \int \frac{1}{t^{-1}} dt - x \int 1 = \frac{3}{4} \int t^{-2} dt$$

$$J = -\frac{3}{4(2+\sqrt[3]{x})} + C$$

61)
$$I = \int \frac{1}{\sqrt{x}(x+1)} dx$$

$$\int x^{2} = t$$

$$x^{2} = t$$

$$\int x^{2} dx = dt$$

$$dx = 2\int x dt$$

$$x = t^{2}$$

$$\int \sqrt{x} = t$$

$$\int \frac{t}{x} dt - x = 2 \int \frac{1}{t'+1} dt$$

$$\int \frac{1}{2} x^{-\frac{1}{2}} dx = dt$$

$$\int \frac{1}{2} x^{-\frac{1}{2}} dx =$$

62)
$$I = \int \frac{1}{1 + x + \sqrt{x + 1}} dx$$

$$\int \sqrt{x + 1} = t \qquad J = 2 \int \frac{t}{t^2 + t} dt - 0 \quad J = 2 \int \frac{t}{t(t + 1)} dt$$

$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t + 1} dt - 0 \qquad J = 2 \int \frac{1}{t} du$$

$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t} du$$

$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t} du$$

$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t} du$$

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$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t} du$$

$$\int (x + 1)^{-1/2} dx = dt \qquad J = 2 \int \frac{1}{t} dt$$

63)
$$I = \int \frac{x^5}{\sqrt{x^3 + 4} - 2} dx$$

$$\int \sqrt{x^{3}+4} = t$$

$$\int \frac{2}{3} \int \frac{t \times 5}{x^{2}(t-2)} dt - 5 \quad I = \frac{2}{3} \int \frac{x^{3}}{t-2} dt$$

$$\int (x^{3}+4)^{\frac{1}{2}} = t$$

$$\int (3x^{2}) dx = dt$$

$$\int = \frac{2}{3} \int (t+2)^{\frac{1}{2}} dt - 5 \quad I = \frac{2}{3} \int (t+2)^{\frac{1}{2}} dt + 5 \quad t = \frac{2}{3} \int (t+$$

64)
$$I = \int \frac{2x + \sqrt{x + 1}}{x^2 + 2x + 1} dx$$